Package 'CompRandFld'

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CheckCorrModel

Check of the Correlation Model

Description

Subroutine called by InitParam. The procedure controls if the correlation model inserted has been implemented.

Usage

CheckCorrModel(corrmodel)

Arguments

corrmodel String; the name of a correlation model, for the description see CovarianceFct.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

FitComposite

CheckInput

Check of the input

Description

Subroutine called by the fitting procedures. The procedure controls the input passed to the fitting procedures.

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Usage

Arguments

coordx	A numeric $(d \times 2)$ -matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
corrmodel	$String; the name of a correlation model, for the description see {\tt CovarianceFct.}\\$
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
fixed	A named list giving the values of the parameters that will be considered as known values. The listed parameters for a given correlation function will be not estimated, i.e. if list (nugget=0) the nugget effect is ignored.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
likelihood	String; the configuration of the composite likelihood. Marginal is the default.
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
model	String; the density associated to the likelihood objects. Gaussian is the default.
optimizer	String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.
replicates	Logical; if FALSE (the default) one spatial random field is considered, instead if TRUE the data are considered as iid replicates of a field.
start	A named list with the initial values of the parameters that are used by the numerical routines in maximization procedure. NULL is the default.
type	String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods.
varest	Logical; if TRUE the estimate' variances and standard errors are returned. FALSE is the default.
vartype	String; the type of estimation method for computing the estimate variances, see FitComposite.
weighted	Logical; if TRUE the likelihood objects are weighted. If FALSE (the default) the composite likelihood is not weighted.
weights	A numeric vector of weights.
winconst	Numeric; a positive real value – if vartype=Sub-Samp – that determines the window size in the sub-sampling estimates of the variances, see FitComposite.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

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CheckLikelihood

Check of the type of Composite-likelihood

Description

Subroutine called by InitParam. The procedure controls the type of the composite-likelihood passed to the FitComposite procedure.

Usage

```
CheckLikelihood(likelihood)
```

Arguments

likelihood String; the configuration of the composite likelihood. Marginal is the default.

Author(s)

 $Simone\ Padoan, < \verb|simone.padoan@epfl.ch>|, \verb|http://people.epfl.ch/simone.padoan|.\\$

See Also

FitComposite

CheckModel

Check of the type of Random Field

Description

Subroutine called by InitParam. The procedure controls the type of random field passed to the fitting procedures.

Usage

```
CheckModel (model)
```

Arguments

model

String; the density associated to the likelihood objects. Gaussian is the default.

Author(s)

```
Simone\ Padoan, < \verb|simone.padoan@epfl.ch>|, \verb|http://people.epfl.ch/simone.padoan|.
```

See Also

```
FitComposite
```

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CheckParam

Check of the Parameters

Description

Subroutine called by InitParam. The procedure controls the validity of the correlation's parameters.

Usage

```
CheckParam(corrmodel, namesparam, numparam)
```

Arguments

corrmodel String; the name of a correlation model.

namesparam String; the names of the parameters.

numparam Numeric; the number of the parameters.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

FitComposite

CheckParamRange

Check of the Parameters' Ranges

Description

Subroutine called by the fitting procedures. The procedure controls the range of the correlation's parameters.

Usage

CheckParamRange(param)

Arguments

param Numeric; a vector of correlation's parameters.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

6 Check VarType

CheckType

Check of the type of likelihood objects

Description

Subroutine called by InitParam. The procedure controls the type of likelihood objects that form the composite-likelihood .

Usage

```
CheckType(type)
```

Arguments

type

String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

FitComposite

CheckVarType

Check of the method for the computation of the estimates' variances

Description

Subroutine called by InitParam. The procedure controls the method used to compute the estimates' variances.

Usage

```
CheckVarType(type)
```

Arguments

type

String; the method used to compute the estimates' variances. If SubSamp (the default) the estimates' variances are computed by the sub-sampling method, see FitComposite.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

CompLikelihood 7

ompLikelihood Optimizes the Composite log-likelihood
--

Description

Subroutine called by FitComposite. The procedure estimates the model parameters by maximisation of the composite log-likelihood.

Usage

```
CompLikelihood(coordx, coordy, corrmodel, data, flagcorr, flagnuis, fixed, grid, likelihood, lonlat, lower, model, namescorr, namesnuis, namesparam, numcoord, numdata, numparam, numparamcorr, optimizer, param, type, upper, varest, vartype, winconst)
```

Arguments

coordx	A numeric ($d \times 2$)-matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
corrmodel	Numeric; the id of the correlation model.
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
flagcorr	A numeric vector of binary values denoting which parameters of the correlation function will be estimated.
flagnuis	A numeric vector of binary values denoting which nuisance parameters will be estimated.
fixed	A numeric vector of parameters that will be considered as known values.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
likelihood	String; the configuration of the compositelikelihood, see FitComposite.
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
lower	A numeric vector with the lower bounds of the parameters' ranges.
model	Numeric; the id value of the density associated to the likelihood objects.
namescorr	String; the names of the correlation parameters.
namesnuis	String; the names of the nuisance parameters.
namesparam	String; the names of the parameters to be maximised.
numcoord	Numeric; the number of coordinates.
numdata	Numeric; the number of data replications in time.
numparam	Numeric; the number of parameters to be maximised.
numparamcorr	Numeric; the number of correlation parameters.

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optimizer String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.

param A numeric vector of parameters' values.

type String; the type of the likelihood objects. If Pairwise (the default) then the

marginal composite likelihood is formed by pairwise marginal likelihoods.

upper A numeric vector with the upper bounds of the parameters' ranges.

varest Logical; if TRUE the estimate' variances and standard errors are returned. FALSE

is the default.

vartype String; the type of estimation method for computing the estimate variances, see

FitComposite.

winconst Numeric; a positive real value – if vartype=Sub-Samp – that determines the

window size in the sub-sampling estimates of the variances, see FitComposite.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

FitComposite

CorrelationFct Computes the Correlation function

Description

Subroutine called by Covariogram. The procedure computes the estimated correlation function for a given fitted model.

Usage

CorrelationFct (corrmodel, lags, param)

Arguments

corrmodel Numeric; the id of the correlation model.

lags A numeric vector of distances between points.

param A numeric vector with the parameter values.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

CorrelationParam 9

CorrelationParam

Lists the Parameters of the Correlation function

Description

Subroutine called by DetectParam and InitParam. The procedure returns the list of the parameter for a given correlation model.

Usage

```
CorrelationParam(corrmodel)
```

Arguments

corrmodel String; the name of a correlation model.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

FitComposite

Covariogram

Computes (and Plots) the covariance function and the variogram

Description

The procedure computes and plots the estimated covariance function and the variogram from a fitted model obtained fitting a random field with the composite-likelihood or using the weighted least square method.

Usage

```
Covariogram(fitted, lags=NULL, answer.cov=FALSE, answer.vario=FALSE, answer.range=FALSE, show.cov=FALSE, show.vario=FALSE, show.range=FALSE, add.cov=FALSE, add.vario=FALSE, pract.range=95, vario, ...)
```

Arguments

fitted	The fitted object obtained from the FitComposite procedure.
lags	A numeric vector of distances.
answer.cov	Logical; if ${\tt TRUE}$ a vector with the estimated covariance function is returned; if ${\tt FALSE}$ (the default) the covariance is not returned.
answer.vario	Logical; if TRUE a vector with the estimated variogram is returned; if FALSE (the default) the variogram is not returned.

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answer.range	Logical; if TRUE the estimated pratical range is returned; if FALSE (the default) the pratical range is not returned.
show.cov	Logical; if TRUE the estimated covariance function is plotted; if FALSE (the default) the covariance function is not plotted.
show.vario	Logical; if TRUE the estimated variogram is plotted; if FALSE (the default) the variogram is not plotted.
show.range	Logical; if TRUE the estimated pratical range is added on the plot; if FALSE (the default) the pratical range is not added.
add.cov	Logical; if TRUE the vector of the estimated covariance function is added on the current plot; if FALSE (the default) the covariance is not added.
add.vario	Logical; if TRUE the vector with the estimated variogram is added on the current plot; if FALSE (the default) the correlation is not added.
pract.range	Numeric; the percent of the sill to be reached.
vario	An object of type Variogram obtained from EVariogram.
	other optional parameters which are passed to plot function.

Value

The returned object is a list with:

```
covariance The vector of the estimated covariance function; variogram The vector of the estimated variogram function; pratical.range

The estimated practial range.
```

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

References

Gaetan, C. and Guyon, X. (2010) Spatial Statistics and Modelling. Spring Verlang, New York.

Examples

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DetectParam

Identifies the Parameters of the Correlation function

Description

Subroutine called by Covariogram and others The procedure returns a list with the correlation model and the list of parameters.

Usage

```
DetectParam(corrmodel, fixed, param)
```

Arguments

corrmodel String; the name of a correlation model.

fixed A numeric vector with the fixed parameters.

A numeric vector with the parameters.

Author(s)

```
Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.
```

See Also

```
FitComposite
```

12 Dist2Dist

Value Distribution		V	alue Distribution to Another Extreme
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Description

the function transforms a sequence of values following an extreme value distribution to a sequence with another desired extreme value distribution.

Usage

```
Dist2Dist(data, from='Gev', to='sFrechet', loc=NULL, scale=NULL, shape=NULL)
```

Arguments

data	A numeric vector or a matrix of extreme values.
from	The name of the original extreme value distribution, i.e. Gev (the default), see
	the Details section.
to	The name of the desired extreme value distribution, i.e. sFrechet (the default), see the Details section.
loc	A numeric value or vector of location parameters.
scale	A numeric value or vector of scale parameters.
shape	A numeric value or vector of shape parameters.

Details

If data is a numeric vector of length n then the dataset is consider as a realisation from an univariate extreme value distribution. Instead, if data is a $(n \times d)$ -matrix then the columns represent the different variables with extreme value distributions and the rows represent the iid replications. Finally, if data is a $(d \times d \times n)$ -matrix then the columns and rows represent the different variables and the third dimension represents the iid replications.

The parameters from and to indicate the original extreme value distribution(s) from which the observations are drawn and the target extreme value distribution(s) that the transformed data will follow. The options are:

- 1. from=Gev (generalised extreme value distribution):
 - to=Uniform, which means uniform distribution;
 - to=sFrechet, which means standard (or unit) Frechet distribution, that is GEV(1,1,1);
 - to=sGumbel, which means standard Gumbel distribution, that is GEV(0,1,1);
 - to=sWeibull, which means standard Weibull distribution, that is GEV(1,1,-1);
 - to=Gev, which means generalised extreme value distribution. Note, that in this case, it is required to insert vectors of location, scale and shape parameters with dimension n in the univariate case, dimension d when data is $(n \times d)$ -matrix and dimension $n \times d$ when data is $(d \times d \times n)$ -matrix.
- 2. from=sFrechet
 - to=Gev.
- 3. from=sGumbel
 - to=Gev.
- 4. from=sWeibull
 - to=Gev.

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Value

A numeric vector or matrix of transformed values following the desired distribution.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan

References

de Haan, L. and Ferreira, A. (2006) Extreme Value Theory An Introduction. Springer Verlang, New York.

See Also

FitGev

EVariogram Empirical Estimation of the Random Fields	e Variogram for Gaussian and Max-Stable
_ ^	e variogram jor Gaussian ana Max-Siable

Description

the function returns an empirical estimate of the variogram for a Gaussian or a max-stable random field.

Usage

```
EVariogram(coordx, coordy, data, cloud=FALSE, extcoeff=FALSE, grid=FALSE, gev=c(0,1,0), lonlat=FALSE, maxdist=NULL, numbins=NULL, replicates=FALSE, type='variogram')
```

Arguments

coordx	A numeric $(d \times 2)$ -matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations (see FitComposite).
cloud	Logical; if TRUE the variogram cloud is computed, otherwise if FALSE (the default) the empirical (binned) variogram is returned.
extcoeff	Logical; if the extremal coefficient estimates need to be returned. Available only if type is equal to madogram or Fmadogram.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
gev	A numeric vector with the three GEV parameters;
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
maxdist	A numeric value denoting the maximum distance, see the Section Details .

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numbins A numeric value denoting the numbers of bins, see the Section **Details**.

replicates Logical; if FALSE (the default) one spatial random field is considered, instead

if TRUE the data are considered as iid replicates of a field.

type A String denoting the type of variogram. Three options are available, variogram

which return the standard variogram and for extreme values the madogram or

Fmadogram.

Details

The numbins parameter indicates the number of adjacent intervals to consider in order to grouped distances with which to compute the (weighted) lest squares.

The maxdist parameter indicates the maximum distance below which the shorter distances will be considered in the calculation of the (weighted) least squares.

Value

Returns an object of class Variogram. An object of class Variogram is a list containing at most the following components:

bins Adjacent intervals of grouped distances if cloud=FALSE. Otherwise the pair-

wise distances if cloud=TRUE;

cloud If the variogram cloud is returned (TRUE) or the empirical variogram (FALSE);

centers The centers of the bins;

extremalcoeff

The extremal coefficient estimates;

lenbins The number of pairs in each bin;

maxdist The maximum distance used for the calculation of the variogram;

variogram The empirical variogram;

type The type of estimated variogram: the standard variogram or the madogram.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

References

Cressie, N. A. C. (1993) Statistics for Spatial Data. New York: Wiley.

Gaetan, C. and Guyon, X. (2010) Spatial Statistics and Modelling. Spring Verlang, New York.

Cooley, D., Naveau, P. and Poncet, P. (2006) *Variograms for spatial max-stable random fields*. Dependence in Probability and Statistics, p. 373–390.

See Also

EVariogram 15

Examples

```
library (RandomFields)
set.seed(2111)
# Set the coordinates of the sites:
x \leftarrow runif(100, 0, 20)
y \leftarrow runif(100, 0, 20)
###
### Example 1. Empirical variogram estimate of one
### spatial realisation of a Gaussian random field.
###
###
# Set the model's parameters:
corrmodel <- "stable"
mean <- 0
variance <- 1
nugget <- 0
scale <- 10
power <- 1.5
# Simulation of a Gaussian random field in the specified points:
sim <- GaussRF(x=x, y=y, model=corrmodel, grid=FALSE,</pre>
            param=c(mean, variance, nugget, scale, power))
# Empirical variogram estimation:
fit <- EVariogram(x, y, sim)</pre>
# Results:
plot(fit$centers, fit$variogram, xlab='h', ylab=expression(gamma(h)),
    ylim=c(0, max(fit$variogram)), xlim=c(0, fit$maxdist), pch=20)
###
### Example 2. Empirical mandogram estimate of one
### spatial realisation of a max-stable random field.
# Simulation of a max-stable random field in the specified points:
sim <- MaxStableRF(x=x, y=y, model=corrmodel, grid=FALSE, maxstable="extr",</pre>
                param=c(mean, variance, nugget, scale, power), n=100)
sim <- t(sim)
sim <- Dist2Dist(sim, to='sGumbel')</pre>
# Empirical madogram estimation:
fit <- EVariogram(x, y, sim, type='madogram', replicates=TRUE,</pre>
               extcoeff=TRUE, cloud=TRUE)
# Results:
```

```
par(mfrow=c(1,2))
plot(fit$centers, fit$variogram, xlab='h', ylab=expression(nu(h)),
      ylim=c(0, max(fit$variogram)), xlim=c(0, fit$maxdist), pch=20)
plot(fit$centers, fit$extremalcoeff, xlab='h', ylab=expression(theta(h)),
      ylim=c(1, 2), xlim=c(0, fit$maxdist), pch=20)
```

FitComposite Maximum Weighted Composite-likelihood Fitting of Gaussian Random Fields

Description

Maximum weighted composite-likelihood fitting for Gaussian and max-stable random fields. The function returns the model parameters' estimates and the estimates' variances by weighted maximisation of the composite-likelihood and allows to fix any of the parameters.

Usage

```
FitComposite(coordx, coordy=NULL, corrmodel, data, fixed=NULL, grid=FALSE, likelihood='Marginal', lonlat=FALSE, model='Gaussian', optimizer='Nelder-Mead', replicates=FALSE, start=NULL, type='Pairwise', varest=FALSE, vartype='SubSamp', weighted=FALSE, weights=NULL, winconst=NULL)
```

Arguments

coordx	A numeric $(d \times 2)$ -matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
corrmodel	String; the name of a correlation model, for the description see the Section Details .
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations (see Details).
fixed	A named list giving the values of the parameters that will be considered as known values. The listed parameters for a given correlation function will be not estimated, i.e. if list(nugget=0) the nugget effect is ignored.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
likelihood	String; the configuration of the composite likelihood. Marginal is the default, see the Section Details .
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
model	String; the type of random field and therefore the densities associated to the likelihood objects. Gaussian is the default, see the Section Details .
optimizer	String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.

replicates	Logical; if FALSE (the default) one spatial random field is considered, instead if TRUE the data are considered as iid replicates of a field.
start	A named list with the initial values of the parameters that are used by the numerical routines in maximization procedure. NULL is the default (see Details).
type	String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods (see Details).
varest	Logical; if TRUE the estimate' variances and standard errors are returned. FALSE is the default.
vartype	String; (Sub-Samp the default) the type of method used for computing the estimates' variances, see the Section Details .
weighted	Logical; if TRUE the likelihood objects are weighted, see the Section Details . If FALSE (the default) the composite likelihood is not weighted.
weights	A numeric vector of weights (see Details).
winconst	Numeric; a positive real value – if vartype=Sub-Samp – that determines the window size in the sub-sampling estimates of the variances (see Details).

Details

The corrmodel parameter allows to select a specific correlation function for the random field. The implemented correlation models are:

- 1. cauchy;
- 2. exponential;
- 3. gauss (Gaussian);
- 4. gencauchy (generalised Cauchy);
- stable (or powered exponential);
- 6. whittlematern (Whittle-Matern).

See for more details CovarianceFct.

With the data parameter:

- If it is a numeric vector, the data are interpreted as a spatial or temporal realisation;
- If it is a numeric $(n \times d)$ -matrix, the d columns represent the different points where the data observed and the n rows represent the available iid replications.
- If it is a numeric $(d \times d \times n)$ -matrix then the data are considered as observations observed at $(d \times d)$ points with eventually n available replications.

The likelihood parameter represents the composite-likelihood configurations. The settings alternatives are:

- 1. Conditional, the composite-likelihood is formed by conditionals likelihoods;
- 2. Marginal, the composite-likelihood is formed by marginals likelihoods;
- 3. Full, the composite-likelihood turns out to be the standard likelihood;

The model paramter represents the type of random field considered, an example is the Gaussian random field. Therefore, this also determines the associated density functions that will define the likelihood objects and then the composite-likelihood. The available options:

• Gaussian, for a Gaussian random field.

The replicates parameter specifies if iid replications of the random field are available. If FALSE, then a realisation of spatial random field is considered. Instead if TRUE the data are considered as iid replications of a spatial random field. For the moment the option of iid replications is implemented only for a spatial random field. The alternative is to work with a realisation of a spatial-temporal random field.

The start parameter allows to specify starting values. If start is omitted the routine is computing the starting values using the weighted moment estimator.

The type parameter represents the type of likelihood used in the composite-likelihood definition. The possible alternatives are listed in the following scheme.

- 1. If a Gaussian random field is considered (model=Gaussian):
 - If the composite is formed by marginal likelihoods (likelihood=Marginal):
 - Pairwise, the composite-likelihood is defined by the pairwise likelihoods;
 - Difference, the composite-likelihood is defined by likelihoods which are obtained as difference of the pairwise likelihoods.
 - If the composite is formed by conditional likelihoods (likelihood=Conditional)
 - Pairwise, the composite-likelihood is defined by the pairwise conditional likelihoods.
 - If the composite is formed by a full likelihood (likelihood=Full):
 - Standard, the likelihood that will be considered is the standard multivariate version;
 - Restricted, the likelihood that will be considered is the restricted version (see **References**).

The vartype parameter—if the varest is TRUE—specifies the method used to compute the estimates' variances. The default Sub—Samp uses the Sub-Sampling method to estimate the variability matrix in the Godambe matrix. Other options are: Theoretical where for the variability matrix it is used the exact expression (for the moment it has been implemented only for the Difference likelihood, see the type field) and Sampling where the variability matrix in this case is estimated by the sample contro-part (available only for iid. replicates of a random field, see the replicates parameter).

The weighted parameter specifies if the likelihoods forming the composite-likelihood must be weighted. If TRUE the weights are selected by opportune procedures that improve the efficient of the maximum composite-likelihood estimator (not implemented yet). If FALSE the efficient improvement procedure is not used.

The weights parameter allows to weight the composite-likelihood by weights insert by the users. These do not imply any gain in efficiency of the maximum composite-likelihood estimator but still be a reasonable setting (not implemented yet!).

Value

Returns an object of class FitComposite. An object of class FitComposite is a list containing at most the following components:

clic The composite information criterion, if the full likelihood is considered then it

conicide with the Akaike information criterion;

coord The vector of coordinates;

convergence A string that denotes if convergence is reached;

corrmodel The correlation model;

data The vector or matrix of data;

fixed The vector of fixed parameters;

iterations The number of iteration used by the numerical routine;

likelihood The configuration of the composite likelihood;

logCompLik The value of the log composite-likelihood at the maximum;

lonlat The type of coordinates;

message Extra message passed from the numerical routines;
model The density associated to the likelihood objects;

param The vector of parameters' estimates;

stderr The vector of standard errors;

sensmat The sensitivity matrix;

varcov The matrix of the variance-covariance of the estimates;

varimat The variability matrix;

type The type of the likelihood objects.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan; Moreno Bevilacqua, <moreno.bevilacqua@unive.it>.

References

Maximum Restricted Likelihood Estimator:

Harville, D. A. (1977) Maximum Likelihood Approaches to Variance Component Estimation and to Related Problems. *Journal of the American Statistical Association*, **72**, 320–338.

Composite-likelihood:

Varin, C. and Vidoni, P. (2005) A Note on Composite Likelihood Inference and Model Selection. *Biometrika*, **92**, 519–528.

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Weighted Composite-likelihood for max-stable random fields:

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See Also

CovarianceFct, WLeastSquare, optim

Examples

```
library (RandomFields)
set.seed(2111)
# Set the coordinates of the points:
x <- runif(100, 0, 20)
y <- runif(100, 0, 20)
###
### Example 1. Maximum composite-likelihood fitting of one
### spatial realisation of a Gaussian random field.
### Composite-likelihood setting: pairwise marginal likelihoods.
###
# Set the model's parameters:
corrmodel <- "stable"
mean <- 0
variance <- 1
nugget <- 0
scale <- 10
power <- 1.5
# Simulation of the Gaussian random field in the specified points:
sim <- GaussRF(x=x, y=y, model=corrmodel, grid=FALSE,</pre>
             param=c(mean, variance, nugget, scale, power))
# Maximum composite-likelihood fitting of the random field:
fit <- FitComposite(x, y, corrmodel, sim)</pre>
# Results:
print(fit)
```

```
###
### Example 2. Maximum composite-likelihood fitting of one
### spatial realisation of a Gaussian random field.
### Composite-likelihood setting: difference likelihoods.
###
# Set the model's parameters:
corrmodel <- "stable"
mean <- 0
variance <- 1
nugget <- 0
scale <- 10
power <- 1.5
# Simulation of the Gaussian random field in the specified points:
sim <- GaussRF(x=x, y=y, model=corrmodel, grid=FALSE,</pre>
            param=c(mean, variance, nugget, scale, power))
# Maximum composite-likelihood fitting of the random field:
fit <- FitComposite(x, y, corrmodel, sim, type='Difference')</pre>
# Results:
print(fit)
###
### Example 3. Maximum likelihood fitting of one
### spatial realisation of a Gaussian random field.
### Likelihood setting: restricted likelihood.
###
# Set the model's parameters:
corrmodel <- "stable"
mean <- 0
variance <- 1
nugget <- 0
scale <- 10
power <- 1.5
# Simulation of the Gaussian random field in the specified points:
sim <- GaussRF(x=x, y=y, model=corrmodel, grid=FALSE,</pre>
            param=c(mean, variance, nugget, scale, power))
# Maximum composite-likelihood fitting of the random field:
fit <- FitComposite(x, y, corrmodel, sim, likelihood='Full',</pre>
                 type='Restricted')
# Results:
print(fit)
```

22 FitGev

FitGev	Maximum-likelihood Fitting of the Generalized Extreme Value Distri- bution
	buton

Description

the function returns the parameters' estimates and the variances of the estimates (if required) of the generalized extreme value distribution for a given dataset of extreme values.

Usage

```
FitGev(data, method='Nelder-Mead', start, varest=FALSE)
```

Arguments

data	A vector of extreme values.
method	The optimization method (see optim for details). 'Nelder-Mead' is the default.
start	A named list with the initial values for the parameters over which the likelihood is to be maximized.
varest	Logical; if TRUE the estimate' variances and the standard errors are returned, instead if FALSE (the default) only the estimate are computed.

Details

If start is omitted the routine is computing the starting values using moment estimators.

Value

The returned object is a list with:

param	The vector of parameters' estimates.
varcov	The matrix of the variance-covariance of the estimates.
stderr	The vector of the standard errors.

Author(s)

```
Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan
```

References

```
Smith, R. L. (1985) Maximum likelihood estimation in a class of non-regular cases. Biometrika, 72, 67–90.
```

de Haan, L. and Ferreira, A. (2006) Extreme Value Theory An Introduction. Springer Verlang, New York.

See Also

```
GevLogLik, optim
```

GevLogLik 23

GevLogLik Log-Likelihood of the Generalized Extreme Value Distribution
--

Description

the function returns the log-likelihood value of the Generalized Extreme Value Distribution for a given set of data and parameters.

Usage

```
GevLogLik (data, numdata, param)
```

Arguments

data A vector of extreme values.

numdata The number of data observations.

param The vector of GEV parameters (location, scale and shape).

Value

The log-likelihood value is returned.

Author(s)

```
Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan
```

References

de Haan, L. and Ferreira, A. (2006) *Extreme Value Theory An Introduction*. Springer Verlang, New York.

|--|--|--|

Description

Subroutine called by the fitting procedures. The procedure initializes the fitting procedure.

Usage

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Arguments

coordx	A numeric $(d \times 2)$ -matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
corrmodel	String; the name of a correlation model.
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
fixed	A named list giving the values of the parameters that will be considered as known values.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
likelihood	String; the configuration of the composite likelihood.
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
model	String; the density associated to the likelihood objects. Gaussian is the default.
parscale	A numeric vector of scaling factor to improve the maximizing procedure, see optim.
paramrange	A numeric vector of parameters ranges, see optim.
replicates	Logical; if FALSE (the default) one spatial random field is considered, instead if TRUE the data are considered as iid replicates of a field.
start	A named list with the initial values of the parameters that are used by the numerical routines in maximization procedure. NULL is the default (see Details).
type	String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods.
vartype	String; the type of estimation method for computing the estimate variances, see the Section Details .
weighted	Logical; if TRUE the likelihood objects are weighted, see FitComposite.

Author(s)

 $Simone\ Padoan, < \verb|simone.padoan@epfl.ch>|, \verb|http://people.epfl.ch/simone.padoan|.\\$

See Also

FitComposite

|--|

Description

Subroutine called by FitComposite. The procedure estimates the model parameters by maximisation of the log-likelihood.

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Usage

```
Likelihood(corrmodel, data, fixed, grid, lower, model, namescorr, namesnuis, namesparam, numcoord, numdata, numpairs, optimizer, param, varest, type, upper)
```

Arguments

corrmodel	Numeric; the id of the correlation model.
data	A numeric vector or a ($n \times d$)-matrix or ($d \times d \times n$)-matrix of observations.
fixed	A numeric vector of parameters that will be considered as known values.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
lower	A numeric vector with the lower bounds of the parameters' ranges.
model	Numeric; the id value of the density associated to the likelihood objects.
namescorr	String; the names of the correlation parameters.
namesnuis	String; the names of the nuisance parameters.
namesparam	String; the names of the parameters to be maximised.
numcoord	Numeric; the number of coordinates.
numdata	Numeric; the number of data replications in time.
numpairs	Numeric; the number of pairwise distances.
optimizer	String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.
param	A numeric vector of parameters' values.
varest	Logical; if ${\tt TRUE}$ the estimate' variances and standard errors are returned. ${\tt FALSE}$ is the default.
type	String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods.
upper	A numeric vector with the upper bounds of the parameters' ranges.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

26 MomEst

LogNormDen	Computes the multivariate log-normal density	

Description

Subroutine called by the Likelihood procedure. The procedure compute the multivariate log-normal density for a given set of data and parameters.

Usage

```
LogNormDen(stdata, detvarcov, ivarcov, numcoord, type)
```

Arguments

stdata A numeric vector $(d \times 1)$ of data.

detvarcov Numeric; the determinant of the variance-covariance matrix. ivarcov The inverse of the variance-covariance matrix $(d \times d)$.

numcoord The number of point's coordinates.

type The numeric id denoting the type of likelihood.

Author(s)

```
Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.
```

See Also

FitComposite

MomEst	Moment Estimator of the Extreme Value Distribution's parameters

Description

Using the moment estimator, the function returns the parameter estimates of the generalized extreme value distribution for a given dataset of extreme values.

Usage

```
MomEst(data, n)
```

Arguments

data A vector of extreme values.

n The number of observations.

SetRangeParam 27

Value

The returned object is a list with:

location The location estimate.

scale The scale estimate.

shape The shape estimate.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan

References

de Haan, L. and Ferreira, A. (2006) Extreme Value Theory An Introduction. Springer Verlang, New York.

See Also

GevLogLik, FitGev

SetRangeParam

Identifies the Parameters' Range

Description

Subroutine called by InitParam and the fitting procedures. The procedure returns the range of the parameters for a given vector of parameters.

Usage

```
SetRangeParam(namesparam, numparam)
```

Arguments

namesparam String; the names of the parameters.

numparam Numeric; the numer of parameters.

Author(s)

```
Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.
```

See Also

```
FitComposite
```

28 WLeastSquare

WLeastSquare	Weighted Least Square Estimation of Random Fields	
WLeastSquare	weightea Least Square Estimation of Random Fields	

Description

the function returns the parameters' estimates and the estimates' variances of a random field obtained by the weighted least squares estimator.

Usage

Arguments

coordx	A numeric $(d \times 2)$ -matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.	
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.	
corrmodel	String; the name of a correlation model, for the description (see ${\tt FitComposite}$).	
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations (see FitComposite).	
fixed	A named list giving the values of the parameters that will be considered as known values. The listed parameters for a given correlation function will be not estimated, i.e. if list(nugget=0) the nugget effect is ignored.	
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.	
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.	
maxdist	A numeric value denoting the maximum distance, see the Section Details .	
model	String; the type of random field. Gaussian is the default, see FitComposite for the different types.	
optimizer	String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.	
numbins	A numeric value denoting the numbers of bins, see the Section Details	
replicates	Logical; if FALSE (the default) one spatial random field is considered, instead if TRUE the data are considered as iid replicates of a field.	
start	A named list with the initial values of the parameters that are used by the numerical routines in maximization procedure. NULL is the default (see FitComposite).	
weighted	Logical; if TRUE then the weighted least square estimator is considered. If FALSE (the default) then the classic least square is used.	

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Details

The numbins parameter indicates the number of adjacent intervals to consider in order to grouped distances with which to compute the (weighted) lest squares.

The maxdist parameter indicates the maximum distance below which the shorter distances will be considered in the calculation of the (weighted) least squares.

Value

Returns an object of class WLS. An object of class WLS is a list containing at most the following components:

bins Adjacent intervals of grouped distances;

coord The vector of coordinates;

convergence A string that denotes if convergence is reached;

corrmodel The correlation model;

data The vector or matrix of data;
fixed The vector of fixed parameters;

iterations The number of iteration used by the numerical routine;
message Extra message passed from the numerical routines;

param The vector of parameters' estimates;

variogram The empirical variogram.

Author(s)

```
Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan; Moreno Bevilacqua, <moreno.bevilacqua@unive.it>.
```

References

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Gaetan, C. and Guyon, X. (2010) Spatial Statistics and Modelling. Spring Verlang, New York.

See Also

```
FitComposite, optim
```

Examples

30 WIsInit

```
### Example 1. Least square fitting of one
### spatial realisation of a Gaussian random field.
### Non weighted version (all weights equals to 1)
# Set the model's parameters:
corrmodel <- "stable"
mean <- 0
variance <- 1
nugget <- 0
scale <- 10
power <- 1.5
# Simulation of the Gaussian random field in the specified points:
sim <- GaussRF(x=x, y=y, model=corrmodel, grid=FALSE,</pre>
            param=c(mean, variance, nugget, scale, power))
# Least square fitting of the random field:
fit <- WLeastSquare(x, y, corrmodel, sim)</pre>
# Results:
print(fit)
###
### Example 1. Weighted least square fitting of one
### spatial realisation of a Gaussian random field.
### Weighted version.
###
# Set the model's parameters:
corrmodel <- "stable"
mean <- 0
variance <- 1
nugget <- 0
scale <- 10
power <- 1.5
# Simulation of the Gaussian random field in the specified points:
sim <- GaussRF(x=x, y=y, model=corrmodel, grid=FALSE,</pre>
            param=c(mean, variance, nugget, scale, power))
# Least square fitting of the random field:
fit <- WLeastSquare(x, y, corrmodel, sim, weighted=TRUE)</pre>
# Results:
print(fit)
```

WlsInit 31

Description

Subroutine called by FitComposite. The function returns opportune starting values for the composite-likelihood fitting procedure based on weighted least squares.

Usage

```
WlsInit(coordx, coordy, corrmodel, data, fixed, grid, likelihood, lonlat, model, parscale, paramrange, replicates, start, type, vartype, weighted)
```

Arguments

coordx	A numeric ($d \times 2$)-matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
corrmodel	String; the name of a correlation model, for the description.
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
fixed	A named list giving the values of the parameters that will be considered as known values.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
likelihood	String; the configuration of the composite likelihood.
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
model	String; the name of the model. Here the default is NULL.
parscale	A numeric vector with scaling values for improving the maximisation routine.
paramrange	A numeric vector with the range of the parameter space.
replicates	Logical; if FALSE (the default) one spatial random field is considered, instead if TRUE the data are considered as iid replicates of a field.
start	A numeric vector with starting values.
type	String; the type of estimation method.
vartype	String; the type of estimation method for computing the estimate variances, see the Section Details .
weighted	Logical; if TRUE the likelihood objects are weighted, see FitComposite.

Author(s)

Simone Padoan, <simone.padoan@epfl.ch>, http://people.epfl.ch/simone.padoan.

See Also

FitComposite, WLeastSquare.

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