data.Normalization(clusterSim)

Types of variable normalization formulas

1	Selection of objects and variables	data matrix $[x_{ij}]$		
2	Variable scale level	ratio	ratio	interval
	Selection of variable normalization formula	n6 – quotient transformation (x/sd) n7 – quotient transformation (x/range) n8 – quotient transformation (x/max) n9 – quotient transformation (x/mean) n10 – quotient transformation (x/sum) n11 – quotient transformation x/sqrt(SSQ)	n1 – standardization n2 – Weber standardization n3 – unitization n4 – unitization with zero minimum n5 – normalization in range [–1, 1]	n1 – standardization n2 – Weber standardization n3 – unitization n4 – unitization with zero minimum n5 – normalization in range [–1 ,1]
	Transformed variable scale level	ratio	interval	interval

(n1)
$$z_{ij} = s_j^{-1} x_{ij} - \bar{x}_j s_j^{-1},$$

(n2)
$$z_{ij} = (x_{ij} - Me_j)/1{,}4826 \cdot MAD_j,$$

(n3)
$$z_{ij} = r_j^{-1} x_{ij} - \bar{x}_j r_j^{-1},$$

(n4)
$$z_{ij} = \left[x_{ij} - \min_i\{x_{ij}\} \right] / r_j$$

(n5)
$$z_{ij} = (x_{ij} - \bar{x}_j)/\max_i \left| x_{ij} - \bar{x}_j \right|$$

(n6)
$$x_{ij}/s_j$$

(n7)
$$x_{ij}/r_j$$

n(8)
$$x_{ij}/\max_i\{x_{ij}\}$$

(n9)
$$x_{ij}/\bar{x}_j$$

(n10)
$$x_{ij}/\sum_{i=1}^{n} x_{ij}$$

(n11)
$$x_{ij}/\sqrt{\sum_{i=1}^{n} x_{ij}^2}$$

where: $x_{ij}(z_{ij})$ – i-th observation on j-th variable (i-th normalized observation on j-th variable),

$\bar{x}_j, s_j$ – mean and standard deviation for j-th variable,

Me_j, MAD_j – median and median absolute deviation for j-th variable,

$r_j = \max_i\{x_{ij}\} - \min_i\{x_{ij}\}$.

References

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