Ichino and Yaguchi dissimilarity measure for variable

$$\phi(A_j, B_j) = |A_j \oplus B_j| - |A_j \otimes B_j| + \gamma (2 \cdot |A_j \otimes B_j| - |A_j| - |B_j|),$$

where: $\phi(A_i, B_i)$ – dissimilarity measure of symbolic variables,

 A_i, B_i – symbolic variables of any type,

- ⊕ Cartesian join,
- ⊗ Cartesian meet,

| - means the length of an interval for continuous data or the number of elements of an set of values,

 γ – parameter <0, $\frac{1}{2}$ >.

Ichino and Yaguchi measure for objects (U_2)

$$d_q(a_1,b_1) = \left(\sqrt[q]{\sum_{j=1}^p \varphi(A_j,B_j)^q}\right),$$

where: $d_q(a_1,b_1)$ - Ichino and Yaguchi measure (sometimes called extended Minkowski metric, see E. Diday [2000]),

q – integer number greater or equal 1,

 $a_1 = (A_1, A_2, \dots, A_n)$, $b_1 = (B_1, B_2, \dots, B_n)$ - two symbolic objects containing p symbolic variables,

 $\varphi(A_i, B_i)$ – Ichino and Yaguchi dissimilarity measure for variables (6).

$$\begin{aligned} & \text{Hausdorff distance measure (H)} \\ & \max \left\{ \max_{\alpha \in [\underline{A}, \overline{A}]} \left\{ \min_{\beta \in [\underline{B}, \overline{B}]} d(\alpha, \beta) \right\}, \max_{\beta \in [\underline{B}, \overline{B}]} \left\{ \min_{\alpha \in [\underline{A}, \overline{A}]} d(\alpha, \beta) \right\} \right\}, \end{aligned}$$

where: $H(a_1,b_1)$ – Hausdorff distance,

 $a_1 = (A_1, A_2, ..., A_p)$, $b_1 = (B_1, B_2, ..., B_p)$ – two symbolic objects containing psymbolic interval-valued variables. Each variable A_i is an interval in a form $[A_i, \overline{A_i}]$, d(...) – Euclidean distance.

References

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