G2 internal cluster quality index - Baker & Hubert adaptation of Goodman & Kruskal's Gamma statistics

$$G2(u) = \frac{s(+) - s(-)}{s(+) + s(-)},$$

$$G2(u) \in [-1, 1],$$

where: s(+) – number of concordant comparisons (within-cluster dissimilarity is strictly less than a between-cluster dissimilarity),

s(-) – number of discordant comparisons (within-cluster dissimilarity is strictly greater than a between-cluster dissimilarity),

u – number of clusters (u = 2, ..., n-1),

n – number of objects.

The value of u, which maximizes G2(u), is regarded as specifying the number of clusters.

References

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