# R Package ecolMod: figures and examples from Soetaert and Herman (2009)

#### Karline Soetaert

Royal Netherlands Institute of Sea Research (NIOZ) Yerseke, The Netherlands

#### Abstract

This document contains some examples of the demos from package **ecolMod**. This package has, in its demo's all the figures of the book: Soetaert K. and P.M.J. Herman (2009). A Practical Guide to Ecological Modelling. Using R as a Simulation Platform. Springer, 372 pp.

Keywords: ecological Modelling, graphics, figures, examples, R.

This vignette is a Sweave (Leisch 2002) application of parts of the demos from package **ecolMod** (Soetaert and Herman 2009), accompanying the book:

Soetaert K. and P.M.J. Herman (2009). A Practical Guide to Ecological Modelling. Using R as a Simulation Platform. Springer, 372 pp.

All figures from this book (>100) were created in  $\mathbf{R}$ . While making these figures, I was not concerned with *how* they are programmed, but rather with the result. Therefore, it is likely that there exist better and more elegant ways to create them.

Some figures make use of packages

- shape (Soetaert 2009b), to draw graphical shapes.
- diagram (Soetaert 2009a), to draw simple graphs, networks, diagrams

These two packages were written in support of the book.

For each chapter of the book, the figures can be displayed by typing

```
demo(chap1)
demo(chap2)
...
demo(chap11)
```

Also, the examples in the book can be found in the examples subdirectory of the package. In this vignette, one (or two) figures for each chapter are created.

# 1. Chapter 1. Introduction

This figure represents the modelling steps and ingredients.

The figure makes use of package **diagram**. After opening a plot, and positioning of the elements (elpos), first the arrows connecting them are drawn (segmentarrow, straightarrow) and the texts written in rounded or diamond-shaped boxes textround, textdiamond, or as plain text.

```
> par(mar = c(0, 0, 0, 0))
> openplotmat()
> elpos <- coordinates (c(1, 1, 1, 1, 1, 1, 1, 1), mx = -0.1)
> segmentarrow(elpos[7, ], elpos[2, ], arr.pos = 0.15, dd = 0.3, arr.side = 3)
> segmentarrow(elpos[7, ], elpos[3, ], arr.pos = 0.15, dd = 0.3, arr.side = 3)
> segmentarrow(elpos[7, ], elpos[4, ], arr.pos = 0.15, dd = 0.3, arr.side = 3)
> pin <- par ("pin")</pre>
> xx <- 0.2
     <- xx*pin[1]/pin[2]*0.15
> yy
> sx
       \leftarrow rep(xx, 8)
> sx[7] < -0.05
> sy
        \leftarrow rep(yy, 8)
> sy[6] <- yy*1.5
> sy[7] <- sx[7]*pin[1]/pin[2]
> for (i in 1:7)
    straightarrow (from = elpos[i, ], to = elpos[i+1, ], lwd = 2, arr.pos = 0.5)
> lab <- c("Problem", "Conceptual model", "Mathematical model", "Parameterisation",
           "Mathematical solution", "", "OK?", "Prediction, Analysis")
> for (i in c(1:6, 8))
    textround(elpos[i, ], sx[i], sy[i], lab = lab[i])
> textround(elpos[6, ], xx, yy*2,
    lab = c("Calibration, sensitivity", "Verification, validation"))
> textdiamond(elpos[7, ], sx[7], sy[7],
    lab = lab[7])
> textplain(c(0.7, elpos[2, 2]), yy*2,
    lab = c("main components", "relationships"), font = 3, adj = <math>c(0, 0.5))
> textplain(c(0.7, elpos[3, 2]), yy,
    "general theory", adj = c(0, 0.5), font = 3)
> textplain(c(0.7, elpos[4, 2]), yy*2,
    lab = c("literature", "measurements"), font = 3, adj = <math>c(0, 0.5))
> textplain(c(0.7, elpos[6, 2]), yy*2,
    lab = c("field data", "lab measurements"), font = 3, adj = <math>c(0, 0.5))
```

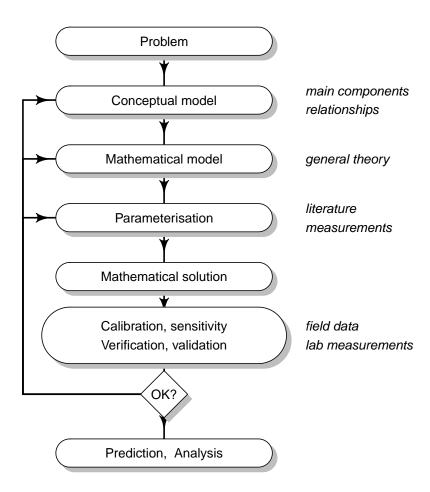


Figure 1: Figure 1.7 from chapter 1

## 2. Chapter 2. Model formulation

This figure makes use of package diagram. It depicts two types of chemical reactions.

```
> par(mfrow = c(1, 2))
> par(mar = c(3, 3, 3, 3))
> # reversible reaction
> openplotmat()
> elpos <- coordinates (c(3, 1))
> treearrow(from = elpos[1:3, ], to = elpos[4, ], arr.side = 2, path = "H")
> treearrow(from = elpos[4, ], to = elpos[1:3, ], arr.side = 2, path = "H")
> labs <- c("C", "D", "D", "E")
> text(0.55, 0.4, expression(k[1]), font = 3, adj = 0, cex = 0.8)
> text(0.55, 0.6, expression(k[2]), font = 3, adj = 0, cex = 0.8)
> for ( i in 1:4)
    textrect (elpos[i, ], 0.1, 0.1, lab = labs[i], cex = 1.5)
> box(col = "grey")
> title("reversible reaction")
> writelabel("A", line = 0, at = -0.05)
> # enzymatic reaction
> #
> openplotmat()
> elpos <- coordinates (c(3, 2, 3))
> elpos <- elpos [-c(5, 6), ]
> elpos[4, 1] <- 0.3333
> elpos[6, 1] <- 0.7
> treearrow(from = elpos[1:2, ], to = elpos[4, ], arr.side = 2, path = "H")
> treearrow(to = elpos[1:2, ], from = elpos[4, ], arr.side = 2, path = "H")
> treearrow(from = elpos[3:4, ], to = elpos[5:6, ], arr.side = 2, path = "H")
> labs <- c("E", "D", "F", "I", "E", "G")
> for ( i in 1:6)
    textrect (elpos[i, ], 0.075, 0.07, lab = labs[i], cex = 1.5)
> text(0.35, 0.6, expression(k[1]), font = 3, adj = 0, cex = 0.8)
> text(0.52, 0.7, expression(k[2]), font = 3, adj = 0, cex = 0.8)
> text(0.72, 0.3, expression(k[3]), font = 3, adj = 0, cex = 0.8)
> box(col = "grey")
> title("enzymatic reaction")
> writelabel("B", line = 0, at = -0.05)
```

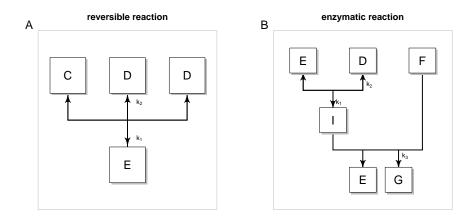


Figure 2: Figure 2.6 from chapter 2

## 3. chapter 3. Spatial components and transport

This figure makes use of package **shape** to draw a filled cylinder. We use it to derive the general transport equation.

```
> par(mfrow = c(1, 1))
> par(mar = c(1, 1, 1, 1))
> plot(0, type = "n", xlim = c(-1, 1), ylim = c(-0.6, 0.5), axes = FALSE,
       xlab = "", ylab = "")
> col <- grey(seq(0.2, 1, length.out = 100))</pre>
> col <- c(col, rev(col))
> cex <- 1.75
> #
> filledcylinder (rx = 0.15, ry = 0.4, len = 1, col = col, lcol = "black",
    1wd = 1, 1colint = grey(0.25), 1wdint = 1, 1tyint = 3,
    topcol = grey(0.5), delt = 1.15)
> #
> segments(-1, 0, -0.5, 0)
> segments(0.5, 0, 1, 0)
> #
> Arrows(-0.8, 0, -0.5, 0, arr.type = "triangle",
    arr.length = 0.5, lwd = 5, arr.adj = 1)
> Arrows(0.5, 0, 0.8, 0, arr.type = "triangle",
    arr.length = 0.5, lwd = 3, arr.adj = 1)
> #
> text(0.0, 0.5, expression(Delta~V), cex = cex*0.9)
> text(-0.5, 0.225, expression(A[x]), cex = cex)
> text(0.5, 0.225, expression(A[x+Delta~x]), cex = cex)
> text(-0.75, 0.065, expression(J[x]), cex = cex)
> text(0.85, 0.065, expression(J[x+Delta~x]), cex = cex)
> #
> segments(-0.5, 0, -0.5, -0.5, 1ty = 3, col = grey(0.25))
> segments(0.5, 0, 0.5, -0.5, lty = 3, col = grey(0.25))
> #
> text(-0.5, -0.55, expression(x), cex = cex)
> text(0.5, -0.55, expression(x+Delta~x), cex = cex)
```

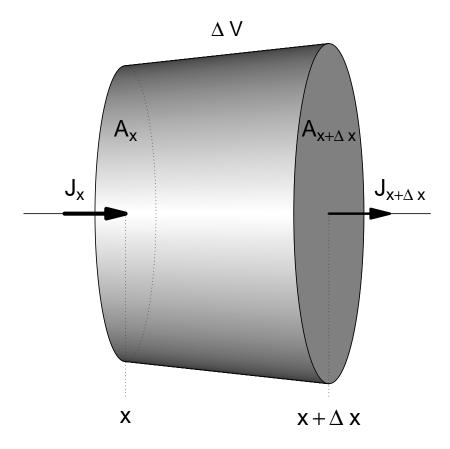


Figure 3: Figure 3.5 from chapter 3  $\,$ 

# 4. chapter 4. Parameterisation

This figure represents a (fictuous) model cost landscape.

The figure has higher resolution in the book. It makes use of R's persp function, which has been draped with a grey colorscale (drapecol). The latter function is included in package shape.

```
> par(mfrow = c(1, 1))
> par(mar = c(1, 1, 1, 1))
> col <- grey(seq(0, 0.9, length.out = 100))
> #
> gg <- outer(seq(3, 9.5, 0.1), seq(-4.8, -1, 0.1),
+ FUN = function(x, y) 4*cos(y)+sin(x)-(sin(x)/sqrt(x)*cos(y)*y^2)^2)
> #
> persp(gg, col = drapecol(gg, col), border = NA, theta = 30, phi = 30,
+ axes = TRUE, box = TRUE, lty = 2, xlab = "parameter 1",
+ ylab = "parameter 2", zlab = "cost", ticktype = "simple", cex = 1.5)
> #
> text(0.15, 0.22, "2", cex = 2)
> text(-0.10, 0.27, "1", cex = 2)
> text(-0.15, -0.25, "global minimum")
> text(0.1, -0.18, "local minimum")
```

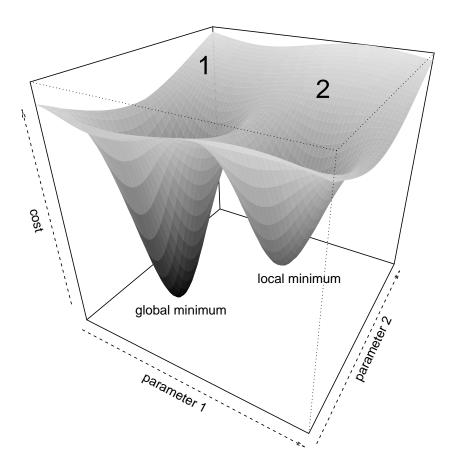


Figure 4: Figure 4.4 from chapter 4

# 5. chapter 5. Model solution - analytical methods

The analytical solution of a diffusion-reaction equation in 1-D, and using cylindrical coordinates is depicted. It makes use of R s function persp, draped with a red-yellow-blue color scheme. Functions drapecol and femmecol made available in package shape.

```
> Ds <- 1
              # diffusion coefficient
> ini <- 1
              # initial condition
      <- 0.05 # growth rate
> k
> #
> plotplane <- function(time, rmax = 5, ...) {
   xx \leftarrow seq(-rmax, rmax, length = 30)
   yy <- xx
   val \leftarrow outer(xx, yy, FUN = function(x, y)
       ini/(4*pi*Ds*time)*exp(k*time-(x*x+y*y)/(4*Ds*time))
   persp(xx, yy, z = val, theta = 150, box = TRUE, axes = TRUE,
       col = drapecol(val, femmecol(100)), zlab = "Density", border = NA, ...)
+ }
> #
> par(mfrow = c(2, 2), mar = c(3, 3, 3, 3))
> plotplane(0.1, main = "0.1 day")
> plotplane(1 , main = "1 day")
> plotplane(2 , main = "2 days")
> plotplane(5 , main = "5 days")
```

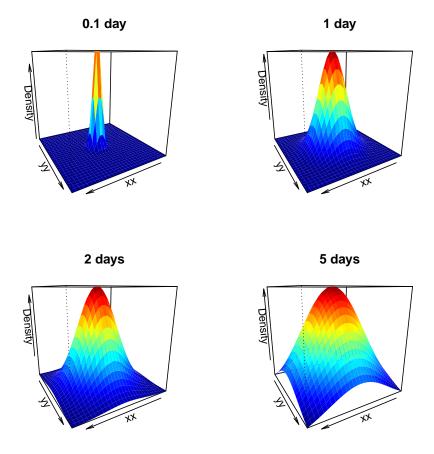


Figure 5: Figure 5.5 from chapter 5

## 6. chapter 6. Model solution numerical methods

Here, a 1-D diffusion-reaction model is implemented, solved using function ode.1D from package **deSolve** (Soetaert, Petzoldt, and Setzer 2009), and the results displayed using R s filled.contour function.

```
> #----#
> # the model equations: #
> #-----#
> model <- function(t, APHIDS, parameters)</pre>
              <- -D*diff(c(0, APHIDS, 0))/deltax
    Flux
    dAPHIDS
              <- -diff(Flux)/delx + APHIDS*r
    list(dAPHIDS )
+ }
> #-----#
> # the model parameters: #
> #----#
         <- 0.3 # m2/day diffusion rate
> r
         <- 0.01 # /day
                          net growth rate
         <- 1
                  # m
                          thickness of boxes
> delx
> numboxes <- 60
> Distance <- seq(from = 0.5, by = delx, length.out = numboxes) # 1 m intervals
         <- c (0.5, rep(1, numboxes-1), 0.5)
> deltax
> #-----#
> # Initial conditions:
> #-----#
             <- rep(0, times = numboxes) # ind/m2 aphid density</pre>
> APHIDS
> APHIDS[30:31] <- 1
> state
              <- c(APHIDS = APHIDS) # initial conditions
> #-----#
> # RUNNING the model: #
> #----#
        <- seq(0, 200, by = 4) # output wanted at these time intervals
> times
         <- ode.1D(state, times, model, parms = 0, nspec = 1)
> DENSITY <- out[, 2:(numboxes +1)]
> #-----#
> # PLOTTING model output: #
> #----#
> par(mfrow = c(1, 1))
> par(oma = c(0, 0, 3, 0)) # set outer margin size (oma)
> filled.contour(x = times, y = Distance, DENSITY, color = topo.colors,
```

# Aphid model

# **Density**

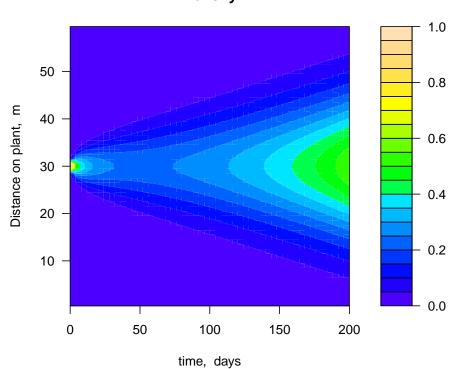


Figure 6: Figure 6.15 from chapter 6

```
+ xlab = "time, days", ylab = "Distance on plant, m",
+ main = "Density")
> mtext(outer = TRUE, side = 3, "Aphid model", cex = 1.5) # margin text
```

## 7. chapter 7. Stability and steady state

The trajectories of a set of differential equations, displaying limit cycles are depicted. The model is solved using function vode from package deSolve (Soetaert et al. 2009). This is the only integrator that can solve this rather difficult set of equations (although even vode complains).

```
par(mfrow = c(1, 2))
eqn <- function (t, state, pars) {
  with (as.list(c(state, pars)),
  dx \leftarrow a*y
               +e*x*(x^2+y^2-1)
              +f*y*(x^2+y^2-1)
  dy <- b*x
  list(c(dx, dy))
  })
}
equation2 <- function(ini, i1 = 5, a = -1, b = 1, e = -1, f = -1,
                       endt = 100, dt = 0.1, ...) {
  times <- seq(0, endt, dt)
  state <- c(x = ini[1], y = ini[2])
        <- as.data.frame(vode(state, times, eqn,</pre>
                          parms = c(a = a, b = b, e = e, f = f))
  lines(out$x, out$y)
  Arrows(out$x[i1], out$y[i1], out$x[i1+1], out$y[i1+1], ...)
}
xlim <- c(-1.5, 1.5)
ylim <- xlim
plot(0, type = "n", xlim = xlim, ylim = ylim, xlab = "", ylab = "",
  axes = FALSE, frame.plot = TRUE)
equation2(c(-0.01, -0.01), i1 = 45)
equation2(c(0.01, 0.01), i1 = 45)
equation2(c(1.1, 1.1), i1 = 5)
equation2(c(-1.1, 1.1), i1 = 5)
equation2(c(-1.1, -1.1), i1 = 5)
equation2(c(1.1, -1.1), i1 = 5)
points(0, 0, pch = 21, cex = 3, bg = "lightgrey", col = "lightgrey")
title("Stable limit cycle")
writelabel("A")
xlim \leftarrow c(-1.5, 1.5)
ylim <- xlim
plot(0, type = "n", xlim = xlim, ylim = ylim, xlab = "", ylab = "",
```

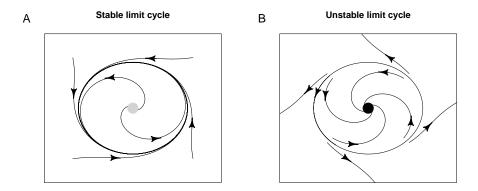


Figure 7: Figure 7.10 from chapter 7

## 8. chapter 8. Multiple time scales and equilibrium processes

This figures depicts the derivation of the Monod function. It makes use of package diagram.

```
> par(mfrow = c(1, 1))
> par(mar = c(1, 1, 1, 1))
> openplotmat()
> rect(0.075, 0.05, 0.575, 0.45, angle = 45, density = 15,
    col = "darkgrey", border = NA)
> elpos <- coordinates (c(4, 2, 4), hor = FALSE)
> elpos <- elpos [-c(3, 4, 7, 10), ]
> treearrow(from = elpos[1:2, ], to = elpos[3, ], lty = 1, path = "V")
> treearrow(from = elpos[3, ], to = elpos[1:2, ], lty = 1, path = "V")
> treearrow(from = elpos[3:4, ], to = elpos[5:6, ], lty = 1, path = "V")
> names <- c("A", "E", "EA", "B", "S", "E")
> for ( i in 1:6) textrect (elpos[i, ], 0.06, 0.06, lab = names[i], cex = 1.5)
> text(0.4, 0.28, expression(k^{"+"}))
> text(0.3, 0.15, expression(k^{-1}))
> text(0.3, 0.4, expression(k^{-1}))
> text(0.735, 0.4, "r")
> text(0.735, 0.65, "r")
> box(col = "grey")
> par(new = TRUE)
> par(fig = c(0, 0.4, 0.6, 1.0))
> par(mar = c(1, 1, 1, 1))
> openplotmat()
> elpos <- coordinates (c(2, 1), hor = FALSE)
> treearrow(from = elpos[1:2, ], to = elpos[3, ], lty = 1, path = "V")
> names <- c("A", "B", "S")
> for ( i in 1:3)
    textrect (elpos[i, ], 0.09, 0.09, lab = names[i], cex = 1.5)
> text(0.55, 0.55, expression(r[f]))
> box(col = "grey")
> par(fig = c(0, 1, 0.0, 1))
>
```

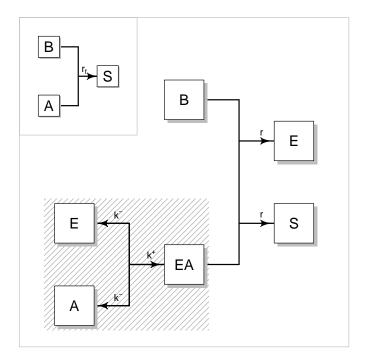


Figure 8: Figure 8.3 from chapter 8

## 9. chapter 9. Discrete time models

A rather spectacular play with a discrete-time parasitoid model. The figure in the book has more detail. Except for function writelabel (from package shape), this figure is made only with R's core functions.

```
> par (mfrow = c(2, 2), mar = c(5.1, 4.1, 4.1, 2.1))
> rH <- 2.82  # rate of increase
> tS <- 100  # searching time
> tH <- 1 # handling time
> A <- tS/tH # attack rate
> ks <- 30
               # 1/tH*a
> Parasite <- function(P_H, ks) {</pre>
+ P <- P_H[1]
+ H <- P_H[2]
+ f \leftarrow A*P/(ks+H)
+ return(c(H*(1-exp(-f))),
            H * exp(rH*(1-H)-f))
+ }
> out <- matrix(nrow = 50, ncol = 2)
> plottraject <- function(ks) {</pre>
    P_H \leftarrow c(0.5, 0.5)
    for (i in 1:100)
      P_H <- Parasite(P_H, ks)</pre>
   for (i in 1:50) {
     P_H <- Parasite(P_H, ks)</pre>
      out[i, ] <- P_H
    }
+ plot (out[, 1], type = "1", ylim = range(out), lwd = 2, xlab = "t",
       ylab = "Population", main = paste("ks = ", ks))
+ lines(out[, 2], lty = 2)
> #plottraject(35)
>
> plottraject(25)
> writelabel("A")
> plottraject(20)
> writelabel("B")
> legend("topright", c("Parasitoid", "Host"), lty = c(1, 2), lwd = c(2, 1))
> ksSeq <- seq(15, 35, 0.2) # sequence of a-values
> plot(0, 0, xlim = range(ksSeq), ylim = c(0., 2), xlab = "ks",
    ylab = "Nt", main = "Bifurcation diagram")
> for ( ks in ksSeq) {
  P_H \leftarrow c(0.5, 0.5)
   for (i in 1:100)
```

```
P_H <- Parasite(P_H, ks) # spinup steps
  for (i in 1:200) {
    P_H <- Parasite(P_H, ks)
     points(ks, P_H[2], pch = ".", cex = 1.5)
   }
+ }
> writelabel("C")
> # domain of attraction
> ks <- 23.09
> dz <- 0.01 # 0.0025
> xlim <- c(0.001, 0.5)
> ylim <- c(0.001, 0.5)
> Initial <- expand.grid(P = seq(xlim[1], xlim[2], dz),</pre>
                        H = seq(ylim[1], ylim[2], dz))
> plot(0, 0, xlim = xlim, ylim = ylim, ylab = "Parasitoid initial",
   xlab = "Host initial", type = "n", main = "Domain of attraction")
> PP <- vector(length = 100)
> for ( ii in 1:nrow(Initial)) {
   ini <- Initial[ii, ]</pre>
+ P_H <- unlist(ini)
  for (i in 1:100)
    P_H <- Parasite (P_H, ks)
+ for (i in 1:20) {
    P_H <- Parasite(P_H, ks)
    PP[i] \leftarrow P_H[1]
  Freq <- length(unique(trunc(PP*10)))</pre>
+ ifelse (Freq == 4, col <- "black", col <- "white")
   rect(ini$P-dz/2, ini$H-dz/2, ini$P+dz/2, ini$H+dz/2,
     col = col, border = col)
+
+ }
> writelabel("D")
```

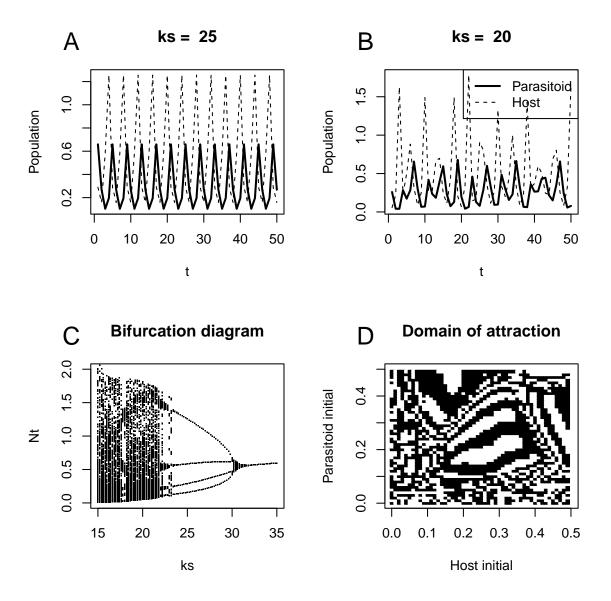


Figure 9: Figure 9.5 from chapter 9

# 10. chapter 9. Discrete time models, b

As there are no nice figures in chapter 10, I depict two figures from chapter 9.

This figure represents the US population transition matrix. First the transition matrix is created, and printed to the screen:

```
> # Fecundity and Survival for each generation
> NumClass <- 10
> Fecundity <- c(0,
                          0.00102, 0.08515, 0.30574, 0.40002,
                 0.28061, 0.1526 , 0.0642 , 0.01483, 0.00089)
> Survival <-c(0.9967, 0.99837, 0.9978, 0.99672, 0.99607,
                 0.99472, 0.99240, 0.98867, 0.98274, NA) # survival from i to i+1
> # Population matrix M
                   <- matrix(data = 0, nrow = NumClass, ncol = NumClass)
> DiffMatrix
> DiffMatrix[1, ] <- Fecundity
> for (i in 1:(NumClass-1)) DiffMatrix[i+1, i] <- Survival[i]</pre>
> DiffMatrix
                                           # print the matrix to screen
                [,2]
        [,1]
                        [,3]
                                [,4]
                                        [,5]
                                                [,6]
                                                       [,7]
                                                               [,8]
                                                                       [,9]
                                                                              [,10]
 [1,] 0.0000 0.00102 0.08515 0.30574 0.40002 0.28061 0.1526 0.06420 0.01483 0.00089
 [2,] 0.9967 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000
 [3,] 0.0000 0.99837 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000
 [4,] 0.0000 0.00000 0.99780 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000
 [5,] 0.0000 0.00000 0.00000 0.99672 0.00000 0.00000 0.00000 0.00000 0.00000
 [6,] 0.0000 0.00000 0.00000 0.00000 0.99607 0.00000 0.00000 0.00000 0.00000
 [7,] 0.0000 0.00000 0.00000 0.00000 0.00000 0.99472 0.0000 0.00000 0.00000 0.00000
 [8,] 0.0000 0.00000 0.00000 0.00000 0.00000 0.00000 0.9924 0.00000 0.00000 0.00000
 [9,] 0.0000 0.00000 0.00000 0.00000 0.00000 0.00000 0.0000 0.98867 0.00000 0.00000
[10,] 0.0000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.98274 0.00000
Plotting this matrix is relatively simple, using diagrams function plotmat:
> par(mfrow = c(1, 1))
         "25-30yr", "30-35yr", "35-40yr", "40-45yr", "45-50yr")
```

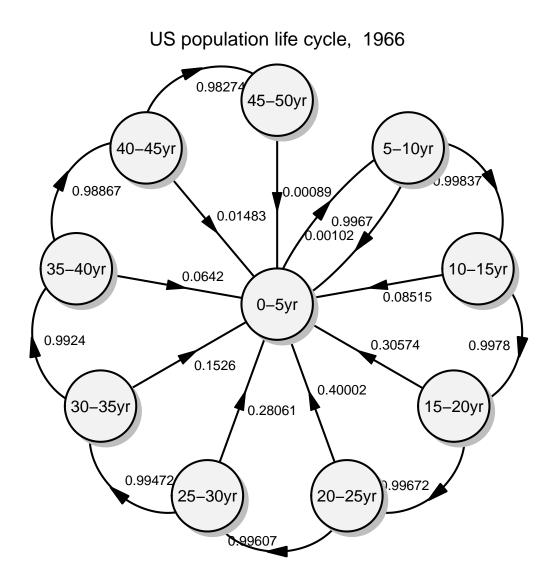


Figure 10: Figure 9.9 from chapter 9

# 11. chapter 11. Testing and validating the model

In this figure, a BOD (Biochemical Oxygen Demand) model is solved numerically, compared with the analytical solution, improved, and model sensitivity assessed.

```
> par(oma = c(0, 0, 2, 0))
> par(mar = c(5.1, 4.1, 4.1, 2.1))
> par(mfrow = c(2, 2))
          = 0.1
> k
                              # /day
                                         - reaeration
> 02sat
          = 300
                             # mmol/m3 - saturated oxygen concentration
          = 0.05
                             # /day
> r
                                         - BOD decay rate
                            # mmol/m3 - Initial oxygen concentration
> 02_0
          = 250
> BOD_0
          = 500
                            # mmol/m3 - Initial BOD concentration
> ks
                              # mmol/m3 - half-saturation concentration
> # numerical model
> numBOD <- function (time, state, pars) {</pre>
+ with (as.list(state),
     d02 < -r*B0D*02/(02+ks)+k*(02sat-02)
     dBOD < -r*BOD*O2/(O2+ks)
     return(list(c(d02, dB0D)))
   } )
+ }
> # analytical solution for 02
> analytical <- function(x, k = 0.1, r = 0.05, 02sat = 300)
+ BOD_0*r*(exp(-k*x)-exp(-r*x)) / (k-r)+02_0*exp(-k*x)+02sat*(1-exp(-k*x))
> # A comparison numerical / analytical model
> # numerical solution plotted as points
> times <- 0:100
> state <- c(02 = 02_0, BOD = BOD_0)
      <- as.data.frame(ode(state, times, numBOD, 0))</pre>
> plot(out$time, out$02, xlab = "time", ylab = "mmol 02/m3",
   lwd = 2, main = "Correctness of solution")
> # analytical solution - added as a curve
> curve(analytical(x, k), lty = 1, lwd = 1, add = TRUE)
> legend("bottomright", c("analytic", "numerical"),
   1wd = c(1, 2), 1ty = c(1, NA), pch = c(NA, 1))
> writelabel("A")
> # B: internal logic
> # wrong use of model : too low reaeration -> negative concentration
> k
        <- 0.01
> times <- 0:200
> state <- c(02 = 02_0, BOD = BOD_0)
> out <- as.data.frame(ode(state, times, numBOD, 0))</pre>
> plot(out$time, out$02, xlab = "time", ylab = "mmol 02/m3",
   main = "Internal logic", type = "1", 1ty = 2)
> abline(h = 0, lty = 3)
```

```
<- 1
> ks
> state <- c(02 = 02_0, BOD = BOD_0)
> out2 <- as.data.frame(ode(state, times, numBOD, 0))</pre>
> lines(out2$time, out2$02, lwd = 2)
> legend("bottomright", c("no 02 limitation", "02 limitation"),
    1wd = c(1, 2), 1ty = c(2, 1)
> writelabel("B")
> # C: global sensitivity
> k
         <- 0.1
        \leftarrow seq(0.0, 0.2, by = 0.002)
> rseq
        <- rseq[rseq != k] # cannot calculate analytical solution for this...</pre>
> min02 <- rseq
> for (i in 1:length(rseq))
+ min02[i] <- min(analytical(times, r = rseq[i]))</pre>
> plot(rseq, min02, type = "1", 1wd = 2 , xlab = "r, /day",
    ylab = "minimum 02, mmol/m3", main = "global sensitivity")
> writelabel("C")
> mtext(side = 3, outer = TRUE, line = 0, "BOD-02 model", cex = 1.25, font = 2)
> # D: local sensitivity
> times <- 0:100
> ss
         <- 1.1
          <- k * ss
                           # /day
> kp
                                       - reaeration
> 02satp <- 02sat*ss
                            # mmo1/m3 - saturated oxygen concentration
> rp
          <- r*ss
                             # /day
                                      - BOD decay rate
> ref <- analytical(times)</pre>
> outk <- analytical(times, k = kp)</pre>
> outs <- analytical(times, O2sat = O2satp)</pre>
> outr <- analytical(times, r = rp)</pre>
> outm <- mean(ref)</pre>
       <- cbind(k = (outk-ref)/outm/0.1,
> ss
+ sat = (outs-ref)/outm/0.1, r = (outr-ref)/outm/0.1)
> plot(times, ref, ylim = range(c(ref, outs)), type = "l", lwd = 2, xlab = "time",
    ylab = "mmol 02/m3", main = "local sensitivity")
> lines(times, outs, lwd = 2, lty = 2)
> arrseq <- seq(10, 100, 10)#c(10, 30, 50, 70, 90)
> Arrows(times[arrseq], ref[arrseq], times[arrseq], outs[arrseq],
    arr.len = 0.25, arr.adj = 1)
> legend("topleft", c(expression(0[2]^**" == 300),
    expression(0[2]^{***} == 330), 1 \text{wd} = 2, 1 \text{ty} = c(1, 2))
> writelabel("D")
> par(new = TRUE)
> par(fig = c(0.7, 0.99, 0.01, 0.35))
> plot(times, ss[, 2], type = "1", lwd = 2,
     xlab = "", ylab = "", axes = FALSE, frame.plot = TRUE)
> points(times[arrseq], ss[arrseq, 2])
> text(mean(times), diff(range(ss[, 2]))/2, expression(S["i, j"]))
```

```
> #
>
> msqr <- sqrt(colSums(ss*ss)/length(times))
> par(fig = c(0, 1, 0, 1))
>
```

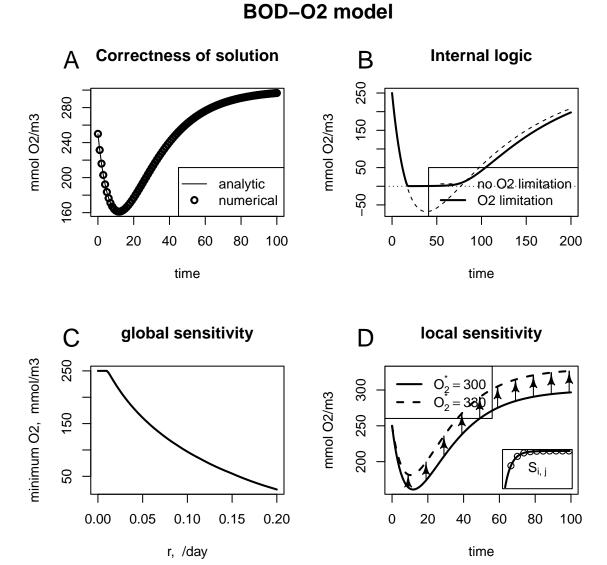


Figure 11: Figure 11.2 from chapter 11

## 12. And finally

More examples can be found in the demo's of package ecolMod.

#### References

- Leisch F (2002). "Sweave: Dynamic Generation of Statistical Reports Using Literate Data Analysis." In W Härdle, B Rönz (eds.), Compstat 2002 Proceedings in Computational Statistics, pp. 575–580. Physica Verlag, Heidelberg. ISBN 3-7908-1517-9, URL http://www.stat.uni-muenchen.de/~leisch/Sweave.
- Soetaert K (2009a). diagram: Functions for visualising simple graphs (networks), plotting flow diagrams. R package version 1.5.
- Soetaert K (2009b). shape: Functions for plotting graphical shapes, colors. R package version 1.2.2.
- Soetaert K, Herman PM (2009). ecolMod: "A practical guide to ecological modelling using R as a simulation platform". R package version 1.3.
- Soetaert K, Petzoldt T, Setzer RW (2009). deSolve: General solvers for initial value problems of ordinary differential equations (ODE), partial differential equations (PDE) and differential algebraic equations (DAE). R package version 1.5.

#### **Affiliation:**

Karline Soetaert

Royal Netherlands Institute of Sea Research (NIOZ)

4401 NT Yerseke, Netherlands E-mail: karline.soetaert@nioz.nl

URL: http://www.nioz.nl