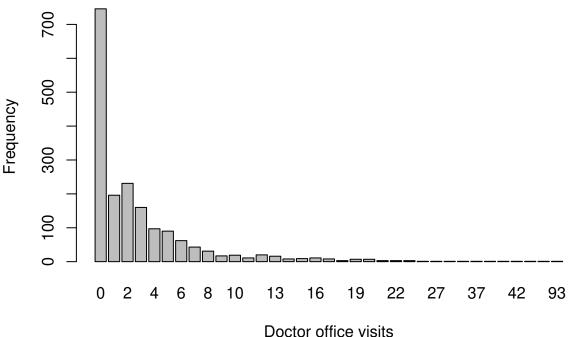
Variable Selection for Zero-inflated and Overdispersed Data with Application to Health Care Demand in Germany

Zhu Wang*

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This document reproduces the data analysis presented in Wang, Ma, and Wang (2015). In an effort to optimize the computing algorithms, the penalized regression can be slightly different. For a description of the theory behind application illustrated here we refer to the original manuscript. Riphahn, Wambach, and Million (2003) utilized a part of the German Socioeconomic Panel (GSOEP) data set to analyze the number of doctor visits. The original data have twelve annual waves from 1984 to 1995 for a representative sample of German households, which provide broad information on the health care utilization, current employment status, and the insurance arrangements under which subjects are protected. The data set contains number of doctor office visits for 1,812 West German men aged 25 to 65 years in the last three months of 1994. As shown in the figure, many doctor office visits are zeros, which can be difficult to fit with a Poisson or negative binomial model. Therefore, zero-inflated negative binomial (ZINB) model is considered.





We include the linear spline variables age30 to age60 and their interaction terms with the health satisfaction health.

^{*}University of Tennessee Health Science Center, zwang145@uthsc.edu

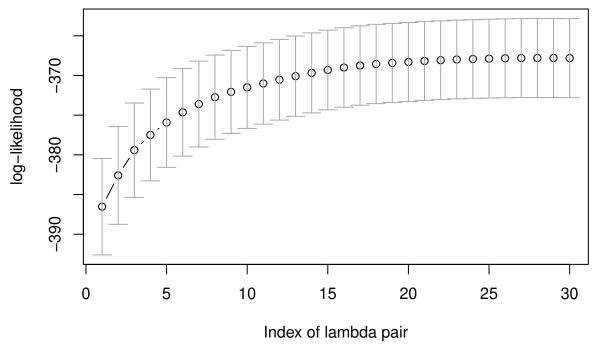
```
dt <- docvisits[,-(2:3)]</pre>
tmp <- model.matrix(~age30*health+age35*health+age40*health+age45*health+age50*health
                    +age55*health+age60*health, data=dt)[,-(1:9)]
dat <- cbind(dt, tmp)</pre>
Full ZINB model with all predictor variables.
require("pscl")
m1 <- zeroinfl(docvisits~.|., data=dat, dist="negbin")</pre>
summary(m1)
##
## Call:
## zeroinfl(formula = docvisits ~ . | ., data = dat, dist = "negbin")
## Pearson residuals:
       Min
                1Q Median
                                3Q
                                       Max
## -1.0733 -0.6596 -0.3944 0.3006
                                    9.9103
## Count model coefficients (negbin with log link):
##
                       Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                       2.412223
                                  0.345625
                                             6.979 2.97e-12 ***
## health
                      -0.163824
                                  0.034487 -4.750 2.03e-06 ***
## handicap
                       0.266916
                                  0.194518
                                             1.372 0.170003
## hdegree
                      -0.002009
                                  0.003292 -0.610 0.541794
## married
                      -0.147205
                                  0.092835 -1.586 0.112815
                                  0.015392 -0.297 0.766150
## schooling
                      -0.004578
## hhincome
                       0.004407
                                  0.016158
                                             0.273 0.785061
## children
                      0.017414
                                  0.088406
                                             0.197 0.843848
## self
                      -0.359935
                                  0.153892 -2.339 0.019341 *
## civil
                      -0.268081
                                  0.160621 -1.669 0.095110
## bluec
                       0.103446
                                 0.086148
                                             1.201 0.229830
## employed
                      -0.093915
                                 0.107228 -0.876 0.381114
## public
                      -0.011404
                                  0.139589 -0.082 0.934889
## addon
                       0.364728
                                  0.232492
                                             1.569 0.116700
## age30TRUE
                       0.094128
                                  0.362776
                                             0.259 0.795277
## age35TRUE
                      -0.254808
                                  0.367280 -0.694 0.487827
                                  0.398899
## age40TRUE
                       0.051516
                                            0.129 0.897242
## age45TRUE
                       0.720536
                                  0.385682
                                             1.868 0.061733
## age50TRUE
                       0.202441
                                  0.341046
                                            0.594 0.552786
## age55TRUE
                      -0.515859
                                  0.307269 -1.679 0.093182 .
                                             1.279 0.200944
## age60TRUE
                       0.400798
                                  0.313401
## `age30TRUE:health` -0.011746
                                  0.052057
                                            -0.226 0.821486
                                  0.054266
## `health:age35TRUE`
                       0.043191
                                             0.796 0.426078
## `health:age40TRUE` -0.016689
                                  0.061665
                                            -0.271 0.786669
## `health:age45TRUE` -0.101236
                                  0.061449
                                            -1.647 0.099458
## `health:age50TRUE` -0.024100
                                  0.053362
                                            -0.452 0.651527
## `health:age55TRUE`
                                             2.573 0.010080 *
                       0.132920
                                  0.051658
## `health:age60TRUE` -0.095085
                                  0.055927
                                            -1.700 0.089100 .
## Log(theta)
                       0.322396
                                  0.090459
                                             3.564 0.000365 ***
##
## Zero-inflation model coefficients (binomial with logit link):
                       Estimate Std. Error z value Pr(>|z|)
                                  0.977635 -2.363
## (Intercept)
                      -2.310575
                                                     0.0181 *
```

```
## health
                       0.227409
                                  0.099828
                                             2.278
                                                      0.0227 *
## handicap
                      -0.334183
                                  0.755147 - 0.443
                                                      0.6581
## hdegree
                      -0.002431
                                  0.015623
                                            -0.156
                                                      0.8763
## married
                                            -1.635
                      -0.403730
                                  0.246993
                                                      0.1021
## schooling
                       0.018518
                                  0.038249
                                             0.484
                                                      0.6283
## hhincome
                      -0.038419
                                  0.044317 -0.867
                                                      0.3860
## children
                       0.505679
                                  0.235329
                                             2.149
                                                      0.0316 *
## self
                      -0.248887
                                  0.477695 -0.521
                                                      0.6024
## civil
                       0.020958
                                  0.383246
                                             0.055
                                                      0.9564
## bluec
                       0.022825
                                  0.222147
                                             0.103
                                                      0.9182
## employed
                      -0.084464
                                  0.297028
                                            -0.284
                                                      0.7761
## public
                      -0.230413
                                  0.338168
                                            -0.681
                                                      0.4956
## addon
                       0.299854
                                  0.524368
                                             0.572
                                                      0.5674
## age30TRUE
                      -1.678718
                                  1.325983
                                            -1.266
                                                      0.2055
                       0.900184
## age35TRUE
                                  1.443436
                                             0.624
                                                      0.5329
## age40TRUE
                      -0.650137
                                  1.442160
                                            -0.451
                                                      0.6521
## age45TRUE
                                  1.200079
                                             2.499
                                                      0.0124 *
                       2.999399
## age50TRUE
                      -2.955447
                                  1.700700
                                            -1.738
                                                      0.0822 .
## age55TRUE
                       0.335945
                                  1.808686
                                             0.186
                                                      0.8526
## age60TRUE
                      -2.336454
                                  2.684804 -0.870
                                                      0.3842
## `age30TRUE:health`
                       0.227952
                                  0.162793
                                             1.400
                                                      0.1614
                                            -0.611
                                                      0.5413
## `health:age35TRUE` -0.110450
                                  0.180807
## `health:age40TRUE`
                       0.115722
                                  0.186281
                                             0.621
                                                      0.5345
## `health:age45TRUE` -0.409613
                                  0.163907 - 2.499
                                                      0.0125 *
## `health:age50TRUE`
                       0.250811
                                  0.220847
                                             1.136
                                                      0.2561
## `health:age55TRUE`
                       0.107929
                                  0.233733
                                             0.462
                                                      0.6443
                                  0.339419
                                                      0.5636
## `health:age60TRUE`
                       0.196009
                                             0.577
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Theta = 1.3804
## Number of iterations in BFGS optimization: 65
## Log-likelihood: -3626 on 57 Df
cat("loglik of zero-inflated model", logLik(m1))
## loglik of zero-inflated model -3625.926
cat("BIC of zero-inflated model", AIC(m1, k=log(dim(dat)[1])))
## BIC of zero-inflated model 7679.476
cat("AIC of zero-inflated model", AIC(m1))
## AIC of zero-inflated model 7365.851
Backward stepwise variable selection with significance level alpha=0.01.
fitbe <- be.zeroinfl(m1, data=dat, dist="negbin", alpha=0.01, trace=FALSE)
summary(fitbe)
##
## Call:
## zeroinfl(formula = eval(parse(text = out)), data = data, dist = dist)
##
## Pearson residuals:
##
                                3Q
       Min
                1Q Median
                                       Max
```

```
## -1.0201 -0.6459 -0.3942 0.2961 8.6647
##
## Count model coefficients (negbin with log link):
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 2.56617
                           0.09553 26.861 < 2e-16 ***
               -0.20133
                           0.01426 -14.117 < 2e-16 ***
## health
                                     3.570 0.000357 ***
## handicap
                0.30305
                           0.08489
## self
               -0.36627
                           0.11778 -3.110 0.001871 **
## civil
               -0.33717
                           0.10434 -3.231 0.001232 **
## Log(theta)
                                     2.628 0.008581 **
              0.23605
                           0.08981
## Zero-inflation model coefficients (binomial with logit link):
               Estimate Std. Error z value Pr(>|z|)
                           0.37217 -8.017 1.08e-15 ***
## (Intercept) -2.98383
                           0.04608
                                     6.533 6.44e-11 ***
## health
                0.30104
## age50TRUE
               -1.00040
                           0.26019 -3.845 0.000121 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Theta = 1.2662
## Number of iterations in BFGS optimization: 19
## Log-likelihood: -3656 on 9 Df
cat("loglik of zero-inflated model with backward selection",logLik(fitbe))
## loglik of zero-inflated model with backward selection -3656.257
cat("BIC of zero-inflated model with backward selection", AIC(fitbe, k=log(dim(dat)[1])))
## BIC of zero-inflated model with backward selection 7380.034
Compute LASSO estimates.
fit.lasso <- zipath(docvisits~.|.,data = dat, family = "negbin", nlambda=100,
                    lambda.zero.min.ratio=0.001, maxit.em=300, maxit.theta=25,
                    theta.fixed=FALSE, trace=FALSE, penalty="enet", rescale=FALSE)
Estimated coefficient parameters with smallest BIC value.
minBic <- which.min(BIC(fit.lasso))</pre>
coef(fit.lasso, minBic)
## $count
##
          (Intercept)
                                                    handicap
                                                                        hdegree
                                  health
                                                                     0.0000000
##
           2.30544059
                             -0.17379228
                                                  0.15521112
##
              married
                                schooling
                                                    hhincome
                                                                        children
##
           0.00000000
                              0.00000000
                                                  0.00000000
                                                                     0.0000000
##
                 self
                                    civil
                                                       bluec
                                                                       employed
##
           0.00000000
                              0.00000000
                                                  0.0000000
                                                                     0.0000000
##
                                                   age30TRUE
                                                                      age35TRUE
               public
                                   addon
           0.05667312
                              0.00000000
##
                                                  0.00000000
                                                                     0.0000000
##
            age40TRUE
                               age45TRUE
                                                   age50TRUE
                                                                      age55TRUE
##
           0.00000000
                              0.00000000
                                                  0.03813017
                                                                     0.09871357
##
            age60TRUE `age30TRUE:health` `health:age35TRUE` `health:age40TRUE`
##
           0.0000000
                                                  0.0000000
                              0.0000000
                                                                     0.0000000
   `health:age45TRUE` `health:age50TRUE` `health:age55TRUE` `health:age60TRUE`
                              0.00000000
                                                  0.00000000
##
           0.00000000
                                                                     0.00000000
```

```
##
## $zero
##
          (Intercept)
                                    health
                                                     handicap
                                                                           hdegree
           -2.7004768
                                                    0.0000000
                                                                         0.0000000
##
                                0.2519975
##
              married
                                 schooling
                                                     hhincome
                                                                          children
            0.0000000
                                0.0000000
                                                    0.0000000
                                                                         0.1958848
##
##
                  self
                                     civil
                                                         bluec
                                                                          employed
##
            0.0000000
                                0.0000000
                                                    0.0000000
                                                                         0.000000
               public
##
                                     addon
                                                    age30TRUE
                                                                         age35TRUE
##
            0.0000000
                                 0.000000
                                                    0.0000000
                                                                         0.000000
##
            age40TRUE
                                 age45TRUE
                                                    age50TRUE
                                                                         age55TRUE
##
            0.0000000
                                 0.0000000
                                                    -0.3975528
                                                                         0.0000000
##
            age60TRUE `age30TRUE:health` `health:age35TRUE` `health:age40TRUE`
            0.000000
##
                                 0.0000000
                                                    0.0000000
                                                                         0.0000000
##
   `health:age45TRUE` `health:age50TRUE` `health:age55TRUE`
                                                               `health:age60TRUE`
##
            0.000000
                                 0.000000
                                                    0.000000
                                                                         0.000000
cat("theta estimate", fit.lasso$theta[minBic])
## theta estimate 1.364578
Compute standard errors of coefficients and theta:
se(fit.lasso, minBic, log=FALSE)
## $count
                                              public
## (Intercept)
                     health
                               handicap
                                                        age50TRUE
                                                                     age55TRUE
   0.15054073 0.01800520 0.10395229 0.09111704 0.10279568
                                                                   0.11073563
##
## $zero
## (Intercept)
                    health
                               children
                                           age50TRUE
   0.28716188 0.03505522 0.15455293
                                         0.18345847
##
## $theta
## [1] 0.1292102
Compute AIC, BIC, log-likelihood values of the selected model.
AIC(fit.lasso)[minBic]
##
      0.048
## 7350.972
BIC(fit.lasso)[minBic]
##
      0.048
## 7411.496
logLik(fit.lasso)[minBic]
## [1] -3664.486
Compute log-likelihood value via 10-fold cross-validation.
n <- dim(dat)[1]</pre>
K <- 10
set.seed(197)
foldid <- split(sample(1:n), rep(1:K, length = n))</pre>
fitcv <- cv.zipath(docvisits ~ . | ., data = dat, family = "negbin", nlambda=100,
                    lambda.count=fit.lasso$lambda.count[1:30],
```

```
lambda.zero= fit.lasso$lambda.zero[1:30],
maxit.em=300, maxit.theta=1, theta.fixed=FALSE,
penalty="enet", rescale=FALSE, foldid=foldid)
```



```
cat("cross-validated loglik", max(fitcv$cv))
```

cross-validated loglik -367.7953

Compute MCP estimates. We compute solution paths for the first 30 pairs of shrinkage parameters (the EM algorithm can be slow), and then evaluate results as for the LASSO estimates. For cross-validation, set maximum number of iterations in estimating scaling parameter 1 (maxit.theta=1) to reduce computation costs.

Estimated coefficient parameters with smallest BIC value.

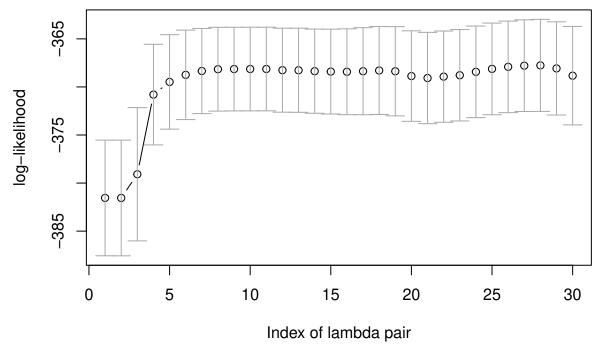
```
minBic <- which.min(BIC(fit.mcp))
coef(fit.mcp, minBic)</pre>
```

```
## $count
##
          (Intercept)
                                    health
                                                      handicap
                                                                            hdegree
##
            2.4857054
                                -0.1952631
                                                     0.2267380
                                                                         0.000000
##
               married
                                 schooling
                                                      hhincome
                                                                           children
##
            0.0000000
                                 0.000000
                                                     0.0000000
                                                                         0.000000
##
                  self
                                     civil
                                                         bluec
                                                                           employed
##
           -0.3694420
                                -0.3314318
                                                     0.0000000
                                                                         0.000000
##
               public
                                     addon
                                                     age30TRUE
                                                                         age35TRUE
```

```
##
            0.0000000
                                 0.0000000
                                                     0.0000000
                                                                         0.0000000
##
            age40TRUE
                                 age45TRUE
                                                     age50TRUE
                                                                         age55TRUE
##
            0.0000000
                                 0.0000000
                                                     0.0000000
                                                                         0.2140696
##
                                           `health:age35TRUE`
            age60TRUE `age30TRUE:health`
                                                               `health:age40TRUE`
##
            0.0000000
                                 0.0000000
                                                     0.0000000
                                                                         0.0000000
##
   `health:age45TRUE`
                      `health:age50TRUE` `health:age55TRUE` `health:age60TRUE`
            0.000000
                                 0.0000000
##
                                                     0.0000000
                                                                         0.0000000
##
##
   $zero
##
          (Intercept)
                                    health
                                                      handicap
                                                                           hdegree
##
           -3.3545126
                                 0.3169537
                                                     0.0000000
                                                                         0.000000
                                                                          children
##
              married
                                 schooling
                                                     hhincome
                                                     0.0000000
##
            0.0000000
                                 0.0000000
                                                                         0.4328507
                                                         bluec
##
                  self
                                     civil
                                                                          employed
##
            0.0000000
                                 0.000000
                                                     0.0000000
                                                                         0.000000
##
               public
                                     addon
                                                     age30TRUE
                                                                         age35TRUE
            0.0000000
##
                                 0.000000
                                                     0.0000000
                                                                         0.000000
##
            age40TRUE
                                 age45TRUE
                                                     age50TRUE
                                                                         age55TRUE
            0.000000
##
                                 0.0000000
                                                    -0.6718362
                                                                         0.000000
##
            age60TRUE `age30TRUE:health`
                                           `health:age35TRUE`
                                                                `health:age40TRUE`
##
            0.000000
                                 0.000000
                                                     0.0000000
                                                                         0.000000
   `health:age45TRUE`
                       `health:age50TRUE` `health:age55TRUE` `health:age60TRUE`
##
                                 0.0000000
            0.0000000
                                                                         0.0000000
##
                                                     0.0000000
cat("theta estimate", fit.mcp$theta[minBic])
## theta estimate 1.276819
Compute standard errors of coefficients and theta:
se(fit.mcp, minBic, log=FALSE)
## $count
## (Intercept)
                               handicap
                                                                     age55TRUE
                     health
                                                self
                                                            civil
    0.12483200
                0.01814956
                             0.10380487
                                          0.12199363 0.11886408
                                                                    0.08564174
##
##
  $zero
##
   (Intercept)
                     health
                               children
                                           age50TRUE
##
     0.4086110
                  0.0450272
                              0.1772860
                                           0.2509333
##
## $theta
## [1] 0.1336077
Compute AIC, BIC, log-likelihood values of the selected model.
AIC(fit.mcp)[minBic]
##
     0.0228
## 7319.663
BIC(fit.mcp) [minBic]
     0.0228
##
## 7380.187
logLik(fit.mcp)[minBic]
```

[1] -3648.831

Compute log-likelihood value via 10-fold cross-validation.



```
cat("cross-validated loglik", max(fitcv$cv))
```

cross-validated loglik -367.7593

Compute SCAD estimates.

Estimated coefficient parameters with smallest BIC value.

```
minBic <- which.min(BIC(fit.scad))
coef(fit.scad, minBic)</pre>
```

##	\$count			
##	(Intercept)	health	handicap	hdegree
##	2.4875256	-0.1951818	0.2258675	0.0000000
##	married	schooling	hhincome	children
##	0.000000	0.0000000	0.0000000	0.0000000
##	self	civil	bluec	employed
##	-0.3692021	-0.3314020	0.0000000	0.0000000
##	public	addon	age30TRUE	age35TRUE
##	0.000000	0.000000	0.000000	0.000000

```
age40TRUE
##
                                age45TRUE
                                                    age50TRUE
                                                                        age55TRUE
##
            0.000000
                                0.0000000
                                                    0.0000000
                                                                        0.2142137
##
            age60TRUE `age30TRUE:health` `health:age35TRUE` `health:age40TRUE`
##
            0.000000
                                                    0.000000
                                0.000000
                                                                        0.000000
##
   `health:age45TRUE`
                       `health:age50TRUE`
                                           `health:age55TRUE`
                                                               `health:age60TRUE`
            0.0000000
                                0.000000
                                                    0.0000000
                                                                        0.0000000
##
##
## $zero
##
          (Intercept)
                                   health
                                                     handicap
                                                                           hdegree
                                                    0.0000000
                                                                        0.000000
##
           -3.3157884
                                0.3142947
##
              married
                                schooling
                                                     hhincome
                                                                          children
            0.000000
                                                    0.0000000
                                                                        0.4137072
##
                                0.0000000
##
                  self
                                     civil
                                                         bluec
                                                                          employed
            0.000000
                                0.0000000
##
                                                    0.0000000
                                                                        0.0000000
##
               public
                                     addon
                                                    age30TRUE
                                                                        age35TRUE
##
            0.000000
                                0.000000
                                                    0.0000000
                                                                        0.000000
##
            age40TRUE
                                age45TRUE
                                                    age50TRUE
                                                                        age55TRUE
##
            0.000000
                                0.0000000
                                                    -0.6729928
                                                                        0.0000000
##
            age60TRUE
                       `age30TRUE:health`
                                           `health:age35TRUE`
                                                                `health:age40TRUE`
##
            0.000000
                                0.0000000
                                                    0.0000000
                                                                        0.000000
##
   `health:age45TRUE`
                       `health:age50TRUE`
                                           `health:age55TRUE`
                                                               `health:age60TRUE`
            0.0000000
                                0.000000
                                                    0.0000000
##
                                                                        0.0000000
cat("theta estimate", fit.scad$theta[minBic])
## theta estimate 1.285932
Compute standard errors of coefficients and theta:
se(fit.scad, minBic, log=FALSE)
## $count
## (Intercept)
                     health
                               handicap
                                                self
                                                            civil
                                                                    age55TRUE
                                                                   0.08555418
##
    0.12477762 0.01812803 0.10376182 0.12195491 0.11884231
##
## $zero
```

```
## $count
## (Intercept) health handicap self civil age55TRUE
## 0.12477762 0.01812803 0.10376182 0.12195491 0.11884231 0.08555418
##
## $zero
## (Intercept) health children age50TRUE
## 0.39924146 0.04438007 0.17474182 0.24738755
##
## $theta
## [1] 0.1336176
```

Compute AIC, BIC, log-likelihood values of the selected model.

```
AIC(fit.scad)[minBic]
```

```
## 0.0228
## 7319.682
```

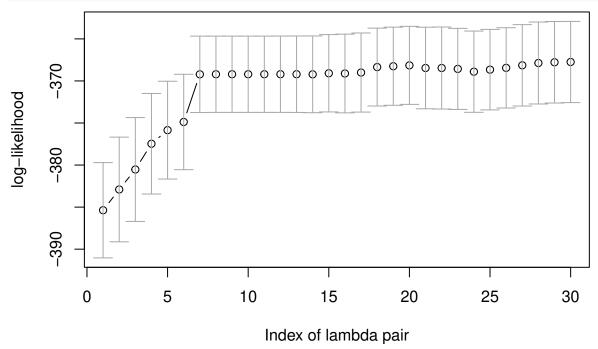
BIC(fit.scad)[minBic]

```
## 0.0228
## 7380.206
```

logLik(fit.scad)[minBic]

[1] -3648.841

Compute log-likelihood value via 10-fold cross-validation.



```
cat("cross-validated loglik", max(fitcv$cv))
```

```
## cross-validated loglik -367.7493
```

```
sessionInfo()
```

```
## R version 4.1.3 (2022-03-10)
## Platform: x86_64-pc-linux-gnu (64-bit)
## Running under: Ubuntu 18.04.6 LTS
##
## Matrix products: default
          /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.7.1
## BLAS:
## LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.7.1
##
## locale:
##
  [1] LC_CTYPE=en_US.UTF-8
                                   LC_NUMERIC=C
  [3] LC_TIME=en_US.UTF-8
                                   LC_COLLATE=en_US.UTF-8
                                   LC_MESSAGES=en_US.UTF-8
   [5] LC_MONETARY=en_US.UTF-8
##
                                   LC_NAME=C
    [7] LC_PAPER=en_US.UTF-8
##
##
   [9] LC_ADDRESS=C
                                   LC_TELEPHONE=C
## [11] LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C
##
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                               datasets methods
                                                                   base
##
## other attached packages:
## [1] pscl_1.5.5
                                     mpath_0.4-2.23 pamr_1.56.1
                      zic_0.9.1
                                                                   survival_3.4-0
## [6] cluster_2.1.4 glmnet_4.1-6
                                     Matrix_1.5-3
```

```
##
## loaded via a namespace (and not attached):
    [1] Rcpp_1.0.9
                             compiler_4.1.3
                                                 highr_0.9
    [4] iterators_1.0.14
                             tools_4.1.3
                                                 rpart_4.1.19
##
##
    [7] digest_0.6.31
                             evaluate_0.19
                                                 lifecycle_1.0.3
## [10] lattice_0.20-45
                             rlang_1.0.6
                                                 foreach_1.5.2
  [13] cli_3.5.0
                             yaml_2.3.6
                                                 parallel_4.1.3
##
                                                 fastmap_1.1.0
## [16] gbm_2.1.8.1
                             xfun_0.35
##
  [19] coda_0.19-4
                             stringr_1.5.0
                                                 knitr_1.41
  [22]
                                                 bst_0.3-24
        vctrs_0.5.1
                             grid_4.1.3
  [25]
        glue_1.6.2
                             WeightSVM_1.7-11
                                                 rmarkdown_2.19
  [28]
        magrittr_2.0.3
                             codetools_0.2-18
                                                 htmltools_0.5.4
  [31] splines_4.1.3
                             MASS_7.3-58.1
                                                 shape_1.4.6
  [34] numDeriv_2016.8-1.1 stringi_1.7.8
                                                 doParallel_1.0.17
```

References

Riphahn, Regina T, Achim Wambach, and Andreas Million. 2003. "Incentive Effects in the Demand for Health Care: A Bivariate Panel Count Data Estimation." *Journal of Applied Econometrics* 18 (4): 387–405.

Wang, Zhu, Shuangge Ma, and Ching-Yun Wang. 2015. "Variable Selection for Zero-Inflated and Overdispersed Data with Application to Health Care Demand in Germany." *Biometrical Journal* 33(29): 5192–5208. http://dx.doi.org/10.1002/bimj.201400143.