# nFactors Example-1

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In this example, the recovery of the dimensionality of a simulated factor structure is explored with different indices available in the nFactors package. The example is inspired from a simulation study by Zwick and Velicer (1986, table 2, p. 437).

The following code is for the initialisation phase. The nFactors and xtable libraries must first be loaded.

```
require(xtable)
library(nFactors)
nFactors <- 3
          <- 0.2
unique
loadings <- 0.5
nsubjects <- 180
repsim
          <- 100
var
          <- 36
          <- 12
pmjc
reppar
          <- 100
          <- 1:11
index
zwick
          <- generateStructure(var=var, mjc=nFactors, pmjc=pmjc,</pre>
                                 loadings=loadings,
                                 unique=unique)
```

A 3 factor solution with 12 variables is then simulated from 36 variables and 180 subjects, showing a correlation of 0.5 on their respective factors and 0.2 on the others. To assure accurate values of the percentiles, 100 replications of the simulation and 100 replications of the parallel analysis are done.

The following code produces statistics concerning the number of factors to retain from the 100 replications of a parallel analysis on 100 sampled correlation matrices (factor solution). Note that only the indices corresponding to the index parameter are considered. Note also that for the sake of this report the

**xtable** function is applied. In a usual R session the **print** function would be used instead. The same commentary applies to the next table which comes from a principal component analysis.

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	oc	af	par	mean.eig	per	cng	b	t.b	p.b	sescree	R2
mean	6.50	1.00	7.76	7.76	7.76	3.00	4.00	25.71	25.71	20.39	1.04
median	6.00	1.00	8.00	8.00	8.00	3.00	4.00	26.00	26.00	19.00	1.00
quantile	6.00	1.00	8.00	8.00	8.00	3.00	4.00	26.00	26.00	19.00	1.00
$\operatorname{sd}$	2.77	0.00	0.79	0.79	0.79	0.00	0.00	3.46	3.46	6.61	0.20
$\min$	1.00	1.00	6.00	6.00	6.00	3.00	4.00	18.00	18.00	7.00	1.00
max	14.00	1.00	9.00	9.00	9.00	3.00	4.00	30.00	30.00	34.00	2.00

Table 1: Distribution of the number of factors to retain according to different indices (factor analysis)

	oc	af	par	mean.eig	per	cng	b	t.b	p.b	sescree	R2
mean	3.50	-2.00	4.76	4.76	4.76	0.00	1.00	22.71	22.71	17.39	-1.96
median	3.00	-2.00	5.00	5.00	5.00	0.00	1.00	23.00	23.00	16.00	-2.00
quantile	3.00	-2.00	5.00	5.00	5.00	0.00	1.00	23.00	23.00	16.00	-2.00
$\min$	-2.00	-2.00	3.00	3.00	3.00	0.00	1.00	15.00	15.00	4.00	-2.00
max	11.00	-2.00	6.00	6.00	6.00	0.00	1.00	27.00	27.00	31.00	-1.00

Table 2: Distribution of residuals of the number of factors to retain according to different indices (factor analysis)

The following code produces statistics about about the number of factors to retain from a replication of a parallel analysis on 100 sampled correlation matrices (principal component solution).

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xtable(mzwick[[2]][,index],

caption="Distribution of the number of factors to retain
according to different indices (principal component analysis)")

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	oc	af	par	mean.eig	per	cng	b	t.b	p.b	sescree	R2
mean	2.63	1.00	2.67	7.96	2.64	3.00	4.00	25.23	25.23	6.80	1.09
median	3.00	1.00	3.00	8.00	3.00	3.00	4.00	26.00	26.00	7.00	1.00
quantile	3.00	1.00	3.00	8.00	3.00	3.00	4.00	26.00	26.00	7.00	1.00
$\operatorname{sd}$	0.56	0.00	0.51	0.85	0.58	0.00	0.00	4.59	4.59	1.59	0.29
$\min$	1.00	1.00	1.00	6.00	1.00	3.00	4.00	2.00	2.00	4.00	1.00
max	3.00	1.00	3.00	10.00	3.00	3.00	4.00	30.00	30.00	12.00	2.00

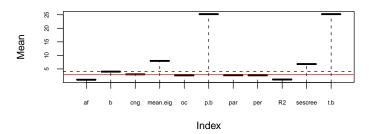
Table 3: Distribution of the number of factors to retain according to different indices (principal component analysis)

	oc	af	par	mean.eig	per	cng	b	t.b	p.b	sescree	R2
mean	-0.37	-2.00	-0.33	4.96	-0.36	0.00	1.00	22.23	22.23	3.80	-1.91
median	0.00	-2.00	0.00	5.00	0.00	0.00	1.00	23.00	23.00	4.00	-2.00
quantile	0.00	-2.00	0.00	5.00	0.00	0.00	1.00	23.00	23.00	4.00	-2.00
$\min$	-2.00	-2.00	-2.00	3.00	-2.00	0.00	1.00	-1.00	-1.00	1.00	-2.00
max	0.00	-2.00	0.00	7.00	0.00	0.00	1.00	27.00	27.00	9.00	-1.00

Table 4: Distribution of residuals of the number of factors to retain according to different indices (principal component analysis)

An index accuracy plot is produced to compare the number of factors to retain from the principal component analysis solution (figure 1). Below it, a plot is produced for the factor analysis solution. This plot shows the number of factors retain by each index. It can be seen that the af and R2 indices underestimate the number of factors, while the p.b and t.p clearly show overestimation. In the context of factor analysis, sescree also shows overestimation. The continuous vertical line indicates the initial number of factors of the structure matrix. The dashed line indicates the median number of factors retained by each index. These plots show a general tendency to orverestimate the number of factors to retain.

#### **Principal Component Analysis**



#### **Factor Analysis**

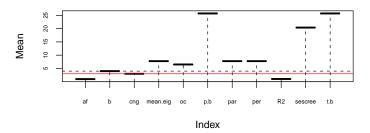
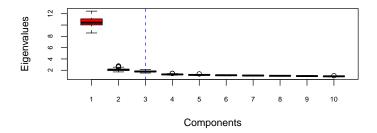


Figure 1: Index accuracy plot of the average number of components retained according to different indices

An eigen boxplot is produced to show the probability distribution of the simulated eigenvalues from the principal component analysis solution (figure 2). Below it, a plot is produced for the factor analysis solution. For the sake of a better graphical presentation, only the first 10 eigenvalues are illustrated. It can be seen that the distribution of the first eigenvalue is asymetric for the principal component analysis, while it is somewhat symetric for the factor analysis.

```
par(mfrow=c(2,1))
boxplot(mzwick, nFactors=3, xlab="Components", cex.axis=0.7,
        eigenSelect=1:10, vLine="blue", col="red")
boxplot(mzwick.fa, nFactors=3, cex.axis=0.7, eigenSelect=1:10,
        vLine="blue", col="red",
        main="Factor Analysis")
par(mfrow=c(1,1))
```

## **Eigen Box Plot**



#### **Factor Analysis**

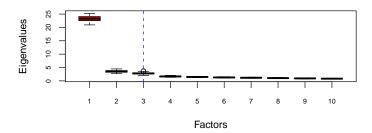


Figure 2: Eigen boxplot (principal component analysis)

### References

Raiche, G., Riopel, M. and Blais, J.-G. (2006). *Non graphical solutions for the Cattell's scree test*. Paper presented at the International Annual meeting of the Psychometric Society, Montreal.

Zwick, W. R. and Velicer, W. F. (1986). Comparison of five rules for determining the number of components to retain. *Psychological Bulletin*, 99, 432-442.