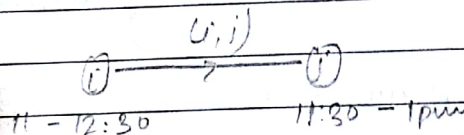


Project management includes the following steps -

- Forward pass →
Backward pass ←
- i) Project planning (Drawing the network)
 - ii) Time estimation (Network analysis)
 - iii) Scheduling
 - iv) Time-cost trade-off
 - v) Resource allocation
 - vi) Project control
- } PERT and CPM are used.

* Network analysis is quite useful for planning, designing, controlling and decision making so that the project could be economically completed in the minimum possible time with limited available resource.

- Planning - Drawing the network and establishing relationship.
- Scheduling - Scheduling computation gives the earliest and the latest start and finish time for each activity and as a by-product they identify the critical path.



CPM (Critical path method)

* Time estimation is a part of scheduling.

* CPM operates on the assumption that time taken by each activity in the project is already known precisely.

* PERT is used when time is not precisely defined.

* For time analysis in CPM, two methods are used -

- 1) Forward pass method (FPM)



t_{ij} : Duration of activity (i, j)

E_j : Earliest occurrence time of event j. It is the earliest time at which an event can occur without affecting the total project time.

ES_{ij} : Earliest start time for activity (i,j) . It is the time at which activity can start without affecting the total project time.

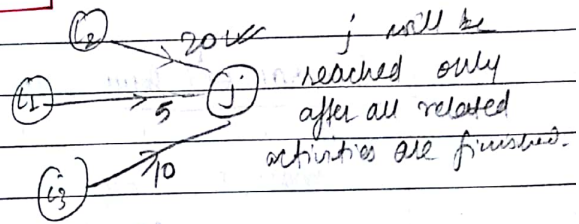
EF_{ij} : Earliest finish time for activity (i,j) . It is the earliest time at which the activity can finish without affecting the total project time.

Assume earliest occurrence time for ~~the~~ initial event of project is 0 i.e., $E_i = 0$

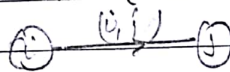
Also, $ES_{ij} = E_i$

$$EF_{ij} = E_i + t_{ij}$$

$$E_j = \max_{i \in \text{predecessors of } j} (E_i + t_{ij})$$



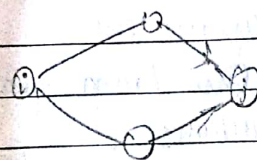
2) Backward pass method (BPM)



L_i : Latest occurrence time of event i . It is the latest time at which event i can occur without affecting the total project time.

LS_{ij} : Latest start time for activity (i,j) . It is the latest time by which the activity must start without affecting the total project time.

LF_{ij} : Latest finish time for activity (i,j) .



$$L_j = E_j$$

for the last event

$$LF_{ij} = L_j$$

$$LS_{ij} = L_j - t_{ij}$$

$$L_i = \min_{j \in \text{successors of } i} (L_j - t_{ij})$$

