

Relational algebra

Fundamental operators

1. Select (σ) $\sigma_r(r)$
2. Project (π)
3. Cartesian product (\times)
4. Rename (ρ)
5. Union (\cup)
6. Set difference ($-$)

Derived

1. Intersection (\cap)
2. Join (\bowtie) σ_r, σ_s
3. Division (\div)

Select

This operⁿ returns a set of tuple satisfying a given predicate.

Ex - Return names of those teachers who teach database.

$\sigma_{\text{course} = \text{'DBMS'}}(\text{teach})$
 \downarrow
 and

Project

~~Selecting names~~

This operⁿ allows display of any no. of columns from a given relation

Ex - select names

$\pi_{\text{name}}(\sigma_{\text{course} = \text{'DBMS'}}(\text{teach}))$
 \downarrow
 attrib to select

→ select & project interchange meanings in SQL & relational algebra.

$\pi_{1,2,3}(S) \rightarrow 1, 2, 3^{\text{rd}}$ column

Rename (ρ)

$\rho_r(\text{student})$

\downarrow
 new name

Cartesian product (\times) → cross join equivalent

Set difference \rightarrow No. of attr must be same.
 i.e., no. of attr are same

R	S	$R \cup S$	$R - S$
a b c	b c a	a b c	a b c
d c a	c d f	d c a	d c a
b f e	b f e	b f e	
		b c a	
		c d f	

Relation algebra queries

- branch (branch-name, branch-city, assets)
- customers (cust-name, cust-street, cust-city)
- account (acc-no, branch-name, balance)
- loan (loan-no, branch-name, amount)
- depositor (cust-name, acc-no)
- ~~borrower~~ (cust-name, loan-no)

- Find all loan above Rs 10000.
- Find loan no of each loan with amount greater than 20000.
- Find names of all customers who have a loan, or an account or both from a bank.
- Find names of all customers who have a loan at the Park street Branch.
- Find names of all customers, " " " " but do not have account at any branch of the bank.
- Find the largest acc. balance.
- Find all customers who have an account at all branches located in Bangalore.

i) $\sigma_{amt > 10000}(\text{loan})$

ii) $\pi_{\text{loan-no}}(\sigma_{amt > 10000}(\text{loan}))$

iii) $\pi_{\text{cust-name}}(\text{borrower}) \cup \pi_{\text{cust-name}}(\text{depositor})$

iv) $\pi_{\text{cust-name}}(\sigma_{\text{branch-name} = \text{'Park street'}}(\text{borrower} \bowtie \text{loan}))$

v) $\pi_{\text{cname}} (\sigma_{\text{branch-name} = \text{'Park Street'}} (\text{borrower} \bowtie \text{loan})) - \pi_{\text{cname}} (\text{depositor})$

vi) Steps

- i) Find those balances that are not the target.
- ii) Rename acct. relation as 'd' so that we can compare each acct. - balance with others.
- iii) Use set diff to find those acct. balances that were not found in earlier steps.

iv) $\pi_{\text{balance}} (\text{account}) - \pi_{\text{balance}} \left(\sigma_{\substack{\text{account} \\ \text{balance} < \text{d.balance}}} (\text{account} \bowtie \text{d.balance}) \right);$

$\pi_{\text{cust-name, branch-name}} (\text{depositor} \bowtie \text{account})$

$\pi_{\text{branch-name}} \left(\sigma_{\substack{\text{branch-city} = \\ \text{'Bangalore'}}} (\text{branch}) \right)$

R	S	
A B C D	C D	
b c e f	e f	
a b i j		
b c g h		$R \div S = \pi_{1,2}(R) - \pi_{1,2}(\pi_{1,2}(R) \times (S - R))$
b c a d		
d i g h		<u>Steps</u>
d i j k		i) $\pi_{1,2}(R)$
d i e f		ii) $\pi_{1,2}(R) \times S$
		iii) $\pi_{1,2}(R) \times (S - R)$
		iv) $\pi_{1,2}$ of step 3 result
		v) $\pi_{1,2}(R) - \text{result of step 4}$