

Quantization error

The value of the error for any sample is less than $\Delta/2$.

i.e., $-\Delta/2 \leq \text{error} \leq +\Delta/2$

$$\text{SNR}_{dB} = 6.02nb + 1.76 \text{ dB}$$

↓
signal to noise
ratio

↓
no. of bits in one sample
(bit rate)

Q.) A telephone subscriber line must have an SNR_{dB} above 40.
What is the min. no. of bits per sample?

$$\text{SNR}_{dB} = 6.02nb + 1.76 = 40$$

$$\Rightarrow nb = (40 - 1.76) / 6.02$$

$$= 6.35$$

* Telephone companies usually design 7 to 8 bits per sample.

Sampling rates:

$f_s = 4f$ (2 times the Nyquist rate, 4 times the max frequency)
oversampling, almost same as Nyquist rate sampling

$f_s = 2f$ (at Nyquist rate, sampling is the best)

$f_s = f$ (at half the Nyquist rate, output is not quite sinusoidal)

* Telephone companies digitize voice by assuming max frequency of 4000 Hz. The sampling rate is therefore 8000 samples per second.

Q. Low pass signal has bandwidth = 200 kHz.

Find minimum sampling rate.

Bandwidth of low pass ~~sampling~~ signal goes from 0 to f , where f = max frequency of the signal.

So we can sample this signal at 2 times the highest frequency (200 kHz). So sampling rate = 400,000 samples per second.

Bit rate = sampling rate \times number of bits per sample

$$\text{Bit rate} = f_s \times n_b$$

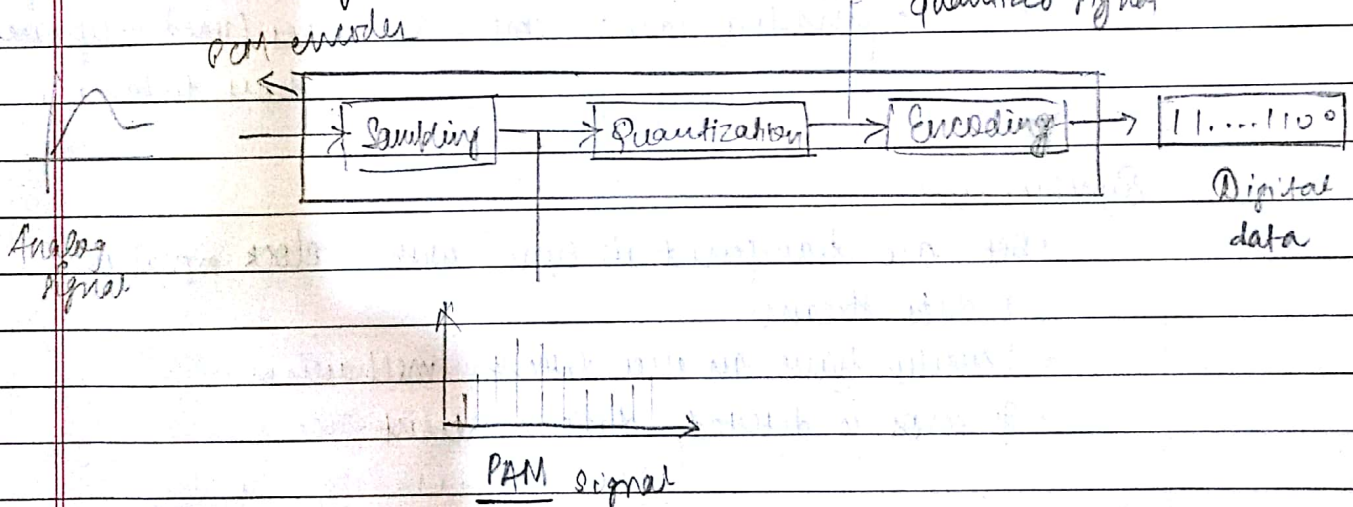
- Q. Digitize human voice assuming sampling rate of 8 bits per sample. And bit rate.

Normally human voice contains frequency from 0 to 4000 Hz.

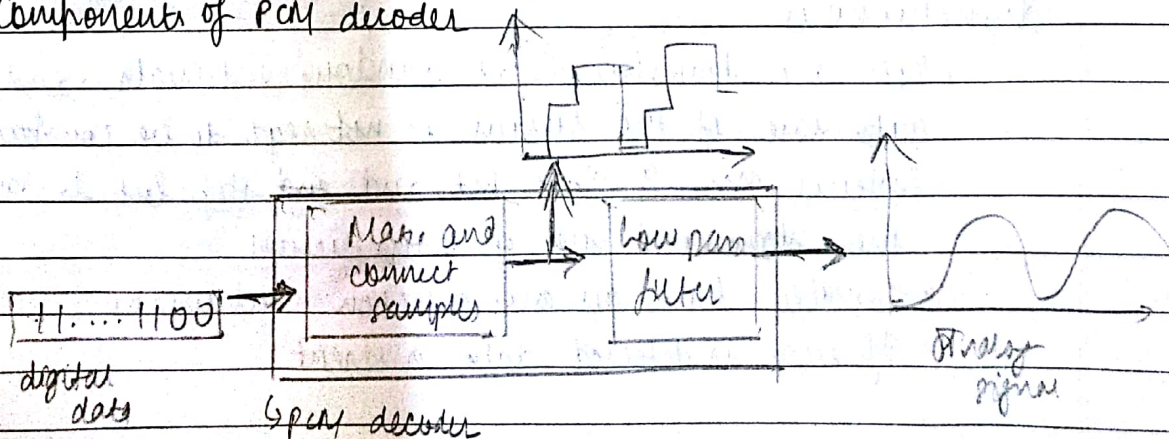
$$f_s = \text{sampling rate} = 2 \times f = 8000 \text{ samples}$$

$$\begin{aligned} \therefore \text{Bit rate} &= f_s \times n_b \\ &= 8000 \times 8 \\ &= 64000 \text{ bits per second} \\ &= 8000 \text{ Bps} \end{aligned}$$

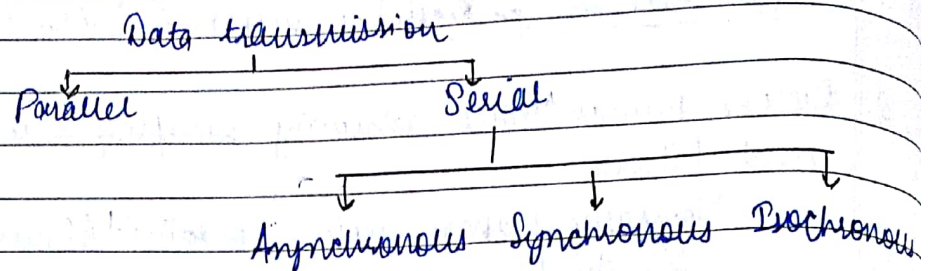
Components of PCM encoder



Components of PCM decoder



Digital transmission modes



Serial mode: 1 bit is sent with each clock tick.

- one comp² channel/wire is needed

Parallel mode: multiple bits are sent with each tick

- multiple channels/wires, bundled in one cable reqd.
- disadvantage: cost = 8x wires (used only over short distances).

Synchronous

- Bits are transferred in sync with a clock signal in a data stream.
- Usually have an error-detection mechanism.
- If error is detected, data is resent.

Asynchronous:

- Bits are transferred at random intervals and the data rate of the stream is not reqd. to be constant.
- Systems use a start bit and ~~end~~ stop bit to signal the start and end of transmission.
- Usually have an error-detection mechanism.
- If error is detected, data is resent.