

Polygon

A closed figure with more than 2 sides

Convex polygon



Concave polygon



Line b/w any two vertices is inside the polygon area completely.

Polygon surface equation

$$Ax + By + Cz + D = 0$$

If $Ax + By + Cz + D < 0$, point inside the area.

3D object representation

~~i) Boundary representation~~

- Broadly representation schemes for solid schemes are divided into two categories:

i) Boundary representation

Describe 3D objects as a set of surfaces that separate the object interior from the environment.

ii) Space partitioning representation (SPR)

They are used with interior properties, by partitioning the spatial region containing an object into a set of small, non-overlapping contiguous solids (usually cubes).

Vertex ~~table~~

Geometric data representation for two adjacent polygon surfaces:

Vertex table	Edge table	Using surface	Polygon surface table
$V_1: x_1, y_1, z_1$	$E_1: V_1, V_2$	S_1	$S_1: E_1, E_2, E_3$
$V_2: x_2, y_2, z_2$	$E_2: V_2, V_3$	S_1	$S_2: E_3, E_4, E_5, E_6$
$V_3: x_3, y_3, z_3$	$E_3: V_1, V_3$	S_1, S_2	
$V_4: x_4, y_4, z_4$	$E_4: V_3, V_4$		
$V_5: x_5, y_5, z_5$	$E_5: V_4, V_5$		
	$E_6: V_1, V_5$		

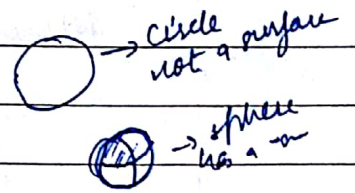
Quadric surface

surface with surface equation of degree 2

$$cx - x^2 + y^2 + z^2 = r^2$$

↓
sphere's cartesian eqⁿ

→ surface eqⁿ of sphere



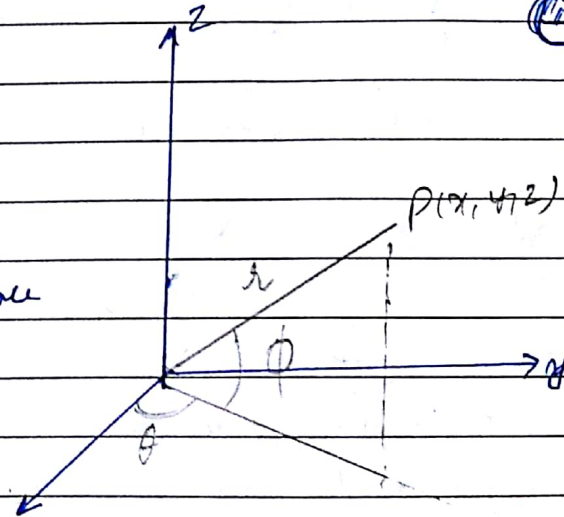
Parametric eqⁿ for sphere

$$x = r \cos \phi \sin \theta$$

$$y = r \sin \phi \sin \theta$$

$$z = r \cos \theta$$

We can represent a ~~3D~~ sphere surface using parametric equations in terms of longitude & latitude.



$$-\frac{\pi}{2} \leq \phi \leq \frac{\pi}{2}$$

$$-\pi \leq \theta \leq \pi$$

Ellipsoid

$$\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 + \left(\frac{z}{c}\right)^2 = 1$$

→ Cartesian eqⁿ

Superquadric

Superellipse

$$\left(\frac{x}{a}\right)^{2/s} + \left(\frac{y}{b}\right)^{2/s} = 1$$

→ we change shape by varying s

Super ellipsoid

$$\left[\left(\frac{x}{s_x} \right)^{2/s_2} + \left(\frac{y}{s_y} \right)^{2/s_2} \right]^{s_2/s_1} + \left(\frac{z}{s_z} \right)^{2/s_1} = 1$$

Blooby object \rightarrow 3D object with no fixed shape

Shape changes with time.

Ex - water droplet, clay, muscle etc.

Line drawing \rightarrow 3 algs

Circle drawing \rightarrow 4 algs

Ellipse drawing \rightarrow 4 algs

\rightarrow Xiang plattok