

Resistive Circuits

(Chapter 3)

Textbook:

Electric Circuits

James W. Nilsson & Susan A. Riedel

9th Edition.

Link to download materials:

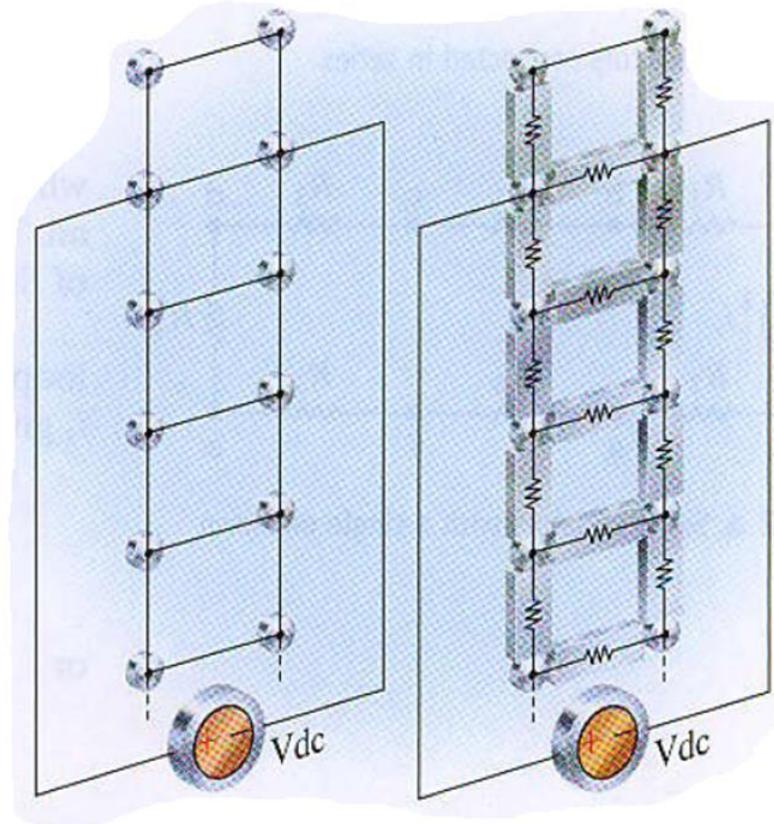
[Blackboard](#)

Practical Perspective A Rear Window Defroster

The rear window defroster grid on an automobile is an example of a resistive circuit that performs a useful function.

How does this grid work to defrost the rear window?

How are the properties of the grid determined?

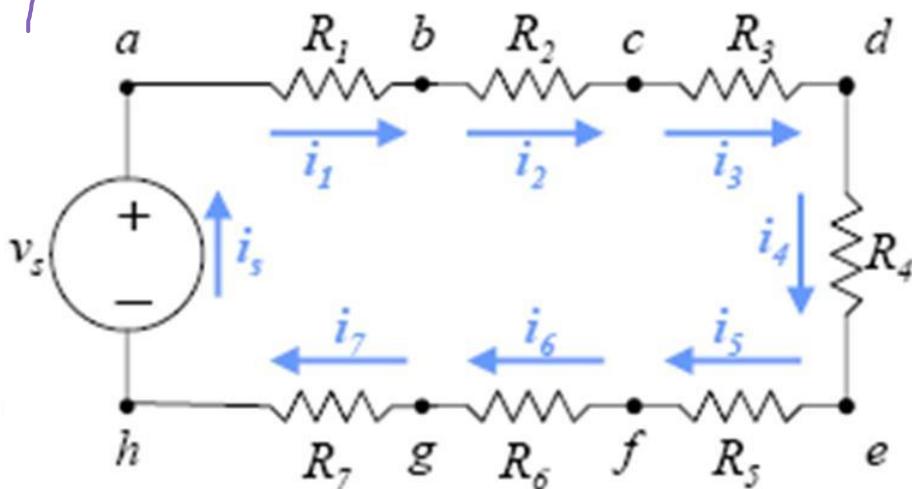


Resistors in series

- Just two elements connected at a single node are said to be in series.
- Applying KCL at all nodes.

$$i_s = i_1 = i_2 = i_3 = i_4 = i_5 = i_6 = i_7$$

$$R_{eq} = R_1 + R_2 + R_3 + \dots$$



Series-connected circuit elements carry the same current

- Applying KVL

$$-v_s + i_s R_1 + i_s R_2 + i_s R_3 + i_s R_4 + i_s R_5 + i_s R_6 + i_s R_7 = 0$$

or $v_s = i_s \underbrace{(R_1 + R_2 + R_3 + R_4 + R_5 + R_6 + R_7)}_{R_{eq}}$

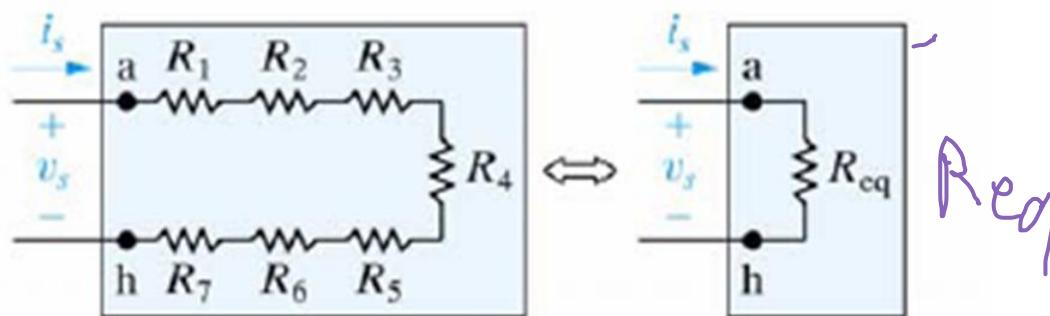
$$R_{eq} = R_1 + R_2 + R_3 + R_4 + R_5 + R_6 + R_7 \rightarrow$$

$$v_s = i_s R_{eq}$$

Resistors in series (cont.)

- In general, if k resistors are connected in series, the equivalent single resistor has a resistance equal to the sum of the k resistances, or

$$R_{eq} = \sum_{i=1}^k R_i = R_1 + R_2 + \dots + R_k$$

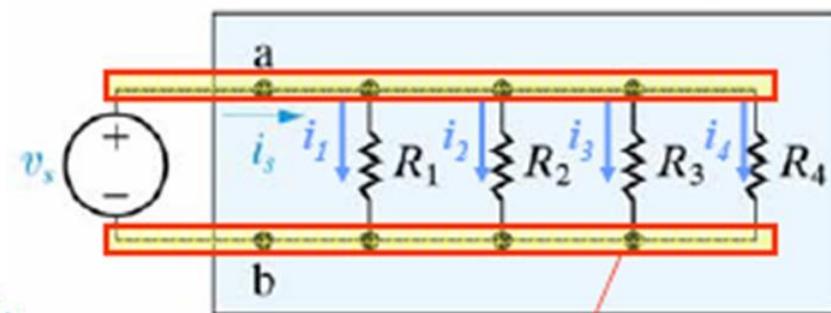


$R_n \dots$

Resistors in parallel

$$R_1 // R_2 \Rightarrow R_{\text{eq}} = \frac{R_1 \times R_2}{R_1 + R_2}$$

- When two elements connect at a single node pair, they are said to be connected in parallel.
- Parallel-connected circuit elements have the **same voltage across their terminals**.
- Applying KCL



- $i_s = i_1 + i_2 + i_3 + i_4$
- From Ohm's law

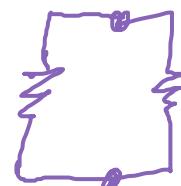
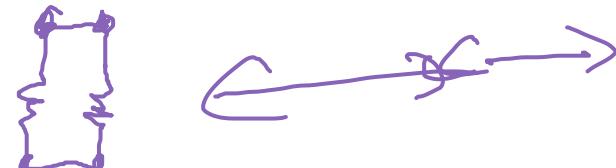
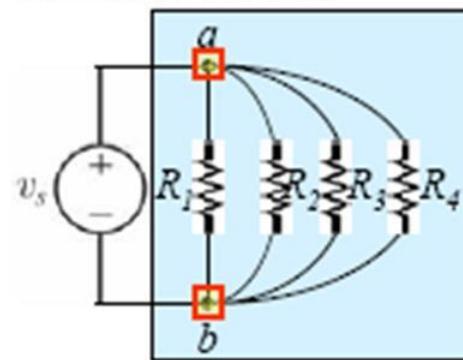
$$i_1 R_1 = i_2 R_2 = i_3 R_3 = i_4 R_4 = v_s$$

- Therefore

$$i_1 = \frac{v_s}{R_1}, i_2 = \frac{v_s}{R_2}, i_3 = \frac{v_s}{R_3} \text{ & } i_4 = \frac{v_s}{R_4}$$

$$i_s = \frac{v_s}{R_1} + \frac{v_s}{R_2} + \frac{v_s}{R_3} + \frac{v_s}{R_4}$$

Same node "No elements connected between nodes"



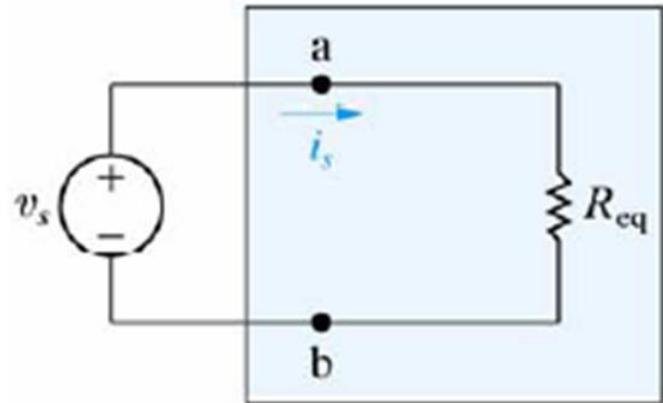
Resistors in parallel (cont.)

$$i_s = v_s \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} \right)$$

$$\frac{i_s}{v_s} = \frac{1}{R_{eq}} = \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} \right)$$

$$\frac{1}{R_{eq}} = \sum_{i=1}^k \frac{1}{R_i} = \left(\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_k} \right)$$

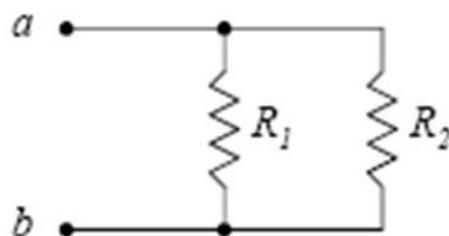
$$G_{eq} = \sum_{i=1}^k G_i = (G_1 + G_2 + \dots + G_k)$$



- Special Case (two resistors in parallel)

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} = \frac{R_1 + R_2}{R_1 R_2}$$

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

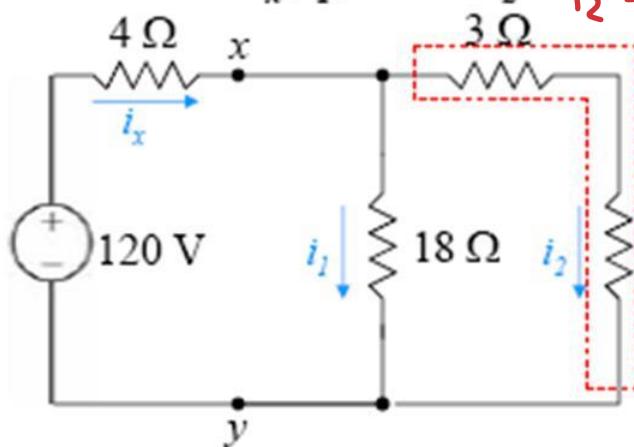


Example 3.1 $R = \frac{U}{I}$

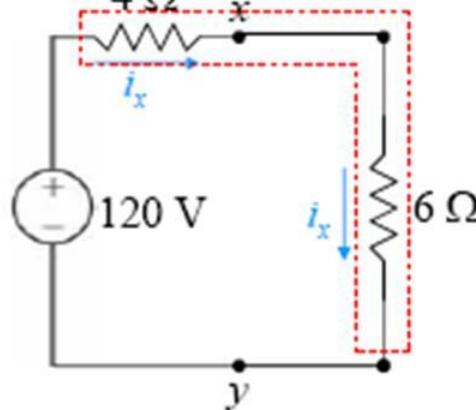
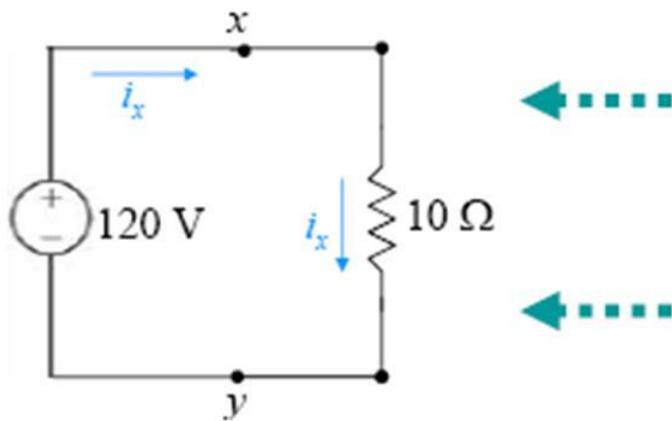
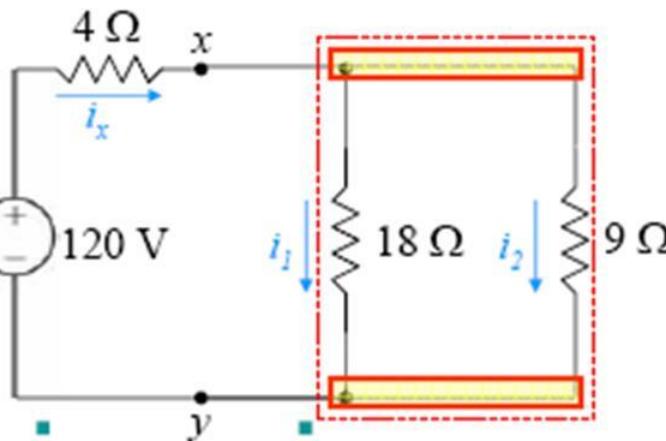
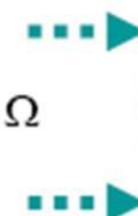
$$i_1 = \frac{120}{\left(\frac{1}{R_{18\Omega}} + \frac{1}{R_{4\Omega}}\right)}$$

$$i_2 = \frac{120}{9}$$

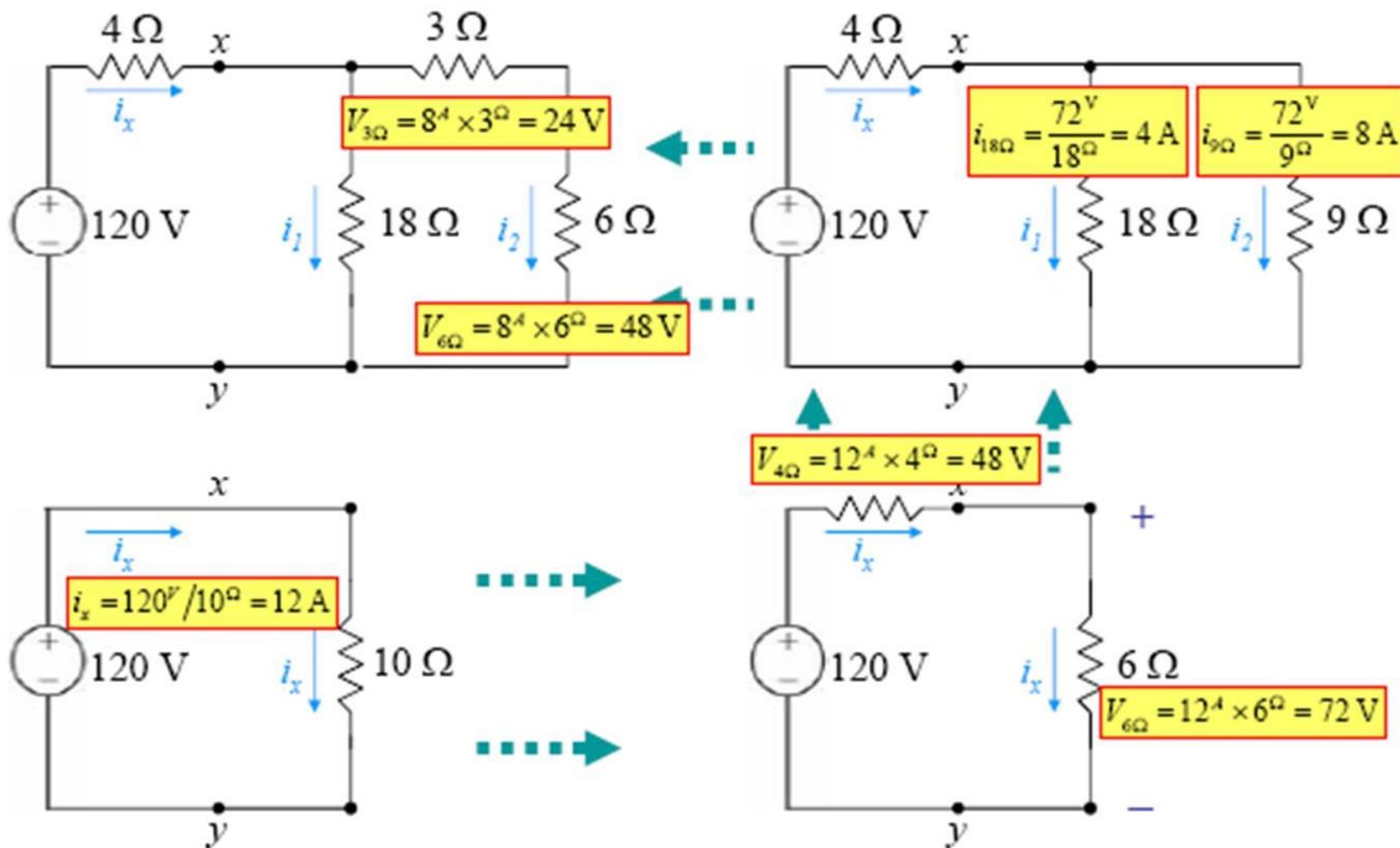
- Find i_x, i_1 , and i_2 ?



$$R = 9$$



Example (Cont.)



First

Assessing Objective 1

- Find (a) v , (b) power delivered to the circuit by the current source, and (c) the power dissipated in the $10\ \Omega$ resistor.

Exp
Time

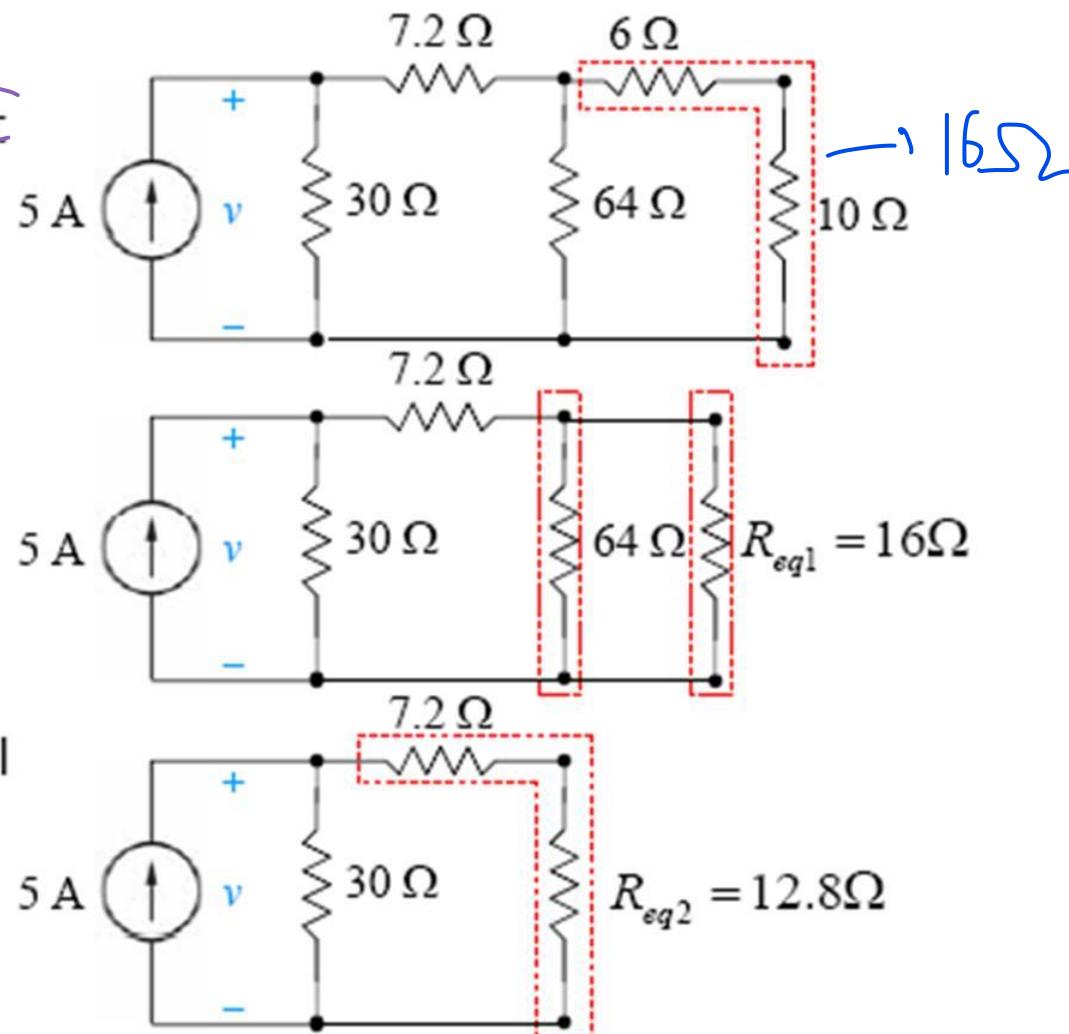
Ans.:

- The $6\ \Omega$ is in series with the $10\ \Omega$,

$$R_{eq1} = 6 + 10 = 16\ \Omega$$

- The $16\ \Omega$ is in parallel with the $64\ \Omega$,

$$R_{eq2} = \frac{16 \times 64}{16 + 64} = 12.8\ \Omega$$



Example (cont.)

- The $12.8\ \Omega$ is in series with the $7.2\ \Omega$,

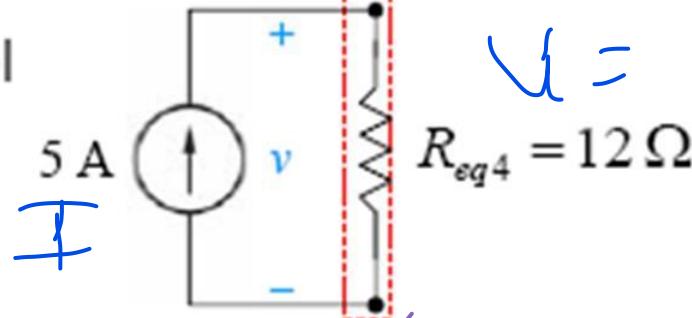
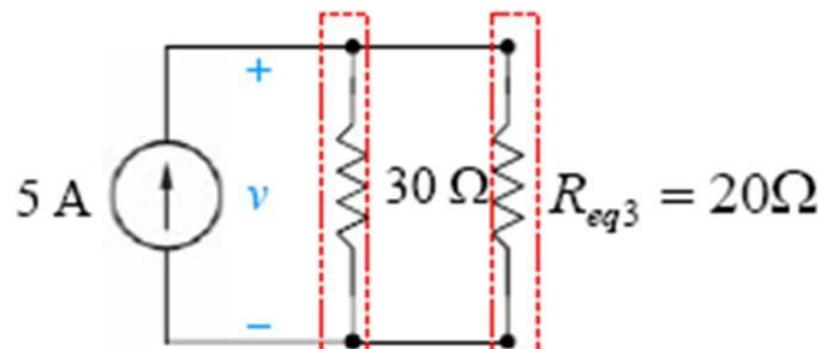
$$R_{eq3} = 7.2 + 12.8 = 20\ \Omega$$

- The $30\ \Omega$ is in parallel with the $20\ \Omega$,

$$R_{eq4} = \frac{30 \times 20}{30 + 20} = 12\ \Omega$$

- Now applying Ohm's Law

- Power delivered by the current source



$$v = i R_{eq4} = 5^A 12\ \Omega = 60\ V$$

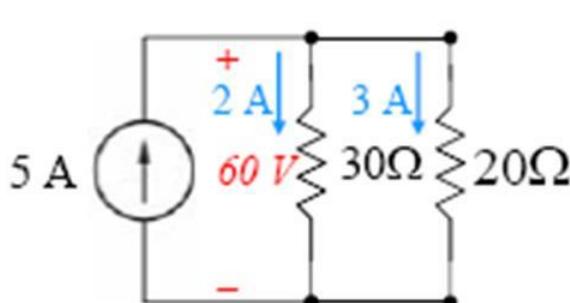
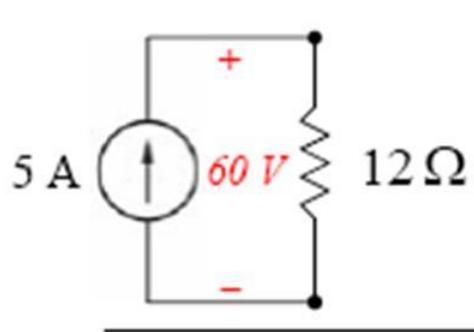
Solve

$$p = iv = 5^A 60\ V = 300\ W$$

~~P~~ Solve

Some 60V // → parallel

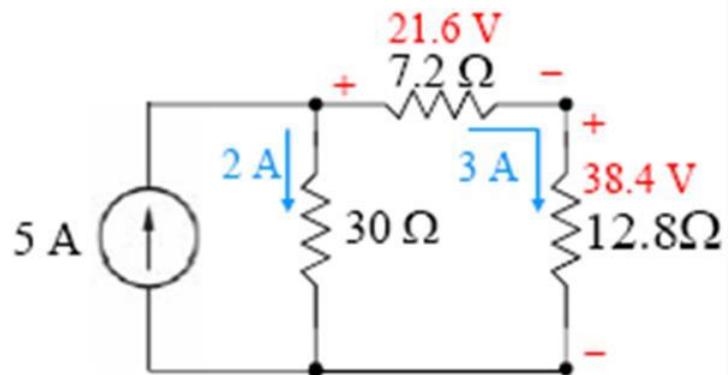
Example (cont.)



$$i_{30\Omega} = \frac{60V}{30\Omega} = 2 A$$

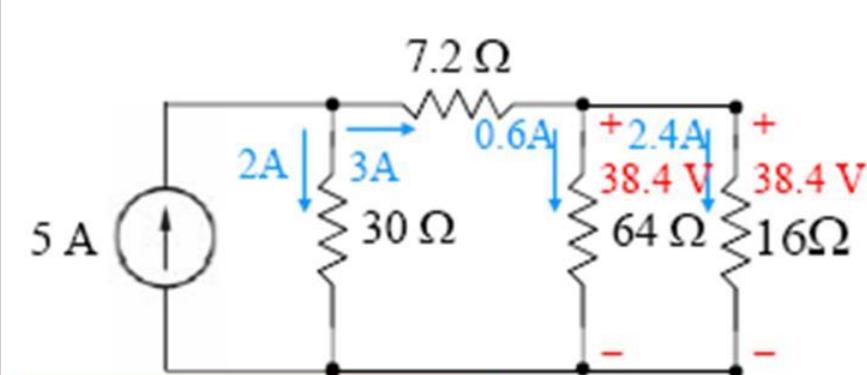
+ → Some I

$$i_{20\Omega} = \frac{60V}{20\Omega} = 3 A$$



$$v_{7.2\Omega} = 3^A \times 7.2\Omega = 21.6 V$$

$$v_{12.8\Omega} = 3^A \times 12.8\Omega = 38.4 V$$



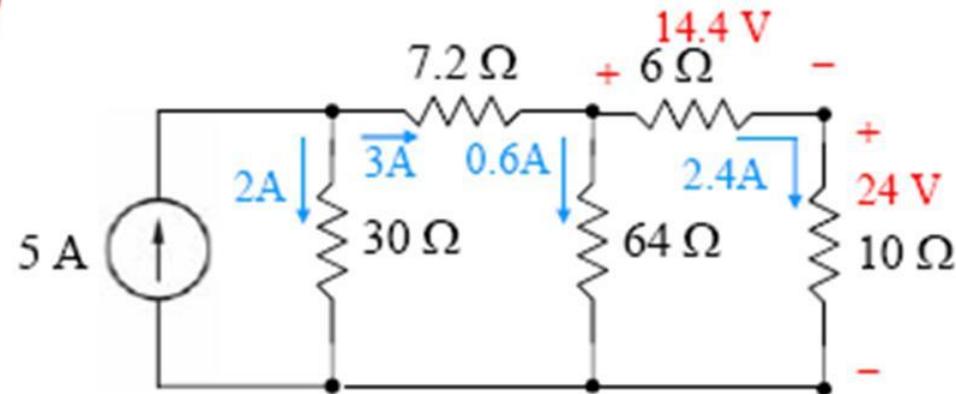
$$i_{64\Omega} = \frac{38.4V}{64\Omega} = 0.6 A$$

~~$$i_{16\Omega} = \frac{38.4V}{16\Omega} = 2.4 A$$~~

Example (cont.)

$$v_{6\Omega} = 2.4^A \times 6\Omega = 14.4 \text{ V}$$

$$v_{10\Omega} = 2.4^A \times 10\Omega = 24 \text{ V}$$



- The power dissipated in the 10Ω resistor

$$p_{10\Omega} = 2.4^A \times 24\text{V} = 57.6 \text{ W}$$

dissipated \rightarrow heat $\rightarrow P > 0$

Power Delivery Source \rightarrow Nguồn phát $\rightarrow P < 0$

Problems

- Find the equivalent resistance R_{ab} for the circuit in Figure.

$R_{5\Omega}$ & $R_{15\Omega}$ are in series

$$R_{eq1} = R_{5\Omega} + R_{15\Omega} = 20\Omega$$

$$R_{eq2} = R_{eq1} // R_{60\Omega} = \frac{20 \times 60}{20 + 60} = 15\Omega$$

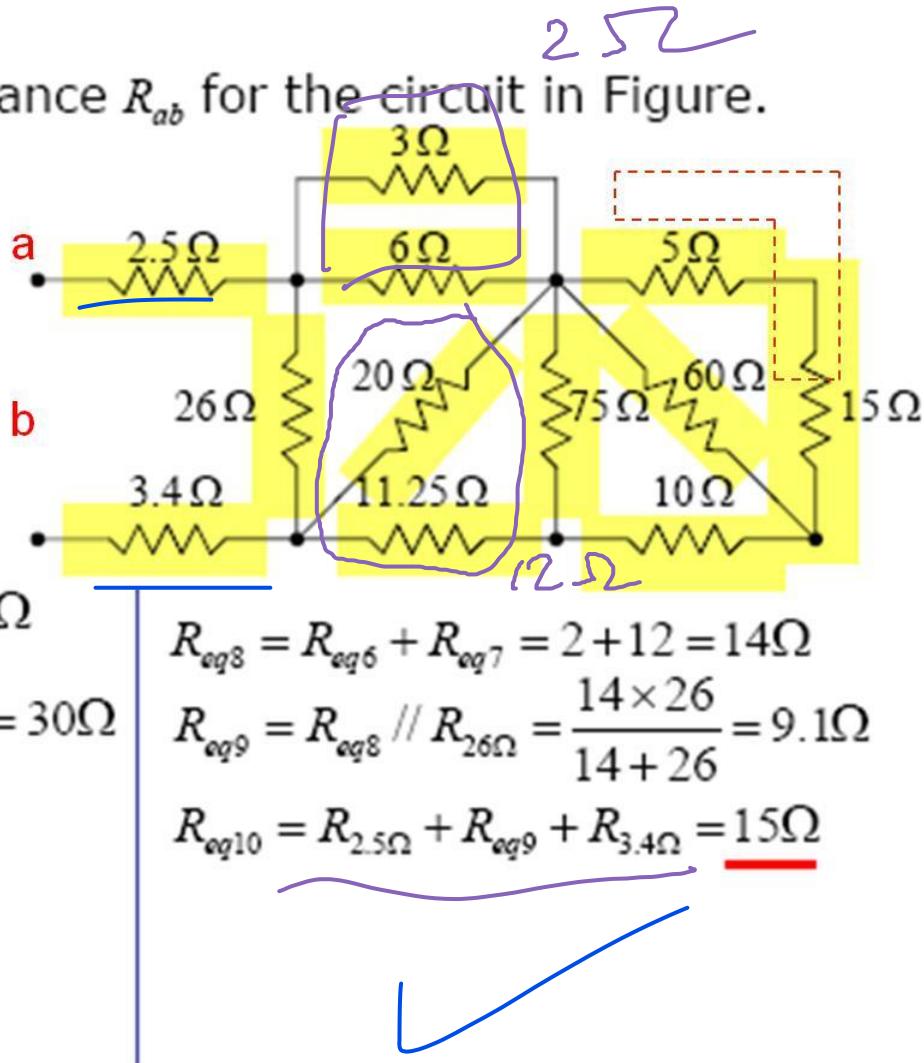
$$R_{eq3} = R_{eq2} + R_{10\Omega} = 15 + 10 = 25\Omega$$

$$R_{eq4} = R_{eq3} // R_{75\Omega} = \frac{25 \times 75}{25 + 75} = 18.75\Omega$$

$$R_{eq5} = R_{eq4} + R_{11.25\Omega} = 18.75 + 11.25 = 30\Omega$$

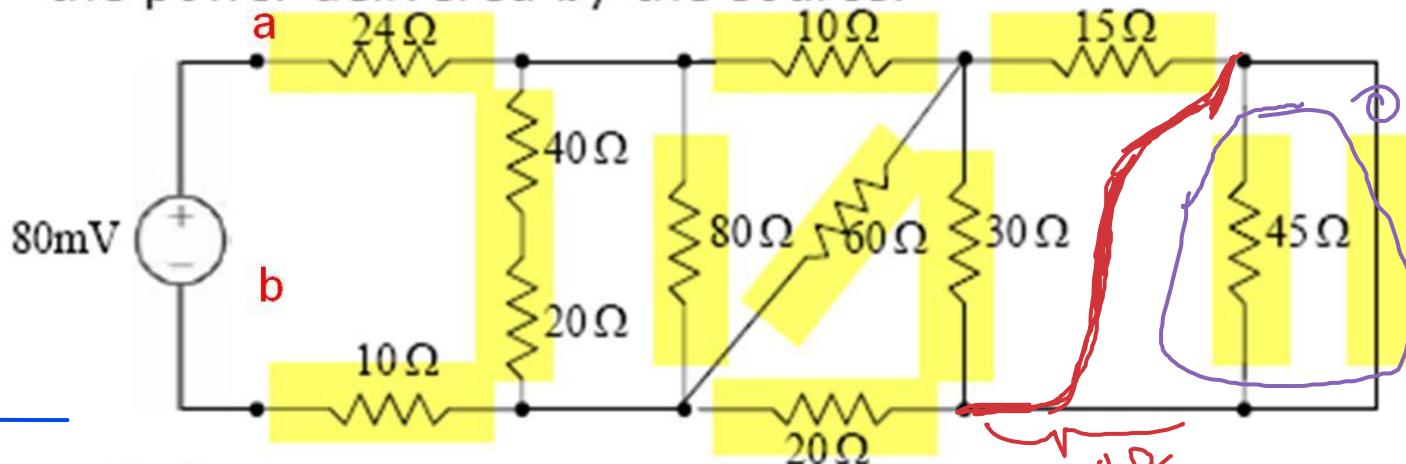
$$R_{eq6} = R_{eq5} // R_{20\Omega} = \frac{30 \times 20}{30 + 20} = 12\Omega$$

$$R_{eq7} = R_{3\Omega} // R_{6\Omega} = \frac{3 \times 6}{3 + 6} = 2\Omega$$



Problems

- In the circuit shown, find the equivalent resistance R_{eq} and the power delivered by the source.



$$R_{eq1} = \frac{45 \times 0}{45 + 0} = 0\Omega \text{ (Short Circuit)}$$

$$R_{eq2} = \frac{15 \times 30}{15 + 30} = 10\Omega$$

$$R_{eq3} = 30 + 20 = 50\Omega$$

$$R_{eq4} = \frac{30 \times 60}{30 + 60} = 20\Omega$$

$$R_{eq5} = 10 + 20 = 30\Omega$$

$$R_{eq6} = \frac{1}{\frac{1}{60} + \frac{1}{80} + \frac{1}{30}} = 16\Omega$$

$$R_{eq7} = 24 + 16 + 10 = 50\Omega$$

$$P_{80mV} = \frac{(80 \times 10^{-3})^2}{50} = 128\mu\text{W}$$

$Ckt \propto 2$ components

In series

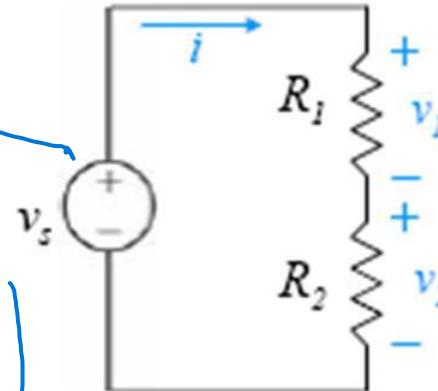
The voltage-divider circuit

Apply KVL

$$v_s = iR_1 + iR_2$$

$$i = \frac{v_s}{R_1 + R_2}$$

$$v_1 = iR_1 = v_s \frac{R_1}{R_1 + R_2} \quad \& \quad v_2 = iR_2 = v_s \frac{R_2}{R_1 + R_2}$$



WT

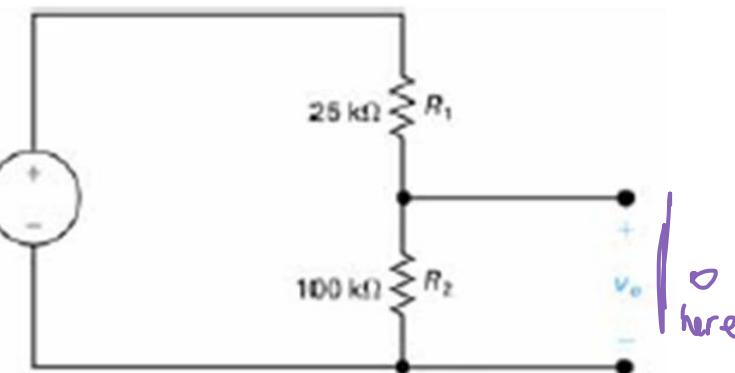
Example:

If the resistors used in the circuit have a tolerance of $\pm 10\%$. Find $v_{o\max}$ and $v_{o\min}$

Ans.:-

$$v_o(\max) = 100 \frac{100 \times 1.1}{100 \times 1.1 + 25 \times 0.9} = 83.02 \text{ V}$$

$$v_o(\min) = 100 \frac{100 \times 0.9}{100 \times 0.9 + 25 \times 1.1} = 76.60 \text{ V}$$



Not APPLY INDUCTIVE

Chuỗi có 2 компоненты

$$i_1 = \frac{U}{R_1} =$$

$$V = i_s \times R_1 // R_2$$

$$= i_s \times \frac{R_1 R_2}{R_1 + R_2}$$

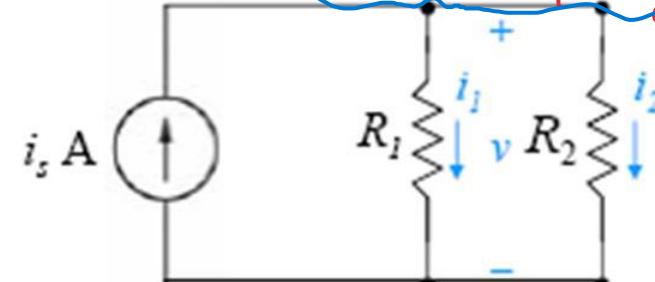
The current-divider circuit

$$R_1 // R_2 \rightarrow R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

Ohm's Law

$$V = i_1 R_1 = i_2 R_2 = i_s R_{eq} = i_s \frac{R_1 R_2}{R_1 + R_2}$$

$$i_1 = \frac{R_2}{R_1 + R_2} i_s \quad \& \quad i_2 = \frac{R_1}{R_1 + R_2} i_s$$



Example:

Find the power dissipated in the 6Ω resistor

Ans.: -

$$6\Omega // 4\Omega + 1.6\Omega$$

$$R_{eq} = \frac{4 \times 6}{4 + 6} + 1.6 = 4\Omega$$

Using Current Divider

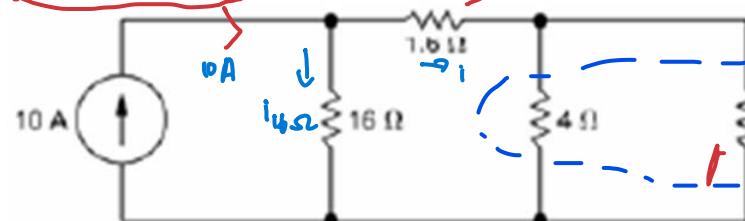
$$i_o = \frac{16}{16 + 4} 10 = 8A$$

$\Rightarrow 16\Omega$ and 4Ω

Using Current Divider

$$i_6 = \frac{4}{4 + 6} 8 = 3.2A$$

4Ω and 6Ω

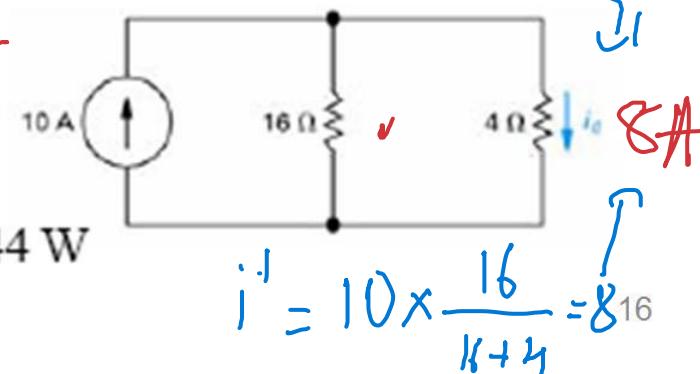


i_6

$i_4\Omega$

$i_{16\Omega}$

$P_{6\Omega}$



$$i_6 = 10 \times \frac{16}{16 + 4} = 8A$$

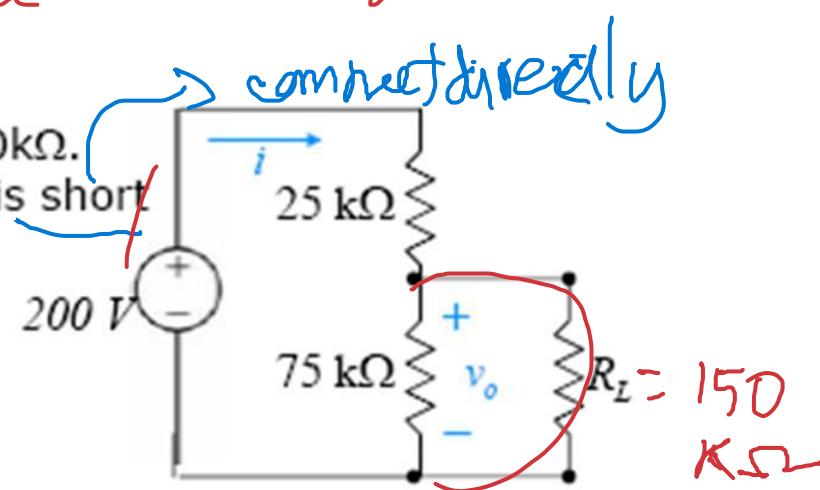
$$P_6 = i_6^2 R_{6\Omega} = 61.44 W$$

Assessing Objective 2

Device \rightarrow Load

→ Remove H

Find (a) v_o at no load, (b) v_o when $R_L = 150\text{k}\Omega$.
 (c) Power dissipated in $25\text{k}\Omega$ if the load is short circuited. (d) max. power in $75\text{k}\Omega$.



Ans.: - $v_o = 200 \times \frac{75k}{75k + 25k} = 150\text{V}$ \rightarrow ~~disconnected R_L~~

(b) $R_{eq} = \frac{75k \times 150k}{75k + 150k} = 50\text{k}\Omega$ \rightarrow $v_o = 200 \times \frac{50k}{50k + 25k} = 133.33\text{V}$ ~~Voltage divider~~

(c) $P_{25\text{k}\Omega} = \frac{V^2}{R_{25\text{k}\Omega}} = \frac{200^2}{25k} = 1.6\text{W}$

(d) $P_{75\text{k}\Omega}^{\text{max}} = \frac{V^2}{R_{75\text{k}\Omega}} = \frac{150^2}{75k} = 0.3\text{W}$

b) $v_o = 200 \times \frac{75k // 150k}{75k // 150k + 25k} = 133.33\text{V}$ ~~connect directly~~

Short circuit -
 take a wire

Assessing Objective

$$V = i_{80\Omega} = i_{120\Omega} = \frac{R}{R + 120\Omega} R \parallel R_{40\Omega - 80\Omega} = R_{eq} = \frac{R \times 120}{R + 120}$$

Find (a) R so $i_{80\Omega} = 4A$, (b) $P_{R\Omega}$, (c) P_{20A}

Ans.:-

$$(a) i_{80\Omega} = 4 = \frac{R}{R + 80 + 40} 20 \Rightarrow R = 30\Omega$$

$$(b) P_{R\Omega} = i_{R\Omega}^2 R = 7680\Omega \quad \cancel{= 20^2 \times 30}$$

$$V = V_1 + V_2$$

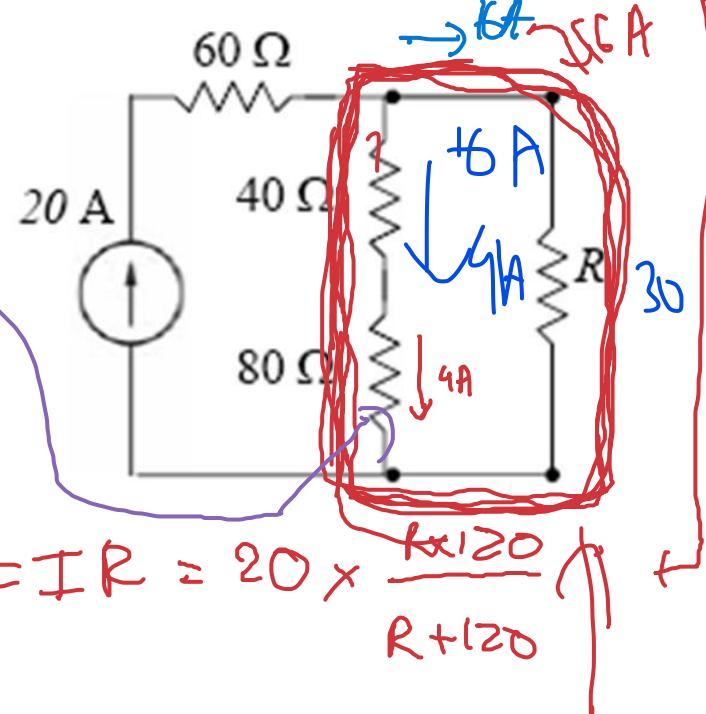
$$(c) V_{20A} = 20^A \times 60\Omega + 4^A \times 120\Omega = 1680V$$

$$P_{20A} = 20^A \times 1680V = 33600W$$

Beginner

$$V = 20 \times 8V \quad R_{eq} = 8\Omega$$

$$= 160V$$



Voltage Division and Current Division

$$i = \frac{v}{R_1 + R_2 + \dots + R_n} = \frac{v}{R_{eq}}$$

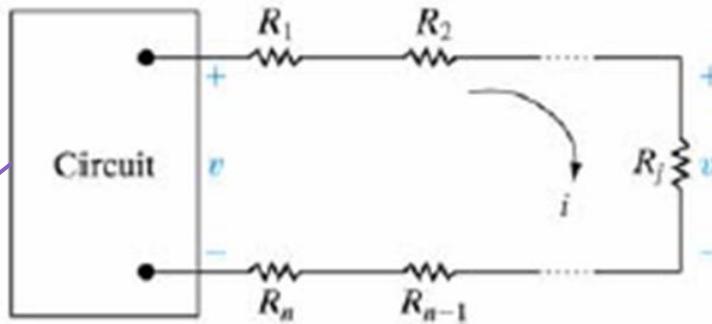
$$v_j = iR_j$$

$$v_j = \frac{R_j}{R_{eq}} v$$

$$\rightarrow R_1 + R_2 + \dots$$

✓ is the same

more than 3 components

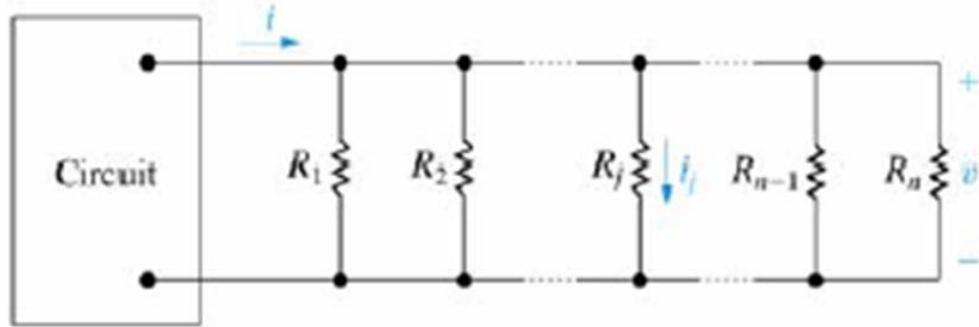


$$v = i(R_1 \parallel R_2 \parallel \dots \parallel R_n) = iR_{eq}$$

$$v = i_j R_j$$

$$i_j = \frac{R_{eq}}{R_j} i$$

R_{eff}



must know R_{eq} to use formulae

Example 3.4

Use current division to find i_o and voltage division to find v_o

Ans.:-

$$R_{eq} = \frac{1}{\frac{1}{80} + \frac{1}{10} + \frac{1}{80} + \frac{1}{24}} = 6 \Omega$$

Current Division

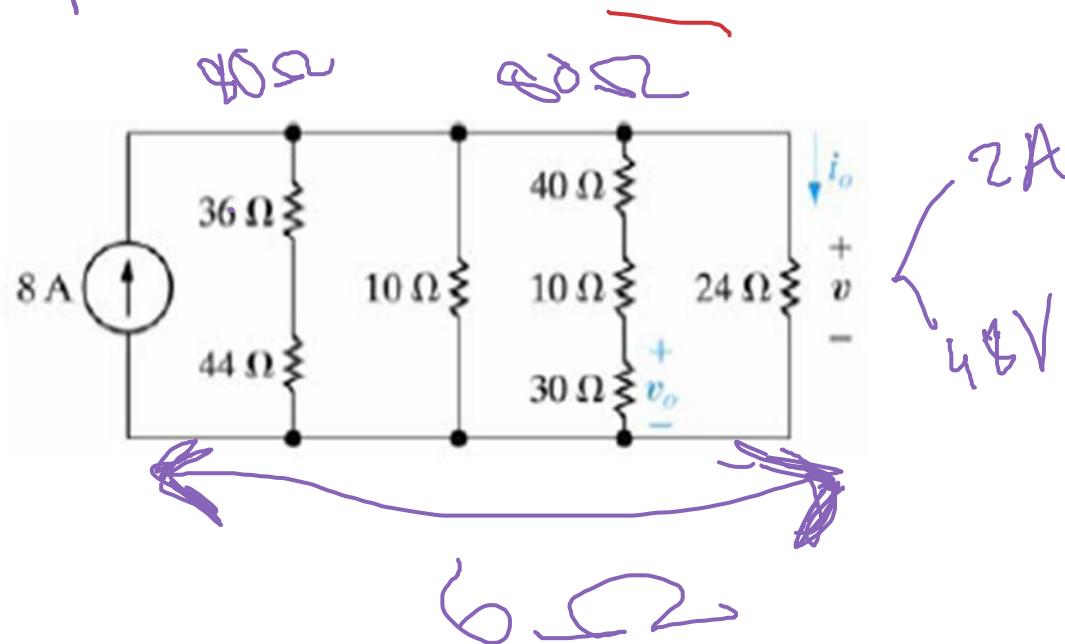
$$i_o = \frac{6}{24} 8A = 2A$$

Ohm's Law

$$v_{24} = 2A \cdot 24 \Omega = 48V$$

Voltage Division

$$v_o = 48V \cdot \frac{30 \Omega}{80 \Omega} = 18V$$



Assessing Objective 3

Use voltage division & current division to find (a) v_o , (b) $i_{40\Omega}$ & $i_{30\Omega}$, (c) $P_{50\Omega}$.

Ans.:-

$$(a) R_{eq1} = \frac{1}{\frac{1}{20} + \frac{1}{30} + \frac{1}{60}} = 10 \Omega$$

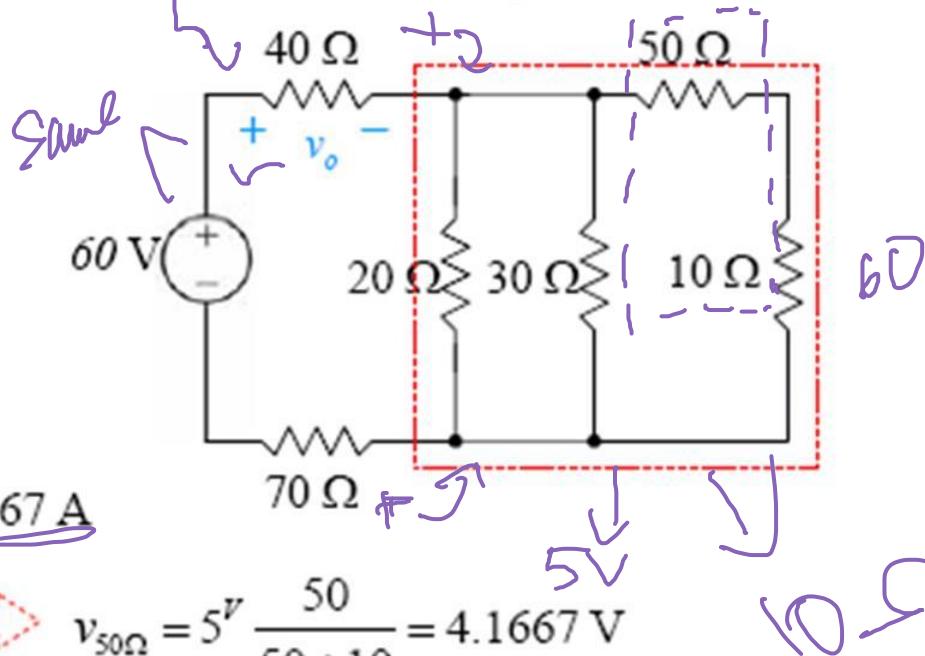
$$v_o = 60V \frac{40}{40+10+70} = 20V$$

$$(b) i_{40\Omega} = \frac{60V}{120\Omega} = 0.5A = \frac{20}{40}$$

$$i_{30\Omega} = i_{40\Omega} \frac{R_{eq1}}{R_{30\Omega}} = 0.5 \cdot \frac{10}{30} = 0.1667A$$

$$(c) v_{R_{eq1}} = 60V \frac{10}{40+10+70} = 5V \Rightarrow v_{50\Omega} = 5V \frac{50}{50+10} = 4.1667V$$

$$P_{50\Omega} = \frac{V_{50\Omega}^2}{R_{50\Omega}} = 0.3472W$$

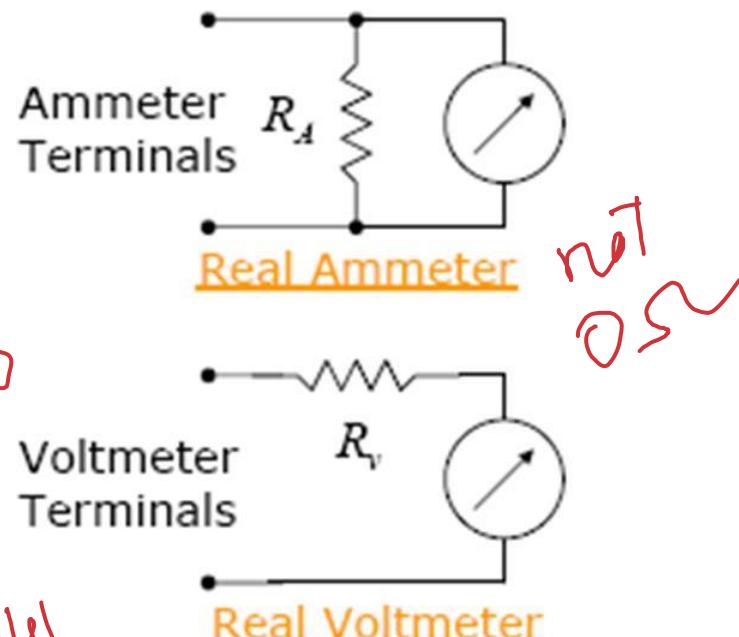
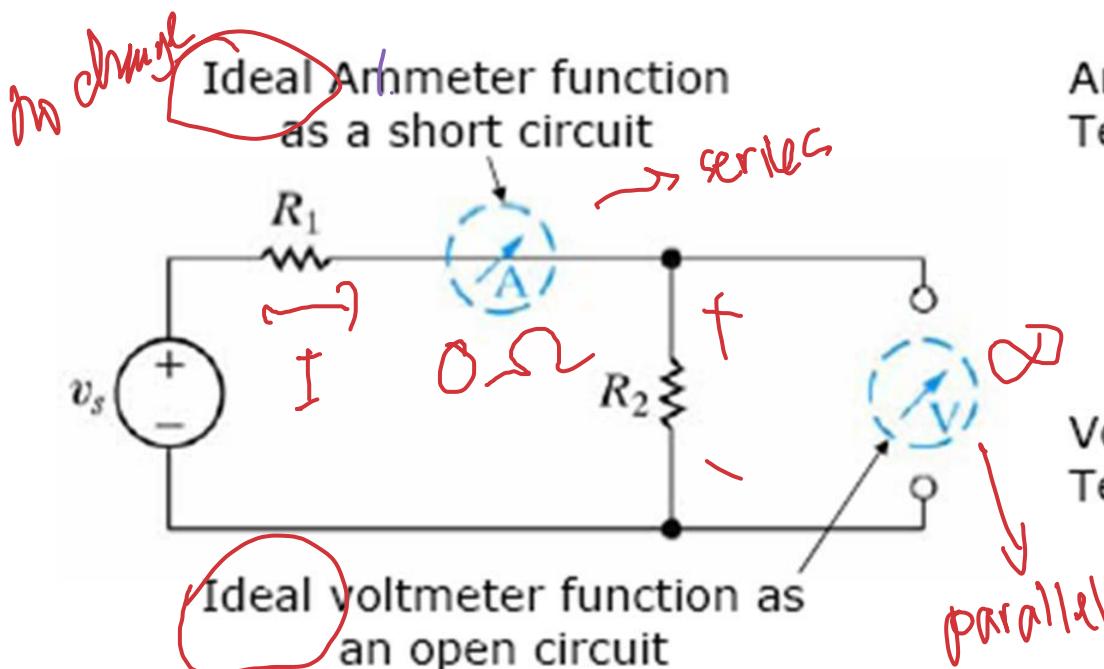


✓ get it

Measuring Voltage and Current

Important In Lab

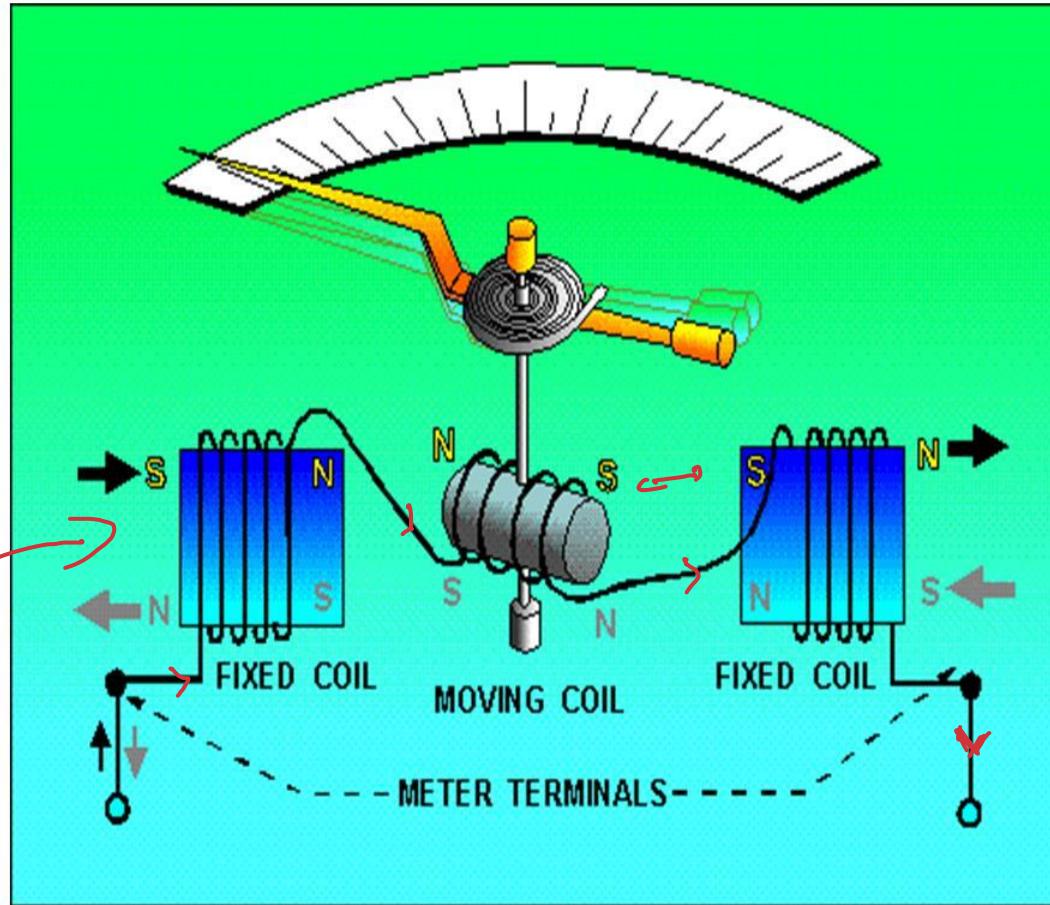
- An ammeter is an instrument designed to measure current; it is placed in series with the circuit element whose current is being measured.
- A voltmeter is an instrument designed to measure voltage; it is placed in parallel with the element whose voltage is being measured.



$$\text{Do not let } v_s \text{ be } 0$$

$$R_A \parallel R_V \text{ for } v_s = 0$$

Magnetic



Application

Example 3.5 & 3.6

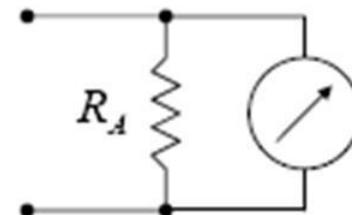
- (a) A 50 mV, 1 mA ammeter with a full scale of 10 mA. Determine R_A .
(b) How much resistance is added to the circuit when the 10 mA meter is inserted to measure current?

ans.:

- (a) Meaning: When 10 mA is to be measured 1 mA will be moving in the coil; accordingly 9 mA will be moving in the R_A .

$$9 \times 10^{-3} R_A = 50 \times 10^{-3} \rightarrow R_A = 50/9 = 5.555 \Omega$$

(b) $R_m = \frac{50 \text{ mV}}{10 \text{ mA}} = 5 \Omega$



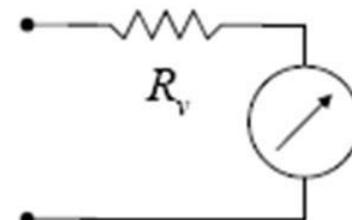
- (a) A 50 mV, 1 mA ammeter with a full scale of 150 V. Determine R_v .
(b) How much resistance is added to the circuit when the 150 V meter is inserted to measure current?

ans.:

(a) $R_{movement} = \frac{50 \text{ mV}}{1 \text{ mA}} = 50 \Omega$, $50 \times 10^{-3} = \frac{50}{R_v + 50} \cdot 150$

$$R_v = 149,950 \Omega$$

(b) $R_m = \frac{150}{10^{-3}} = 150,000 \Omega$



Measuring Resistance-The Wheatstone Bridge

- To find R_x , the value of R_3 is adjusted until there is no current in the meter.

$i_g = 0$ Means balanced bridge.

& $V_{ab} = 0$ "same potential at a as b"

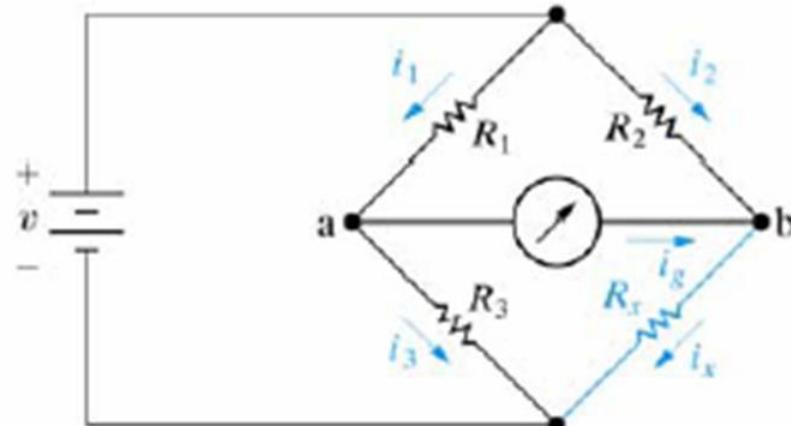
KCL $i_1 = i_3$ & $i_2 = i_x$

KVL $i_3 R_3 = i_x R_x$ & $i_1 R_1 = i_2 R_2$

$$i_1 R_3 = i_2 R_x$$

$$\frac{i_1}{i_2} = \frac{R_2}{R_1} = \frac{R_x}{R_3}$$

$$R_x = \frac{R_2}{R_1} R_3$$



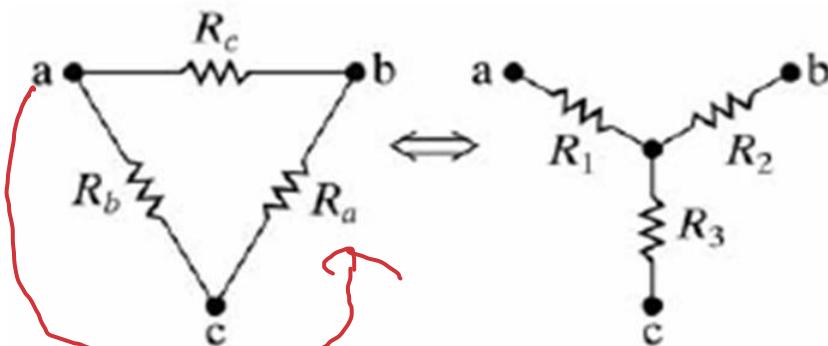
$$V_{R_3} = f R_x$$

$$\frac{V_x R_3}{R_3 + R_1} = \frac{V}{R_2 + R_x}$$

$$\Rightarrow R_x = \frac{R_2 R_3}{R_1}$$

Last Section

The Δ -to-Y transformation (Delta-to-Wye/Pi-to-Tee)



- The resistance between terminals a and b must be the same whether we use Δ -connected set or the Y-connected circuit.

$$R_{ab} = \frac{R_c(R_a + R_b)}{R_a + R_b + R_c} = R_1 + R_2$$

$$R_{bc} = \frac{R_a(R_b + R_c)}{R_a + R_b + R_c} = R_2 + R_3$$

$$R_{ca} = \frac{R_b(R_c + R_a)}{R_a + R_b + R_c} = R_1 + R_3$$

$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}$$

$$R_2 = \frac{R_c R_a}{R_a + R_b + R_c}$$

$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$

$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

$$R_c = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

Example 3.7

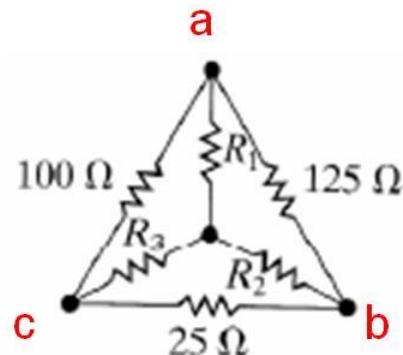
$$R_A = 25, R_B = 10\Omega$$

$$R_C = 125$$

Find the current and power supplied by the 40 V source.

Ans.:

We can convert $\Delta(100, 125, 25 \Omega)$
or $\Delta(25, 40, 37.5 \Omega)$



$$R_1 = \frac{100 \times 125}{100 + 125 + 25} = 50 \Omega$$

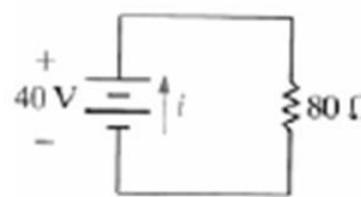
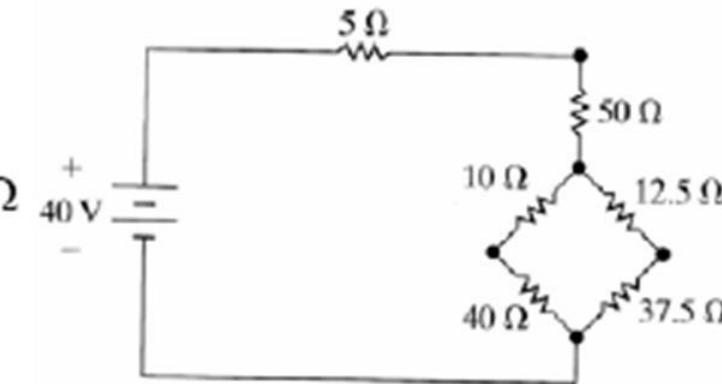
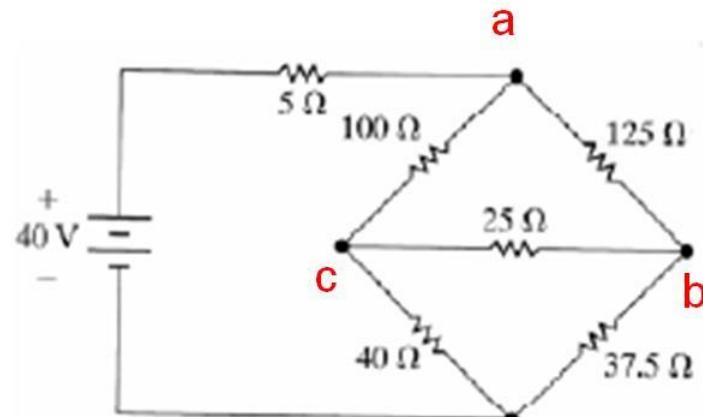
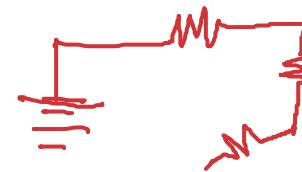
$$R_2 = \frac{125 \times 25}{100 + 125 + 25} = 12.5 \Omega$$

$$R_3 = \frac{100 \times 25}{100 + 125 + 25} = 10 \Omega$$

$$R_{eq} = 5 + 50 + \frac{(10 + 40) \times (12.5 + 37.5)}{(10 + 40) + (12.5 + 37.5)} = 80 \Omega$$

$$i = \frac{40V}{80\Omega} = 0.5 \text{ A}$$

$$P = 0.5 \text{ A} \times 40 \text{ V} = 20 \text{ W}$$



Assessing Objective 6

$$R_1 = 5\Omega, R_2 = 10\Omega, R_3 = 20\Omega$$

Use Y-to-Δ transformation to find v .

Ans.:

$$R_a = \frac{20 \times 10 + 10 \times 5 + 5 \times 20}{5} = 70\Omega$$

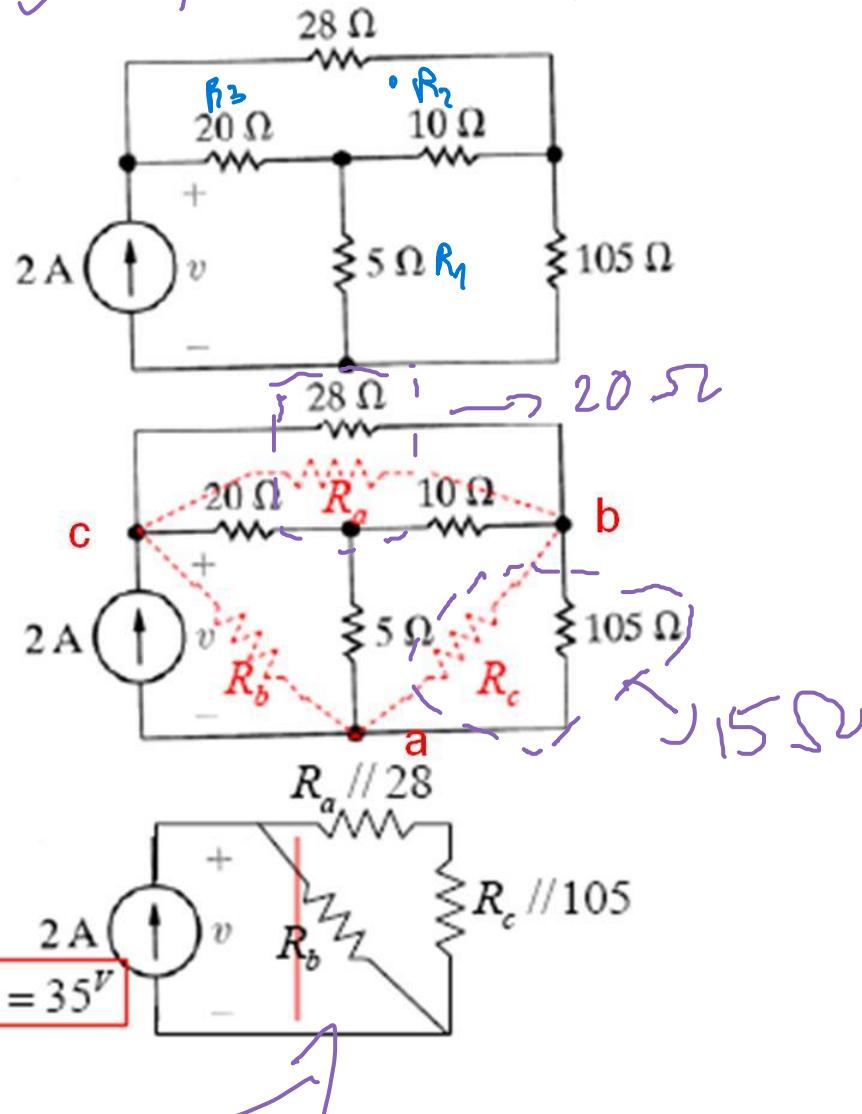
$$R_b = \frac{20 \times 10 + 10 \times 5 + 5 \times 20}{10} = 35\Omega$$

$$R_c = \frac{20 \times 10 + 10 \times 5 + 5 \times 20}{20} = 17.5\Omega$$

$$R_{eq1} = \frac{28 \times 70}{28 + 70} = 20\Omega$$

$$R_{eq2} = \frac{17.5 \times 105}{17.5 + 105} = 15\Omega$$

$$R_{eq3} = \frac{35 \times (20 + 15)}{35 + (20 + 15)} = 17.5\Omega$$



$$v = 2^A \times 17.5\Omega = 35v$$

Problem

$$V_i = V \frac{R_i}{R_{eq}}$$

Select R_1 , R_2 & R_3 in the circuit to meet the following design requirements:

- a) The total power supplied is 36 W.
- b) $v_1 = 12 \text{ V}$, $v_2 = 6 \text{ V}$, and $v_3 = -12 \text{ V}$.

Ans.:-

$$(a) P_{24V} = \frac{V^2}{R_{eq}} = \frac{(24)^2}{R_1 + R_2 + R_3} = 36$$

$$R_1 + R_2 + R_3 = 16 \Omega$$

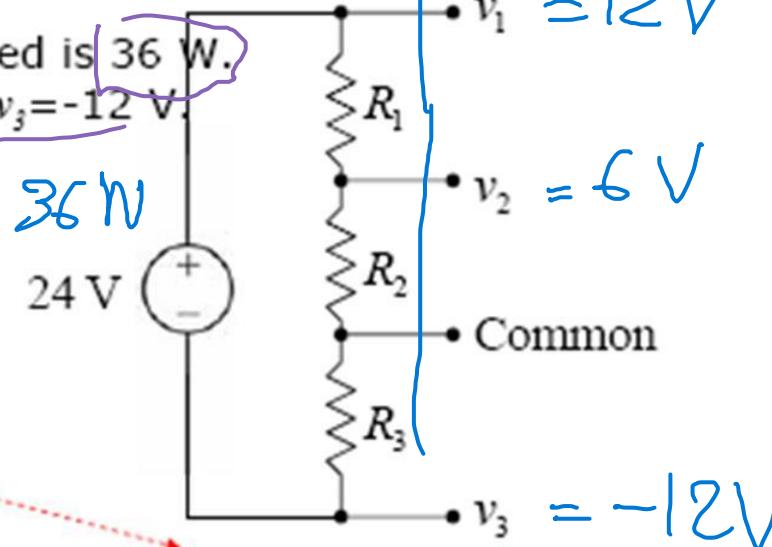
(b) Using Voltage dividers

$$v_1 = 24V \frac{R_1 + R_2}{R_1 + R_2 + R_3} = 12V, R_1 + R_2 = \frac{12}{24} \times (R_1 + R_2 + R_3) = 8 \Omega, R_1 + R_2 = 8 \Omega$$

$$v_2 = 24V \frac{R_2}{R_1 + R_2 + R_3} = 6V, R_2 = \frac{6}{24} \times (R_1 + R_2 + R_3) = 4 \Omega$$

$$v_3 = -24V \frac{R_3}{R_1 + R_2 + R_3} = -12V, R_3 = 8 \Omega$$

In series \rightarrow
 $R_{eq} = 16 \Omega$
 $= 12V$



$$\boxed{R_2 = 4 \Omega}$$

$$\boxed{R_1 = 4 \Omega}$$

Problem

$$i_g = i \frac{R_{eq}}{R_j}$$

Specify the value of the resistors in the circuit to meet the following design criteria: $i_g = 8 \text{ mA}$; $v_g = 4 \text{ V}$, $i_1 = 2i_2$; $i_2 = 10i_3$; and $i_3 = i_4$.

Ans.:-

$$v_g = i_g R_{eq} \quad \left\{ \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} \right.$$

$$4 \text{ V} = 8 \times 10^{-3} \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} \right)$$

$$\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} = 2 \times 10^{-3}$$

$$i_j = \frac{v}{R_j} = \frac{R_{eq}}{R_j} i$$

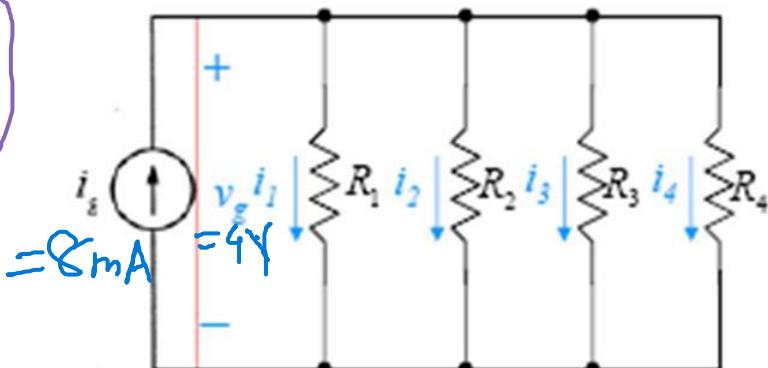
$$i_1 = 2i_2 = \frac{R_{eq}}{R_1} i_g = 2 \frac{R_{eq}}{R_2} i_g, \quad R_2 = 2R_1$$

$$i_2 = 10i_3 \rightarrow R_3 = 10R_2$$

$$i_3 = i_4 \rightarrow R_3 = R_4$$

$$R_1 = 800 \Omega$$

$$R_2 = 1.6 \text{ k}\Omega$$



$$i_g = i \frac{R_{eq}}{R_j}$$

$$\frac{1}{R_1} + \frac{1}{2R_1} + \frac{1}{20R_1} + \frac{1}{20R_1} = \frac{32}{20R_1} = 2 \times 10^{-3}$$

$$R_3 = R_4 = 1.6 \text{ k}\Omega$$

Problem No R in v_o \rightarrow can not use Ohm's law $\frac{300 \times 200}{500}$

Find v_o ?

Ans.: -

Using current dividers

$$i_1 = \frac{200 + 1000}{300 + 300 + 200 + 1000} \times 15 \text{ mA}$$

$$i_1 = 10 \text{ mA}$$

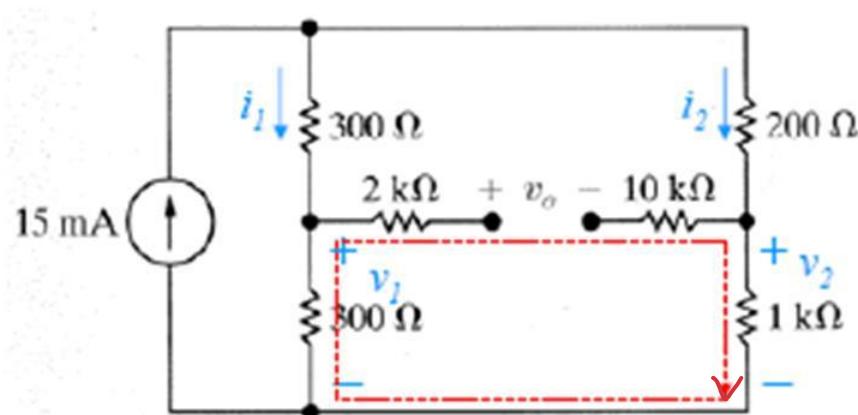
$$i_2 = \frac{300 + 300}{300 + 300 + 200 + 1000} \times 15 \text{ mA}$$

$$i_2 = 5 \text{ mA}$$

$$v_1 = 10 \times 10^{-3} \times 300 = 3 \text{ V}, \quad v_2 = 5 \times 10^{-3} \times 1000 = 5 \text{ V}$$

$$\text{Applying KVL } v_o + v_2 - v_1 = 0 \Rightarrow v_o = v_1 - v_2 = 3 - 5$$

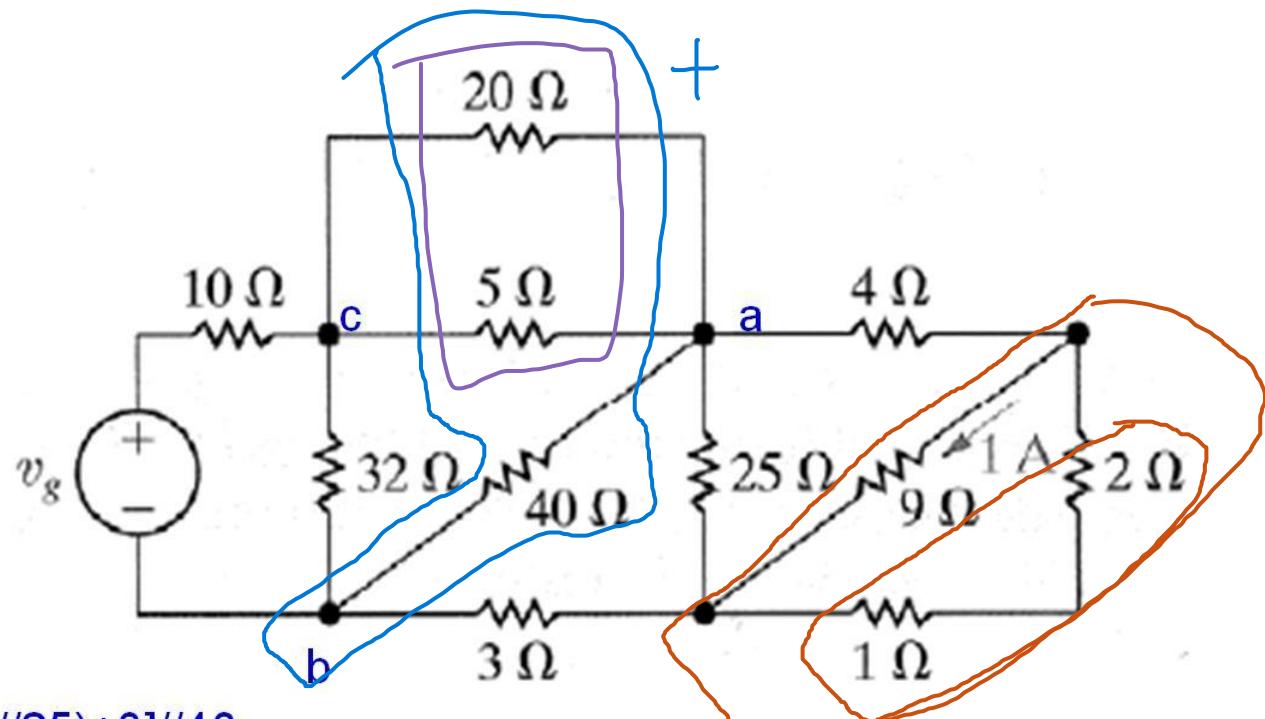
$$v_o = -2 \text{ V}$$



Open circuit $\Rightarrow i = 0$
 $\rightarrow R \rightarrow \infty$

Problem

Find (a) v_g , (b) power dissipated in 20Ω .



$$\begin{aligned}
 V_{9\Omega} &= 9V \rightarrow I_{2,1\Omega} \rightarrow \\
 I_{4\Omega} &\rightarrow V_{25\Omega} \rightarrow I_{25\Omega} \rightarrow \\
 I_{3\Omega} &\rightarrow V_{40\Omega} \rightarrow I_{40\Omega}
 \end{aligned}$$

$$Z_{ab} = [((2+1)/9 + 4) / 25 + 3] / 40$$

$$V_{ab} = V_{40\Omega} = V_{32\Omega} Z_{ab} / (Z_{ab} + 20/5) \rightarrow V_{32\Omega} \rightarrow I_{32\Omega} \rightarrow I_g = I_{40\Omega} + I_{3\Omega} + I_{32\Omega}$$

$$Z_{cb} = (Z_{ab} + (20/5)) / 32 \rightarrow V_g = I_g (10 + Z_{cb}) \rightarrow P_{20\Omega}$$

Problem

- Find v_x when the device in (b) is connected to the circuit.

Ans.:

$$R_{eq1} = \frac{40 \times 10}{40 + 10} = 8 \Omega$$

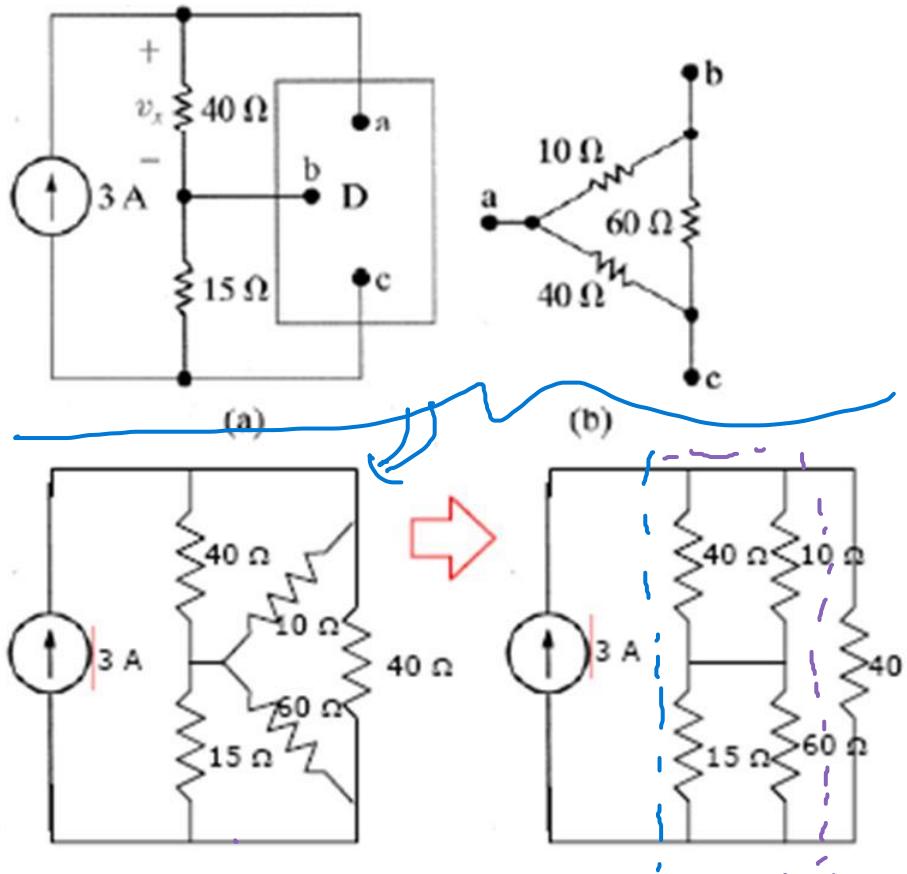
$$R_{eq2} = \frac{60 \times 15}{60 + 15} = 12 \Omega$$

$$R_{eq3} = 8 + 12 = 20 \Omega$$

$$i_{Req3} = 3 \frac{40}{20 + 40} = 2 \text{ A}$$

$$i_{40\Omega} = 2 \frac{10}{10 + 40} = 0.4 \text{ A}$$

$$v_x = 0.4 \times 40 \Omega = 16 \text{ V}$$



$$\frac{20 \times 40}{20 + 40} = 13.33$$

$$V = IR \Leftrightarrow$$

$$R = 20 \Omega$$

Problem


Series


parallel

- Find the resistance seen by the ideal voltage source in the circuit.
- If v_{ab} equals 400 V, how much power is dissipated in the $31\ \Omega$ resistor.

Ans.:

$$R_{eq_{ab}} = 80\ \Omega$$

$$P_{31\Omega} = 279\ \text{W}$$

Convert upper and lower delta circuits to Y circuits, we have a simpler circuit

