Controlling Model Complexity

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Overview

- Introduction
 - BioTech Opportunities of Scale
 - BioTech Firms in Atlanta
- Algorithms and Models
 - Models are Algorithms Fit to Data
 - Model Complexity
 - Example of Model Complexity and Overfitting
- Regularization
 - Control the Complexity
 - Early Stopping
 - Control Model Complexity
 - Introducing Sparsity
 - ElasticNet
- Second Section

BioTech - Opportunities of Scale

- Cost of sequencing a single person's genome \$3 bln 1989 2001 to under \$1k today
- Twelve years to sequence one versus multiple person's genome in under a week
- Sequence DNA from skin cancer tumor versus sequence DNA from skin cells
- Individualized treatments
- Labiotech.eu: "The Robots are Coming: Is AI the Future of Biotech?"

Biotech Firms in Atlanta



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The most promising inventions and discoveries at Georgia's universities often lead to the launch of new companies. GRA Ventures invests in these companies at crucial early-stage points and provides guidance that's essential to new enterprises. Here's what's in the GRA Ventures portfolio right now. More about GRA Ventures >

Sort by research area: Show all Life sciences Technology

3Ti Blood transfusion diagnostics

Abby Med Therapeutics for malignant gliomas Abeome Research reagents Accuitis Pharmaceutica

Models are Algorithms Fit to Data

$$y = f(x) \tag{1}$$

- x called features or independent variables
- \bullet y response variable, predicted quantity, dependent variable dataset

Models are Algorithms Fit to Data

$$y = f(x) \tag{2}$$

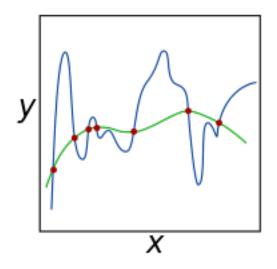
- Use future x data in the model to generate a y
- ullet If y is a set of classes, the problem is called a classification problem
- ullet Otherwise, y is a continuous variable and it's a regression problem
- Separate dataset into training, (validation), test sets, reflecting the characteristics of the undivided dataset

Model Complexity

$$y = f(x) \tag{3}$$

- Parsimonious models
- Computation time for fit determine model parameters from the data
- Choosing hyperparameters free parameters

Example of Model Complexity and Overfitting



• Overfitting - low training error, high test error - lack of generalization

Regularization - Control the Complexity

- Fitting or training a model is an ill-posed problem
- Every model or algorithm requires a fit process to determine unknown parameters
- The fit process is eventually recast as an optimization problem
- Simpler model
- Sparse model
- Basic principle cost function + a complexity penalty

Regularization - Early Stopping

- Regularization in time
- When the model performance doesn't improve on the validation set, stop
- Evaluate once more on test set to estimate generalization error
- Often used with neural networks and tree-based algorithms

Regularization - Control Model Complexity

$$y = f(x) \tag{4}$$

$$y = f(x)$$

$$C(x,y) = \min_{f} \sum_{i=1}^{n} ||f(x_i) - y_i||^2 + \lambda ||f||^2$$
(5)

- All parameters are driven to zero (but not all are non-zero)
- The underlying optimization problem can be solved with minimizers which require first and second derivatives
- These methods are sometimes faster than minizers which do not use gradient information
- There may be explicit matrix solutions

Regularization - Introducing Sparsity

- We want the model to have many hidden parameters zero
- Sometimes use the number of non-zero parameters
- ullet Use the sum of the absolute value $|eta_1+eta_2+\cdots+eta_m|$
- This drives parameters to zero, except for a few
- Correlated features have a few representatives included, the others are not included

Regularization - ElasticNet

$$y = f(x) \tag{6}$$

$$C(x,y) = \min_{f} \sum_{i=1}^{n} \|f(x_i) - y_i\|^2 + \lambda \left(\|f\|^2 + (1-\alpha)\|f\| \right)$$
 (7)

- Use the measures $||.||^2$ and |.| together
- λ and α are hyperparameters that must be chosen via cross-validation or some other method
- Correlated features are assigned equal weights

Table

Treatments	Response 1	Response 2
Treatment 1	0.0003262	0.562
Treatment 2	0.0015681	0.910
Treatment 3	0.0009271	0.296

Table: Table caption

Theorem

Theorem (Mass-energy equivalence)

 $E = mc^2$

Verbatim

Example (Theorem Slide Code)

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\begin{frame}
\frametitle{Theorem}
\begin{theorem}[Mass--energy equivalence]
$E = mc^2$
\end{theorem}
\end{frame}
```

Figure

Uncomment the code on this slide to include your own image from the same directory as the template .TeX file.

Citation

An example of the \cite command to cite within the presentation:

This statement requires citation [Smith, 2012].

References



John Smith (2012)

Title of the publication

Journal Name 12(3), 45 - 678.

The End