

# Matroids And their Graphs

o.mcdonnell4@nuigalway.ie

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**Definition 0.1.** If  $M$  is a matroid, then there exists a bijection from the ground set of  $M_i$  to the ground set of  $M_j$ , such that a set is independent in the first matroid if and only if it is independent in the second matroid, then  $M_i$  and  $M_j$  are said to be isomorphic

## Exercise: 2.4

Let  $E$  be a set,  $\{1, 2, 3\}$  then

i) Show there are exactly eight non-isomorphic matroids on  $E$ . Along with the corresponding Graph of each matroid

**Solution:**

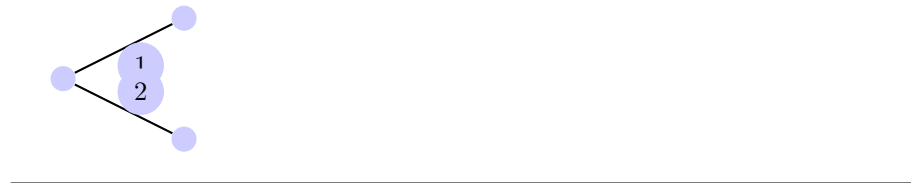
$\{\emptyset\}$



$\{\{\emptyset\}, \{1\}\} \cong \{\{\emptyset\}, \{2\}\} \cong \{\{\emptyset\}, \{3\}\}$



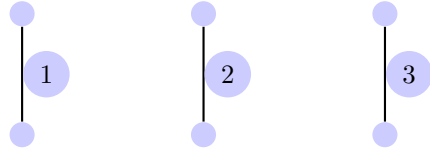
$\{\{\emptyset\}, \{1\}, \{2\}, \{1, 2\}\} \cong \{\{\emptyset\}, \{1\}, \{3\}, \{1, 3\}\} \cong \{\{\emptyset\}, \{2\}, \{3\}, \{2, 3\}\}$



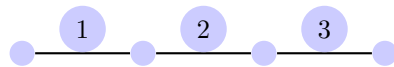
$\{\{\emptyset\}, \{1\}, \{2\}\}$



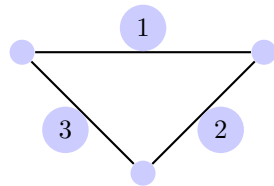
$\{\{\emptyset\}, \{1\}, \{2\}, \{3\}\}$



$\{\{\emptyset\}, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{2, 3\}\}$



$\{\{\emptyset\}, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}\}$



$\{\{\emptyset\}, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}\}$

