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Dinic.cc 1/27

```
// Adjacency list implementation of Dinic's
blocking flow algorithm.
// This is very fast in practice, and only loses
to push-relabel flow.
//
// Running time:
    O(|V|^2 |E|)
// INPUT:
// - graph, constructed using AddEdge()
     - source
// - sink
// OUTPUT:
// - maximum flow value
// - To obtain the actual flow values, look at
all edges with
        capacity > 0 (zero capacity edges are
residual edges).
#include <cmath>
#include <vector>
#include <iostream>
#include <queue>
using namespace std;
const int INF = 2000000000;
struct Edge {
  int from, to, cap, flow, index;
  Edge (int from, int to, int cap, int flow, int
index) :
   from (from), to (to), cap (cap), flow (flow),
index(index) {}
};
```

```
struct Dinic {
  int N;
  vector<vector<Edge> > G;
  vector<Edge *> dad;
  vector<int> Q;
  Dinic(int N) : N(N), G(N), dad(N), Q(N) {}
  void AddEdge(int from, int to, int cap) {
    G[from].push back(Edge(from, to, cap, 0,
G[to].size()));
    if (from == to) G[from].back().index++;
    G[to].push back(Edge(to, from, 0, 0,
G[from].size() - 1));
  long long BlockingFlow(int s, int t) {
    fill(dad.begin(), dad.end(), (Edge *) NULL);
    dad[s] = &G[0][0] - 1;
    int head = 0, tail = 0;
    Q[tail++] = s;
    while (head < tail) {</pre>
      int x = O[head++];
      for (int i = 0; i < G[x].size(); i++) {</pre>
       Edge &e = G[x][i];
       if (!dad[e.to] && e.cap - e.flow > 0) {
          dad[e.to] = &G[x][i];
          Q[tail++] = e.to;
    if (!dad[t]) return 0;
    long long totflow = 0;
    for (int i = 0; i < G[t].size(); i++) {</pre>
      Edge *start = \&G[G[t][i].to][G[t][i].index];
      int amt = INF;
      for (Edge *e = start; amt && e != dad[s]; e
= dad[e->from]) {
       if (!e) { amt = 0; break; }
```

```
amt = min(amt, e->cap - e->flow);
}
if (amt == 0) continue;
for (Edge *e = start; amt && e != dad[s]; e

= dad[e->from]) {
    e->flow += amt;
    G[e->to][e->index].flow -= amt;
}
    totflow += amt;
}
return totflow;
}

long long GetMaxFlow(int s, int t) {
    long long totflow = 0;
    while (long long flow = BlockingFlow(s, t))
        totflow += flow;
    return totflow;
}
};
```

MinCostMaxFlow.cc 2/27

```
// Implementation of min cost max flow algorithm using adjacency  
// matrix (Edmonds and Karp 1972). This  
implementation keeps track of  
// forward and reverse edges separately (so you  
can set cap[i][j] !=  
// cap[j][i]). For a regular max flow, set all  
edge costs to 0.  
//  
// Running time, O(|V|^2) cost per augmentation  
//  
max flow:  
O(|V|^3) augmentations  
//  
MAX_EDGE_COST) augmentations
```

```
- graph, constructed using AddEdge()
       - source
     - sink
// OUTPUT:
// - (maximum flow value, minimum cost value)
       - To obtain the actual flow, look at
positive values only.
#include <cmath>
#include <vector>
#include <iostream>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
typedef long long L;
typedef vector<L> VL;
typedef vector<VL> VVL;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
const L INF = numeric limits<L>::max() / 4;
struct MinCostMaxFlow {
  int N;
  VVL cap, flow, cost;
  VI found;
  VL dist, pi, width;
  VPII dad;
  MinCostMaxFlow(int N) :
    N(N), cap(N, VL(N)), flow(N, VL(N)), cost(N,
VL(N)),
    found(N), dist(N), pi(N), width(N), dad(N) {}
  void AddEdge(int from, int to, L cap, L cost) {
    this->cap[from][to] = cap;
    this->cost[from][to] = cost;
```

// INPUT:

```
void Relax(int s, int k, L cap, L cost, int dir)
   L val = dist[s] + pi[s] - pi[k] + cost;
   if (cap && val < dist[k]) {
     dist[k] = val;
     dad[k] = make pair(s, dir);
     width[k] = min(cap, width[s]);
  L Dijkstra(int s, int t) {
   fill(found.begin(), found.end(), false);
   fill(dist.begin(), dist.end(), INF);
   fill(width.begin(), width.end(), 0);
   dist[s] = 0;
   width[s] = INF;
   while (s !=-1) {
      int best = -1;
     found[s] = true;
     for (int k = 0; k < N; k++) {</pre>
       if (found[k]) continue;
        Relax(s, k, cap[s][k] - flow[s][k],
cost[s][k], 1);
        Relax(s, k, flow[k][s], -\cos t[k][s], -1);
       if (best == -1 || dist[k] < dist[best])</pre>
best = k;
      s = best;
   for (int k = 0; k < N; k++)
     pi[k] = min(pi[k] + dist[k], INF);
   return width[t];
 pair<L, L> GetMaxFlow(int s, int t) {
   L totflow = 0, totcost = 0;
   while (L amt = Dijkstra(s, t)) {
```

```
totflow += amt;
for (int x = t; x != s; x = dad[x].first) {
    if (dad[x].second == 1) {
        flow[dad[x].first][x] += amt;
        totcost += amt * cost[dad[x].first][x];
    } else {
        flow[x][dad[x].first] -= amt;
        totcost -= amt * cost[x][dad[x].first];
    }
}
return make_pair(totflow, totcost);
}
```

PushRelabel.cc 3/27

```
// Adjacency list implementation of FIFO push
relabel maximum flow
// with the gap relabeling heuristic. This
implementation is
// significantly faster than straight Ford-
Fulkerson. It solves
// random problems with 10000 vertices and 1000000
edges in a few
// seconds, though it is possible to construct
test cases that
// achieve the worst-case.
// Running time:
// O(|V|^3)
//
// INPUT:
// - graph, constructed using AddEdge()
    - source
//
      - sink
```

```
// OUTPUT:
// - maximum flow value
                                                            void Enqueue(int v) {
// - To obtain the actual flow values, look at
                                                              if (!active[v] && excess[v] > 0) { active[v] =
all edges with
                                                          true; Q.push(v); }
// capacity > 0 (zero capacity edges are
residual edges).
                                                            void Push(Edge &e) {
#include <cmath>
                                                              int amt = int(min(excess[e.from], LL(e.cap -
#include <vector>
                                                          e.flow)));
#include <iostream>
                                                              if (dist[e.from] <= dist[e.to] || amt == 0)
#include <queue>
                                                          return:
                                                              e.flow += amt;
using namespace std;
                                                              G[e.to][e.index].flow -= amt;
                                                              excess[e.to] += amt;
typedef long long LL;
                                                              excess[e.from] -= amt;
                                                              Enqueue (e.to);
struct Edge {
  int from, to, cap, flow, index;
  Edge (int from, int to, int cap, int flow, int
                                                            void Gap(int k) {
                                                              for (int v = 0; v < N; v++) {</pre>
index):
   from (from), to (to), cap(cap), flow (flow),
                                                                if (dist[v] < k) continue;</pre>
index(index) {}
                                                                count[dist[v]]--;
                                                                dist[v] = max(dist[v], N+1);
};
                                                                count[dist[v]]++;
struct PushRelabel {
                                                                Enqueue (v);
 int N;
                                                              }
 vector<vector<Edge> > G;
 vector<LL> excess;
 vector<int> dist, active, count;
                                                            void Relabel(int v) {
 queue<int> Q;
                                                              count[dist[v]]--;
                                                              dist[v] = 2*N;
                                                              for (int i = 0; i < G[v].size(); i++)</pre>
  PushRelabel(int N) : N(N), G(N), excess(N),
                                                                if (G[v][i].cap - G[v][i].flow > 0)
dist(N), active(N), count(2*N) {}
                                                                  dist[v] = min(dist[v], dist[G[v][i].to] +
 void AddEdge(int from, int to, int cap) {
                                                          1);
   G[from].push back(Edge(from, to, cap, 0,
                                                              count[dist[v]]++;
G[to].size()));
                                                              Enqueue (v);
   if (from == to) G[from].back().index++;
   G[to].push back(Edge(to, from, 0, 0,
G[from].size() - 1));
                                                            void Discharge(int v) {
```

```
for (int i = 0; excess[v] > 0 && i <</pre>
G[v].size(); i++) Push(G[v][i]);
   if (excess[v] > 0) {
      if (count[dist[v]] == 1)
       Gap(dist[v]);
      else
       Relabel(v);
  }
  LL GetMaxFlow(int s, int t) {
    count[0] = N-1;
   count[N] = 1;
   dist[s] = N;
    active[s] = active[t] = true;
   for (int i = 0; i < G[s].size(); i++) {</pre>
      excess[s] += G[s][i].cap;
      Push (G[s][i]);
    while (!Q.empty()) {
      int v = Q.front();
     Q.pop();
      active[v] = false;
     Discharge(v);
   LL totflow = 0;
   for (int i = 0; i < G[s].size(); i++) totflow</pre>
+= G[s][i].flow;
   return totflow;
} ;
```

MinCostMatching.cc 4/27

```
// Min cost bipartite matching via shortest
augmenting paths
// This is an O(n^3) implementation of a shortest
augmenting path
// algorithm for finding min cost perfect
matchings in dense
// graphs. In practice, it solves 1000x1000
problems in around 1
// second.
//
// cost[i][j] = cost for pairing left node i
with right node j
// Lmate[i] = index of right node that left node
i pairs with
// Rmate[j] = index of left node that right node
j pairs with
// The values in cost[i][j] may be positive or
negative. To perform
// maximization, simply negate the cost[][]
#include <algorithm>
#include <cstdio>
#include <cmath>
#include <vector>
using namespace std;
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
double MinCostMatching (const VVD &cost, VI &Lmate,
VI &Rmate) {
  int n = int(cost.size());
```

```
int s = 0;
 // construct dual feasible solution
                                                               while (Lmate[s] != -1) s++;
 VD u(n);
 VD v(n);
                                                               // initialize Dijkstra
 for (int i = 0; i < n; i++) {</pre>
                                                               fill(dad.begin(), dad.end(), -1);
   u[i] = cost[i][0];
                                                               fill(seen.begin(), seen.end(), 0);
   for (int j = 1; j < n; j++) u[i] = min(u[i],
                                                               for (int k = 0; k < n; k++)
                                                                 dist[k] = cost[s][k] - u[s] - v[k];
cost[i][j]);
 }
 for (int j = 0; j < n; j++) {
                                                               int j = 0;
   v[j] = cost[0][j] - u[0];
                                                               while (true) {
   for (int i = 1; i < n; i++) v[j] = min(v[j],
cost[i][j] - u[i]);
                                                                // find closest
                                                                 i = -1;
                                                                 for (int k = 0; k < n; k++) {
                                                                  if (seen[k]) continue;
 // construct primal solution satisfying
complementary slackness
                                                                  if (j == -1 \mid | dist[k] < dist[j]) j = k;
 Lmate = VI(n, -1);
 Rmate = VI(n, -1);
                                                                 seen[j] = 1;
  int mated = 0;
 for (int i = 0; i < n; i++) {</pre>
                                                                 // termination condition
   for (int j = 0; j < n; j++) {
                                                                 if (Rmate[j] == -1) break;
     if (Rmate[j] != -1) continue;
     if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10)</pre>
                                                                 // relax neighbors
                                                                 const int i = Rmate[j];
                                                                 for (int k = 0; k < n; k++) {
       Lmate[i] = j;
                                                                  if (seen[k]) continue;
       Rmate[j] = i;
       mated++;
                                                                   const double new dist = dist[j] +
       break:
                                                           cost[i][k] - u[i] - v[k];
                                                                   if (dist[k] > new dist) {
                                                                    dist[k] = new dist;
                                                                     dad[k] = j;
 VD dist(n);
 VI dad(n);
                                                               }
 VI seen(n);
                                                               // update dual variables
 // repeat until primal solution is feasible
                                                               for (int k = 0; k < n; k++) {</pre>
  while (mated < n) {</pre>
                                                                 if (k == j || !seen[k]) continue;
                                                                 const int i = Rmate[k];
    // find an unmatched left node
                                                                 v[k] += dist[k] - dist[j];
```

```
u[i] -= dist[k] - dist[j];

lu[s] += dist[j];

// augment along path
while (dad[j] >= 0) {
    const int d = dad[j];
    Rmate[j] = Rmate[d];
    Lmate[Rmate[j]] = j;
    j = d;
}
Rmate[j] = s;
Lmate[s] = j;

mated++;
}

double value = 0;
for (int i = 0; i < n; i++)
    value += cost[i][Lmate[i]];

return value;</pre>
```

MaxBipartiteMatching.cc 5/27

```
// This code performs maximum bipartite matching. // // Running time: O(|E| |V|) -- often much faster in practice // INPUT: w[i][j] = edge between row node i and column node j // OUTPUT: mr[i] = assignment for row node i, -1 if unassigned
```

```
mc[j] = assignment for column node j,
-1 if unassigned
//
             function returns number of matches
made
#include <vector>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
bool FindMatch (int i, const VVI &w, VI &mr, VI
&mc, VI &seen) {
 for (int j = 0; j < w[i].size(); j++) {</pre>
    if (w[i][j] && !seen[j]) {
      seen[j] = true;
      if (mc[j] < 0 \mid | FindMatch(mc[j], w, mr, mc,
seen)) {
        mr[i] = j;
        mc[j] = i;
        return true;
  return false;
int BipartiteMatching(const VVI &w, VI &mr, VI
&mc) {
 mr = VI(w.size(), -1);
  mc = VI(w[0].size(), -1);
  int ct = 0;
  for (int i = 0; i < w.size(); i++) {</pre>
   VI seen(w[0].size());
    if (FindMatch(i, w, mr, mc, seen)) ct++;
  return ct;
```

MinCut.cc 6/27

```
// Adjacency matrix implementation of Stoer-Wagner
min cut algorithm.
//
// Running time:
// O(|V|^3)
// INPUT:
// - graph, constructed using AddEdge()
// OUTPUT:
// - (min cut value, nodes in half of min cut)
#include <cmath>
#include <vector>
#include <iostream>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
const int INF = 1000000000;
pair<int, VI> GetMinCut(VVI &weights) {
  int N = weights.size();
 VI used(N), cut, best cut;
  int best weight = -1;
  for (int phase = N-1; phase >= 0; phase--) {
   VI w = weights[0];
   VI added = used;
   int prev, last = 0;
   for (int i = 0; i < phase; i++) {</pre>
     prev = last;
     last = -1:
```

```
for (int j = 1; j < N; j++)
        if (!added[j] && (last == -1 || w[j] >
w[last])) last = j;
      if (i == phase-1) {
       for (int j = 0; j < N; j++)</pre>
weights[prev][j] += weights[last][j];
        for (int j = 0; j < N; j++)
weights[j][prev] = weights[prev][j];
       used[last] = true;
        cut.push back(last);
        if (best weight == -1 || w[last] <</pre>
best weight) {
         best cut = cut;
         best weight = w[last];
      } else {
       for (int j = 0; j < N; j++)
          w[j] += weights[last][j];
       added[last] = true;
  return make pair(best weight, best cut);
```

ConvexHull.cc 7/27

```
// Compute the 2D convex hull of a set of points
using the monotone chain
// algorithm. Eliminate redundant points from the
hull if REMOVE_REDUNDANT is
// #defined.
//
// Running time: O(n log n)
//
// INPUT: a vector of input points, unordered.
```

```
// OUTPUT: a vector of points in the convex
hull, counterclockwise, starting
              with bottommost/leftmost point
#include <cstdio>
#include <cassert>
#include <vector>
#include <algorithm>
#include <cmath>
using namespace std;
#define REMOVE REDUNDANT
typedef double T;
const T EPS = 1e-7;
struct PT {
 T \times, \forall;
 PT() {}
 PT(T x, T y) : x(x), y(y) {}
 bool operator<(const PT &rhs) const { return</pre>
make pair(y,x) < make pair(rhs.y,rhs.x); }</pre>
 bool operator==(const PT &rhs) const { return
make pair(y, x) == make pair(rhs.y, rhs.x); }
T cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
T area2(PT a, PT b, PT c) { return cross(a,b) +
cross(b,c) + cross(c,a); }
#ifdef REMOVE REDUNDANT
bool between (const PT &a, const PT &b, const PT
&c) {
  return (fabs(area2(a,b,c)) < EPS && (a.x-
b.x)*(c.x-b.x) <= 0 && (a.y-b.y)*(c.y-b.y) <= 0);
#endif
void ConvexHull (vector<PT> &pts) {
  sort(pts.begin(), pts.end());
```

```
pts.erase(unique(pts.begin(), pts.end()),
pts.end());
  vector<PT> up, dn;
  for (int i = 0; i < pts.size(); i++) {</pre>
    while (up.size() > 1 \&\& area2(up[up.size()-2],
up.back(), pts[i]) >= 0) up.pop back();
    while (dn.size() > 1 \&\& area2(dn[dn.size()-2],
dn.back(), pts[i]) <= 0) dn.pop back();
    up.push back(pts[i]);
    dn.push back(pts[i]);
  pts = dn;
  for (int i = (int) up.size() - 2; i >= 1; i--)
pts.push back(up[i]);
#ifdef REMOVE REDUNDANT
  if (pts.size() <= 2) return;</pre>
  dn.clear();
  dn.push back(pts[0]);
  dn.push back(pts[1]);
  for (int i = 2; i < pts.size(); i++) {</pre>
    if (between(dn[dn.size()-2], dn[dn.size()-1],
pts[i])) dn.pop back();
    dn.push back(pts[i]);
  if (dn.size() >= 3 \&\& between(dn.back(), dn[0],
dn[1])) {
    dn[0] = dn.back();
    dn.pop back();
  }
  pts = dn;
#endif
```

Geometry.cc 8/27

// C++ routines for computational geometry.

```
return PT(p.x*cos(t)-p.y*sin(t),
#include <iostream>
                                                          p.x*sin(t)+p.y*cos(t));
#include <vector>
#include <cmath>
#include <cassert>
                                                          // project point c onto line through a and b
                                                          // assuming a != b
                                                          PT ProjectPointLine(PT a, PT b, PT c) {
using namespace std;
                                                            return a + (b-a) *dot(c-a, b-a) /dot(b-a, b-a);
double INF = 1e100;
double EPS = 1e-12;
                                                          // project point c onto line segment through a and
struct PT {
                                                          PT ProjectPointSegment(PT a, PT b, PT c) {
  double x, y;
                                                            double r = dot(b-a,b-a);
  PT() {}
  PT(double x, double y) : x(x), y(y) {}
                                                           if (fabs(r) < EPS) return a;</pre>
                                                           r = dot(c-a, b-a)/r;
  PT (const PT &p) : x(p.x), v(p.v)
  PT operator + (const PT &p) const { return
                                                           if (r < 0) return a;</pre>
                                                           if (r > 1) return b;
PT(x+p.x, y+p.y); }
                                                            return a + (b-a)*r;
  PT operator - (const PT &p) const { return
PT(x-p.x, y-p.y); }
  PT operator * (double c)
                               const { return
PT(x*c, y*c);
                                                          // compute distance from c to segment between a
  PT operator / (double c)
                               const { return
                                                          and b
PT(x/c, y/c);
                                                          double DistancePointSegment(PT a, PT b, PT c) {
                                                            return sgrt(dist2(c, ProjectPointSegment(a, b,
} ;
                                                          c)));
double dot (PT p, PT q)
                           return
p.x*q.x+p.y*q.y; }
double dist2(PT p, PT q)
                           { return dot(p-q,p-q);
                                                          // compute distance between point (x,y,z) and
                                                          plane ax+by+cz=d
double cross(PT p, PT q) { return p.x*q.y-
                                                          double DistancePointPlane (double x, double y,
                                                          double z,
p.y*q.x; }
ostream & operator << (ostream & os, const PT & p) {
                                                                                    double a, double b,
  os << "(" << p.x << "," << p.v << ")";
                                                          double c, double d)
                                                            return fabs(a*x+b*v+c*z-d)/sgrt(a*a+b*b+c*c);
// rotate a point CCW or CW around the origin
PT RotateCCW90 (PT p) { return PT (-p.y,p.x); }
PT RotateCW90 (PT p) { return PT (p.y, -p.x); }
                                                          // determine if lines from a to b and c to d are
PT RotateCCW(PT p, double t) {
                                                          parallel or collinear
                                                          bool LinesParallel(PT a, PT b, PT c, PT d) {
```

```
return fabs(cross(b-a, c-d)) < EPS;</pre>
                                                           // compute center of circle given three points
bool LinesCollinear(PT a, PT b, PT c, PT d) {
                                                           PT ComputeCircleCenter(PT a, PT b, PT c) {
  return LinesParallel(a, b, c, d)
                                                             b = (a+b)/2;
                                                             c = (a+c)/2;
      && fabs(cross(a-b, a-c)) < EPS
                                                             return ComputeLineIntersection (b,
      && fabs(cross(c-d, c-a)) < EPS;
                                                           b+RotateCW90(a-b), c, c+RotateCW90(a-c));
}
// determine if line segment from a to b
intersects with
                                                           // determine if point is in a possibly non-convex
// line segment from c to d
                                                           polygon (by William
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
                                                           // Randolph Franklin); returns 1 for strictly
  if (LinesCollinear(a, b, c, d)) {
                                                           interior points, 0 for
    if (dist2(a, c) < EPS || dist2(a, d) < EPS ||</pre>
                                                           // strictly exterior points, and 0 or 1 for the
      dist2(b, c) < EPS \mid | dist2(b, d) < EPS)
                                                           remaining points.
                                                           // Note that it is possible to convert this into
return true;
                                                           an *exact* test using
    if (dot(c-a, c-b) > 0 \&\& dot(d-a, d-b) > 0 \&\&
dot(c-b, d-b) > 0)
                                                           // integer arithmetic by taking care of the
      return false;
                                                           division appropriately
                                                           // (making sure to deal with signs properly) and
    return true;
                                                           then by writing exact
  if (cross(d-a, b-a) * cross(c-a, b-a) > 0)
                                                           // tests for checking point on polygon boundary
return false;
                                                           bool PointInPolygon(const vector<PT> &p, PT q) {
  if (cross(a-c, d-c) * cross(b-c, d-c) > 0)
                                                             bool c = 0;
                                                             for (int i = 0; i < p.size(); i++){</pre>
return false;
                                                               int j = (i+1)%p.size();
  return true;
                                                               if ((p[i].y <= q.y && q.y < p[j].y ||</pre>
                                                                 p[j].y \le q.y \&\& q.y < p[i].y) \&\&
// compute intersection of line passing through a
                                                                 q.x < p[i].x + (p[j].x - p[i].x) * (q.y -
                                                           p[i].y) / (p[j].y - p[i].y)
// with line passing through c and d, assuming
                                                                 c = !c;
that unique
// intersection exists; for segment intersection,
                                                             return c;
check if
// segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d)
                                                           // determine if point is on the boundary of a
                                                           polygon
 b=b-a; d=c-d; c=c-a;
                                                           bool PointOnPolygon(const vector<PT> &p, PT q) {
  assert(dot(b, b) > EPS && dot(d, d) > EPS);
                                                             for (int i = 0; i < p.size(); i++)</pre>
  return a + b*cross(c, d)/cross(b, d);
```

```
if (dist2(ProjectPointSegment(p[i],
p[(i+1) p.size()], q), q) < EPS
     return true;
                                                          // This code computes the area or centroid of a
   return false;
                                                          (possibly nonconvex)
                                                          // polygon, assuming that the coordinates are
                                                          listed in a clockwise or
                                                          // counterclockwise fashion. Note that the
// compute intersection of line through points a
and b with
                                                          centroid is often known as
// circle centered at c with radius r > 0
                                                          // the "center of gravity" or "center of mass".
vector<PT> CircleLineIntersection(PT a, PT b, PT
                                                          double ComputeSignedArea(const vector<PT> &p) {
                                                            double area = 0;
c, double r) {
 vector<PT> ret;
                                                            for(int i = 0; i < p.size(); i++) {</pre>
                                                               int j = (i+1) % p.size();
 b = b-a;
 a = a-c;
                                                               area += p[i].x*p[j].y - p[j].x*p[i].y;
 double A = dot(b, b);
 double B = dot(a, b);
                                                            return area / 2.0;
 double C = dot(a, a) - r*r;
 double D = B*B - A*C;
 if (D < -EPS) return ret;</pre>
                                                          double ComputeArea(const vector<PT> &p) {
  ret.push back(c+a+b*(-B+sqrt(D+EPS))/A);
                                                            return fabs(ComputeSignedArea(p));
 if (D > EPS)
   ret.push back(c+a+b*(-B-sqrt(D))/A);
  return ret;
                                                          PT ComputeCentroid(const vector<PT> &p) {
                                                            PT c(0,0);
                                                            double scale = 6.0 * ComputeSignedArea(p);
// compute intersection of circle centered at a
                                                            for (int i = 0; i < p.size(); i++) {</pre>
with radius r
                                                               int j = (i+1) % p.size();
// with circle centered at b with radius R
                                                               c = c + (p[i]+p[j])*(p[i].x*p[j].y -
vector<PT> CircleCircleIntersection(PT a, PT b,
                                                          p[j].x*p[i].y);
double r, double R) {
  vector<PT> ret;
                                                            return c / scale;
 double d = sqrt(dist2(a, b));
 if (d > r+R \mid \mid d+min(r, R) < max(r, R)) return
                                                          // tests whether or not a given polygon (in CW or
  double x = (d*d-R*R+r*r)/(2*d);
                                                          CCW order) is simple
 double y = sqrt(r*r-x*x);
                                                          bool IsSimple(const vector<PT> &p) {
                                                            for (int i = 0; i < p.size(); i++) {</pre>
 PT v = (b-a)/d;
 ret.push back(a+v*x + RotateCCW90(v)*y);
                                                              for (int k = i+1; k < p.size(); k++) {</pre>
 if (y > 0)
                                                                 int j = (i+1) % p.size();
   ret.push back(a+v*x - RotateCCW90(v)*y);
                                                                 int l = (k+1) % p.size();
  return ret;
                                                                if (i == 1 || j == k) continue;
```

```
if (SegmentsIntersect(p[i], p[j], p[k],
                                                                   << LinesParallel(PT(1,1), PT(3,5), PT(5,9),
                                                            PT(7,13)) << endl;
p[1]))
        return false;
                                                              // expected: 0 0 1
                                                              cerr << LinesCollinear(PT(1,1), PT(3,5),</pre>
 return true;
                                                            PT(2,1), PT(4,5)) << " "
                                                                   << LinesCollinear(PT(1,1), PT(3,5),
                                                            PT(2,0), PT(4,5)) << " "
int main() {
                                                                   << LinesCollinear(PT(1,1), PT(3,5),
                                                            PT(5,9), PT(7,13)) << endl;
 // expected: (-5,2)
 cerr << RotateCCW90(PT(2,5)) << endl;</pre>
                                                             // expected: 1 1 1 0
                                                              cerr << SegmentsIntersect(PT(0,0), PT(2,4),</pre>
 // expected: (5,-2)
                                                            PT(3,1), PT(-1,3)) << " "
 cerr << RotateCW90(PT(2,5)) << endl;</pre>
                                                                    << SegmentsIntersect(PT(0,0), PT(2,4),
                                                            PT(4,3), PT(0,5)) << " "
 // expected: (-5,2)
                                                                   << SegmentsIntersect(PT(0,0), PT(2,4),
                                                            PT(2,-1), PT(-2,1)) << " "
 cerr << RotateCCW(PT(2,5),M PI/2) << endl;</pre>
                                                                    << SegmentsIntersect(PT(0,0), PT(2,4),
 // expected: (5,2)
                                                            PT(5,5), PT(1,7)) << endl;
  cerr << ProjectPointLine(PT(-5,-2), PT(10,4),</pre>
PT(3,7)) << endl;
                                                              // expected: (1,2)
                                                              cerr << ComputeLineIntersection(PT(0,0),</pre>
                                                            PT(2,4), PT(3,1), PT(-1,3)) << endl;
 // expected: (5,2) (7.5,3) (2.5,1)
 cerr << ProjectPointSegment(PT(-5,-2), PT(10,4),</pre>
PT(3,7)) << " "
                                                              // expected: (1,1)
                                                              cerr << ComputeCircleCenter(PT(-3,4), PT(6,1),</pre>
       << ProjectPointSegment(PT(7.5,3), PT(10,4),</pre>
PT(3,7)) << " "
                                                            PT(4,5)) << endl;
       << ProjectPointSegment(PT(-5,-2),</pre>
PT(2.5,1), PT(3,7)) << endl;
                                                              vector<PT> v;
                                                              v.push back(PT(0,0));
 // expected: 6.78903
                                                              v.push back(PT(5,0));
 cerr << DistancePointPlane(4,-4,3,2,-2,5,-8) <<</pre>
                                                              v.push back(PT(5,5));
                                                              v.push back(PT(0,5));
endl;
 // expected: 1 0 1
                                                              // expected: 1 1 1 0 0
                                                              cerr << PointInPolygon(v, PT(2,2)) << " "</pre>
 cerr \ll LinesParallel(PT(1,1), PT(3,5), PT(2,1),
                                                                   << PointInPolygon(v, PT(2,0)) << " "
PT(4,5)) << " "
                                                                    << PointInPolygon(v, PT(0,2)) << " "
       << LinesParallel(PT(1,1), PT(3,5), PT(2,0),
PT(4,5)) << " "
                                                                    << PointInPolygon(v, PT(5,2)) << " "
                                                                   << PointInPolygon(v, PT(2,5)) << endl;
```

```
// expected: 0 1 1 1 1
  cerr << PointOnPolygon(v, PT(2,2)) << " "</pre>
       << PointOnPolygon(v, PT(2,0)) << " "
       << PointOnPolygon(v, PT(0,2)) << " "
       << PointOnPolygon(v, PT(5,2)) << " "
       << PointOnPolygon(v, PT(2,5)) << endl;
 // expected: (1,6)
               (5,4) (4,5)
 //
               blank line
              (4,5) (5,4)
  //
               blank line
              (4,5) (5,4)
 vector<PT> u = CircleLineIntersection(PT(0,6),
PT(2,6), PT(1,1), 5);
 for (int i = 0; i < u.size(); i++) cerr << u[i]</pre>
<< " "; cerr << endl;
  u = CircleLineIntersection(PT(0,9), PT(9,0),
PT(1,1), 5);
  for (int i = 0; i < u.size(); i++) cerr << u[i]</pre>
<< " "; cerr << endl;
 u = CircleCircleIntersection(PT(1,1), PT(10,10),
  for (int i = 0; i < u.size(); i++) cerr << u[i]</pre>
<< " "; cerr << endl;
 u = CircleCircleIntersection(PT(1,1), PT(8,8),
  for (int i = 0; i < u.size(); i++) cerr << u[i]</pre>
<< " "; cerr << endl;
 u = CircleCircleIntersection(PT(1,1),
PT(4.5, 4.5), 10, sqrt(2.0)/2.0);
  for (int i = 0; i < u.size(); i++) cerr << u[i]</pre>
<< " "; cerr << endl;
 u = CircleCircleIntersection(PT(1,1),
PT(4.5,4.5), 5, sqrt(2.0)/2.0);
  for (int i = 0; i < u.size(); i++) cerr << u[i]</pre>
<< " "; cerr << endl;
 // area should be 5.0
 // centroid should be (1.1666666, 1.166666)
```

```
PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5)
};

vector<PT> p(pa, pa+4);
PT c = ComputeCentroid(p);
cerr << "Area: " << ComputeArea(p) << endl;
cerr << "Centroid: " << c << endl;

return 0;
}</pre>
```

JavaGeometry.java 9/27

```
// In this example, we read an input file
containing three lines, each
// containing an even number of doubles, separated
by commas. The first two
// lines represent the coordinates of two
polygons, given in counterclockwise
// (or clockwise) order, which we will call "A"
and "B". The last line
// contains a list of points, p[1], p[2], ...
// Our goal is to determine:
// (1) whether B - A is a single closed shape
(as opposed to multiple shapes)
// (2) the area of B - A
// (3) whether each p[i] is in the interior of B
- A
//
// INPUT:
// 0 0 10 0 0 10
// 0 0 10 10 10 0
    8 6
// 5 1
// OUTPUT:
    The area is singular.
    The area is 25.0
```

```
// Point belongs to the area.
                                                                  return Math.abs(area)/2;
// Point does not belong to the area.
import java.util.*;
                                                              // compute the area of an Area object
import java.awt.geom.*;
                                                          containing several disjoint polygons
import java.io.*;
                                                              static double computeArea(Area area) {
                                                                  double totArea = 0;
                                                                  PathIterator iter =
public class JavaGeometry {
                                                          area.getPathIterator(null);
                                                                  ArrayList<Point2D.Double> points = new
   // make an array of doubles from a string
   static double[] readPoints(String s) {
                                                          ArrayList<Point2D.Double>();
        String[] arr = s.trim().split("\s++");
        double[] ret = new double[arr.length];
                                                                  while (!iter.isDone()) {
        for (int i = 0; i < arr.length; i++)</pre>
                                                                      double[] buffer = new double[6];
                                                                      switch (iter.currentSegment(buffer)) {
ret[i] = Double.parseDouble(arr[i]);
       return ret;
                                                                      case PathIterator.SEG MOVETO:
                                                                      case PathIterator.SEG LINETO:
                                                                          points.add(new
                                                          Point2D.Double(buffer[0], buffer[1]));
   // make an Area object from the coordinates of
a polygon
                                                                          break:
   static Area makeArea(double[] pts) {
                                                                      case PathIterator.SEG CLOSE:
        Path2D.Double p = new Path2D.Double();
                                                                          totArea +=
        p.moveTo(pts[0], pts[1]);
                                                          computePolygonArea(points);
        for (int i = 2; i < pts.length; i += 2)</pre>
                                                                          points.clear();
                                                                          break;
p.lineTo(pts[i], pts[i+1]);
        p.closePath();
       return new Area(p);
                                                                      iter.next();
                                                                  return totArea;
   // compute area of polygon
   static double
computePolygonArea(ArrayList<Point2D.Double>
                                                              // notice that the main() throws an Exception
points) {
                                                          -- necessary to
        Point2D.Double[] pts = points.toArray(new
                                                              // avoid wrapping the Scanner object for file
                                                          reading in a
Point2D.Double[points.size()]);
        double area = 0;
                                                              // try { ... } catch block.
        for (int i = 0; i < pts.length; i++) {</pre>
                                                              public static void main(String args[]) throws
            int j = (i+1) % pts.length;
                                                          Exception {
            area += pts[i].x * pts[j].y - pts[j].x
* pts[i].y;
                                                                  Scanner scanner = new Scanner (new
                                                          File("input.txt"));
```

```
// also,
       // Scanner scanner = new Scanner
(System.in);
       double[] pointsA =
readPoints(scanner.nextLine());
       double[] pointsB =
readPoints(scanner.nextLine());
       Area areaA = makeArea(pointsA);
       Area areaB = makeArea(pointsB);
       areaB.subtract(areaA);
       // also,
       // areaB.exclusiveOr (areaA);
       // areaB.add (areaA);
       // areaB.intersect (areaA);
       // (1) determine whether B - A is a single
closed shape (as
              opposed to multiple shapes)
       boolean isSingle = areaB.isSingular();
       // also,
       // areaB.isEmpty();
       if (isSingle)
           System.out.println("The area is
singular.");
       else
           System.out.println("The area is not
singular.");
       // (2) compute the area of B - A
       System.out.println("The area is " +
computeArea(areaB) + ".");
       // (3) determine whether each p[i] is in
the interior of B - A
       while (scanner.hasNextDouble()) {
           double x = scanner.nextDouble();
           assert(scanner.hasNextDouble());
           double y = scanner.nextDouble();
```

```
if (areaB.contains(x,y)) {
                System.out.println ("Point belongs
to the area.");
                System.out.println ("Point does
not belong to the area.");
        // Finally, some useful things we didn't
use in this example:
       //
        // Ellipse2D.Double ellipse = new
Ellipse2D.Double (double x, double y,
        //
double w, double h);
        //
               creates an ellipse inscribed in box
        //
with bottom-left corner (x,y)
               and upper-right corner (x+y,w+h)
        // Rectangle2D.Double rect = new
Rectangle2D.Double (double x, double y,
double w, double h);
        //
        // creates a box with bottom-left
corner (x,y) and upper-right
               corner (x+y, w+h)
        // Each of these can be embedded in an
Area object (e.g., new Area (rect)).
```

Geom3D.java 10/27

```
public class Geom3D {
  // distance from point (x, y, z) to plane aX +
bY + cZ + d = 0
 public static double ptPlaneDist(double x,
double y, double z,
      double a, double b, double c, double d) {
   return Math.abs(a*x + b*y + c*z + d) /
Math.sqrt(a*a + b*b + c*c);
 }
 // distance between parallel planes aX + bY + cZ
+ d1 = 0 and
 // aX + bY + cZ + d2 = 0
 public static double planePlaneDist(double a,
double b, double c,
     double d1, double d2) {
   return Math.abs(d1 - d2) / Math.sqrt(a*a + b*b
+ c*c);
 }
  // distance from point (px, py, pz) to line (x1,
y1, z1) - (x2, y2, z2)
 // (or ray, or segment; in the case of the ray,
the endpoint is the
  // first point)
  public static final int LINE = 0;
  public static final int SEGMENT = 1;
  public static final int RAY = 2;
  public static double ptLineDistSq(double x1,
double y1, double z1,
      double x2, double y2, double z2, double px,
double py, double pz,
      int type) {
    double pd2 = (x1-x2)*(x1-x2) + (y1-y2)*(y1-y2)
+ (z1-z2)*(z1-z2);
   double x, y, z;
   if (pd2 == 0) {
     x = x1;
     y = y1;
      z = z1;
```

```
} else {
      double u = ((px-x1)*(x2-x1) + (py-y1)*(y2-x1)
y1) + (pz-z1)*(z2-z1)) / pd2;
    x = x1 + u * (x2 - x1);
    y = y1 + u * (y2 - y1);
    z = z1 + u * (z2 - z1);
    if (type != LINE && u < 0) {
      x = x1;
       y = y1;
        z = z1;
     if (type == SEGMENT && u > 1.0) {
      x = x2;
      y = y2;
        z = z2;
    }
    return (x-px) * (x-px) + (y-py) * (y-py) + (z-
pz)*(z-pz);
  public static double ptLineDist(double x1,
double v1, double z1,
      double x2, double y2, double z2, double px,
double py, double pz,
      int type) {
    return Math.sqrt(ptLineDistSq(x1, y1, z1, x2,
y2, z2, px, py, pz, type));
```

Delaunay.cc 11/27

```
// Slow but simple Delaunay triangulation. Does
not handle
// degenerate cases (from O'Rourke, Computational
Geometry in C)
```

```
double zn = (x[j]-x[i])*(y[k]-
// Running time: O(n^4)
                                                           y[i]) - (x[k]-x[i])*(y[j]-y[i]);
                                                                               bool flag = zn < 0;</pre>
// INPUT: x[] = x-coordinates
                                                                               for (int m = 0; flag && m < n;</pre>
            v[] = v-coordinates
                                                           m++)
                                                                                   flag = flag && ((x[m] -
// OUTPUT: triples = a vector containing m
                                                           x[i])*xn +
triples of indices
                                                                                                   (y[m]-
//
                       corresponding to triangle
                                                           y[i])*yn +
vertices
                                                                                                   (z[m]-
                                                           z[i])*zn <= 0);
#include<vector>
                                                                               if (flag)
using namespace std;
                                                           ret.push back(triple(i, j, k));
typedef double T;
struct triple {
                                                                   return ret;
   int i, j, k;
   triple() {}
   triple(int i, int j, int k) : i(i), j(j), k(k)
                                                           int main()
{ }
} ;
                                                               T xs[]={0, 0, 1, 0.9};
                                                               T ys[]=\{0, 1, 0, 0.9\};
vector<triple> delaunayTriangulation(vector<T>& x,
                                                               vector<T> x(&xs[0], &xs[4]), y(&ys[0],
vector<T>& y) {
                                                           &ys[4]);
       int n = x.size();
                                                               vector<triple> tri = delaunayTriangulation(x,
       vector < T > z(n);
                                                           y);
       vector<triple> ret;
                                                               //expected: 0 1 3
       for (int i = 0; i < n; i++)</pre>
                                                               // 0 3 2
            z[i] = x[i] * x[i] + y[i] * y[i];
                                                               int i;
       for (int i = 0; i < n-2; i++) {</pre>
                                                               for(i = 0; i < tri.size(); i++)</pre>
            for (int j = i+1; j < n; j++) {</pre>
                                                                   printf("%d %d %d\n", tri[i].i, tri[i].j,
               for (int k = i+1; k < n; k++) {</pre>
                                                           tri[i].k);
                    if (j == k) continue;
                                                               return 0;
                    double xn = (y[j]-y[i])*(z[k]-
z[i]) - (y[k]-y[i])*(z[j]-z[i]);
                    double yn = (x[k]-x[i])*(z[j]-
z[i]) - (x[j]-x[i])*(z[k]-z[i]);
```

Euclid.cc 12/27

```
// This is a collection of useful code for solving
problems that
// involve modular linear equations. Note that
all of the
// algorithms described here work on nonnegative
integers.
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int,int> PII;
// return a % b (positive value)
int mod(int a, int b) {
  return ((a%b)+b)%b;
// computes gcd(a,b)
int gcd(int a, int b) {
 int tmp;
 while(b) {a%=b; tmp=a; a=b; b=tmp;}
 return a;
// computes lcm(a,b)
int lcm(int a, int b) {
 return a/gcd(a,b)*b;
// returns d = \gcd(a,b); finds x,y such that d =
int extended euclid(int a, int b, int &x, int &y)
```

```
int xx = y = 0;
  int yy = x = 1;
  while (b) {
    int q = a/b;
   int t = b; b = a%b; a = t;
   t = xx; xx = x-q*xx; x = t;
    t = yy; yy = y-q*yy; y = t;
  return a;
// finds all solutions to ax = b \pmod{n}
VI modular linear equation solver(int a, int b,
int n) {
 int x, y;
  VI solutions;
  int d = extended euclid(a, n, x, y);
 if (!(b%d)) {
   x = mod (x*(b/d), n);
   for (int i = 0; i < d; i++)</pre>
      solutions.push back(mod(x + i*(n/d), n));
  return solutions;
// computes b such that ab = 1 \pmod{n}, returns -1
on failure
int mod inverse(int a, int n) {
 int x, y;
  int d = extended euclid(a, n, x, y);
 if (d > 1) return -1;
 return mod(x,n);
// Chinese remainder theorem (special case): find
z such that
// z % x = a, z % y = b. Here, z is unique modulo
M = 1cm(x,y).
// Return (z,M). On failure, M=-1.
PII chinese_remainder_theorem(int x, int a, int y,
```

```
int s, t;
  int d = extended euclid(x, y, s, t);
  if (a%d != b%d) return make pair(0, -1);
  return make pair(mod(s*b*x+t*a*y,x*y)/d, x*y/d);
// Chinese remainder theorem: find z such that
// z % x[i] = a[i] for all i. Note that the
solution is
// unique modulo M = lcm i (x[i]). Return (z,M).
// failure, M = -1. Note that we do not require
the a[i]'s
// to be relatively prime.
PII chinese remainder theorem(const VI &x, const
VI &a) {
 PII ret = make pair(a[0], x[0]);
 for (int i = 1; i < x.size(); i++) {</pre>
   ret = chinese remainder theorem (ret.second,
ret.first, x[i], a[i]);
   if (ret.second == -1) break;
 }
 return ret;
// computes x and y such that ax + by = c; on
failure, x = y = -1
void linear diophantine (int a, int b, int c, int
&x, int &y) {
 int d = gcd(a,b);
 if (c%d) {
  x = y = -1;
  } else {
   x = c/d * mod inverse(a/d, b/d);
   y = (c-a*x)/b;
int main() {
 // expected: 2
```

```
cout << gcd(14, 30) << endl;
  // expected: 2 -2 1
  int x, y;
  int d = \text{extended euclid}(14, 30, x, y);
  cout << d << " " << x << " " << y << endl;
  // expected: 95 45
  VI sols = modular linear equation solver(14, 30,
100);
  for (int i = 0; i < (int) sols.size(); i++) cout</pre>
<< sols[i] << " ";
  cout << endl;</pre>
  // expected: 8
  cout << mod inverse(8, 9) << endl;</pre>
  // expected: 23 56
                11 12
  int xs[] = {3, 5, 7, 4, 6};
  int as[] = \{2, 3, 2, 3, 5\};
  PII ret = chinese remainder theorem(VI (xs,
xs+3), VI(as, as+3));
  cout << ret.first << " " << ret.second << endl;</pre>
  ret = chinese remainder theorem (VI(xs+3, xs+5),
VI(as+3, as+5));
  cout << ret.first << " " << ret.second << endl;</pre>
  // expected: 5 -15
  linear diophantine (7, 2, 5, x, y);
  cout << x << " " << y << endl;
```

GaussJordan.cc 13/27

```
// Gauss-Jordan elimination with full pivoting.
//
```

```
// Uses:
                                                                   if (pj == -1 || fabs(a[j][k]) >
// (1) solving systems of linear equations
                                                           fabs (a[pj][pk])) \{ pj = j; pk = k; \}
(AX=B)
                                                               if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix</pre>
// (2) inverting matrices (AX=I)
                                                           is singular." << endl; exit(0); }</pre>
// (3) computing determinants of square matrices
                                                               ipiv[pk]++;
                                                               swap(a[pj], a[pk]);
// Running time: O(n^3)
                                                               swap(b[pj], b[pk]);
                                                               if (pj != pk) det *= -1;
// INPUT: a[][] = an nxn matrix
                                                               irow[i] = pj;
//
             b[][] = an nxm matrix
                                                               icol[i] = pk;
// OUTPUT: X = an nxm matrix (stored in
                                                               T c = 1.0 / a[pk][pk];
                                                               det *= a[pk][pk];
b[][])
            A^{-1} = an nxn matrix (stored in
                                                               a[pk][pk] = 1.0;
//
                                                               for (int p = 0; p < n; p++) a[pk][p] *= c;</pre>
a[][])
                                                               for (int p = 0; p < m; p++) b[pk][p] *= c;</pre>
//
            returns determinant of a[][]
                                                               for (int p = 0; p < n; p++) if (p != pk) {
#include <iostream>
                                                                 c = a[p][pk];
#include <vector>
                                                                 a[p][pk] = 0;
#include <cmath>
                                                                 for (int q = 0; q < n; q++) a[p][q] -=</pre>
                                                           a[pk][q] * c;
                                                                 for (int q = 0; q < m; q++) b[p][q] -=</pre>
using namespace std;
                                                           b[pk][q] * c;
const double EPS = 1e-10;
                                                             }
typedef vector<int> VI;
typedef double T;
                                                             for (int p = n-1; p >= 0; p--) if (irow[p] !=
typedef vector<T> VT;
                                                           icol[p]) {
typedef vector<VT> VVT;
                                                               for (int k = 0; k < n; k++)
                                                           swap(a[k][irow[p]], a[k][icol[p]]);
T GaussJordan(VVT &a, VVT &b) {
  const int n = a.size();
  const int m = b[0].size();
                                                            return det;
 VI irow(n), icol(n), ipiv(n);
  T \det = 1;
                                                           int main() {
                                                             const int n = 4;
 for (int i = 0; i < n; i++) {</pre>
    int pj = -1, pk = -1;
                                                             const int m = 2;
   for (int j = 0; j < n; j++) if (!ipiv[j])</pre>
                                                             double A[n][n] = {
      for (int k = 0; k < n; k++) if (!ipiv[k])</pre>
                                                           \{1,2,3,4\},\{1,0,1,0\},\{5,3,2,4\},\{6,1,4,6\}\};
                                                             double B[n][m] = \{ \{1,2\}, \{4,3\}, \{5,6\}, \{8,7\} \};
```

```
VVT a(n), b(n);
  for (int i = 0; i < n; i++) {</pre>
   a[i] = VT(A[i], A[i] + n);
   b[i] = VT(B[i], B[i] + m);
 double det = GaussJordan(a, b);
 // expected: 60
 cout << "Determinant: " << det << endl;</pre>
 // expected: -0.233333 0.166667 0.133333
0.0666667
 //
               0.166667 0.166667 0.333333 -
0.333333
 //
              0.233333 0.833333 -0.133333 -
0.0666667
              0.05 -0.75 -0.1 0.2
 cout << "Inverse: " << endl;</pre>
 for (int i = 0; i < n; i++) {</pre>
   for (int j = 0; j < n; j++)
      cout << a[i][j] << ' ';
   cout << endl;</pre>
 // expected: 1.63333 1.3
 //
              -0.166667 0.5
 //
               2.36667 1.7
               -1.85 -1.35
  cout << "Solution: " << endl;</pre>
  for (int i = 0; i < n; i++) {</pre>
   for (int j = 0; j < m; j++)
      cout << b[i][i] << ' ';
   cout << endl;</pre>
 }
```

ReducedRowEchelonForm.cc 14/27

```
// Reduced row echelon form via Gauss-Jordan
elimination
// with partial pivoting. This can be used for
computing
// the rank of a matrix.
// Running time: O(n^3)
//
// INPUT: a[][] = an nxn matrix
// OUTPUT: rref[][] = an nxm matrix (stored in
a[][])
           returns rank of a[][]
#include <iostream>
#include <vector>
#include <cmath>
using namespace std;
const double EPSILON = 1e-10;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
int rref(VVT &a) {
 int n = a.size();
  int m = a[0].size();
  int r = 0;
  for (int c = 0; c < m && r < n; c++) {
    int j = r;
    for (int i = r+1; i < n; i++)</pre>
      if (fabs(a[i][c]) > fabs(a[j][c])) j = i;
    if (fabs(a[j][c]) < EPSILON) continue;</pre>
```

```
swap(a[j], a[r]);
                  T s = 1.0 / a[r][c];
                  for (int j = 0; j < m; j++) a[r][j] *= s;</pre>
                  for (int i = 0; i < n; i++) if (i != r) {</pre>
                           T t = a[i][c];
                           for (int j = 0; j < m; j++) a[i][j] -= t *</pre>
a[r][j];
               }
                  r++;
        return r;
int main() {
          const int n = 5;
         const int m = 4;
         double A[n][m] = {
\{16, 2, 3, 13\}, \{5, 11, 10, 8\}, \{9, 7, 6, 12\}, \{4, 14, 15, 1\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{13, 13\}, \{
,21,21,13} };
        VVT a(n);
        for (int i = 0; i < n; i++)</pre>
                  a[i] = VT(A[i], A[i] + n);
         int rank = rref (a);
         // expected: 4
         cout << "Rank: " << rank << endl;</pre>
         // expected: 1 0 0 1
                                                                  0 1 0 3
                                                                   0 0 1 -3
                                                                      0 0 0 2.78206e-15
                                                                   0 0 0 3.22398e-15
          cout << "rref: " << endl;</pre>
          for (int i = 0; i < 5; i++) {
                  for (int j = 0; j < 4; j++)
                           cout << a[i][j] << ' ';
                  cout << endl;</pre>
          }
```

FFT_new.cpp 15/27

```
#include <cassert>
#include <cstdio>
#include <cmath>
struct cpx
 cpx(){}
 cpx(double aa):a(aa){}
 cpx (double aa, double bb):a(aa),b(bb) {}
 double a;
 double b;
 double modsq(void) const
   return a * a + b * b;
  cpx bar (void) const
    return cpx(a, -b);
};
cpx operator +(cpx a, cpx b)
 return cpx(a.a + b.a, a.b + b.b);
cpx operator *(cpx a, cpx b)
 return cpx(a.a * b.a - a.b * b.b, a.a * b.b +
a.b * b.a);
cpx operator / (cpx a, cpx b)
```

```
cpx r = a * b.bar();
 return cpx(r.a / b.modsq(), r.b / b.modsq());
                                                          // Usage:
                                                          // f[0...N-1] and g[0..N-1] are numbers
                                                          // Want to compute the convolution h, defined by
cpx EXP(double theta)
                                                          // h[n] = sum \ of \ f[k]g[n-k] \ (k = 0, ..., N-1).
                                                          // Here, the index is cyclic; f[-1] = f[N-1], f[-1]
 return cpx(cos(theta), sin(theta));
                                                          2] = f[N-2], etc.
                                                          // Let F[0...N-1] be FFT(f), and similarly, define
const double two pi = 4 * acos(0);
                                                          G and H.
                                                          // The convolution theorem says H[n] = F[n]G[n]
// in:
         input array
                                                          (element-wise product).
// out: output array
                                                          // To compute h[] in O(N log N) time, do the
// step: {SET TO 1} (used internally)
                                                          following:
// size: length of the input/output {MUST BE A
                                                          // 1. Compute F and G (pass dir = 1 as the
POWER OF 2}
                                                          argument).
// dir:
         either plus or minus one (direction of
                                                          // 2. Get H by element-wise multiplying F and G.
the FFT)
                                                          // 3. Get h by taking the inverse FFT (use dir =
// RESULT: out[k] = \sum {j=0}^{size - 1} in[j] *
                                                          -1 as the argument)
exp(dir * 2pi * i * j * k / size)
                                                                  and *dividing by N*. DO NOT FORGET THIS
void FFT(cpx *in, cpx *out, int step, int size,
                                                          SCALING FACTOR.
int dir)
                                                          int main(void)
  if(size < 1) return;</pre>
 if(size == 1)
                                                            printf("If rows come in identical pairs, then
                                                          everything works. \n");
   out[0] = in[0];
   return;
                                                            cpx a[8] = \{0, 1, cpx(1,3), cpx(0,5), 1, 0, 2,
                                                          0 };
  FFT(in, out, step * 2, size / 2, dir);
                                                            cpx b[8] = \{1, cpx(0,-2), cpx(0,1), 3, -1, -3,
  FFT(in + step, out + size / 2, step * 2, size /
                                                          1, -2};
2, dir);
                                                            cpx A[8];
  for(int i = 0 ; i < size / 2 ; i++)</pre>
                                                            cpx B[8];
                                                            FFT(a, A, 1, 8, 1);
   cpx even = out[i];
                                                            FFT(b, B, 1, 8, 1);
    cpx odd = out[i + size / 2];
    out[i] = even + EXP(dir * two pi * i / size) *
                                                            for(int i = 0 ; i < 8 ; i++)</pre>
    out[i + size / 2] = even + EXP(dir * two pi *
                                                              printf("%7.21f%7.21f", A[i].a, A[i].b);
(i + size / 2) / size) * odd;
                                                            printf("\n");
```

```
for(int i = 0 ; i < 8 ; i++)</pre>
    cpx Ai(0,0);
    for(int j = 0 ; j < 8 ; j++)</pre>
      Ai = Ai + a[j] * EXP(j * i * two pi / 8);
    printf("%7.21f%7.21f", Ai.a, Ai.b);
  printf("\n");
  cpx AB[8];
  for(int i = 0 ; i < 8 ; i++)</pre>
   AB[i] = A[i] * B[i];
  cpx aconvb[8];
  FFT (AB, aconvb, 1, 8, -1);
  for(int i = 0 ; i < 8 ; i++)</pre>
    aconvb[i] = aconvb[i] / 8;
  for(int i = 0 ; i < 8 ; i++)</pre>
    printf("%7.21f%7.21f", aconvb[i].a,
aconvb[i].b);
  printf("\n");
  for(int i = 0 ; i < 8 ; i++)</pre>
    cpx aconvbi(0,0);
    for(int j = 0 ; j < 8 ; j++)
      aconvbi = aconvbi + a[j] * b[(8 + i - j) %
81;
    printf("%7.21f%7.21f", aconvbi.a, aconvbi.b);
  printf("\n");
 return 0;
```

Simplex.cc 16/27

```
// Two-phase simplex algorithm for solving linear
programs of the form
//
//
     maximize
                  C^T X
//
      subject to Ax \le b
                   x >= 0
// INPUT: A -- an m x n matrix
// b -- an m-dimensional vector
        c -- an n-dimensional vector
        x -- a vector where the optimal solution
will be stored
// OUTPUT: value of the optimal solution (infinity
if unbounded
           above, nan if infeasible)
// To use this code, create an LPSolver object
with A, b, and c as
// arguments. Then, call Solve(x).
#include <iostream>
#include <iomanip>
#include <vector>
#include <cmath>
#include <limits>
using namespace std;
typedef long double DOUBLE;
typedef vector<DOUBLE> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
const DOUBLE EPS = 1e-9;
struct LPSolver {
```

```
if (D[i][s] <= 0) continue;</pre>
 int m, n;
                                                                    if (r == -1 || D[i][n+1] / D[i][s] <</pre>
 VI B, N;
                                                            D[r][n+1] / D[r][s] ||
 VVD D;
                                                                        D[i][n+1] / D[i][s] == D[r][n+1] /
 LPSolver (const VVD &A, const VD &b, const VD &c)
                                                           D[r][s] \&\& B[i] < B[r]) r = i;
                                                                  if (r == -1) return false;
   m(b.size()), n(c.size()), N(n+1), B(m), D(m+2)
VD(n+2)) {
                                                                  Pivot(r, s);
   for (int i = 0; i < m; i++) for (int j = 0; j
< n; j++) D[i][j] = A[i][j];
    for (int i = 0; i < m; i++) { B[i] = n+i;</pre>
D[i][n] = -1; D[i][n+1] = b[i];
                                                              DOUBLE Solve(VD &x) {
    for (int j = 0; j < n; j++) { N[j] = j;</pre>
                                                                int r = 0;
D[m][j] = -c[j];
                                                                for (int i = 1; i < m; i++) if (D[i][n+1] <</pre>
   N[n] = -1; D[m+1][n] = 1;
                                                           D[r][n+1]) r = i;
                                                                if (D[r][n+1] \le -EPS) {
                                                                  Pivot(r, n);
 void Pivot(int r, int s) {
                                                                  if (!Simplex(1) || D[m+1][n+1] < -EPS)</pre>
   for (int i = 0; i < m+2; i++) if (i != r)</pre>
                                                           return -numeric limits<DOUBLE>::infinity();
     for (int j = 0; j < n+2; j++) if (j != s)
                                                                  for (int i = 0; i < m; i++) if (B[i] == -1)
       D[i][j] = D[r][j] * D[i][s] / D[r][s];
   for (int j = 0; j < n+2; j++) if (j != s)
                                                                   int s = -1;
D[r][i] /= D[r][s];
                                                                   for (int j = 0; j <= n; j++)
   for (int i = 0; i < m+2; i++) if (i != r)</pre>
                                                                    if (s == -1 || D[i][j] < D[i][s] ||</pre>
                                                            D[i][j] == D[i][s] \&\& N[j] < N[s]) s = j;
D[i][s] /= -D[r][s];
                                                                    Pivot(i, s);
   D[r][s] = 1.0 / D[r][s];
   swap(B[r], N[s]);
                                                                if (!Simplex(2)) return
 bool Simplex(int phase) {
                                                           numeric limits<DOUBLE>::infinity();
   int x = phase == 1 ? m+1 : m;
                                                               x = VD(n);
   while (true) {
                                                                for (int i = 0; i < m; i++) if (B[i] < n)</pre>
     int s = -1;
                                                           x[B[i]] = D[i][n+1];
      for (int j = 0; j <= n; j++) {</pre>
                                                                return D[m] [n+1];
      if (phase == 2 && N[j] == -1) continue;
                                                            }
       if (s == -1 || D[x][j] < D[x][s] || D[x][j]
                                                           };
== D[x][s] && N[j] < N[s]) s = j;
                                                            int main() {
      if (D[x][s] >= -EPS) return true;
      int r = -1;
                                                              const int m = 4;
      for (int i = 0; i < m; i++) {</pre>
                                                              const int n = 3;
```

```
DOUBLE A[m][n] = {
   \{ 6, -1, 0 \},
   \{-1, -5, 0\},
   { 1, 5, 1 },
   \{-1, -5, -1\}
  DOUBLE b[m] = \{ 10, -4, 5, -5 \};
  DOUBLE c[n] = \{ 1, -1, 0 \};
 VVD A(m);
 VD b ( b, b + m);
 VD c(c, c+n);
 for (int i = 0; i < m; i++) A[i] = VD(A[i],
A[i] + n);
 LPSolver solver (A, b, c);
 VD x;
 DOUBLE value = solver.Solve(x);
 cerr << "VALUE: "<< value << endl;
 cerr << "SOLUTION:";</pre>
 for (size t i = 0; i < x.size(); i++) cerr << "</pre>
" << x[i];
  cerr << endl;
 return 0;
```

FastDijkstra.cc 17/27

```
// Implementation of Dijkstra's algorithm using
adjacency lists
// and priority queue for efficiency.
//
// Running time: O(|E| log |V|)
#include <queue>
```

#include <stdio.h> using namespace std; const int INF = 2000000000; typedef pair<int, int> PII; int main(){ int N, s, t; scanf ("%d%d%d", &N, &s, &t); vector<vector<PII> > edges(N); for (int i = 0; i < N; i++) {</pre> int M; scanf ("%d", &M); for (int j = 0; j < M; j++) {</pre> int vertex, dist; scanf ("%d%d", &vertex, &dist); edges[i].push back (make pair (dist, vertex)); // note order of arguments here } // use priority queue in which top element has the "smallest" priority priority queue<PII, vector<PII>, greater<PII> > 0; vector<int> dist(N, INF), dad(N, -1); Q.push (make pair (0, s)); dist[s] = 0;while (!Q.empty()){ PII p = Q.top();if (p.second == t) break; Q.pop(); int here = p.second; for (vector<PII>::iterator it=edges[here].begin(); it!=edges[here].end(); if (dist[here] + it->first < dist[it-</pre> >second]){ dist[it->second] = dist[here] + it->first;

```
dad[it->second] = here;
    Q.push (make_pair (dist[it->second], it-
>second));
    }
}

printf ("%d\n", dist[t]);
if (dist[t] < INF)
    for(int i=t;i!=-1;i=dad[i])
        printf ("%d%c", i, (i==s?'\n':' '));

return 0;
}</pre>
```

SCC.cc 18/27

```
#include<memory.h>
struct edge{int e, nxt;};
int V, E;
edge e[MAXE], er[MAXE];
int sp[MAXV], spr[MAXV];
int group cnt, group num[MAXV];
bool v[MAXV];
int stk[MAXV];
void fill forward(int x)
 int i;
 v[x]=true;
 for (i=sp[x];i;i=e[i].nxt) if (!v[e[i].e])
fill forward(e[i].e);
  stk[++stk[0]]=x;
void fill backward(int x)
 int i;
 v[x] = false;
  group num[x]=group cnt;
```

```
for (i=spr[x];i;i=er[i].nxt) if (v[er[i].e])
fill_backward(er[i].e);
}
void add_edge(int v1, int v2) //add edge v1->v2
{
    e [++E].e=v2; e [E].nxt=sp [v1]; sp [v1]=E;
    er[ E].e=v1; er[E].nxt=spr[v2]; spr[v2]=E;
}
void SCC()
{
    int i;
    stk[0]=0;
    memset(v, false, sizeof(v));
    for(i=1;i<=V;i++) if(!v[i]) fill_forward(i);
    group_cnt=0;
    for(i=stk[0];i>=1;i--)
if(v[stk[i]]) {group_cnt++; fill_backward(stk[i]);}
}
```

SuffixArray.cc 19/27

```
// Suffix array construction in O(L log^2 L) time.
Routine for
// computing the length of the longest common
prefix of any two
// suffixes in O(log L) time.
//
// INPUT: string s
//
// OUTPUT: array suffix[] such that suffix[i] =
index (from 0 to L-1)
// of substring s[i...L-1] in the list of
sorted suffixes.
// That is, if we take the inverse of the
permutation suffix[],
// we get the actual suffix array.
```

```
#include <vector>
#include <iostream>
#include <string>
using namespace std;
struct SuffixArray {
  const int L;
 string s;
 vector<vector<int> > P;
 vector<pair<int,int>,int> > M;
  SuffixArray(const string &s) : L(s.length()),
s(s), P(1, vector < int > (L, 0)), M(L) {
    for (int i = 0; i < L; i++) P[0][i] =</pre>
int(s[i]);
   for (int skip = 1, level = 1; skip < L; skip</pre>
*= 2, level++) {
     P.push back(vector<int>(L, 0));
      for (int i = 0; i < L; i++)</pre>
       M[i] = make pair(make pair(P[level-1][i], i
+ \text{ skip} < L ? P[level-1][i + \text{ skip}] : -1000), i);
      sort(M.begin(), M.end());
      for (int i = 0; i < L; i++)</pre>
       P[level][M[i].second] = (i > 0 &&
M[i].first == M[i-1].first) ? P[level][M[i-
1].second] : i;
   }
 vector<int> GetSuffixArray() { return P.back();
  // returns the length of the longest common
prefix of s[i...L-1] and s[j...L-1]
  int LongestCommonPrefix(int i, int j) {
    int len = 0;
   if (i == j) return L - i;
   for (int k = P.size() - 1; k >= 0 && i < L &&</pre>
j < L; k--) {
      if (P[k][i] == P[k][j]) {
```

```
i += 1 << k;
       \dot{j} += 1 << k;
       len += 1 << k;
    return len;
};
int main() {
 // bobocel is the 0'th suffix
 // obocel is the 5'th suffix
 // bocel is the 1'st suffix
 // ocel is the 6'th suffix
  // cel is the 2'nd suffix
  // el is the 3'rd suffix
  // l is the 4'th suffix
  SuffixArray suffix("bobocel");
  vector<int> v = suffix.GetSuffixArray();
 // Expected output: 0 5 1 6 2 3 4
 for (int i = 0; i < v.size(); i++) cout << v[i]</pre>
<< " ";
 cout << endl;</pre>
 cout << suffix.LongestCommonPrefix(0, 2) <<</pre>
endl;
```

BIT.cc 20/27

```
#include <iostream>
using namespace std;
#define LOGSZ 17
int tree[(1<<LOGSZ)+1];</pre>
```

```
int N = (1 << LOGSZ);
// add v to value at x
void set(int x, int v) {
 while (x \le N)
   tree[x] += v;
   x += (x \& -x);
// get cumulative sum up to and including x
int get(int x) {
 int res = 0;
 while(x) {
   res += tree[x];
   x = (x \& -x);
  return res;
// get largest value with cumulative sum less than
or equal to x;
// for smallest, pass x-1 and add 1 to result
int getind(int x) {
  int idx = 0, mask = N;
  while (mask && idx < N) {</pre>
   int t = idx + mask;
   if(x >= tree[t]) {
     idx = t;
     x -= tree[t];
   mask >>= 1;
  return idx;
```

UnionFind.cc 21/27

```
//union-find set: the vector/array contains the
parent of each node
int find(vector <int>& C, int x) {return (C[x]==x)
? x : C[x]=find(C, C[x]);} //C++
int find(int x) {return
(C[x]==x) ?x:C[x]=find(C[x]);} //C
```

KDTree.cc 22/27

```
// A straightforward, but probably sub-optimal KD-
tree implmentation that's
// probably good enough for most things (current
it's a 2D-tree)
// - constructs from n points in O(n lg^2 n) time
// - handles nearest-neighbor query in O(lg n) if
points are well distributed
// - worst case for nearest-neighbor may be
linear in pathological case
// Sonny Chan, Stanford University, April 2009
// -----
#include <iostream>
#include <vector>
#include <limits>
#include <cstdlib>
using namespace std;
// number type for coordinates, and its maximum
typedef long long ntype;
const ntype sentry = numeric limits<ntype>::max();
```

```
// point structure for 2D-tree, can be extended to
                                                               // computes bounding box from a bunch of
                                                           points
struct point {
                                                               void compute(const vector<point> &v) {
                                                                   for (int i = 0; i < v.size(); ++i) {</pre>
   ntype x, y;
                                                                       x0 = min(x0, v[i].x); x1 = max(x1, v[i].x)
   point(ntype xx = 0, ntype yy = 0) : x(xx),
y(yy) \{ \}
                                                           v[i].x);
                                                                       y0 = min(y0, v[i].y); y1 = max(y1,
};
                                                           v[i].y);
bool operator==(const point &a, const point &b)
    return a.x == b.x && a.y == b.y;
                                                               // squared distance between a point and this
                                                           bbox, 0 if inside
// sorts points on x-coordinate
                                                               ntype distance(const point &p) {
bool on x(const point &a, const point &b)
                                                                   if (p.x < x0) {
                                                                       if (p.y < y0)
                                                                                            return
   return a.x < b.x;</pre>
                                                           pdist2(point(x0, y0), p);
                                                                       else if (p.y > y1)
                                                                                            return
                                                           pdist2(point(x0, y1), p);
// sorts points on y-coordinate
                                                                                            return
bool on y (const point &a, const point &b)
                                                           pdist2(point(x0, p.y), p);
                                                                   else if (p.x > x1) {
   return a.y < b.y;</pre>
                                                                       if (p.y < y0)
                                                                                            return
                                                           pdist2(point(x1, y0), p);
// squared distance between points
                                                                       else if (p.y > y1)
                                                                                            return
ntype pdist2(const point &a, const point &b)
                                                           pdist2(point(x1, y1), p);
                                                                       else
                                                                                            return
   ntype dx = a.x-b.x, dy = a.y-b.y;
                                                           pdist2(point(x1, p.y), p);
   return dx*dx + dy*dy;
                                                                   else {
                                                                       if (p.y < y0)
                                                                                            return
// bounding box for a set of points
                                                          pdist2(point(p.x, y0), p);
struct bbox
                                                                       else if (p.y > y1)
                                                                                            return
                                                           pdist2(point(p.x, y1), p);
    ntype x0, x1, y0, y1;
                                                                       else
                                                                                            return 0;
   bbox(): x0(sentry), x1(-sentry), y0(sentry),
y1(-sentry) {}
                                                           };
```

```
// stores a single node of the kd-tree, either
                                                                     if (bound.x1-bound.x0 >= bound.y1-
internal or leaf
                                                         bound.y0)
struct kdnode
                                                                         sort(vp.begin(), vp.end(), on x);
                                                                     // otherwise split on y-coordinate
   bool leaf;
                   // true if this is a leaf node
                                                                     else
(has one point)
                                                                         sort(vp.begin(), vp.end(), on y);
   point pt;
                   // the single point of this is
a leaf
                                                                     // divide by taking half the array for
                   // bounding box for set of
   bbox bound;
                                                         each child
points in children
                                                                     // (not best performance if many
                                                         duplicates in the middle)
   kdnode *first, *second; // two children of
                                                                     int half = vp.size()/2;
this kd-node
                                                                     vector<point> vl(vp.begin(),
                                                         vp.begin()+half);
   kdnode() : leaf(false), first(0), second(0) {}
                                                                     vector<point> vr(vp.begin()+half,
   ~kdnode() { if (first) delete first; if
                                                         vp.end());
(second) delete second; }
                                                                     first = new kdnode(); first-
                                                         >construct(v1);
                                                                     second = new kdnode(); second-
   // intersect a point with this node (returns
squared distance)
                                                         >construct(vr);
   ntype intersect(const point &p) {
       return bound.distance(p);
                                                         };
   // recursively builds a kd-tree from a given
                                                         // simple kd-tree class to hold the tree and
cloud of points
                                                         handle queries
                                                         struct kdtree
   void construct(vector<point> &vp)
       // compute bounding box for points at this
                                                             kdnode *root;
node
       bound.compute(vp);
                                                             // constructs a kd-tree from a points (copied
                                                         here, as it sorts them)
       // if we're down to one point, then we're
                                                             kdtree(const vector<point> &vp) {
a leaf node
                                                                 vector<point> v(vp.begin(), vp.end());
       if (vp.size() == 1) {
                                                                 root = new kdnode();
           leaf = true;
                                                                 root->construct(v);
           pt = vp[0];
                                                             ~kdtree() { delete root; }
       else {
           // split on x if the bbox is wider
                                                             // recursive search method returns squared
than high (not best heuristic...)
                                                         distance to nearest point
```

```
ntype search(kdnode *node, const point &p)
        if (node->leaf) {
            // commented special case tells a
point not to find itself
             if (p == node->pt) return sentry;
              return pdist2(p, node->pt);
        ntype bfirst = node->first->intersect(p);
        ntype bsecond = node->second-
>intersect(p);
        // choose the side with the closest
bounding box to search first
       // (note that the other side is also
searched if needed)
        if (bfirst < bsecond) {</pre>
            ntype best = search(node->first, p);
            if (bsecond < best)</pre>
                best = min(best, search(node-
>second, p));
            return best;
        else {
            ntype best = search(node->second, p);
            if (bfirst < best)</pre>
                best = min(best, search(node-
>first, p));
            return best;
    // squared distance to the nearest
    ntype nearest(const point &p) {
        return search(root, p);
};
```

LongestIncreasingSubsequen ce.cc 23/27

```
// Given a list of numbers of length n, this
routine extracts a
// longest increasing subsequence.
//
// Running time: O(n log n)
```

```
// INPUT: a vector of integers
// OUTPUT: a vector containing the longest
increasing subsequence
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
#define STRICTLY INCREASING
VI LongestIncreasingSubsequence(VI v) {
 VPII best;
 VI dad(v.size(), -1);
  for (int i = 0; i < v.size(); i++) {</pre>
#ifdef STRICTLY INCREASIG
   PII item = make pair(v[i], 0);
   VPII::iterator it = lower bound(best.begin(),
best.end(), item);
   item.second = i;
#else
   PII item = make pair(v[i], i);
   VPII::iterator it = upper bound(best.begin(),
best.end(), item);
#endif
   if (it == best.end()) {
      dad[i] = (best.size() == 0 ? -1 :
best.back().second);
     best.push back(item);
   } else {
     dad[i] = dad[it->second];
     *it = item;
   }
```

```
VI ret;
for (int i = best.back().second; i >= 0; i =
dad[i])
   ret.push_back(v[i]);
  reverse(ret.begin(), ret.end());
  return ret;
}
```

Dates.cc 24/27

```
// Routines for performing computations on dates.
In these routines,
// months are expressed as integers from 1 to 12,
days are expressed
// as integers from 1 to 31, and years are
expressed as 4-digit
// integers.
#include <iostream>
#include <string>
using namespace std;
string dayOfWeek[] = {"Mon", "Tue", "Wed", "Thu",
"Fri", "Sat", "Sun"};
// converts Gregorian date to integer (Julian day
number)
int dateToInt (int m, int d, int y) {
 return
    1461 * (y + 4800 + (m - 14) / 12) / 4 +
    367 * (m - 2 - (m - 14) / 12 * 12) / 12 -
    3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
    d - 32075;
```

```
// converts integer (Julian day number) to
Gregorian date: month/day/year
void intToDate (int jd, int &m, int &d, int &y) {
  int x, n, i, j;
 x = id + 68569;
 n = 4 * x / 146097;
 x = (146097 * n + 3) / 4;
 i = (4000 * (x + 1)) / 1461001;
 x = 1461 * i / 4 - 31;
 j = 80 * x / 2447;
 d = x - 2447 * j / 80;
 x = 1 / 11;
 m = j + 2 - 12 * x;
 y = 100 * (n - 49) + i + x;
// converts integer (Julian day number) to day of
week
string intToDay (int jd) {
 return dayOfWeek[jd % 7];
int main (int argc, char **argv) {
  int jd = dateToInt (3, 24, 2004);
 int m, d, y;
 intToDate (jd, m, d, y);
 string day = intToDay (jd);
 // expected output:
 // 2453089
 // 3/24/2004
 // Wed
  cout << id << endl
   << m << "/" << d << "/" << v << endl
   << day << endl;
```

LogLan.java 25/27

```
// Code which demonstrates the use of Java's
regular expression libraries.
// This is a solution for
// Loglan: a logical language
// http://acm.uva.es/p/v1/134.html
// In this problem, we are given a regular
language, whose rules can be
// inferred directly from the code. For each
sentence in the input, we must
// determine whether the sentence matches the
regular expression or not. The
// code consists of (1) building the regular
expression (which is fairly
// complex) and (2) using the regex to match
sentences.
import java.util.*;
import java.util.regex.*;
public class LogLan {
    public static String BuildRegex () {
       String space = " +";
       String A = "([aeiou])";
       String C = "([a-z&&[^aeiou]])";
       String MOD = "(g" + A + ")";
       String BA = "(b" + A + ")";
       String DA = "(d" + A + ")";
       String LA = "(1" + A + ")";
       String NAM = "([a-z]*" + C + ")";
       String PREDA = "(" + C + C + A + C + A +
"|" + C + A + C + C + A + ")";
```

```
String predstring = "(" + PREDA + "(" +
space + PREDA + ")*)";
                                                                   // Other useful String manipulation
       String predname = "(" + LA + space +
                                                       methods include
predstring + "|" + NAM + ")";
       String preds = "(" + predstring + "(" +
                                                                   // s.compareTo(t) < 0 if s < t,
space + A + space + predstring + ")*)";
                                                       lexicographically
       String predclaim = "(" + predname + space +
                                                                   // s.indexOf("apple") returns index
BA + space + preds + "|" + DA + space +
                                                        of first occurrence of "apple" in s
           preds + ")";
                                                                   // s.lastIndexOf("apple") returns
       String verbpred = "(" + MOD + space +
                                                        index of last occurrence of "apple" in s
predstring + ")";
                                                                   // s.replace(c,d) replaces
       String statement = "(" + predname + space +
                                                        occurrences of character c with d
verbpred + space + predname + "|" +
                                                                   // s.startsWith("apple) returns
           predname + space + verbpred + ")";
                                                        (s.indexOf("apple") == 0)
       String sentence = "(" + statement + "|" +
                                                                   // s.toLowerCase() /
predclaim + ")";
                                                       s.toUpperCase() returns a new lower/uppercased
                                                       string
       return "^" + sentence + "$";
                                                                   //
                                                                   // Integer.parseInt(s) converts s
                                                       to an integer (32-bit)
   public static void main (String args[]) {
                                                                         Long.parseLong(s) converts s to
                                                       a long (64-bit)
       String regex = BuildRegex();
                                                                         Double.parseDouble(s) converts s
       Pattern pattern = Pattern.compile (regex);
                                                       to a double
       Scanner s = new Scanner(System.in);
                                                                   String sentence = "";
       while (true) {
                                                                   while (true) {
                                                                      sentence = (sentence + " " +
           // In this problem, each sentence
                                                       s.nextLine()).trim();
consists of multiple lines, where the last
                                                                      if (sentence.equals("#")) return;
           // line is terminated by a period. The
code below reads lines until
                                                       (sentence.charAt(sentence.length()-1) == '.')
           // encountering a line whose final
                                                       break;
character is a '.'. Note the use of
           //
               s.length() to get length of
                                                                   // now, we remove the period, and
                                                       match the regular expression
string
           // s.charAt() to extract characters
from a Java string
                                                                   String removed period =
           // s.trim() to remove whitespace
                                                       sentence.substring(0, sentence.length()-1).trim();
from the beginning and end of Java string
```

Primes.cc 26/27

```
// O(sgrt(x)) Exhaustive Primality Test
#include <cmath>
#define EPS 1e-7
typedef long long LL;
bool IsPrimeSlow (LL x)
  if(x<=1) return false;</pre>
  if(x<=3) return true;</pre>
  if (!(x%2) || !(x%3)) return false;
  LL s=(LL) (sqrt((double)(x))+EPS);
  for (LL i=5; i<=s; i+=6)</pre>
    if (!(x%i) || !(x%(i+2))) return false;
  return true;
// Primes less than 1000:
        2
               3
                      5
                                  11
                                        13
                                               17
19
      23
             29
                   31
                          37
//
              43
                                  59
                                        61
       41
                    47
                                               67
71
      73
             79
                   83
                          89
//
       97
             101
                   103
                          107
                                 109
                                       113
                                              127
131
      137
             139
                   149
                          151
//
      157
             163
                   167
                          173
                                179
                                       181
                                              191
193
      197
             199
                   211
                          223
```

```
//
      227
             229
                   233
                         239
                                241
                                      251
                                             257
263
      269
             271
                   277
                         281
//
      283
             293
                   307
                         311
                                313
                                      317
                                             331
337
      347
             349
                   353
                         359
//
      367
             373
                   379
                         383
                                389
                                      397
                                             401
409
      419
             421
                         433
                   4.31
//
      439
                   449
                         457
                                      463
                                             467
             443
                                461
479
                         503
      487
             491
                   499
//
      509
             521
                   523
                         541
                                      557
                                547
                                             563
569
      571
             577
                   587
                         593
//
      599
             601
                   607
                          613
                                617
                                      619
                                             631
641
      643
             647
                   653
                         659
//
      661
             673
                   677
                          683
                                691
                                       701
                                             709
719
      727
             733
                   739
                          743
//
      751
             757
                   761
                          769
                                       787
                                773
                                             797
809
      811
             821
                   823
                         827
//
             839
                         857
      829
                   853
                                859
                                      863
                                             877
881
      883
             887
                   907
                         911
             929
                         941
                                      953
//
      919
                   937
                                947
                                             967
971
      977
             983
                   991
                         997
// Other primes:
      The largest prime smaller than 10 is 7.
//
      The largest prime smaller than 100 is 97.
//
      The largest prime smaller than 1000 is 997.
//
      The largest prime smaller than 10000 is
9973.
//
      The largest prime smaller than 100000 is
99991.
//
      The largest prime smaller than 1000000 is
999983.
//
      The largest prime smaller than 10000000 is
9999991.
//
      The largest prime smaller than 100000000 is
99999989.
//
      The largest prime smaller than 1000000000 is
999999937.
      The largest prime smaller than 10000000000
is 9999999967.
      The largest prime smaller than 100000000000
```

KMP.cpp 27/27

```
/*
Searches for the string w in the string s (of
length k). Returns the
0-based index of the first match (k if no match is
found). Algorithm
runs in O(k) time.
*/

#include <iostream>
#include <string>
#include <vector>

using namespace std;

typedef vector<int> VI;

void buildTable(string& w, VI& t)
{
    t = VI(w.length());
    int i = 2, j = 0;
    t[0] = -1; t[1] = 0;
```

```
while(i < w.length())</pre>
    if(w[i-1] == w[j]) { t[i] = j+1; i++; j++; }
    else if (j > 0) j = t[j];
    else { t[i] = 0; i++; }
int KMP(string& s, string& w)
 int m = 0, i = 0;
 VI t;
  buildTable(w, t);
  while (m+i < s.length())</pre>
    if(w[i] == s[m+i])
      if(i == w.length()) return m;
    else
      m += i-t[i];
      if(i > 0) i = t[i];
 return s.length();
int main()
  string a = (string) "The example above
illustrates the general technique for assembling
    "the table with a minimum of fuss. The
principle is that of the overall search: "+
    "most of the work was already done in getting
to the current position, so very "+
```

```
"little needs to be done in leaving it. The
only minor complication is that the "+
    "logic which is correct late in the string
erroneously gives non-proper "+
    "substrings at the beginning. This
necessitates some initialization code.";

string b = "table";

int p = KMP(a, b);
  cout << p << ": " << a.substr(p, b.length()) <<
" " << b << endl;
}</pre>
```