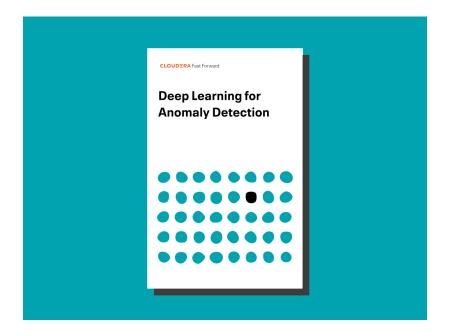
# Deep Learning for Anomaly Detection



This is an applied research report by Cloudera Fast Forward, focused on Deep Learning Approaches for Anomaly Detection. Read our full report on using deep learning for anomaly detection below or download it (<u>PDF</u>, <u>ePub</u>, <u>mobi</u>). Also be sure to check out our anomaly detection prototypes: <u>Blip</u> and <u>Anomagram</u>.

Our reports focus on emerging capabilities that are still changing due to algorithmic breakthrough, hardware breakthrough, technological commoditization, and data availability. Accompanying our reports are working prototypes that exhibit the capabilities of the algorithm and offer detailed technical advice on its practical application.

#### **CHAPTER 1**

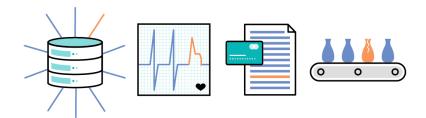
### Introduction

"An outlier is an observation which deviates so much from other observations as to arouse suspicions that it was generated by a different mechanism" – Hawkins, *Identification of Outliers* (1980)

Anomalies, often referred to as outliers, abnormalities, rare events, or deviants, are data points or patterns in data that do not conform to a notion of normal behavior. Anomaly detection, then, is the task of finding those patterns in data that do not adhere to expected norms, given previous observations. The capability to recognize or detect anomalous behavior can provide highly useful insights across industries. Flagging unusual cases or enacting a planned response when they occur can save businesses time, costs, and customers. Hence, anomaly detection has found diverse applications in a variety of domains, including IT analytics, network intrusion analytics, medical diagnostics, financial fraud protection, manufacturing quality control, marketing and social media analytics, and more.

# Applications of Anomaly Detection

We'll begin by taking a closer look at some possible use cases, before diving into different approaches to anomaly detection in the next chapter.



Anomaly detection is relevant to several usecases - Network intrusion detection, Medical diagnosis, Fraud detection and manufacturing defect detection.

#### **Network Intrusion Detection**

Network security is critical to running a modern viable business, yet all computer systems suffer from security vulnerabilities which are both technically difficult and economically punishing to resolve once exploited. Business IT systems collect data about their own network traffic, user activity in the system, types of connection requests, and more. While most activity will be benign and routine, analysis of this data may provide insights into unusual (anomalous) activity within the network after and ideally before a substantive attack. In practice, the damage incurred during an intrusion event often escalates faster than most teams are able to mount an effective response. Thus, it becomes critical to have special-purpose intrusion detection systems (IDSs) in place that can surface potential threat events and anomalous probing early and in a reliable manner.

### **Medical Diagnosis**

In many medical diagnosis applications, a variety of data points (e.g., X-rays, MRIs, ECGs) indicative of health status are collected as part of diagnostic processes. Some of these data points are also collected by end-user medical devices (e.g., glucose monitors, pacemakers, smart watches). Anomaly detection approaches can be applied to highlight situations of abnormal readings that may be indicative of health conditions or precursor signals of medical incidents.

#### **Fraud Detection**

In 2018, fraud was estimated to have a global financial cost of over £3.89 trillion (\$5 trillion). Within the financial services industry, it is critical for service providers to quickly and correctly identify and react to fraudulent transactions. In the most straightforward cases, a transaction may be identified as fraudulent by comparison to the historical transactions by a given party or to all other transactions occurring within the same time period for a peer group. Here, fraud can be cast as a deviation from normal transaction data and addressed using anomaly detection approaches. Even as financial fraud is further clustered into card-based, check-based, unauthorized account access, or authorized payment-based categories, the core concepts of baselining an individual's standard behavior and looking for signals of unusual activity apply.

### **Manufacturing Defect Detection**

Within the manufacturing industry, an automated approach to the task of detecting defects, particularly in items manufactured in large volumes, is vital to quality assurance (QA). This task can be cast as an anomaly detection exercise, where the goal is to identify manufactured items that significantly or even slightly differ from ideal (normal) items that have passed QA tests. The amount of acceptable deviation is determined by the company and customers, as well as industry and regulatory standards.

#### Use Case Example

ScoleMans have been making drywall panels for years and are the leading regional supplier for construction companies. Occasionally, some of the wall panels they produce have defects: cracks, chips at the edges, paint/coating issues, etc. As part of their QA process they

capture both RGB and thermal images of each produced panel, which their QA engineers use to flag defective units. They want to automate this process i.e., develop tools that automatically identify these defects. This is possible using a deep anomaly detection model. In particular, ScoleMans can use an autoencoder or GAN-based model built with convolutional neural network blocks (see <a href="Chapter 3. Deep Learning for Anomaly Detection">Chapter 3. Deep Learning for Anomaly Detection</a> for more information) to create a model of normal data based on images of normal panels. This model can then be used to tag new images as normal or abnormal, andset thresholds for alerts.

Similarly, the task of predictive maintenance can be cast as an anomaly detection problem. For example, anomaly detection approaches can be applied to data from machine sensors (vibrations, temperature, drift, etc.), where abnormal sensor readings can be indicative of impending failures.

As these examples suggest, anomaly detection is critical in a variety of areas. Detecting and correctly classifying as anomalous something previously unseen is a challenging problem that has been tackled in many different manners over the years. While there are many approaches, as we'll see in the next chapters, the traditional machine learning (ML) techniques are suboptimal when it comes to high-dimensional data and sequence datasets because they fail to capture the complex structures in the data.

This report, with its accompanying prototype, explores deep learning-based approaches that first learn to model normal behavior and then exploit this knowledge to identify anomalies. While they're capable of yielding remarkable results on complex and high-dimensional data, there are several factors that influence the choice of approach when building an anomaly detection application. In this report we survey the options, highlighting their pros and cons.

#### **CHAPTER 2**

# Background

In this chapter, we provide an overview of approaches to anomaly detection based on the type of data available, how to evaluate an anomaly detection model, how each approach constructs a model of normal behavior, and why deep learning models are valuable. We conclude with a discussion of pitfalls that may be encountered while deploying these models.

## **Anomaly Detection Approaches**

Anomaly detection approaches can be categorized in terms of the type of data needed to train the model. In most use cases, it is expected that anomalous samples represent a very small percentage of the entire dataset. Thus, even when labeled data is available, normal data samples are more readily available than abnormal samples. This assumption is critical for most applications today. In the following sections, we touch on how the availability of labeled data impacts the choice of approach.

## **Supervised Learning**

When learning with supervision, machines rely on examples that illustrate the relationship between the input features and the output. The goal of supervised anomaly detection algorithms is to incorporate application-specific knowledge into the anomaly detection process. With sufficient normal and anomalous examples, the anomaly detection task can be reframed as a classification task where the machines can learn to accurately predict whether a given example is an anomaly or not. That said, for many anomaly detection use cases the proportion of normal versus anomalous examples is highly imbalanced; while there may be multiple anomalous classes, each of them could be quite underrepresented.

Supervised Learning Training nm1 nm1 nm1 nm1 abn abn abn abn nml nml nm1 nml abn abn abn abn

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An illustration of supervised learning.

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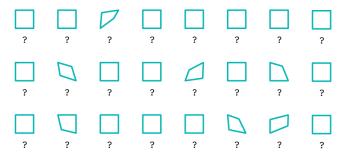
nm1

This approach assumes that one has labeled examples for all types of anomalies that could occur and can correctly classify them. In practice, this is usually not the case, as anomalies can take many different forms, with novel anomalies emerging at test time. "Thus, approaches that generalize well and are more effective at identifying previously unseen anomalies are preferable.

# **Unsupervised learning**

With unsupervised learning, one does not possess examples that illustrate the relationship between the input features and the output. Instead, machines learn by finding structure within the input features. Because, as mentioned previously, labeled anomalous data is relatively rare, unsupervised approaches are more popular than supervised ones in the anomaly detection field. hat said, the nature of the anomalies one hopes to detect is often highly specific. Thus, many of the anomalies found in a completely unsupervised manner could correspond to noise, and may not be of interest for the task at hand.

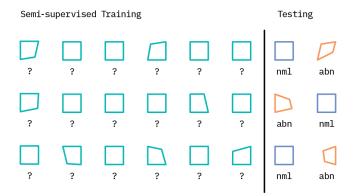
Unsupervised Learning Training



An illustration of unsupervised learning.

## Semi-supervised learning

Semi-supervised learning approaches represent a sort of middle ground, employing a set of methods that take advantage of large amounts of unlabeled data as well as small amounts of labeled data. Many real-world anomaly detection use cases are well suited to semi-supervised learning, in that there are a huge number of normal examples available to be learned from, but relatively few examples of the more unusual or abnormal classes of interest. Following the assumption that most data points within an unlabeled dataset are normal, one can train a robust model on an unlabeled dataset and evaluate its performance (and tune the model's parameters) using a small amount of labeled data. [1]

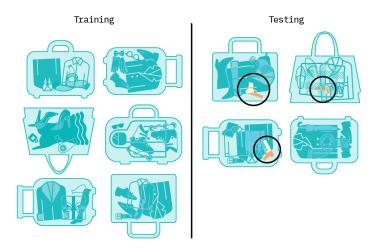


An illustration of semi-supervised learning

This hybrid approach is well suited to applications like network intrusion detection, where one may have multiple examples of the normal class and some examples of intrusion classes, but new kinds of intrusions may arise over time.

To give another example, consider X-ray screening for aviation or border security. Anomalous items posing a security threat are not commonly encountered and can take many forms. In addition, the nature of any anomaly posing a potential threat may evolve due to a range of external factors. Exemplary data of anomalies can therefore be difficult to obtain in any useful quantity.

To give another example, in the case of border security or X-ray screening for aviation, anomalous items posing a security threat are not commonly encountered. Exemplary data of anomalies can be difficult to obtain in any quantity, since no such events may have occurred in the first place. In addition, the nature of any anomaly posing a potential threat may evolve due to a range of external factors.



Exemplary data in certain applications can be difficult to obtain

Such situations may require the determination of abnormal classes as well as novel classes, for which little or no labeled data is available. In cases like these, a semi-supervised classification approach that enables detection of both known and previously unseen anomalies is an ideal solution.

# **Evaluating Models: Accuracy Is Not Enough**

As mentioned in the previous section, in anomaly detection applications it is expected that the distribution between the normal and abnormal class(es) may be highly skewed. This is commonly referred to as the *class imbalance problem*. A model that learns from such skewed data may not be robust: it may be accurate when classifying examples within the normal class, but perform poorly when classifying anomalous examples.

For example, consider a dataset consisting of 1,000 images of luggage passing through a security checkpoint. 950 images are of normal pieces of luggage, and 50 are abnormal. A classification model that always classifies

an image as normal can achieve high overall accuracy for this dataset (95%), even though its accuracy rate for classifying abnormal data is 0%.

Such a model may also misclassify normal examples as anomalous (false positives, FP), or misclassify anomalous examples as normal ones (false negatives, FN). As we consider both of these types of errors, it becomes obvious that the traditional accuracy metric (total number of correct classifications divided by total classifications) is insufficient in evaluating the skill of an anomaly detection model.

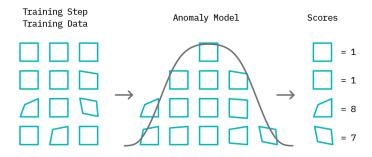
Two important metrics have been introduced that provide a better measure of model skill: *precision* and *recall*. Precision is defined as the number of *true positives* (TP) divided by the number of true positives plus the number of *false positives* (FP), while recall is the number of true positives divided by the number of true positives plus the number of false negatives (FN). Depending on the use case or application, it may be desirable to optimize for either precision or recall.

Optimizing for precision may be useful when the cost of failure is low, or to reduce human workload. Optimizing for high recall may be more appropriate when the cost of a false negative is very high; for example, in airport security, where it is better to flag many items for human inspection (low cost) in order to avoid the much higher cost of incorrectly admitting a dangerous item onto a flight. While there are several ways to optimize for precision or recall, the manner in which a threshold is set can be used to reflect the precision and recall preferences for each specific use case.

You now have an idea of why an unsupervised or semi-supervised approach to anomaly detection is desirable, and what metrics are best to use for evaluating these models. In the next section, we focus on semi-supervised approaches and discuss how they work.

# Anomaly Detection as Learning Normal Behavior

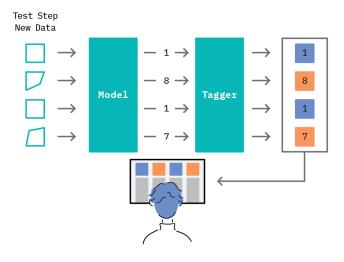
The underlying strategy for most approaches to anomaly detection (AD) is to first model normal behavior, and then exploit this knowledge to identify deviations (anomalies). This approach typically falls under the semi-supervised learning category and is accomplished through two steps in the AD loop. The first step, referred to as the training step, involves building a model of normal behavior using available data. Depending on the specific anomaly detection method, this training data may contain both normal and abnormal data points, or only normal data points (see <a href="Chapter 3. Deep Learning for Anomaly Detection">Chapter 3. Deep Learning for Anomaly Detection</a> for additional details on AD methods). Based on this model, an anomaly score is then assigned to each data point that represents a measure of deviation from normal behavior.



The training step in the anomaly detection loop: based on data (which may or may not contain abnormal samples), the AD model learns a model of normal behavior which it uses to assign anomaly scores.

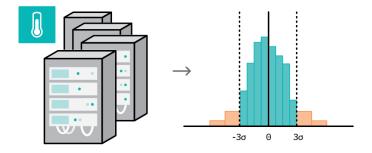
The second step in the anomaly detection loop, the test step, introduces the concept of threshold-based anomaly tagging. Based on the range of scores assigned by the model, one can select a threshold rule that drives the anomaly tagging process; e.g., scores above a given threshold are tagged as anomalies, while those below it are tagged as normal. The idea of a threshold is valuable, as it provides the analyst an easy lever with which to tune the "sensitivity" of the anomaly tagging process. Interestingly, while most methods for anomaly detection follow this

general approach, they differ in how they model normal behavior and generate anomaly scores.



The test step in the anomaly detection loop.

To further illustrate this process, consider the scenario where the task is to detect abnormal temperatures (e.g., spikes), given data from the temperature sensors attached to servers in a data center. We can use a statistical approach to solve this problem (see the table in the following section for an overview of common methods). In step 1, we assume the samples follow a normal distribution, and we can use sample data to learn the parameters of this distribution (mean and variance). We assign an anomaly score based on a sample's deviation from the mean and set a threshold (e.g., any value more than 3 standard deviations from the mean is an anomaly). In step 2, we then tag all new temperature readings and generate a report.



Anomaly scoring

# Approaches to Modeling Normal Behavior

Given the importance of the anomaly detection task, multiple approaches have been proposed and rigorously studied over the last few decades. To provide a high-level summary, we categorize the more popular techniques into four main areas: clustering, nearest neighbor, classification, and statistical. The following table provides a summary of the assumptions and anomaly scoring strategies employed by approaches within each category, and some examples of each.

AD Method	Assumptions	Anomaly Scoring
Clustering	Normal data points	Distance from near
	belong to a cluster (or	cluster centroid
	lie close to its	
	centroid) in the data	
	while anomalies do not	
	belong to any clusters.	

AD Method	Assumptions	Anomaly Scoring
Nearest Neighbour	Normal data instances occur in dense neighborhoods while anomalous data are far from their nearest neighbors	Distance from _k_t nearest neighbour
Classification	<ul> <li>A classifier can be learned which distinguishes between normal and anomalous with the given feature space</li> <li>Labeled data exists for normal and abnormal classes</li> </ul>	A measure of classi estimate (likelihood that a data point belongs to the norn class
Statistical	Given an assumed stochastic model, normal data instances fall in high-probability regions of the model while abnormal data points lie in low-probability regions.	Probability that a d point lies in a high- probability region in the assumed distribution

The majority of these approaches have been applied to univariate time series data; a single data point generated by the same process at various time steps (e.g., readings from a temperature sensor over time); and assume linear relationships within the data. Examples include KNN, k-means clustering, ARMA, ARIMA, etc. However, data is increasingly high-dimensional (e.g., multivariate datasets, images, videos), and the detection of anomalies may require the joint modeling of interactions between each variable. For these sorts of problems, deep learning approaches (the focus of this report) such as autoencoders, VAEs, sequence-to-sequence models, and GANs present some benefits.

# Why Use Deep Learning for Anomaly Detection

Deep learning approaches, when applied to anomaly detection, offer several advantages.

Deep learning approaches, when applied to anomaly detection, offer several advantages. First, these approaches are designed to work with multivariate data of different data types across each variable. This makes it easy to integrate information from multiple sources, and eliminates challenges associated with individually modeling anomaly for each variable and aggregating the results. Deep learning approaches are also well adapted to jointly modeling the interactions between multiple variables with respect to a given task; and beyond the specification of generic hyperparameters (number of layers, units per layer, etc.), deep learning models require minimal tuning to achieve good results.

Performance is another advantage. Deep learning methods offer the opportunity to model complex, nonlinear relationships within data, and leverage this for the anomaly detection task. The performance of deep learning models can also potentially scale with the availability of appropriate training data, making them suitable for data-rich problems.

#### NM: We need to move this somewhere else

Finally, while deep learning methods can be complex (leading to their reputation as black box models), interpretability techniques such as LIME (see our previous report, "Interpretability") and <u>Deep SHAP</u> provide opportunities for analysts to inspect their behavior and make them more interpretable.

## What Can Go Wrong?

There are a proliferation of algorithmic approaches that can help one tackle an anomaly detection task and build solid models, at times even with just normal samples. But do they really work? What could possibly go wrong? Here are some of the issues that need to be considered:

Contaminated normal examples: In large-scale applications that have huge volumes of data, it's possible that within the large unlabeled dataset that's considered the normal class a small percentage of the examples may actually be anomalous, or simply be poor training examples. And while

some models (like a one-class SVM or isolation forest) can account for this, there are others that may not be robust to detecting anomalies.

Computational complexity: Anomaly detection scenarios can sometimes have low latency requirements i.e., it may be necessary to be able to speedily retrain existing models as new data becomes available, and perform inference. This can be computationally expensive at scale, even for linear models for univariate data. Deep learning models also incur additional compute costs to estimate their large number of parameters. To address these issues, it is recommended to explore trade-offs that balance the frequency of retraining and overall accuracy.

Human supervision: One major challenge with unsupervised and semisupervised approaches is that they can be noisy and may generate a large amount of false positives. In turn, false positives incur labor costs associated with human review. Given these costs, an important goal for anomaly detection systems is to incorporate the results of human review (as labels) to improve model quality.

Definition of anomaly: In many data domains, the boundary between normal and anomalous behavior is not precisely defined and is continually evolving. Unlike in other task domains where dataset shift occurs sparingly, anomaly detection systems should anticipate and account for (frequent) changes in the distribution of the data. In many cases, this can be achieved by frequent retraining of the models.

Threshold selection: The process of selecting a good threshold value can be challenging. In a semi-supervised setting (the approaches covered above), one has access to a pool of labeled data. Using these labels, and some domain expertise, it is possible to determine a suitable threshold. Specifically, one can explore the range of anomaly scores for each data point in the validation set and select as a threshold the point that yields the best performance metric (accuracy, precision, recall). In the absence of labeled data, and assuming that most data points are normal, one can use statistics such as standard deviation and percentiles to infer a good threshold.

#### **CHAPTER 3**

# Deep Learning for Anomaly Detection

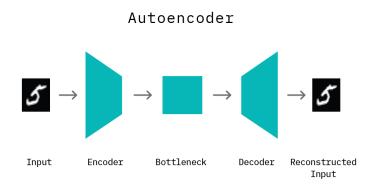
As data becomes high dimensional, it is increasingly challenging to effectively learn a model of normal behavior. In this chapter, we will review a set of relevant deep learning model architectures and how they can be applied to the task of anomaly detection. As discussed in <a href="Chapter 2.">Chapter 2.</a>
<a href="Background">Background</a>, anomaly detection involves first learning a model of normal behavior, then generating anomaly scores that can be used to identify anomalous activity.

The deep learning approaches discussed here typically consist of two principal components: an encoder that learns to generate an internal representation of the input data, and a decoder that attempts to reconstruct the original input based on this internal representation. While the exact techniques for encoding and decoding vary across models, the overall benefit they offer is the ability to learn the distribution of normal input data and construct a measure of anomaly respectively.

### **Autoencoders**

Autoencoders are neural networks designed to learn a low-dimensional representation, given some input data. They consist of two components: an encoder that learns to map input data to a low-dimensional representation (termed the *bottleneck*), and a decoder that learns to map this low-dimensional representation back to the original input data. By structuring the learning problem in this manner, the encoder network learns an efficient "compression" function that maps input data to a salient lower-dimensional representation, such that the decoder network is able to successfully reconstruct the original input data. The model is trained by minimizing the reconstruction error, which is the difference (mean squared error) between the original input and the reconstructed output produced by the decoder. In practice, autoencoders have been applied as a

dimensionality reduction technique, as well as in other use cases such as noise removal from images, image colorization, unsupervised feature extraction and data compression.



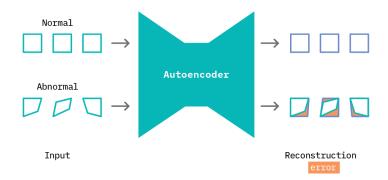
The components of an autoencoder

It is important to note that the mapping function learned by an autoencoder is specific to the training data distribution. That is, an autoencoder will typically not succeed at reconstructing data that is significantly different from the data it has seen during training. As we will see later in this chapter, this property of learning a distribution-specific mapping (as opposed to a generic linear mapping) is particularly useful for the task of anomaly detection.

# Modeling Normal Behavior and Anomaly Scoring

Applying an autoencoder for anomaly detection follows the general principle of first modeling normal behavior and subsequently generating an anomaly score for each new data sample. To model normal behavior, we follow a semi-supervised approach where we train the autoencoder on normal data samples. This way, the model learns a mapping function that successfully reconstructs normal data samples with a very small

reconstruction error. This behavior is replicated at test time, where the reconstruction error is small for normal data samples, and large for abnormal data samples. To identify anomalies, we use the reconstruction error score as an anomaly score and flag samples with reconstruction errors above a given threshold.



The use of autoencoders for anomaly detection.

This process is illustrated in the following figure. As the autoencoder attempts to reconstruct abnormal data, it does so in a manner that is weighted toward normal samples (square shapes). The difference between what it reconstructs and the input is the reconstruction error. We can specify a threshold and flag anomalies as samples with a reconstruction error above the given threshold.

### **Variational Autoencoders**

A variational autoencoder (VAE) is an extension of the autoencoder. Similar to an autoencoder, it consists of an encoder and a decoder network component, but it also includes important changes in the structure of the learning problem to accommodate variational inference. As opposed to learning a mapping from the input data to a fixed bottleneck vector (a point estimate), a VAE learns a mapping from input to a distribution, and learns

to reconstruct the original data by sampling from this distribution using a latent code. In Bayesian terms, the prior is the distribution of the latent code, the likelihood is the distribution of the input given the latent code, and the posterior is the distribution of the latent code, given our input. The components of a VAE serve to derive good estimates for these terms.

The encoder network learns the parameters (mean and variance) of a distribution that outputs a latent code vector, given the input data (posterior). In other words, one can draw samples of the bottleneck vector that "correspond" to samples from the input data. The nature of this distribution can vary depending on the nature of the input data (e.g., while Gaussian distributions are commonly used, Bernoulli distributions can be used if the input data is known to be binary).

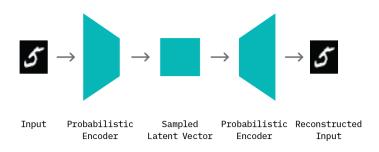
On the other hand, the decoder learns a distribution that outputs the original input data point (or something really close to it), given a latent bottleneck sample (likelihood). Typically, an isotropic Gaussian distribution is used to model this reconstruction space.

The VAE model is trained by minimizing the difference between the estimated distribution produced by the model and the real distribution of the data. This difference is estimated using the Kullback-Leibler divergence, which quantifies the distance between two distributions by measuring how much information is lost when one distribution is used to represent the other. Similar to autoencoders, VAEs have been applied in use cases such as unsupervised feature extraction, dimensionality reduction, image colorization, image denoising, etc. In addition, given that they use model distributions, they can be leveraged for controlled sample generation.

The probabilistic Bayesian components introduced in VAEs lead to a few useful benefits. First, VAEs enable Bayesian inference; essentially, we can now sample from the learned encoder distribution and decode samples that do not explicitly exist in the original dataset, but belong to the same data distribution. Second, VAEs learn a disentangled representation of a data distribution i.e., a single unit in the latent code is only sensitive to a single generative factor. This allows some interpretability of the output of VAEs, as we can vary units in the latent code for controlled generation of samples. Third, a VAE provides true probability measures that offer a principled approach to quantifying uncertainty when applied in practice

(for example, the probability that a new data point belongs to the distribution of normal data is 80%).



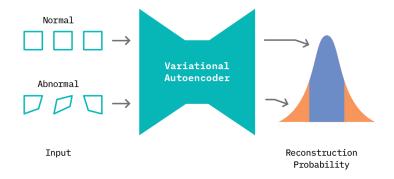


A variational autoencoder

# Modeling Normal Behavior and Anomaly Scoring

Similar to an autoencoder, we begin by training the VAE on normal data samples. At test time, we can compute an anomaly score in two ways. First, we can draw samples of the latent code z from the encoder given our input data, sample reconstructed values from the decoder using z, and compute a mean reconstruction error. Anomalies are flagged based on some threshold on the reconstruction error.

Alternatively, we can output a mean and a variance parameter from the decoder, and compute the probability that the new data point belongs to the distribution of normal data on which the model was trained. If the data point lies in a low-density region (below some threshold), we flag that as an anomaly. We can do this because we're modeling a distribution as opposed to a point estimate.



Two approaches to anomaly scoring with a VAE: we have the option of outputting the mean reconstruction probability (i.e., the probability that a sample belongs to the normal data distribution).

## Generative Adversarial Networks

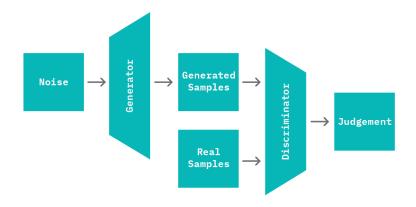
Generative adversarial networks (GANs) are neural networks designed to learn a generative model of an input data distribution. In their classic formulation, they're composed of a pair of (typically feed-forward) neural networks termed a generator, G, and discriminator, D. Both networks are trained jointly and play a competitive skill game with the end goal of learning the distribution of the input data, X.

**NM:** we use "images" instead of "input datapoints or samples" below check The generator network G learns a mapping from random noise of a fixed dimension (Z) to samples X\_ that closely resemble members of the input data distribution. The discriminator D learns to correctly discern real samples that originated in the source data (X) from fake samples (X\_) that are generated by G. At each epoch during training, the parameters of G are updated to maximize its ability to generate samples that are indistinguishable by D, while the parameters of D are updated to maximize

its ability to to correctly discern true samples X from generated samples X\_. As training progresses, G becomes proficient at producing samples that are similar to X, and D also upskills on the task of distinguishing real from fake samples.

In this classic formulation of GANs, while G learns to model the source distribution X well (it learns to map random noise from Z to the source distribution), there is no straightforward approach that allows us to harness this knowledge for controlled inference i.e., to generate a sample that is similar to a given known sample. While we can conduct a broad search over the latent space with the goal of recovering the most representative latent noise vector for an arbitrary sample, this process is compute-intensive and very slow in practice.

To address these issues, recent research studies have explored new formulations of GANs (known as BiGANs) that enable just this sort of controlled adversarial inference by introducing an encoder network, E.^[[See e.g. Jeff Donahue et al., "Adversarial Feature Learning" (2016), arXiv:1605.09782, and Samet AkCay et al., "GANomaly: Semi-Supervised Anomaly Detection via Adversarial Training" (2018), arXiv:1805.06725.] In simple terms, the encoder learns the reverse mapping of the generator; it learns to generate a fixed vector Z\_, given a sample. Given this change, the input to the discriminator is also modified; the discriminator now takes in pairs of input that include the latent representation (Z, and Z\_), in addition to the data samples (X and X\_). The encoder E is then jointly trained with the generator G; G learns an induced distribution that outputs samples of X given a latent code z, while E learns an induced distribution that outputs Z, given a sample X.



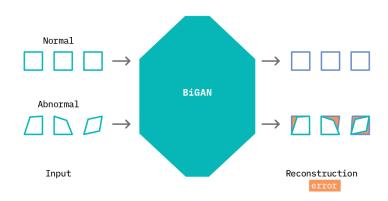
A traditional GAN (A) and a BiGAN (B).

Again, the mappings learned by components in the GAN are specific to the data used in training. For example, the generator component of a GAN trained on images of cars will always output an image that looks like a car, given any latent code. At test time, we can leverage this property to infer how different a given input sample is from the data distribution on which the model was trained.

# Modeling Normal Behavior and Anomaly Scoring

To model normal behavior, we train a BiGAN on normal data samples. At the end of the training process, we have an encoder E that has learned a mapping from data samples (X) to latent code space (Z\_), a discriminator D that has learned to distinguish real from generated data, and a Generator G that has learned a mapping from latent code space to sample space. Note that these mappings are specific to the distribution of normal data that has been seen during training. At test time, we perform the following steps to generate an anomaly score for a given sample X. First, we obtain a latent space value z from the encoder given X, which is fed to the generator and yields a sample X\_. Next, we can compute an anomaly score based on the reconstruction loss (difference between X and X\_) and the discriminator

loss (cross entropy loss or feature differences in the last dense layer of the discriminator, given both X and X ).



A BiGAN applied to the task of anomaly detection.

## **Sequence to Sequence Models**

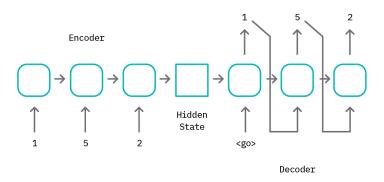
Sequence to sequence models are a class of neural networks mainly designed to learn mappings between data that are best represented as sequences. Data containing sequences can be challenging as each token in a sequence may have some form of temporal dependence on other tokens a relationship that has to be modeled to achieve good results. For example, consider the task of language translation where a sequence of words in one language needs to be mapped to a sequence of words in a different language. To excel at such a task, a model must take into consideration the (contextual) location of each word/token within the broader sentence; this allows it to generate an appropriate translation (See our previous report on Natural Language Processing to learn more about this area.)

On a high level, sequence to sequence models typically consist of an encoder, E, that generates a hidden representation of the input tokens, and a decoder, D, that takes in the encoder representation and

sequentially generates a set of output tokens. Traditionally, the encoder and decoder are composed of long short-term memory (LSTM) blocks, that are particularly suitable for modeling temporal relationships within input data tokens.

// RH: with the total number of steps determining the length of the output token? Or is it the reverse? While sequence to sequence models excel at modeling data with temporal dependence, they can be slow during inference each individual token in the model output is sequentially generated at each time step, where the total number of steps is the length of the output token).

We can use this encoder/decoder structure for anomaly detection by revising the sequence to sequence model to function like an autoencoder, training the model to output the same tokens as the input, shifted by 1. This way, the encoder learns to generate a hidden representation that allows the decoder to reconstruct input data that is similar to examples seen in the training dataset.



A sequence to sequence models

# Modeling Normal Behavior and Anomaly Scoring

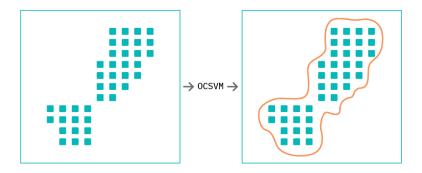
To identify anomalies, we take a semi-supervised approach where we train the sequence to sequence model on normal data. At test time, we can then compare the difference (mean squared error) between the output sequence generated by the model and its input. As in the approaches discussed previously, we can use this value as an anomaly score.

## One-Class Support Vector Machines

In this section, we discuss *one-class support vector machines* (OCSVMs), a non-deep learning approach to classification that we will use later (see <u>Chapter 4. Prototype</u>) as a baseline.

Traditionally, the goal of classification approaches is to help distinguish between different classes, using some training data. However, consider a scenario where we have data for only one class, and the goal is to determine whether test data samples are similar to the training samples. OCSVMs were introduced for exactly this sort of task: *novelty detection*, or the detection of unfamiliar samples. SVMs have proven very popular for classification, and they introduced the use of kernel functions to create nonlinear decision boundaries (hyperplanes) by projecting data into a higher dimension. Similarly, OCSVMs learn a decision function which specifies regions in the input data space where the probability density of the data is high. An OCSVM model is trained with various hyperparameters:

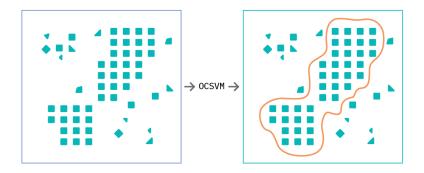
- nu specifies the fraction of outliers (data samples that do not belong to our class of interest) that we expect in our data.
- kernel specifies the kernel type to be used in the algorithm;
   examples include RBF, polynomial (poly), and linear. This enables
   SVMs to use a nonlinear function to project the input data to a higher dimension.
- gamma is a parameter of the RBF kernel type that controls the influence of individual training samples; this affects the "smoothness" of the model.



An OCSVM classifier learns a decision boundary around data seen during training.

# Modeling Normal Behavior and Anomaly Scoring

To apply OCSVM for anomaly detection, we train an OCSVM model using normal data, or data containing a small fraction of abnormal samples. Within most implementations of OCSVM, the model returns an estimate of how similar a data point is to the data samples seen during training. This estimate may be the distance from the decision boundary (the separating hyperplane), or a discrete class value (+1 for data that is similar and -1 for data that is not). Either type of score can be used as an anomaly score.



At test time, An OCSVM model classifies data points outside the learned decision boundary as anomalies (assigned class of -1).

### **Additional Considerations**

// RH: Possible to add some text between these headings?

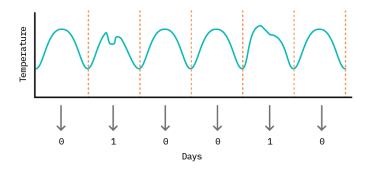
#### **Anomalies as Rare Events**

For the training approaches discussed thus far, we operate on the assumption of the availability of "normal" labeled data, which is then used to learn a model of normal behavior. In practice, it is often the case that labels do not exist or can be expensive to obtain. However, it is also a common observation that anomalies (by definition) are relatively infrequent events and therefore constitute a small percentage of the entire event dataset (for example, the occurrence of fraud, machine failure, cyberattacks, etc.). Our experiments (see <a href="Chapter 4. Prototype">Chapter 4. Prototype</a> for more discussion) have shown that the neural network approaches discussed above remain robust in the presence of a small percentage of anomalies (less than 10%). This is mainly because introducing a small fraction of anomalies does not significantly affect the network's model of normal behavior. For scenarios where anomalies are known to occur

sparingly, our experiments show that it's possible to relax the requirement of assembling a dataset consisting only of labeled normal samples for training.

# Discretizing Data and Handling Stationarity

To apply deep learning approaches for anomaly detection (as with any other task), we need to construct a dataset of training samples. For problem spaces where data is already discrete, we can use the data as is (e.g., a dataset of images of wall panels, where the task is to find images containing abnormal panels). When data exists as a time series, we can construct our dataset by discretizing the series into training samples. Typically this involves slicing the data into chunks with comparable statistical properties. For example, given a series of recordings generated by a data center temperature sensor, we can discretize the data into daily or weekly time slices and construct a dataset based on these chunks. This becomes our basis for anomaly comparison (e.g., the temperature pattern for today is anomalous compared to patterns for the last 20 days). The choice of the discretization approach (daily, weekly, averages, etc.) will often require some domain expertise; the one requirement is that each discrete sample be comparable. For example, given that temperatures may spike during work hours compared to non-work hours in the scenario we're considering, it may be challenging to discretize this data by hour as different hours exhibit different statistical properties.



Temperature readings for a data center over several days can be discretized (sliced) into daily 24-hour readings and labeled (0 for a normal average daily temperature, 1 for an abnormal temperature) to construct a dataset.

This notion of constructing a dataset of comparable samples is related to the idea of stationarity. A stationary series is one in which properties of the data (mean, variance) do not vary with time. Examples of nonstationary data include data containing trends (e.g., rising global temperatures) or with seasonality (e.g., hourly temperatures within each day). These variations need to be handled during discretization. We can remove trends by applying a differencing function to the entire dataset. To handle seasonality, we can explicitly include information on seasonality as a feature of each discrete sample; for instance, to discretize by hour, we can attach a categorical variable representing the hour of the day. A common misconception regarding the application of neural networks capable of modeling temporal relationships such as LSTMs is that they automatically learn/model properties of the data useful for predictions (including trends and seasonality). However, the extent to which this is possible is dependent on how much of this behavior is represented in each training sample. For example, to automatically account for trends or patterns across the day, we can discretize data by hour with an additional

categorical feature for hour of day, or discretize by day (24 features for each hour).

Note: For most machine learning algorithms, it is a requirement that samples be *independent* and *identically distributed*. Ensuring we construct comparable samples (i.e., handle trends and seasonality) from time series data allows us to satisfy the latter requirement, but not the former. This can affect model performance. In addition, constructing a dataset in this way raises the possibility that the learned model may perform poorly in predicting output values that lie outside the distribution (range of values) seen during training i.e., if there is a distribution shift. This greatly amplifies the need to retrain the model as new data arrives, and complicates the model deployment process. In general, discretization should be applied with care.

### Selecting a Model

There are several factors that can influence the primary approach taken when it comes to detecting anomalies. These include the data properties (time series vs. non-time series, stationary vs. non-stationary, univariate vs. multivariate, low-dimensional vs. high-dimensional), latency requirements, uncertainty reporting, and accuracy requirements. More importantly, deep learning methods are not always the best approach! To provide a framework for navigating this space, we offer the following recommendations:

### **Data Properties**

- Time series data: As discussed in the previous section, it is important
  to correctly discretize the data and to handle stationarity before
  training a model. In addition, for discretized data with temporal
  relationships, the use of LSTM layers as part of the encoder or decoder
  can help model these relationships.
- Univariate vs Multivariate: Deep learning methods are well suited to
  data that has a wide range of features: they're recommended for highdimensional data, such as images, and work well for modeling the
  interactions between multiple variables. For most univariate datasets,
  linear models<sup>[3]</sup> are both fast and accurate and thus typically preferred.

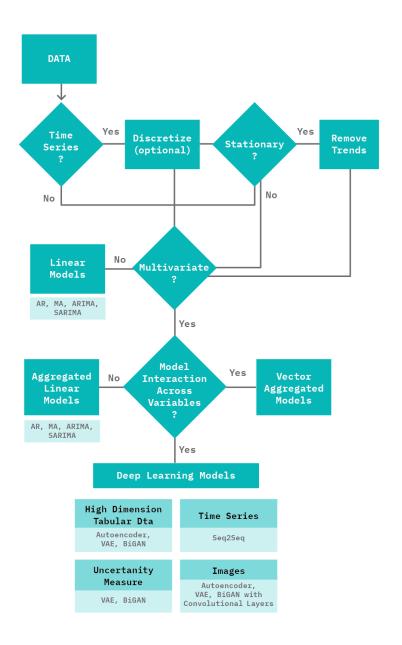
// RH: That's a lot of acronyms to throw at the reader (in the footnote). It would be helpful to point them to a reference they can look at to explain them all ("For a survey of linear models, see...").
Keep the formatting consistent with refs in earlier footnotes or just include a URL.

### **Business Requirements**

- Latency: Deep learning models are slower than linear models. For scenarios that include high volumes of data and have low latency requirements, linear models are recommended (e.g., for detecting anomalies in authentication requests for 200,000 work sites, with each machine generating 500 requests per second).
- **Accuracy**: Deep learning approaches tend to be robust, providing better accuracy, precision, and recall.
- Uncertainty: For scenarios where it is a requirement to provide a
  principled estimate of uncertainty for each anomaly classification,
  deep learning models such as VAEs and BiGANs are recommended.

# General Considerations in Selecting a Deep Learning Approach

When the (discretized) data contains sequences with temporal dependencies, a sequence to sequence model can model these relationships, yielding better results. For scenarios requiring principled estimates of uncertainty, a VAE and GAN based approaches are suitable. For scenarios where the data is images, AE's VAEs and GANs designed with convolution blocks are suitable.



The steps for selecting an approach to anomaly detection.

// RH: Add intro to table (something like "The following table highlights the pros and cons of the different types of models, to give you an idea of what kinds of data they are most useful for."?) Also, in the GAN row of the table, what do you mean by "learning of data manifold"? And is it necessary to say "(useful for high-dimensional image data)" in item 2, given item 3?

The following table highlights the pros and cons of the different types of models, to give you an idea under what kind of scenarios they are recommended.

Model	Pros	Cons
AutoEncoder	Flexible approach to modeling complex non-linear patterns in data	<ul> <li>Does not suppor variational inferenc (estimates of uncertainty)</li> <li>Requires a large dataset for training</li> </ul>
Variational AutoEncoder	Supports     variational inference     (probabilistic measure     of uncertainty)	Requires a large amount of training data, training can to a while

Model	Pros	Cons
GAN (BiGAN)	Supports variational inference (probabilistic measure of uncertainty)  Use of discriminator signal allows better learning of data manifold (useful for high dimensional image data).  Performs well for high dimensional data (images)  GANs trained in semi-supervised learning mode have shown great promise, even with very few labeled data <sup>[4]</sup>	Requires a large amount of training data, and longer training time (epocl to arrive at stable results <sup>[5]</sup> Training can be unstable (GAN mod collapse)
Sequence to Sequence Model	Well suited for data with temporal components (e.g., discretized time series data)	Slow inference     (compute scales will     sequence length will     needs to be fixed)     Training can be set in the second when data contains features with no temporal dependent of the supports     Variational inference (probabilistic measure)

Model	Pros	Cons
One Class SVM	<ul> <li>Does not require a large amount of data</li> <li>Fast to train</li> <li>Fast inference time</li> </ul>	Limited capacity capturing complex relationships withir data     Requires careful parameter selectio (kernel, nu, gamma that need to be carefully tuned.     Does not model probability distribution, harder compute estimates confidence.

#### **CHAPTER 4**

# **Prototype**

In this section, we provide an overview of the data and experiments used to evaluate each of the approaches mentioned in the <> chapter. We also introduce two prototypes we built to demonstrate results from the experiments and how we designed each prototype.

## **Datasets**

#### **KDD**

The <u>KDD network intrusion dataset</u> is a dataset of TCP connections that have been labelled as normal or representative of network attacks.

A connection is a sequence of TCP packets starting and ending at some well defined times, between which data flows to and from a source IP address to a target IP address under some well defined protocol."

These attacks fall into four main categories - denial of service, unauthorized access from a remote machine, unauthorized access to local superuser privileges, and surveillance e.g. port scanning. Each TCP connection is represented as a set of attributes or features (derived based on domain knowledge) pertaining to each connection such as the number of failed logins, connection duration, data bytes from source to destination etc. The dataset is comprised of a training set (97278 normal traffic samples, 396743 attack traffic samples) and a test set (63458 normal packet samples, 185366 attack traffic samples). To make the data more realistic, the test portion of the dataset contains 14 additional attack types that are not in the train portion; thus, a good model should generalize well and detect attacks unseen at during training.

#### **ECG5000**

The <u>ECG5000</u> contains examples of ECG signals from a patient. Each data sample, which corresponds to an extracted heartbeat containing 140 points, has been labelled as normal or being indicative of heart conditions related to congestive heart failure. Given an ECG signal sample, the task is to predict if it is normal or abnormal. ECG5000 is well suited to a prototype for a few reasons — it is visual (signals can be visualized easily) and it is based on real data associated with a concrete use case (heart disease detection). While the task itself is not extremely complex, the data is multidimensional (140 values per sample which allows us demonstrate the value of a deep model), but small enough to rapidly train and run inference.

# Benchmarking Experiment Setup

We sought to compare each of the models discussed earlier using the KDD dataset. We preprocessed the data to keep only 18 continuous features (for easy reproducibility). Feature scaling (0-1 minmax scaling) is also applied to the data; scaling parameters are learned from training data and then applied to test data. We then trained each model using normal samples (97,278 samples) and evaluated it on the entire training set.

We implemented each model using comparable parameters (see table below) that allow us to benchmark them in terms of training (mean time per training epoch, mean training time to best accuracy), inference (mean inference time), storage (size of weights, number of parameters), and performance (ROC, precision, recall). The deep learning models (AE, VAE, Seq2seq, BiGAN) were implemented in Tensorflow (keras api); each model was trained till best accuracy measured on the same validation dataset, using the <u>Adam optimizer</u> and a learning rate of 0.01. OCSVM was implemented using the <u>Sklearn OCSVM</u> library using the <u>rbf</u> kernel and parameters (nu=0.01 and gamma=0.5). Additional details on the parameters for each model are summarized in the table below for reproducibility. These experiments were run on an Intel® Xeon® CPU @ 2.30GHz

Table ...

## **Observations**

#### **Training**

In terms of training, ocsvm and an autoencoder were the fastest to implement and train. While the BiGAN based model also demonstrated very good accuracy, it was the most challenging to train. This is in part due to a known stability issue (mostly fluctuating accuracy during training) [6] associated with GANs. Overall, the BiGAN approach, required more training epochs to arrive at stable results compared to the other deep methods.

#### **Inference and Storage**

Being the least complex model, OCSVM had the fastest inference time (12x faster than an autoencoder). In terms of storage, the biGAN model has the largest number of parameters and overall size of weights. These values have implications for the number of concurrent models

#### **Performance**

For the current KDD dataset, we found that the autoencoder had the best performance.

# **Web Application Prototypes**

We built two prototypes that demonstrate results and insights from our experiments. The first prototype – is built on on the KDD dataset used in the experiments above and is a visualization of the performance of 4 approaches to anomaly detection. The second prototype is an interactive explainer that focuses on the autoencoder model and results from applying it to detecting anomalies in ECG data.

# Prototype I - Grant to Add Prototype Name

This prototype is built on the KDD network intrusion dataset

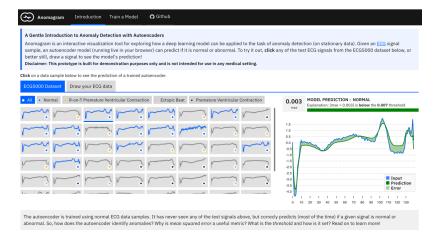
## **Prototype II - Anomagram**

This section describes Anomagram - an interactive web based experience where the user can build, train and evaluate an autoencoder to detect anomalous ECG signals. It utilizes the ECG5000 dataset mentioned above <<>>.

#### **UX Goals for Anomagram**

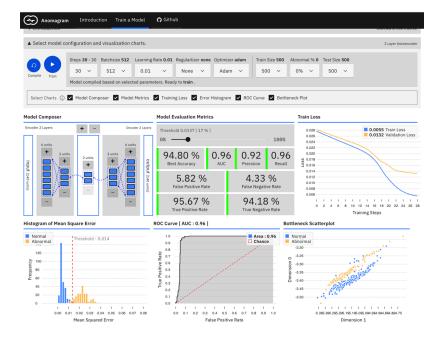
Anomagram is designed as part of a growing area interactive visualizations (see Neural Network Playground [3], ConvNet Playground, GANLab, GAN dissection, etc) that help communicate technical insights on how deep learning models work. It is entirely browser based and implemented in Tensorflow.js. This way, users can explore live experiments with no installations required. Importantly, Anomagram moves beyond the user of toy/synthetic data and situates learning within the context of a concrete task (anomaly detection for ECG data). The overall user experience goals for Anomagram are summarized as follows.

Goal 1: Provide an introduction to Autoencoders and how they can be applied to the task of anomaly detection. This is achieved via the *Introduction* module (see screenshot below). This entails providing definitions of concepts (reconstruction error, thresholds etc) paired with interactive visualizations that demonstrate concepts (e.g. an interactive visualization for inference on test data, a visualization of the structure of an autoencoder, a visualization of error histograms as training progresses, etc). fd



Introduction module view.

Goal 2: Provide an interactive, accessible experience that supports technical learning by doing. This is mostly accomplished within the *Train a Model* module (see screenshot below) and is designed for users interested in additional technical depth. It entails providing a direct manipulation interface that allows the user to specify a model (add/remove layers and units within layers), modify model parameters (training steps, batchsize, learning rate, regularizer, optimizer, etc), modify training/test data parameters (data size, data composition), train the model, and evaluate model performance (visualization of accuracy, precision, recall, false positive, false negative, ROC etc metrics) as each parameter is changed. Who should use Anomagram? Anyone interested in an accessible way to learn about autoencoders and anomaly detection . Useful for educators (tool to support guided discussion of the topic), entry level data scientists, and non-ML experts (citizen data scientists, software developers, designers etc).



Train a Model module view.

#### **Interface Affordances and Insights**

This section discusses some explorations the user can perform with Anomagram, and some corresponding insights.

Craft (Adversarial) Input: Anomalies by definition can take many different and previously unseen forms. This makes the assessment of anomaly detection models more challenging. Ideally, we want the user to conduct their own evaluations of a trained model e.g. by allowing them to upload their own ECG data. In practice, this requires the collection of digitized ECG data with similar preprocessing (heartbeat extraction) and range as the ECG5000 dataset used in training the model. This is challenging. The next best way to allow testing on examples contributed by the user is to provide a simulator — hence the draw your ECG data feature. This provides a (html) canvas on which the user can draw signals and observe the model's behaviour. Drawing strokes are converted to an array, with interpolation for incomplete drawings (total array size=140) and fed to the model. While this approach has limited realism (users may not have sufficient domain expertise to draw meaningful signals), it provides an

opportunity to craft various types of (adversarial) samples and observe the model's performance. Insights: The model tends to expect reconstructions that are close to the mean of normal data samples. Using the Draw your ecg data feature, the user can draw (adversarial) examples of input data and observe model predictions/performance.



Using the Draw your ecg data feature, the user can draw (adversarial) examples of input data and observe model predictions/performance.

Visually Compose a Model: Users can intuitively specify an autoencoder architecture using a direct manipulation model composer. They can add layers and add units to layers using clicks. This architecture is then used to specify the model's parameters each time the model is compiled. This follows a similar approach used in "A Neural Network Playground"[3]. The model composer connector lines are implemented using the leaderline library. Relevant lines are redrawn or added as layers are added or removed from the model. Insights: There is no marked difference between a smaller model (1 layer) and a larger model (e.g. 8 layers) for the current task. This is likely because the task is not especially complex (a visualization of PCA points for the ECG dataset suggests it is linearly separable). Users can visually compose the autoencoder model — add remove layers in the encoder and decoder. To keep the encoder and decoder symmetrical, add/remove operations on either is mirrored.

Effect of Learning Rate, Batchsize, Optimizer, Regularization: The user can select from 6 optimizers (Adam, Adamax, Adadelta, Rmsprop, Momentum, Sgd), various learning rates, and regularizers (l1, l2, l1l2). Insights: Adam reaches peak accuracy with less steps compared to other optimizers. Training time increases with no benefit to accuracy as batchsize is reduced (when using Adam). A two layer model will quickly overfit on the data; adding regularization helps address this to some extent. Try them out!

Effect of Threshold Choices on Precision/Recall: Earlier in this report (see background section on <>) we highlight the importance of metrics such as precision and recall and why accuracy is not enough. To support this discussion, the user can visualize how threshold choices impact each of these metrics. Insights: As threshold changes, accuracy can stay the same but, precision and recall can vary. This further illustrates how the threshold can be used by an analyst as a lever to reflect their precision/recall preferences.

**Effect of Data Composition**: We may not always have labelled normal data to train a model. However, given the rarity of anomalies (and domain expertise), we can assume that unlabelled data is mostly comprised of normal samples. However, this assumption raises an important question - does model performance degrade with changes in the percentage of abnormal samples in the dataset? In the train a model section, you can specify the percentage of abnormal samples to include when training the autoencoder model. Insights: We see that with 0% abnormal data, the model AUC is ~96%. Great! At 30% abnormal sample composition, AUC drops to ~93%. At 50% abnormal data points, there is just not enough information in the data that allows the model to learn a pattern of normal behaviour. It essentially learns to reconstruct normal and abnormal data well and mse is no longer a good measure of anomaly. At this point, model performance is only slightly above random chance (AUC of 56%).

#### CHAPTER 5

# Landscape

In this section, we review the landscape of open source tools, service vendor offerings, their trade-offs, and when to use each.

# Open Source Tools and Frameworks

Popular open source machine learning libraries or packages in Python and R include implementations of algorithmic techniques that can be applied to anomaly detection tasks. Algorithms (e.g., clustering, OC-SVM, isolation forests) exist as part of a general-purpose framework like scikit-learn and do not cater specifically to anomaly detection. In addition, generic packages for univariate time series forecasting (e.g., Facebook's <u>Prophet</u>) have been applied widely to anomaly detection tasks where anomalies are identified based on the difference between the true value and a forecast.

In this section of the report, our focus is on comprehensive toolboxes that specifically address the task of anomaly detection.

## **Python Outlier Detection (PyOD)**

<u>PyOD</u> is an open-source Python toolbox for performing scalable outlier detection on multivariate data. Uniquely, it provides access to a wide range of outlier detection algorithms, including established outlier ensembles and more recent neural network-based approaches, under a single, well-documented API.

#### Distinct advantages:

 It contains more than 20 algorithms which cover both classical techniques such as local outlier factor and recent neural network architectures such as autoencoders or adversarial models.

- PyOD implements combination methods for merging the results of multiple detectors and outlier ensembles which are an emerging set of models.
- It includes a unified API, detailed documentation, and interactive examples across all algorithms for clarity and ease of use.
- All models are covered by unit testing with cross-platform continuous integration, code coverage, and code maintainability checks.
- Optimization instruments are employed when possible: just-in-time (JIT) compilation and parallelization are enabled in select models for scalable outlier detection. Lastly, PyOD is compatible with both Python 2 and 3 across major operating systems.

## Seldon's Anomaly Detection Package

<u>Seldon.io</u> is known for its open source machine learning deployment solution for Kubernetes, which can in principle be used to serve arbitrary models. In addition, the Seldon team has recently released <u>alibi-detect</u> - a Python package focused on outlier, adversarial, and concept drift detection. The package aims to cover both online and offline detectors for tabular data, text, images and time series. The outlier detection methods should allow the user to identify global, contextual and collective outliers.

They have identified anomaly detection as a sufficiently important capability to warrant a dedicated attention in the framework, and have implemented several models to use "out-the-box." The existing models include seq2seq LSTMs, variational auto-encoders, spectral residual for time series, gaussian mixture models, isolation forests, Mahalanobis distance, and others. Note that they also provide examples and documentation on how to use along with their platform.

In the Seldon Core architecture, anomaly detection methods may be implemented as either a model or an input transformer. In the latter case, they can be composed with other data transformations to process inputs to another model. This nicely illustrates one role anomaly detection can play in machine learning systems: flagging bad inputs before they pass through the rest of a pipeline.

## R packages

The following section reviews R packages that have been created for anomaly detection. Interestingly, most of them deal with time series data.

#### Twitter's Anomaly Detection package

Twitter's <u>AnomalyDetection</u> is an open-source R package to automatically detect anomalies. It is applicable across a wide variety of contexts (for example, detecting anomalies in system metrics after a new software release, user engagement after an A/B test, or problems in econometrics, financial engineering, political and social sciences). It can help detect global/local anomalies as well as positive/negative (i.e., a point-in-time increase/decrease in values) anomalies.

The primary algorithm, Seasonal Hybrid ESD (S-H-ESD), builds upon the Generalized ESD test for detecting anomalies - which can be global as well as local. This is achieved by employing time series decomposition and using robust statistical metrics, i.e., median together with ESD. In addition, for a long time series (say, 6 months of minutely data), the algorithm employs piecewise approximation.

Besides time series, the package can also be used to detect anomalies in a vector of numerical values when the corresponding timestamps are not available. The package provides rich visualization support. The user can specify the direction of anomalies, the window of interest (such as last day, last hour), as well as enable/disable piecewise approximation, and the x- and y-axis are annotated to assist visual data analysis.

## Anomalize package

The <u>anomalize</u> package, open sourced by Business Science, does time series anomaly detection that goes inline with other <u>Tidyverse packages</u> (or packages supporting tidy data).

Anomalize has three main functions:

- Decompose: separates out the time series into seasonal, trend, and remainder components
- Anomalize: applies anomaly detection methods to the remainder component

 Recompose: calculates upper and lower limits that separate the "normal" data from the anomalies

#### **Tsoutliers package**

This <u>package</u> implements a procedure based on the approach described in <u>Chen and Liu (1993)</u> for automatic detection of outliers in time series. Time series data often undergoes non-systematic changes that alter the dynamics of the data transitory or permanently. The approach considers innovational outliers, additive outliers, level shifts, temporary changes, and seasonal level shifts - while fitting a time series model.

# Numenta's HTM (Hierarchical Temporal Memory)

Research organization <u>Numenta</u> has introduced hierarchical temporal memory (HTM) \— a machine learning model for anomaly detection. At the core of HTM are time-based learning algorithms that store and recall temporal patterns. Unlike most other machine learning methods, HTM algorithms learn time-based patterns in unlabeled data on a continuous basis. They are robust to noise, and high capacity - meaning they can learn multiple patterns simultaneously. The HTM algorithms are documented and available through its open source project, NuPIC (Numenta Platform for Intelligent Computing). The HTM technology is suited to address a number of problems, particularly those with the following characteristics: streaming data, underlying patterns in data change over time, subtle patterns, and time-based patterns.

One of the first commercial applications developed using NuPIC is <u>Grok</u>, which performs IT analytics, giving insight into IT systems to identify unusual behavior and reduce business downtime. Another is <u>Cortical.io</u>, which enables applications in natural language processing.

The NuPIC platform also offers several tools such as the HTM Studio and the Numenta Anomaly Benchmark (NAB). HTM Studio is a desktop tool that finds anomalies in time series without the need to program, code, or set parameters. NAB is a novel benchmark for evaluating and comparing algorithms for anomaly detection in streaming, real-time applications. It is

composed of over 50 labeled real-world and artificial time series data files, plus a novel scoring mechanism designed for real-time applications.

Besides this, there are example applications available on NuPIC that include sample code and white papers for: tracking anomalies in the stock market, ogue behavior detection - finding anomalies in human behavior, geospatial tracking - finding anomalies in objects moving through space and time

Numenta is a technology provider and does not create go-to-market solutions for specific use cases. The company licenses their technology and application code to developers, organizations, and companies who wish to build upon their technology. Numenta has several different types of licenses, including open source, trial, and commercial licenses.

Developers can use Numenta technology within NuPIC using the AGPL v3 open source license. Their HTM Studio is a free, desktop tool allows you to test whether our Hierarchical Temporal Memory (HTM) algorithms will find anomalies in your data without having to program, code or set parameters.

# **Anomaly Detection as a Service**

In this section, we survey a sample of anomaly detection service providers. Most of these providers can access data from public cloud databases, provide some kind of dashboard/report format to view/analyze data, have an alert mechanism when an anomaly occurs, and view underlying causes. An anomaly detection solution should try to reduce the time to detect and speed up the time to resolution by identifying KPIs and attributes that are causing the alert.

#### **Anodot**

#### **Capabilities**

Anodot is a real-time analytics and automated anomaly detection system that detects and turns outliers in time series data into business insights. They explore anomaly detection from the perspective of forecasting, where anomalies are identified based on deviations from expected forecasts. As part of their product, they do two things:

- Business monitoring: the system does SAAS monitoring, finds anomalies and helps with root cause analysis
- Business forecasting: forecasting, what if, and optimization.

#### **Data requirements**

Anodot supports multiple input data sources including direct uploads, or integrations with Amazon's S3 or Google Cloud storage. They are data agnostic and can track a variety of metrics, e.g., revenue, number of sales, the number of page visits, number of daily active users, etc.

#### Modeling approach/technique(s)

Anodot analyzes all the business metrics in real-time and at scale by running its ML algorithms on the live data stream itself, without reading or writing into a database. Every data point that flows into Anodot from all data sources is correlated with the relevant metric's existing normal model, and either flagged as an anomaly or serves to update the normal model. They believe that no single model can be used to cover all metrics. To allocate the optimal model for each metric, they first create a library of model types for different signal types (metrics that are stationary, nonstationary, multimodal, discrete, irregularly sampled, sparse, stepwise, etc.). Each new metric goes through a classification phase, and is matched with the optimal model. The model then learns "normal behavior" for each metric, which is a prerequisite to identifying anomalous behavior. To accommodate this kind of learning in real-time at scale, they use sequential adaptive learning algorithms which initialize a model of what is normal on the fly, and then compute the relation of each new data point going forward.

#### Point anomalies or intervals

Instead of flagging individual data points as anomalies, Anodot highlights intervals. Points within the entire duration of the interval are considered anomalous, preventing redundant alerts.

#### **Thresholding**

While users can specify static thresholds which trigger alerts, Anodot also provides automatic defaults where no thresholding input from the user is required.

#### **Root cause investigation**

Anodot helps investigate why the alert was triggered. It tries to understand how different active anomalies correlate (to expedite root cause investigation) and shortens the time to resolution. Anodot bands groups together different anomalies (or "incidents") which tell the story of the phenomena. These can be (a) multiple anomalous values in the same dimension (e.g., a drop in traffic from sources A and B, but not C, D or E), or (b) correlation between different anomalous KPIs, such as visits, conversions, orders revenue, error rate. Each incident has an Anomap, a graphic distribution of the dimensions most impacted. This is essentially a heat map that makes it easier to understand the whole picture.

#### **User Interface**

The Anodot interface enables the user to visualize and explore alerts. With the receipt of every alert, users are prompted to give the alert a binary score (good catch / bad catch). This input is fed back into the learning model to further tune it by providing real-life indications about the validity of its performance. By training the algorithms with direct feedback on anomalies, users can influence the system's functionality and results.

#### **Delivery**

Notifications can be forwarded to every user through his/her choice of channel(s). Anodot notification integrations include—but are not limited to —Slack, API, email, pagerduty, Jira, Microsoft Teams OpsGenie, etc.

## **Amazon's QuickSight**

## **Capabilities**

Amazon <u>QuickSight</u> is a cloud-native BI service that allows its users to create dashboards and visualizations to communicate business insights. In winter 2019, Amazon's machine learning capability was integrated with

QuickSight to provide anomaly detection, forecasting, and auto-narrative capabilities as part of the BI tool. It is a licensed software and pricing is usage-based; you only pay for the active usage, regardless of the number of users. That said, the pay-per-session could end up being expensive since anomaly detection tasks are compute intensive

#### **Data requirements**

QuickSight requires you to connect or import structured data directly query a SQL-compatible source, or ingest the data into SPICE. There is a requirement on the number of historical data points varying based on the task (analyzing anomalies or forecasting). There are also restrictions on the number of category dimensions that could be included (for example, product category, region, segment).

## Modeling approach/technique(s)

QuickSight provides a point and click solution to learn anomalous behavior and generate forecasts. It utilizes a built-in version of the Random Cut Forest (RCF) online algorithm, which can not only be noisy, but lead to large amounts of false positive alerts. On the plus side, it provides a customizable narrative feature that explains key takeaways from the insights generated. For instance, it could provide a summary of how the revenue compares to a previous period or a 30-day average, and/or highlight the event (in case of an anomaly).

#### Point anomalies or intervals

Anomalous events are presented discretely, on a point-by-point basis. So if an anomaly lasts more than a single time unit, the system will flag several events which could be noisy and redundant.

## **Thresholding**

Anomaly detection with QuickSight employs a thresholding approach to trigger anomalous events. The user provides a threshold value (low, medium, high, very high) that determines how sensitive the detector is to detected anomalies. Expect to see more anomalies when the setting is low, and fewer anomalies when the setting is set to high. This sensitivity is

determined based on standard deviations of the anomaly score generated by the RCF algorithm. This approach could be very tedious - especially when there are multiple time series being analyzed across various data hierarchy combinations - and introduces manual intervention.

#### **Root cause investigation**

One can interactively explore the anomalies on the Quicksight dashboard/report to help understand the root cause. QuickSight performs a contribution analysis which highlights the factors that significantly contribute to an anomaly. If you have dimensions in your data that are not being used in the anomaly detection, you can add up to four of them for contribution analysis. In addition, it can support interactive "what-if" queries. In these, some of the forecasts can be altered and treated as hypotheticals to provide conditional forecasts.

#### **User interface**

Quicksight anomaly detection provides a basic reporting interface. From a UI perspective, it is fairly unexceptional. For instance, it lacks a way to understand the overall picture with anomalous points. (Do the anomalies have some common contributing factors?) Furthermore, the forecasted values do not have confidence intervals associated with them, which would help the end-user visually understand the magnitude of the anomaly. As it stands, there is no basis for comparison.

#### **Delivery**

The QuickSight dashboards can be embedded within applications, shared among users, and/or be sent via email - as long as the recipients have a QuickSight subscription.

#### Outlier.ai

## **Capabilities**

<u>Outlier.ai</u> is a licensed software that uses artificial intelligence to automate the process of business analytics. It can connect to databases provided by cloud services and automatically provides insights to your inbox - without

the need to create reports or write queries. Outlier works with customers across industry segments, applying machine learning to automatically serve up business critical insights.

#### **Data requirements**

Outlier.ai can connect to databases provided by cloud services.

#### Modeling approach/technique(s)

Unknown

#### Point anomalies or intervals

Anomalous events are presented discretely, on a point-by-point basis.

#### **Thresholding**

N/A

## **Root cause investigation**

Outlier.ai allows customers to not only surface key insights about business changes automatically, but also identify the likely root causes of those changes; this feature guides teams in making quick, informed business decisions. Teams can easily share stories through PDF, PowerPoint optimized images, or an auto-generated email, annotated with their comments.

#### **User interface**

The UI is very similar to most standard BI tools, making it fairly user-friendly.

## **Delivery**

The dashboards can be embedded within applications, shared among users, and/or be sent via email.

#### Vectra.ai

#### **Capabilities**

In simple terms, Vectra's flagship platform, <u>Cognito</u> can be described as an intrusion detection system. This cloud-based, network detection-and-response system performs a number of cybersecurity related tasks including network traffic monitoring and anomaly detection. For this latter task, metadata collected from captured packets (rather than via deep-packet inspection) is analyzed using a range of behavioral detection algorithms. This provides insights about outlier characteristics that can be applied in a wide range of cybersecurity detection-and-response use cases. Cognito works with both encrypted and unencrypted traffic.

#### Data requirements

It can connect to databases provided by cloud services. Cognitio also uses metadata drawn from Active Directory and DHCP logs.

## Modeling approach/ technique(s)

According to a <u>whitepaper</u> published by Vectra, a mix of ML approaches are used to deliver the cybersecurity features the platform supports, in both global and local (network) contexts. For example, supervised learning techniques (such as Random Forest) can help to address cyberthreats associated with suspicious HTTP traffic patterns. Drawing on large-scale analysis of many types of malicious traffic and content as well as domain expertise, RF can be used to identify patterns of command-and-control behavior that don't exist in benign HTTP traffic. Vectra also uses unsupervised ML techniques such as k-means clustering to identify valid credentials that have potentially been stolen from a compromised host. This type of theft is the basis of cyberattacks such as pass-the-hash and golden ticket. Elsewhere, deep learning has proven effective in detecting suspicious domain activity; specifically, the detection of algorithmically-generated domains that are set up by cyberattackers as the front-end of their command-and-control infrastructure.

#### Point anomalies or intervals

Anomalous events are presented discretely, on a point-by-point basis.

#### **Thresholding**

The scoring of compromised hosts by the Vectra Threat Certainty Index allows security teams to define threshold levels based on combined scoring.

#### **Root cause investigation**

All detection events are correlated to specific hosts that show signs of threat behaviors. In turn, all context is assimilated into an up-to-the-moment score of the overall risk to the organization.

#### **User interface**

Vectra.ai's Cognito platform delivers detection information via a simple dashboard which displays information such as: a prioritized (in terms of risk) list of compromised hosts, changes in a host's threat and certainty scores, and 'key assets' that show signs of attack.

#### **Delivery**

The platform supports information-sharing by security teams on demand, or on a set schedule managed by its customizable reporting engine. Real-time notifications about network hosts - with attack indicators that have been identified (with the highest degree of certainty) as posing the biggest risk - is also a supported feature.

## Yahoo's Anomaly Detector - Sherlock

#### **Capabilities**

Sherlock is an open source anomaly detection service built on top of Druid (an open-source, distributed data store). It leverages the Java library, Extensible Generic Anomaly Detection System (EGADS) to detect anomalies in time-series data. It's fast and scalable. It allows users to schedule jobs on an hourly, daily, weekly, or monthly basis (although it also

supports ad hoc real-time anomaly detection requests). Anomaly reports can be viewed from Sherlock's interface, or received via email.

#### **Data requirements**

Sherlock accesses time series data via Druid JSON queries and uses a Redis backend to store job metadata, the anomaly reports (and other information) it generates, as well as a persistent job queue. These anomaly reports can be accessed via direct requests using the Sherlock client API or delivered via scheduled email alerts.

#### Modeling approach/ technique(s)

Sherlock takes a time-series modeling based approach to anomaly detection using three important modules from the EGADS library - time series modelling, anomaly detection, and alerting. The times-series modeling module supports the use of historical data to learn trends and seasonality in the data using model classes such as ARIMA. The resulting values are applied to the anomaly detection models that comprise the Anomaly Detection module. These models support a number of detection scenarios that are relevant in a cybersecurity context (e.g., outlier detection and change point detection). The Alerting module uses the error metric produced from anomaly detection models and outputs candidate anomalies based on dynamically learnt thresholds, learning to filter out irrelevant anomalies over time.

#### Point anomalies or intervals

Anomalous events are presented both discretely, on a point-by-point basis, and as intervals.

#### **Threshold**

Thresholds are learnt dynamically. No thresholding input from the user is required/supported.

#### Root cause analysis

#### **User interface**

Sherlock's user interface is built with <u>Spark Java</u> - a UI framework for building web applications. The UI enables users to submit instant anomaly analyses, create and launch detection jobs, and view anomalies on both a heatmap and a graph.

## **Delivery**

Scheduled anomaly requests are delivered via email or directly via API-based queries.

#### CHAPTER 6

# **Ethics**

Machine learning models that learn to solve tasks independently from data are susceptible to biases and other issues that may raise ethical concerns. Anomaly detection models have specific risks and mitigation tactics. In anomaly detection, when the definition of "normal" is independently learned and applied without controls, it may inadvertently reflect societal biases that can lead to harm. This presents risks to human welfare in scenarios where anomaly detection applications intersect with human behavior. It should go without saying that in relation to humans, we must resist the assumption that different is bad.

# **Diversity Matters**

Although anomalies are often scrutinized, their absence in the data may be even worse! Consider a model that is trained on x-ray images of normal luggage content that only uses images of luggage packed by citizens of North America. This could lead to unusually high stop and search rates for users from other parts of the world, where items packed might differ greatly.

To limit the potential harm of a machine learning model's tendency to assume that "different is bad," we can use a larger (or more varied) dataset, and provide human supervision of the model (both measures reduce the likelihood of errors). In the above example, this translates to using more varied x-ray image data to expand the machine's view of what is normal, and using human review to ensure that positive predictions aren't false positives.

# **Explainability**

In many anomaly detection applications, the system presents anomalous instances to the end user - a decision maker to provide a verdict (label) which can then be fed back to the model to refine it further. Unfortunately,

some applications may not provide enough explanation about why an instance was considered anomalous, leaving the end user with no particular guidance on where to begin investigation. Blindly relying on such applications may cause or in certain cases exacerbate bias.

## **Additional Use Cases**

Ethical considerations are important in every use of machine learning, particularly when the use case affects humans. Below are a few use cases in which this is particularly true of anomaly detection.

## **Data Privacy**

Protecting an individual's data has been a growing concern in the last few years, culminating in recent data privacy laws like the GDPR and CCPA. These laws don't just consider and penalize data breaches, but also guide and limit how an individual's personal data can be used and processed. Thus, when anomaly detection methods are used on protected data, privacy is paramount.

To give an example, in <<Chapter 3. Deep Learning for Anomaly Detection>> we discussed autoencoders, a type of neural network that has been widely used for anomaly detection. It contains an encoder network which reduces the dimension of the input data, and a decoder network which aims to reconstruct the input. The learning goal of autoencoders is to minimize the reconstruction error, which is consequently the loss function. Because the dimensionality reduction brings information loss, and the learning goal encourages to preserve the information that is common to most training samples, anomalies that contain rare information could be identified by measuring model loss.

In certain use cases, these identified anomalies could correspond to individuals. Improper disclosure of such data can have adverse consequences for a data subject's private information, or even lead to civil liability or bodily harm. One way to minimize these effects is to use a technique called differential privacy<sup>[7]</sup> on the data before it is fed into an anomaly detection system. This technique essentially adds a small amount of noise to the data, in order to mask individual identities while maintaining the accuracy of aggregated statistics. When coupled with an anomaly

detection system, differential privacy has been shown to reduce the false positives [8], thus protecting the privacy of more individuals who would otherwise have been scrutinized by being singled out.

## **Health Care Diagnostics**

Anomaly detection can be applied in health care scenarios to provide quick and early warnings for medical conditions. For example, a model can surface chest x-rays that substantially differ from normal chest x-rays, or highlight images of tissue samples as containing abnormalities. These analyses can have tremendous consequences for the patient. A false negative means an undetected disease, and a false positive means unnecessary - and potentially painful or even harmful - treatment.

For other machine learning tasks (e.g., churn prediction, resume review), we strive to remove racial or socioeconomic factors from the equation. In health care diagnostics, it may be both appropriate and advantageous to focus on them.

To the extent that an anomaly to be detected is connected with a certain group of people, models can be tailored to that group. For example, sickle-cell disease is more prevalent in parts of Africa and Asia than in Europe and the Americas. A diagnostic system for detecting this disease should include enough samples of Asian and African patients and acknowledgement of their ethnicity to make sure the disease is identified.

In any event, it is important to ensure that these systems remain curated (i.e., a medical professional verifies results) and that the models are correctly evaluated (precision, recall) before being put into production.

## Security

Similar to the luggage example we've already referenced, home or business security systems trained to identify anomalies also present a problem of the "different is bad" variety. These systems need to have enough data - in terms of quantity and variability - to prevent bias that would make them more likely to identify people of different races or socioeconomic status as anomalies based on, for example, their color or clothing.

#### **Content Moderation**

Blind reliance on anomaly detection systems for content moderation can lead to false positives that limit or silence system users based on the language or types of devices they use. Content moderation software should be monitored for patterns of inappropriate blocking or reporting, and should have a user appeal/review process.

#### **Financial Services**

Determining what harmful anomalies are in financial services is complex. On one hand, fraudsters are actively trying to steal and launder money, and move it around the world. On the other hand, nearly all transactions are legitimate services for valuable customers. Fraudsters affirmatively emulate normal business, making anomalies especially difficult to identify. As a result, financial services organizations should consider first whether anomaly detection is desirable in their use cases, and then consider the potential ethical and practical risks.

For example, banks use customer data to offer mortgages or student loans. A lack of diverse data could lead to unfavorable results for certain demographic groups. These biased algorithms can result in costly mistakes, reduce customer satisfaction, and damage a brand's reputation. To combat this, one should pose questions (like the following) that can help check for bias in the data or model:

- Fact check: do the detected anomalies mostly belong to underrepresented groups?
- · Are there enough features that explain minority groups?
- Has model performance been evaluated for each subgroup within your data?

## **Innovation**

As we have seen, the term anomaly can carry negative connotations. The nature of anomaly detection is identifying samples that are different from the bulk of the other samples - but as discussed, assuming that "different is bad" is not necessarily fair in many cases. Perhaps instead of associating

faulty interpretations with anomalies, pursuing them to reveal new truths could be helpful.

After all, progress in science is often triggered by anomalous activities that lead to innovation!

#### **CHAPTER 7**

# **Conclusion**

Anomaly detection is a classic problem, common to many business domains. In this report, we have explored how a set of deep learning approaches can be applied in a semi-supervised setting for addressing the anomaly detection task. We think this focus is useful for the following reasons:

- While deep learning has demonstrated superior performance for many business tasks, there is fairly limited information on how anomaly detection can be cast as a deep learning problem and how deep models perform.
- A semi-supervised approach is desirable in handling unseen, unknown anomalies and does not incur vast data labeling costs for businesses.
- Traditional machine learning approaches are suboptimal for handling high dimensional, complex data and modeling interactions between each variable.

In our <>, we show how deep learning models can achieve competitive performance on a multivariate tabular dataset (network intrusion detection). This is in concurrence with results from existing research that show superior performance of deep learning models for high dimensional data such as images (cite).

Overall, while deep learning approaches are useful, there are a few challenges that may limit their deployment in production settings.

 Latency: Compared to linear models (such as AR, ARMA, etc.) or shallow machine learning models (such as One Class SVM), deep learning models can have significant latency associated with inference. This makes it expensive to apply them within streaming data (high volume, high velocity) use cases at scale. For example, our experiments show that inference with OCSVM is 12x faster than with an autoencoder.

- Data Requirements: Deep learning models typically require a large dataset (tens of thousands of samples) for effective training. Further, deep models are prone to overfitting and need to be carefully evaluated to address this. Many anomaly use cases can frequently have few data points (e.g., daily sales data for two years will generate 712 samples, which may be insufficient to train a model). In such scenarios, linear models designed to work with smaller datasets are a better option.
- Managing Distribution Shift: In many scenarios, the underlying process generating data may legitimately change such that a datapoint that was previously anomalous becomes normal. The changes could be gradual, cyclical, or even abrupt in nature. This phenomenon, although not unique to anomaly detection, is known as concept drift. With respect to anomaly detection, one way to handle this is to frequently retrain the model as new data arrives or trigger retraining when concept drift is detected. It can be challenging to maintain this continuous learning approach for deep models, as training time can be significant.

Going forward, we expect the general approaches discussed in the report to continually evolve and mature. As examples, see recent extensions to the encoder-decoder model approach that are based on  $\mathsf{GMMs}^{[\underline{9}]}$ ,  $\mathsf{LSTMs}^{[\underline{10}]}$ ,  $\mathsf{CNNs}^{[\underline{11}]}$ , and  $\mathsf{GANs}^{[\underline{12}]}$ . Like everything else in machine learning, there is no "one size fits all"; no one model works best for every problem. The right approach always depends on the use case and data.

- 1. See e.g. Lukas Ruff et al., "Deep Semi-Supervised Anomaly Detection" (2019), arXiv:1906.02694. ←
- 2. For a survey of existing techniques, see Varun Chandola et al., "Anomaly Detection, A Survey" (2009), ACM Computing Surveys 41(3), https://dl.acm.org/doi/10.1145/1541880.1541882. €
- 3. Approaches such as AR, MA, ARMA, ARIMA, SARIMA, and VAR models. ←
- 4. <u>Deep Learning for Anomaly Detection: A Survey</u> €

- 5. <u>Improved Techniques for Training GANs</u> *←*
- 6. Improved Techniques for Training GANs ←
- 7. Differential Privacy, Dwork 2006 ←
- 8. Robust Anomaly Detection and Backdoor Attack Detection Via

  <u>Differential Privacy</u>
- 9. <u>Deep Autoencoding Gaussian Mixture Model for Unsupervised</u>
  <u>Anomaly Detection</u> ←
- 10. <u>Sequential VAE-LSTM for Anomaly Detection on Time Series</u> *←*
- 11. Time-Series Anomaly Detection Service at Microsoft  $\stackrel{\smile}{\sim}$
- 12. MAD-GAN: Multivariate Anomaly Detection for Time Series Data with Generative Adversarial Networks ←