



Synchronization of Physical Clocks

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Outline

Getting
Computer Clocks
Synchronized

- Generalities
- Cristian's algorithm
- Berkeley algorithm
- Network Time Protocol

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Generalities

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Time References

Every node has an internal clock, whose value has to be kept as close as possible to a reference time.

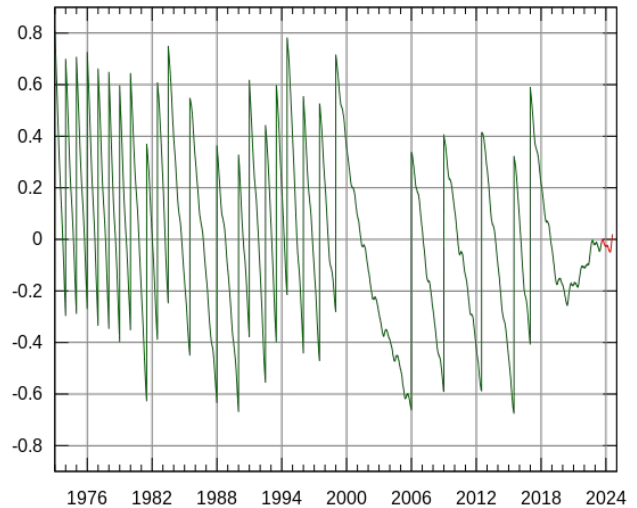
- **UTC** - coordinated universal time, primary reference for the scientific community, and based on International Atomic Time
- **UT1** - successor of GMT, “solar-based” reference time
- **Unix (POSIX) time** - nr. of seconds elapsed since 00:00:00 (UTC), Thursday, 1 January 1970, minus in-between *leap seconds*

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Leap Seconds?

Earth's rotation slowdown and irregularities make UT1 deviate from UTC.

Thus, corrections are needed.



From Wikipedia

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Chart aside: UT1-UTC vs UTC

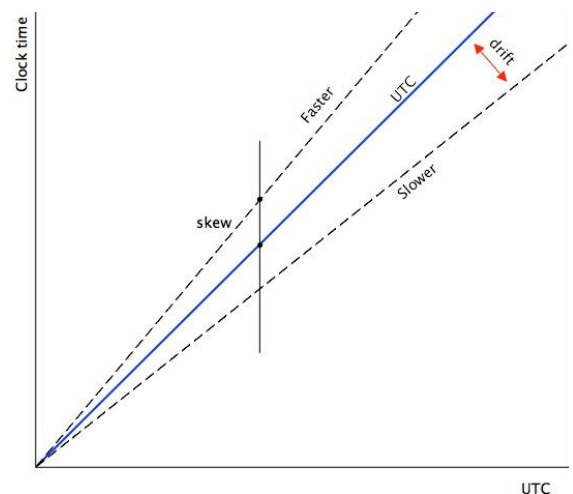
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Non-Aligned Clocks

Skew - difference in instantaneous reads of two clocks

Drift - difference in the rate of clocks.

Keeping two clocks synchronized means imposing an upper bound D on any of their instantaneous reads.



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External vs Internal Synchronization

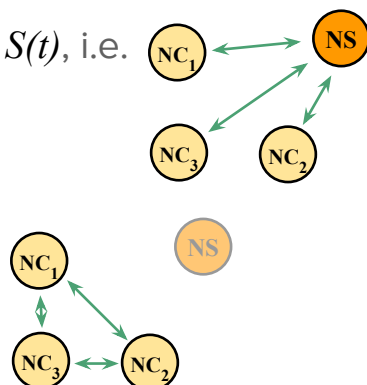
External: w.r.t. a trusted source of reference time $S(t)$, i.e.

$$|S(t) - C_i(t)| < D \quad \forall i$$

Internal: agreement within a group of nodes, i.e.

$$|C_i(t) - C_j(t)| < D \quad \forall i, j$$

If a system is externally synchronized with an accuracy D , then its internal clocks agree within a bound of $2D$

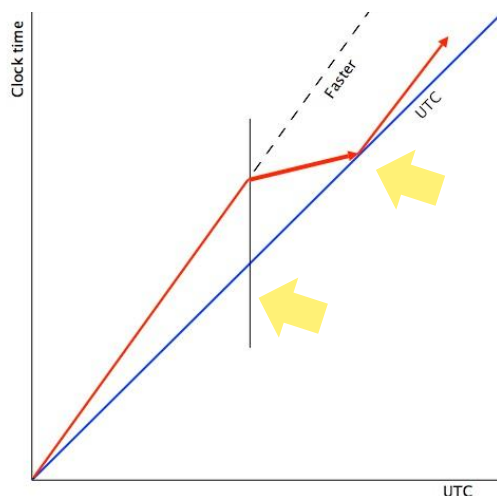


Resetting a Clock

Important: clock *monotonicity* must be assured!

No way to set back a clock: instead, its pace should be slowed down up to the point the correct value is reached.

Typical example: the “make” compilation utility.



Cristian's Algorithm

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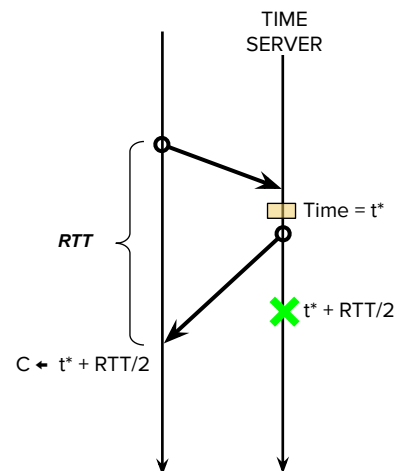
Idea: Exploit Round Trip Time

RTT can be measured by the client.

If $RTT \ll 1$, assuming req/reply latencies to be the same does not yield an excessive error, thus:

$$C \approx t^* + RTT/2$$

In practice, several tries can be done, so to possibly get lower RTTs.



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Internal Synchronization: The Berkeley Algorithm, and Beyond

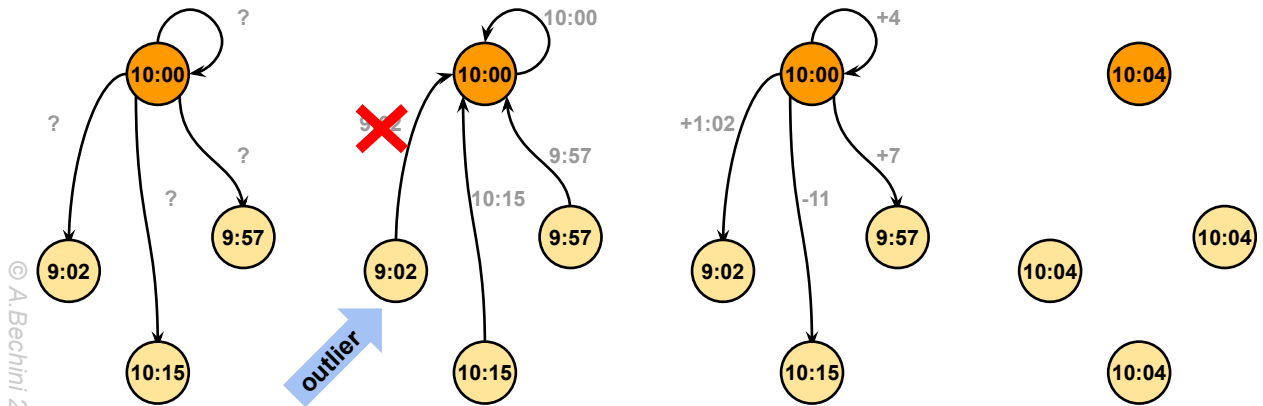
A Centralized Solution

Developed for groups of UNIX computers.

One process/node acts as master (*time daemon*); Successive steps:

- The time daemon asks all the others for their clock values.
- Each node answers back its actual time value;
the master annotate each RTT as well.
- The time daemon computes a *proper* average.
- The time daemon sends each node the **clock correction value**
(why not broadcasting the time?)

Berkeley Algorithm: an Illustration



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Decentralized Averaging Algorithm

Each node has a daemon, with approximated UTC.

- Periodically, each node broadcasts its own time.
- On each node, the new time value is obtained by averaging the local time and the received values.

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NTP - Network Time Protocol

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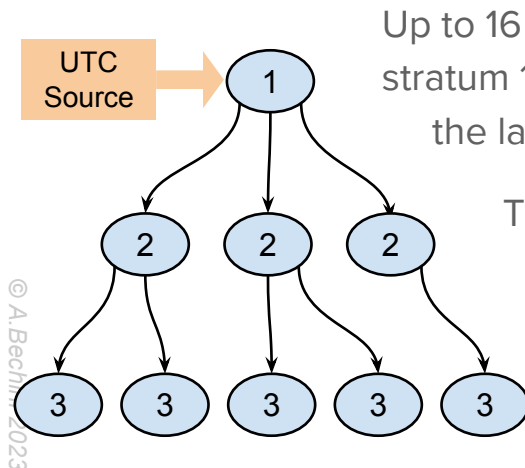
NTP - Overview

To enable clients across Internet to get synchronized with UTC.

- Scalable to large networks
- Statistical techniques to filter data
- Authentication against interference
- Hierarchy of time servers, spread across the Internet
- Messages sent over UDP

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Time Servers' Hierarchy - Strata



Up to 16 strata:

stratum 1 is connected to an UTC source;
the last one is “not synchronized”.

Time servers synchronize in 3 modes:

Multicast mode

Procedure Call mode

Symmetric mode

NTP Modes

- Multicast: 1+ servers multicast the time to the other nodes;
suitable for LANs
- Procedure Call: more accurate because of latency compensation,
using an approach based on Cristian's algorithm
- Symmetric: the most accurate and expensive,
used between servers in the upper (most precise) strata;
Pairs of servers exchange messages carrying the timestamp
for the involved events

Symmetric Mode

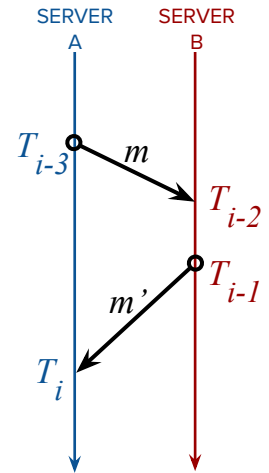
From the exchanged messages, a process must be able to get an estimate o_i of the actual offset o to fix its clock

$$\begin{cases} T_{i-2} = T_{i-3} + t_m + o \\ T_i = T_{i-1} + t_{m'} - o \end{cases} \quad \begin{cases} o = T_{i-2} - T_{i-3} - t_m \\ o = T_i - T_{i-1} + t_{m'} \end{cases}$$

$$RTT = t_m + t_{m'} = \Delta T_A - \Delta T_B = (T_i - T_{i-3}) - (T_{i-1} - T_{i-2})$$

$$o = \frac{1}{2} (T_{i-2} - T_{i-3} + T_{i-1} - T_i - t_m + t_{m'}) = o_i + \frac{1}{2} (t_{m'} - t_m)$$

$$o_i - \frac{1}{2} RTT \leq o \leq o_i + \frac{1}{2} RTT$$



Symmetric Mode: How to Fix Time

Estimated offset: $o_i = \frac{1}{2} (T_{i-2} - T_{i-3} + T_{i-1} - T_i)$

Accuracy (upper bound): RTT

- To fix the time, several pairs $\langle o_i, RTT \rangle$ are collected, and the most accurate value is used.