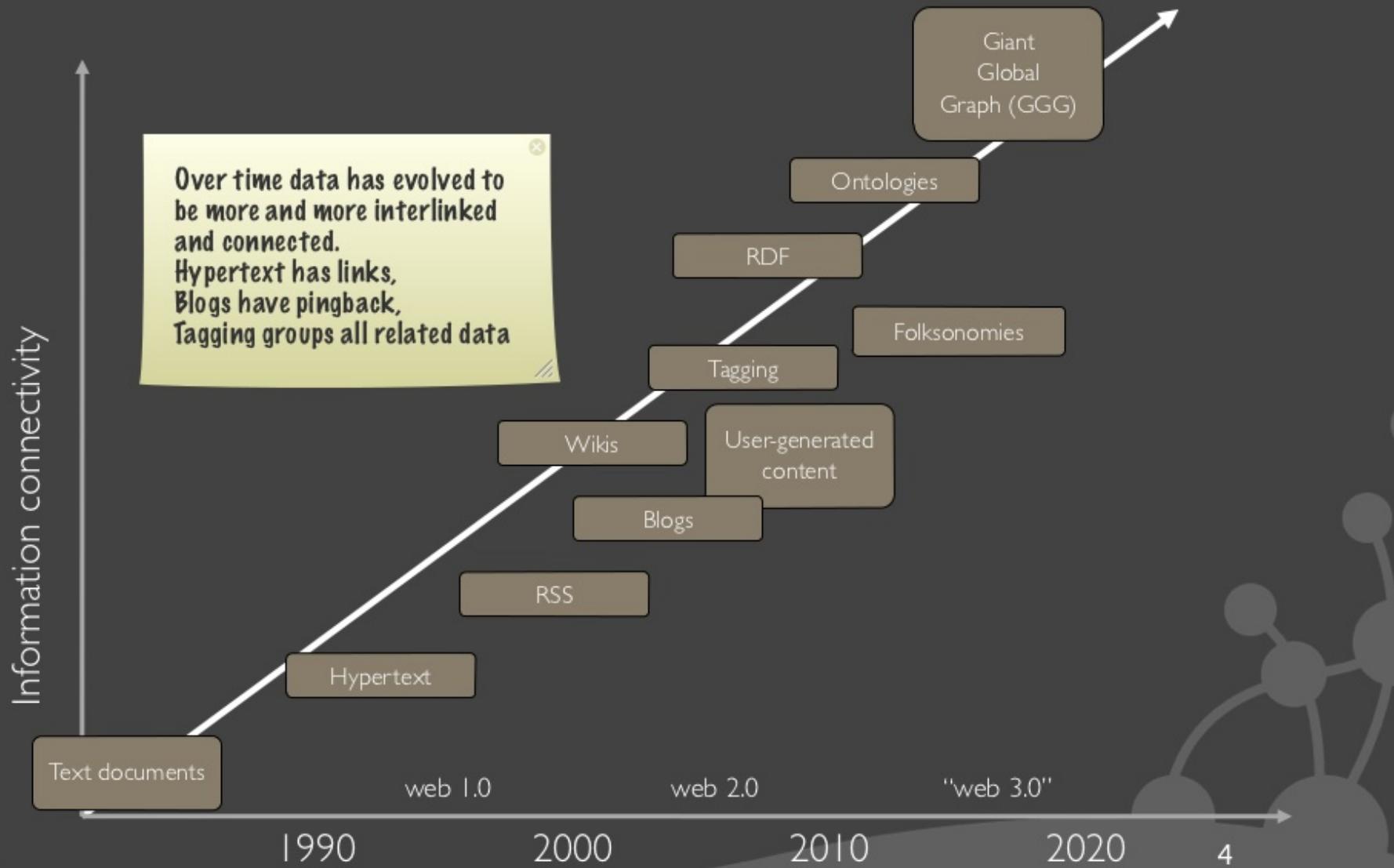
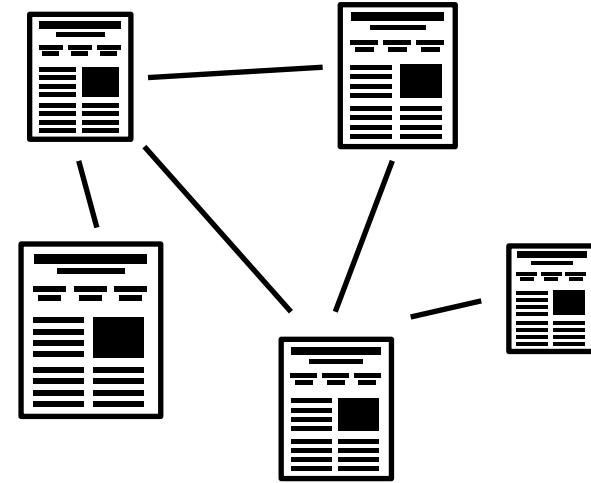
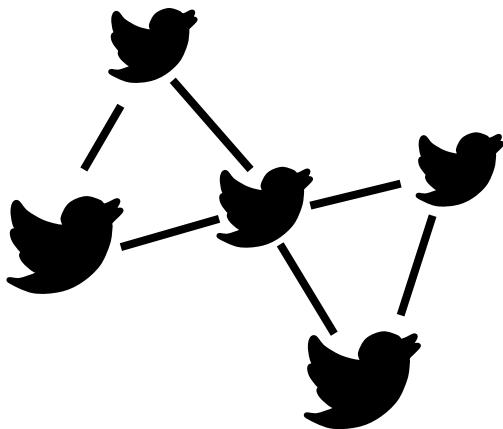


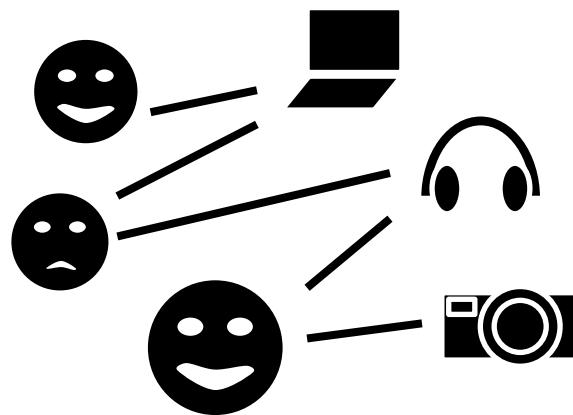
GraphDB: Neo4j

Trend 2: Connectedness

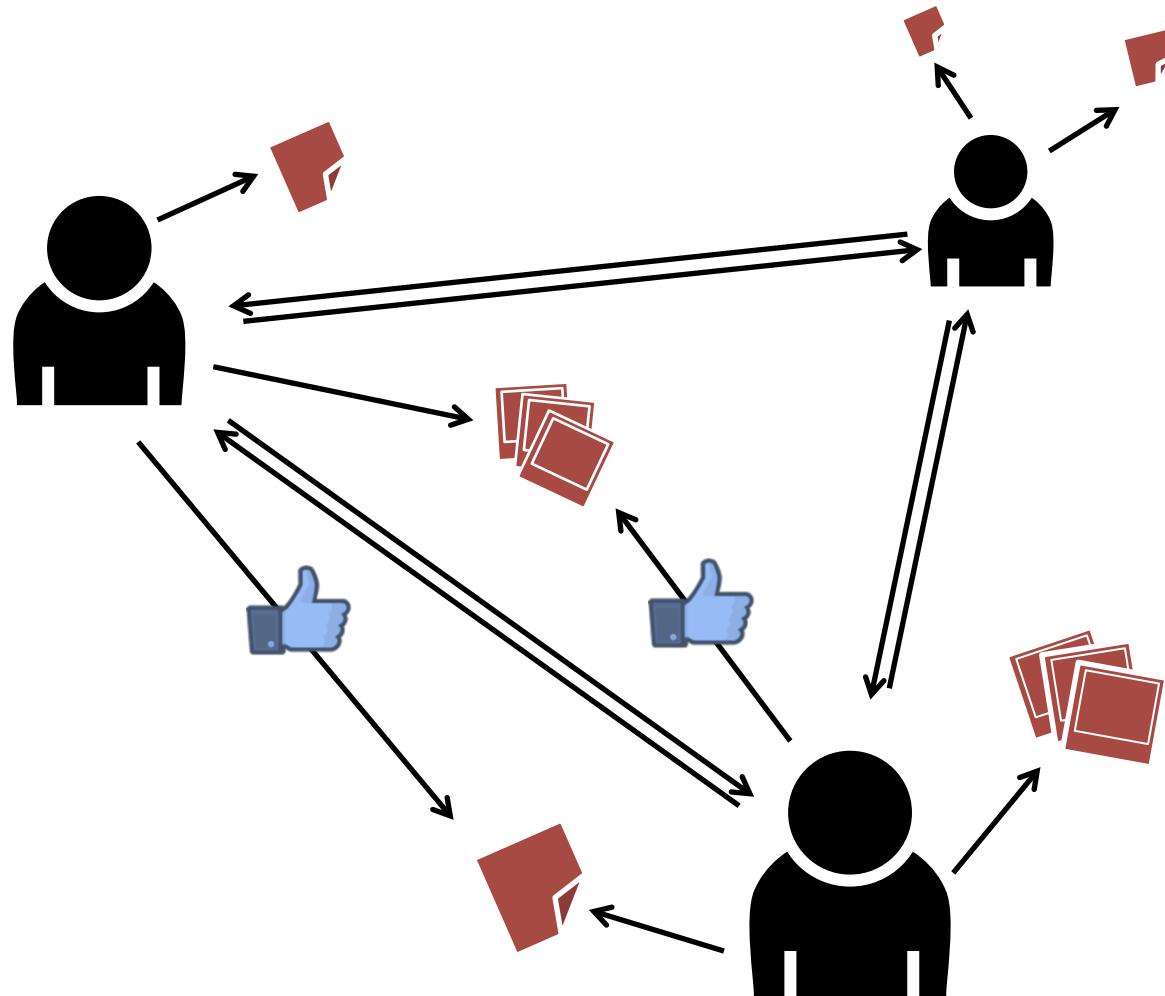




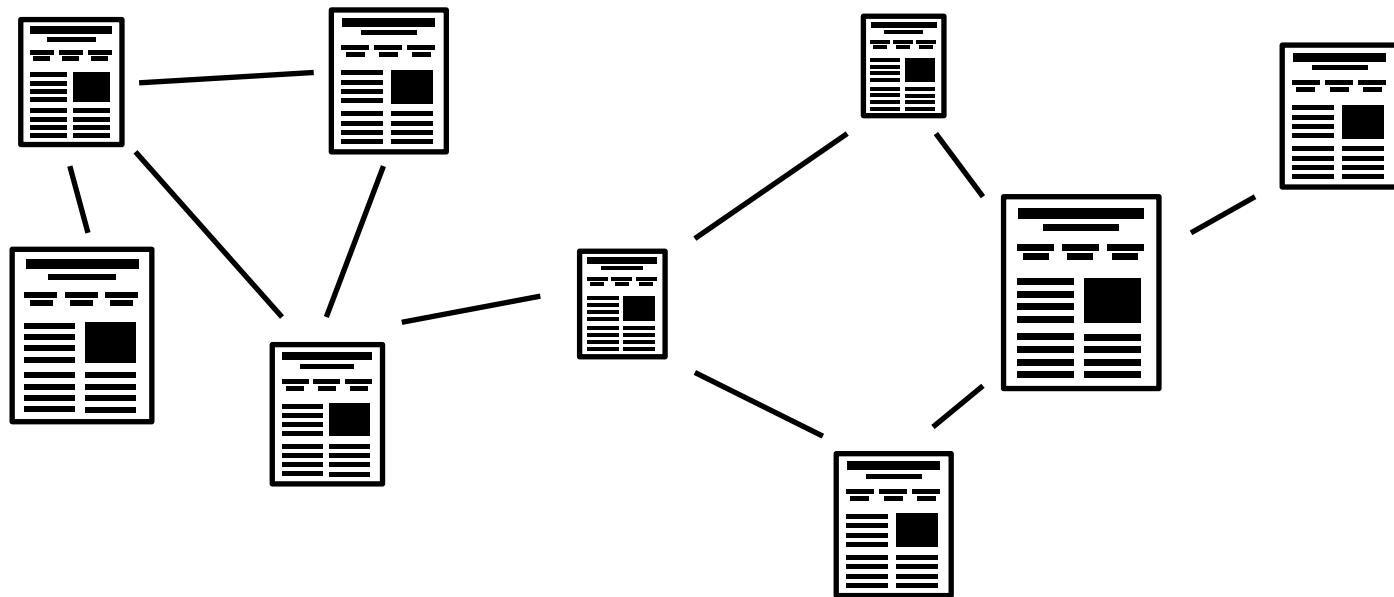
Graphs are Everywhere



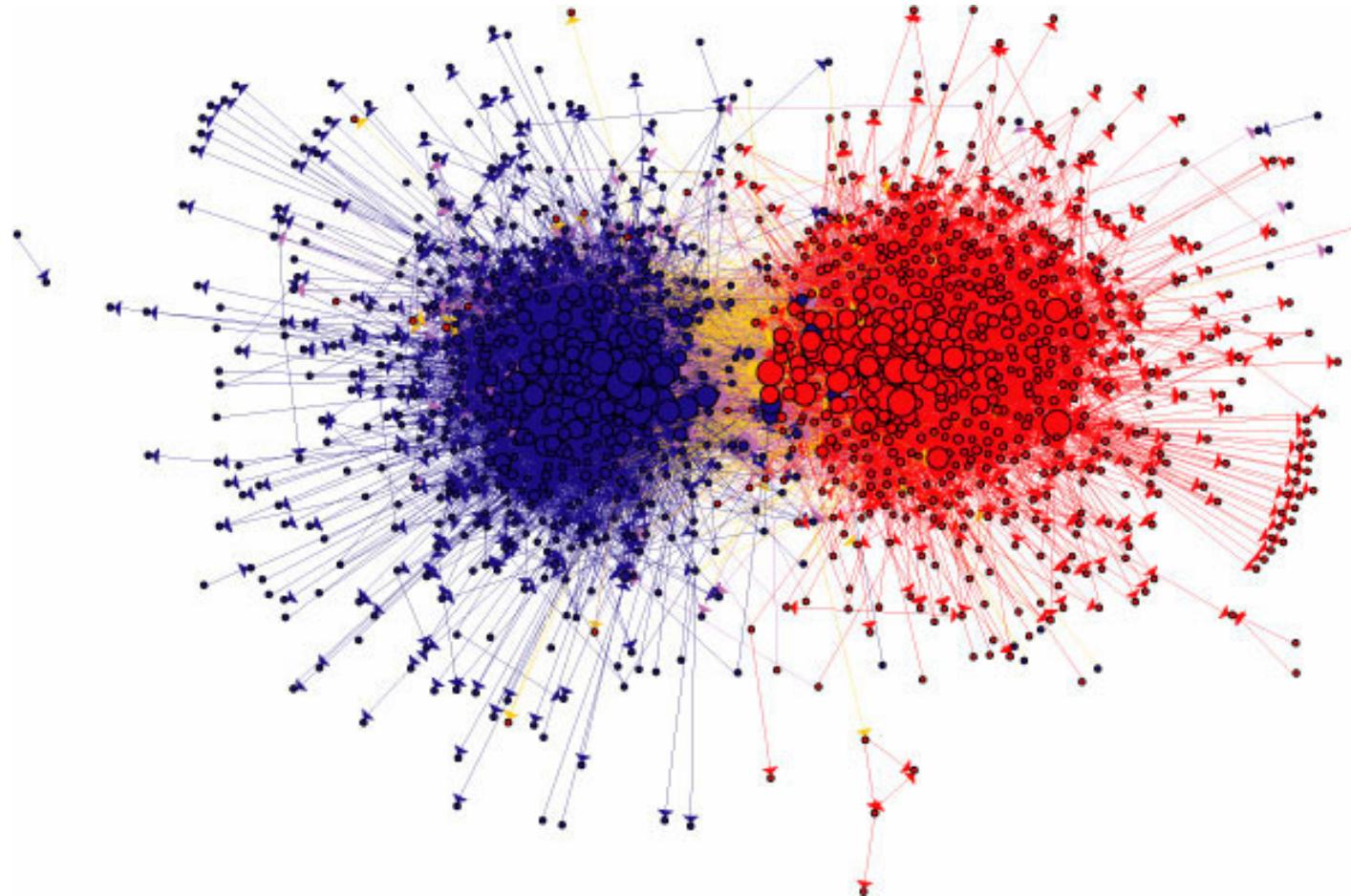
Social Networks



Web Graphs



Web Graphs

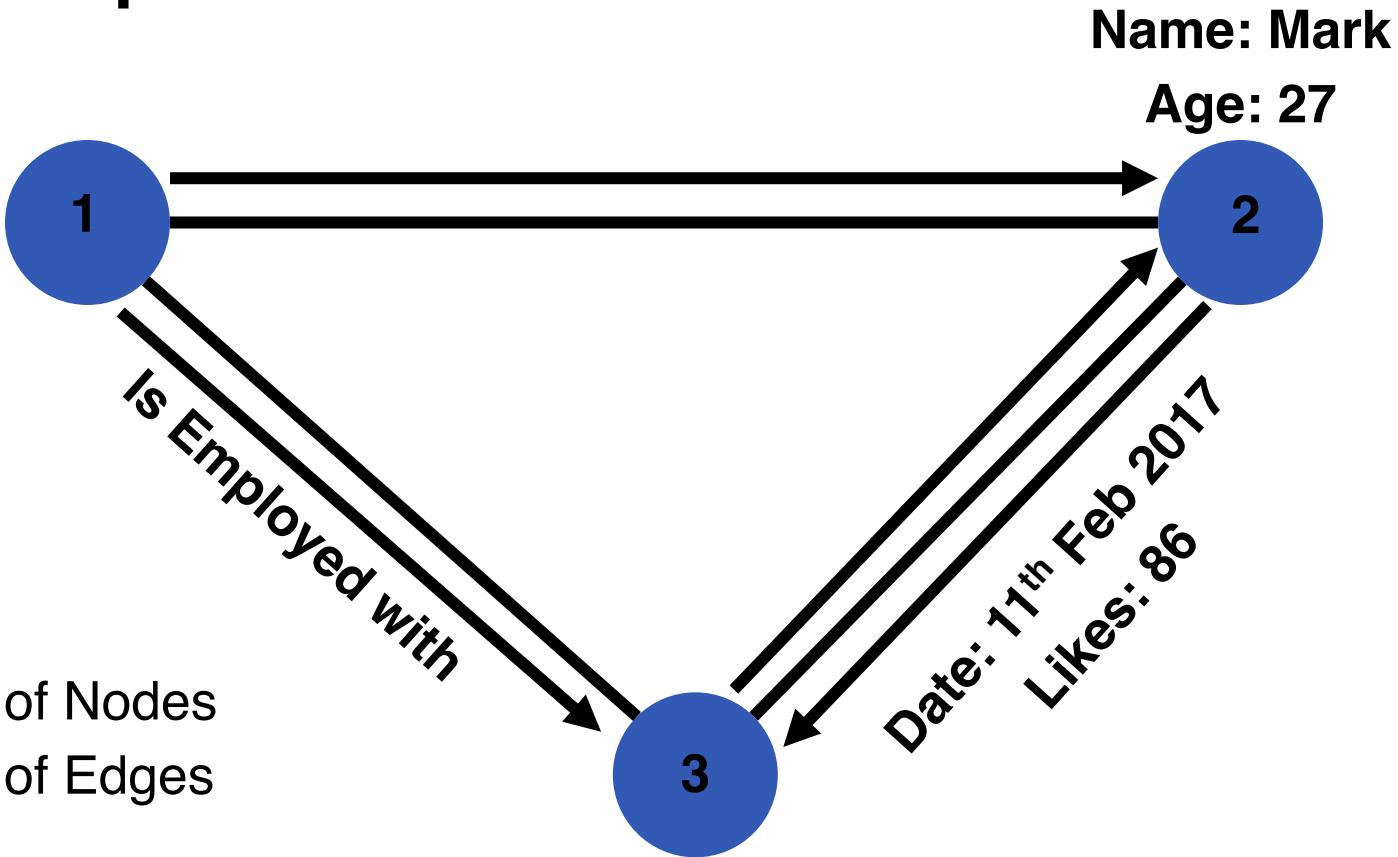


“The political blogosphere and the 2004 U.S. election: divided they blog.”
Adamic and Glance, 2005.

User-Item Graphs



Graph Representation

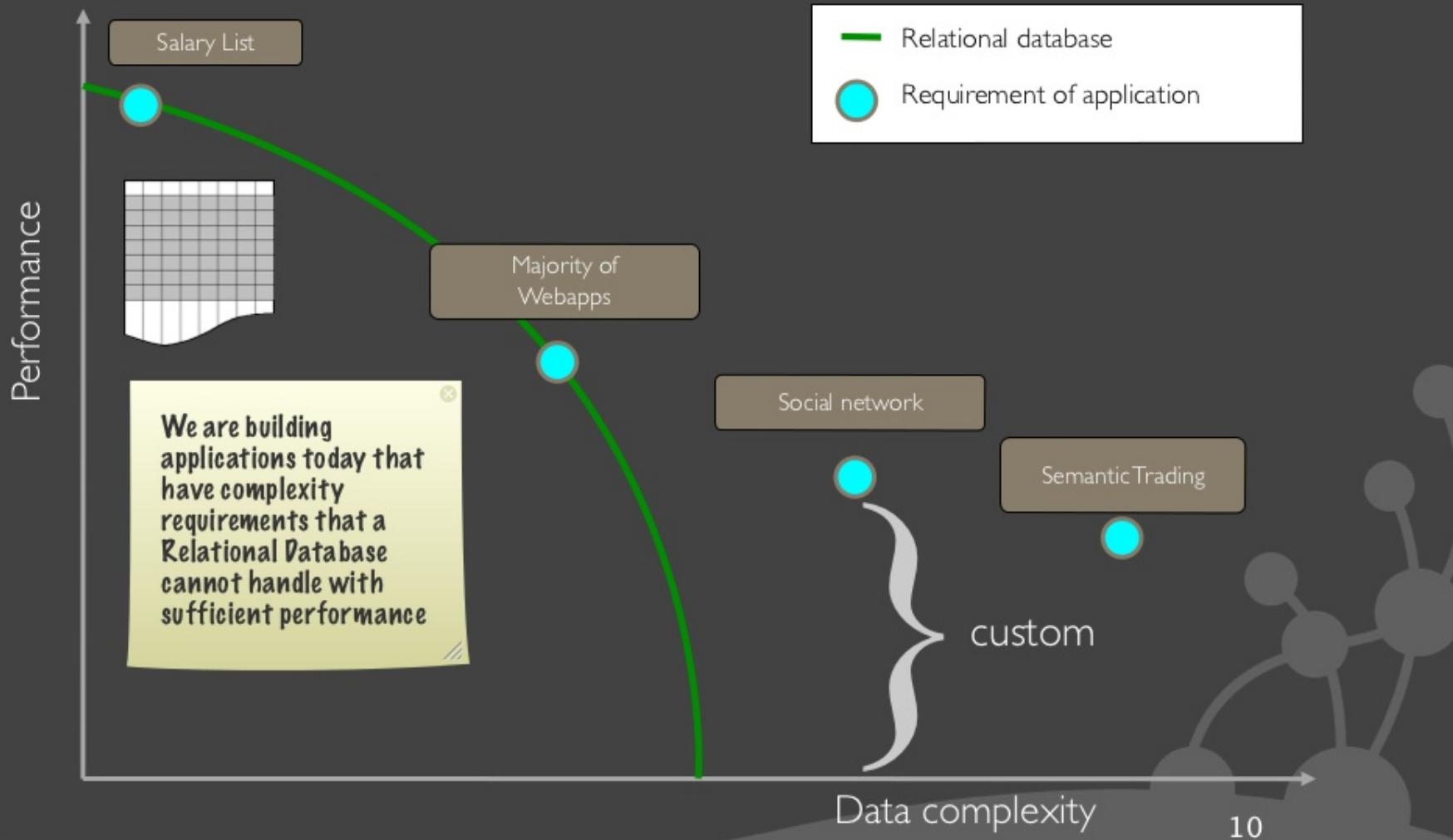


Edges can be directed or undirected

Nodes can have a label and multiple attributes

- ⁸ Edges can have a label and multiple attributes

RDBMS performance



Neo4j

Introduction

- Intended not so much to store information about things
- But to tie them together and record their connections with each other
- Stores data as a graph
- Can store highly variable data
- Small enough to be embedded in any application
- But able to scale up easily

Neo4j

- GraphDB
- Non-relational (NoSQL)
- Schema free
- Open Source Software

Graphs are all around us

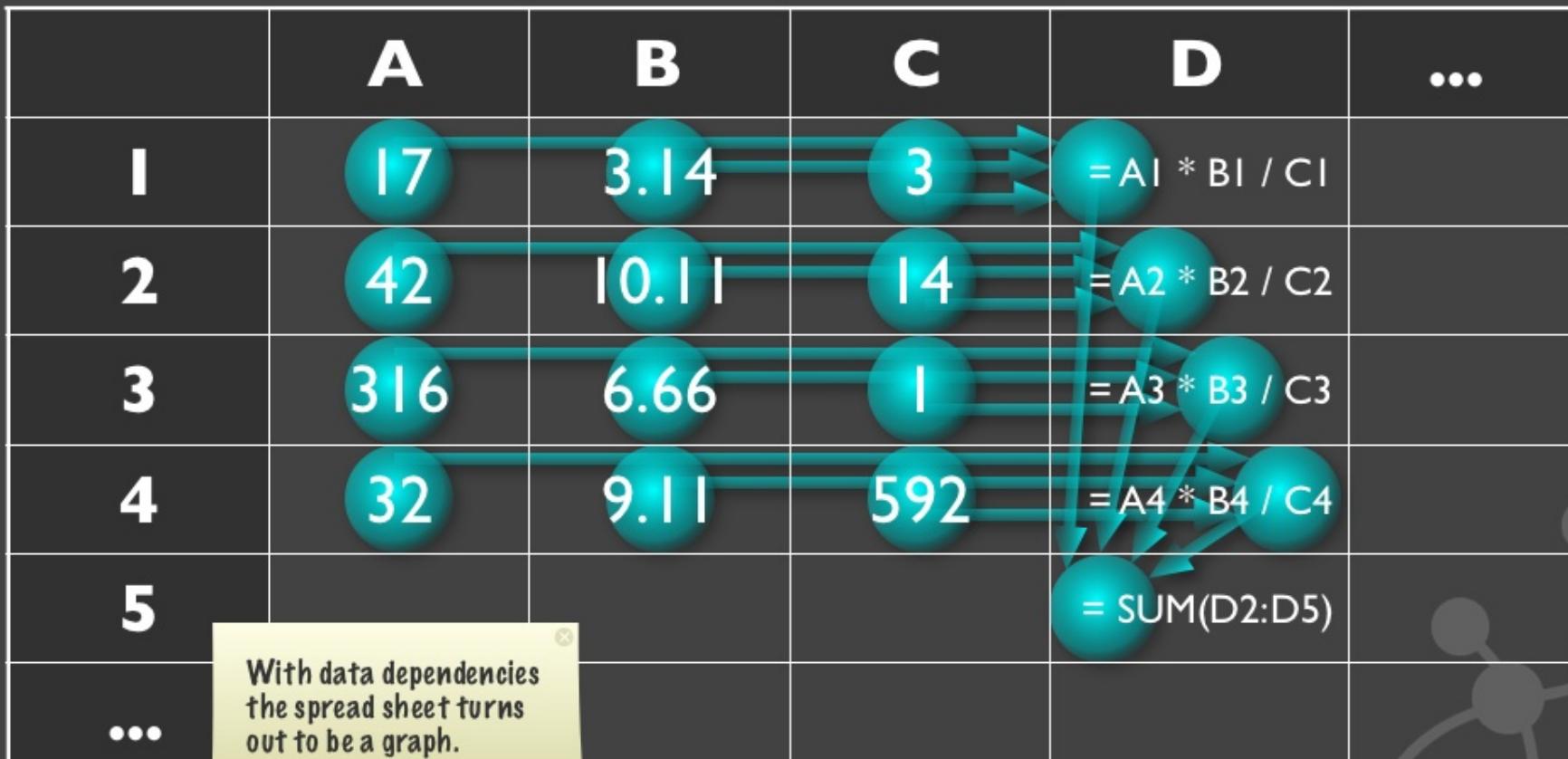
	A	B	C	D	...
1	17	3.14	3	=A1 * B1 / C1	
2	42	10.11	14	=A2 * B2 / C2	
3	316	6.66	1	=A3 * B3 / C3	
4	32	9.11	592	=A4 * B4 / C4	
5				= SUM(D2:D5)	
...					

With data dependencies
the spread sheet turns
out to be a graph.

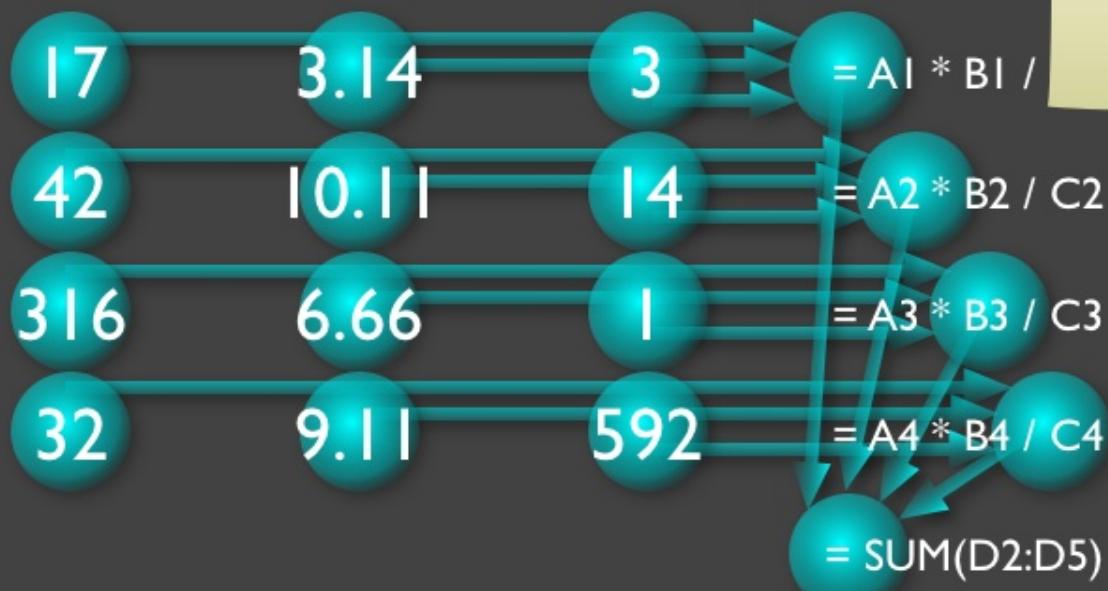
Graphs are all around us

	A	B	C	D	...
1	17	3.14	3	=A1 * B1 / C1	
2	42	10.11	14	=A2 * B2 / C2	
3	316	6.66	1	=A3 * B3 / C3	
4	32	9.11	592	=A4 * B4 / C4	
5				= SUM(D2:D5)	
...					

With data dependencies
the spread sheet turns
out to be a graph.

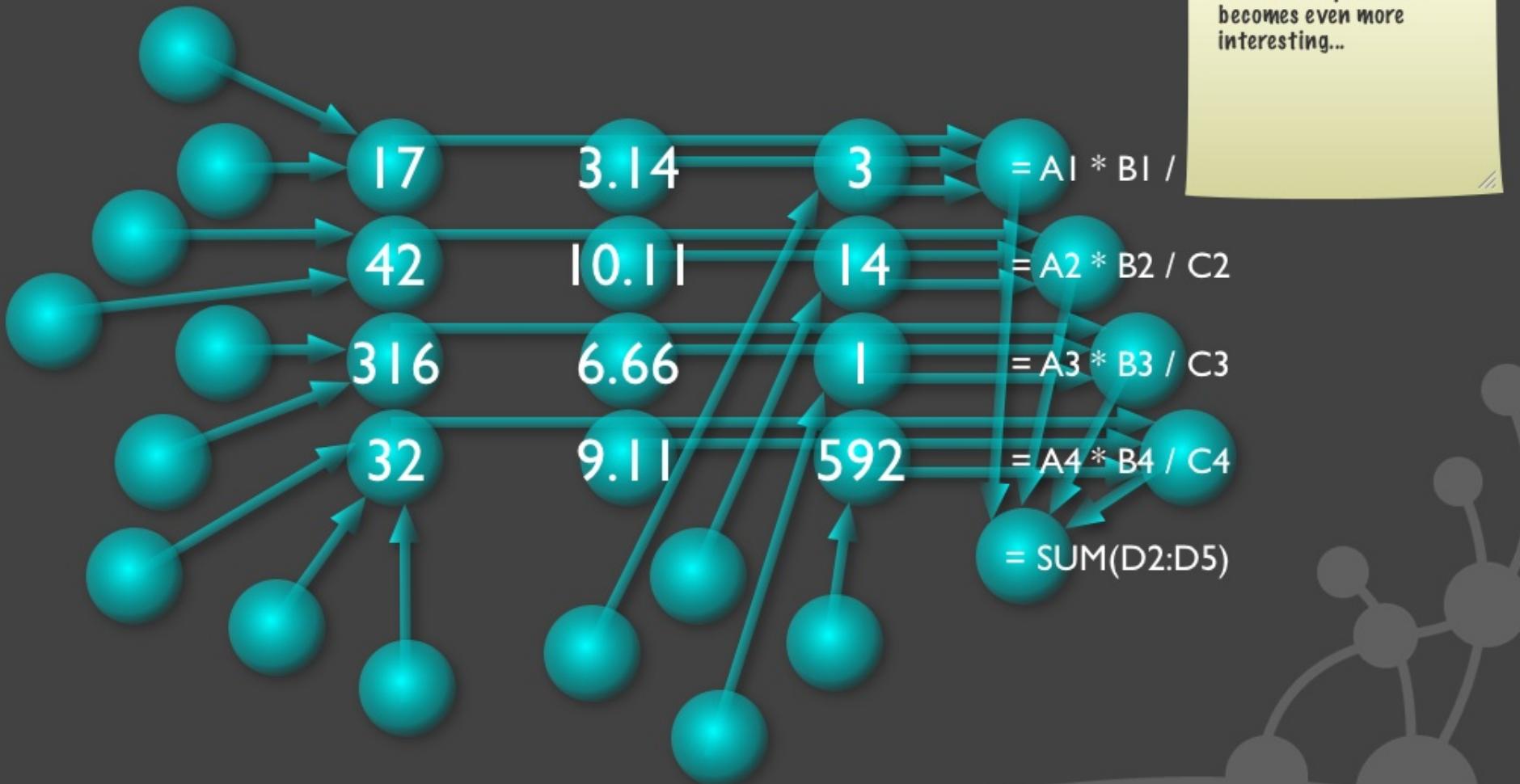


Graphs are all around us



If we add external data sources the problem becomes even more interesting...

Graphs are all around us



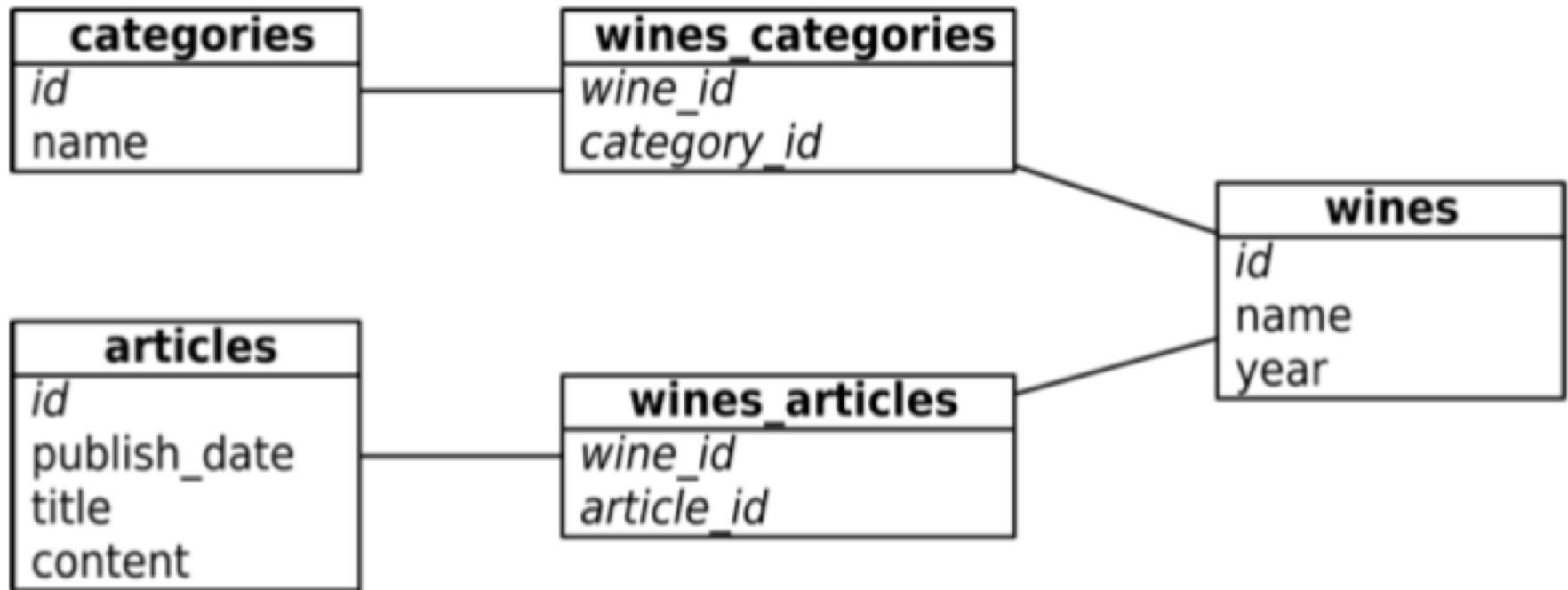
Wine suggestion engine

Wines are categorized by:

- Different varieties
- Regions
- Wineries
- Vintages
- Designations
- ...

We need to keep track of other things, like articles describing those wines, and to enable users to track their favorite wines

Wine suggestion engine: Relational Model



Wine suggestion engine: Graph Model



Query Languages

- Traversal APIs
- SPARQL (“SQL for linked data”)
- Gremlin
- Cypher

Example

Friends of Friends | Common Friends | Connecting Paths

Friends of Friends

Find all of Joe's second-degree friends

MATCH

```
(person:Person)-[:KNOWS]-(friend:Person)-[:KNOWS]-  
(foaf:Person)
```

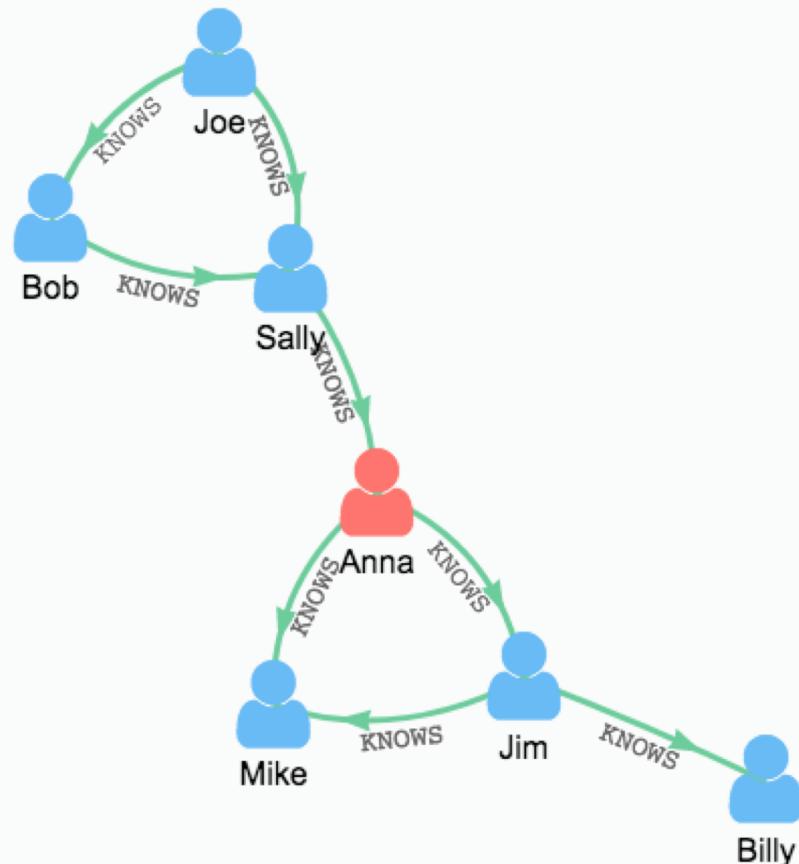
WHERE

```
person.name = "Joe"  
AND NOT (person)-[:KNOWS]-(foaf)
```

RETURN

```
foaf
```

Joe knows Sally, and Sally knows Anna. Bob is excluded from the result because, in addition to being a 2nd-degree friend through Sally, he's also a first-degree friend.

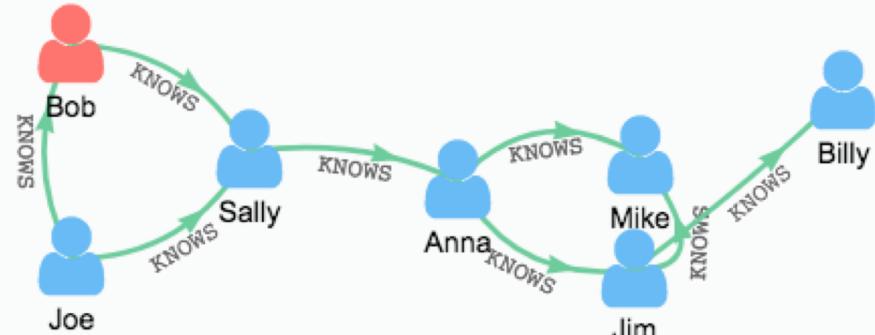


Common Friends

Find friends in common between Joe and Sally

```
MATCH
  (user:Person)-[:KNOWS]-(friend)-
  [ :KNOWS ]-(foaf:Person)
WHERE
  user.name = "Joe" AND foaf.name = "Sally"
RETURN
  friend.name AS friend
```

Joe and Sally both know Bob.

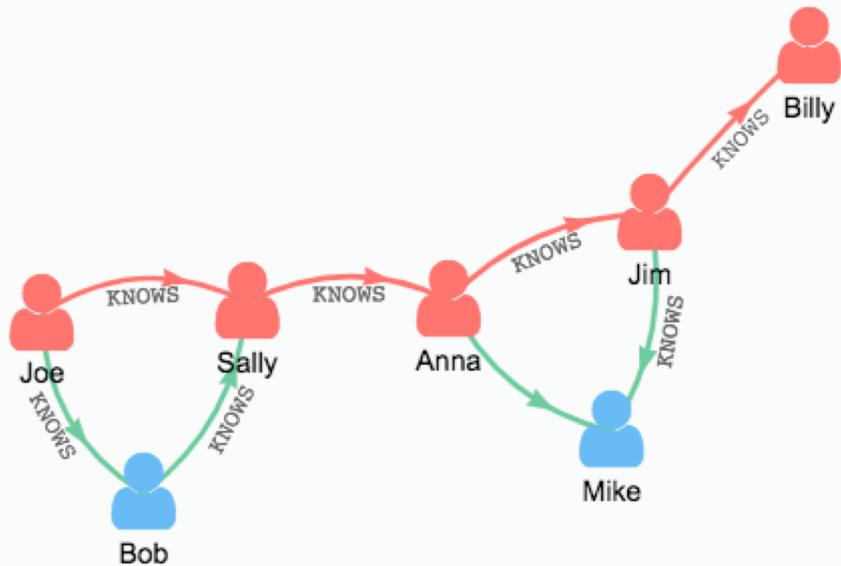


Connecting Paths

Find all paths, up to 6 degrees, between Joe and Billy

```
MATCH
  path = shortestPath(
    (p1:Person)-[:KNOWS*..6]-(p2:Person)
  )
WHERE
  p1.name = "Joe" AND p2.name = "Billy"
RETURN
  path
```

There's only one shortest path between Joe and Billy in this dataset, so that path is returned.



Spark GraphX

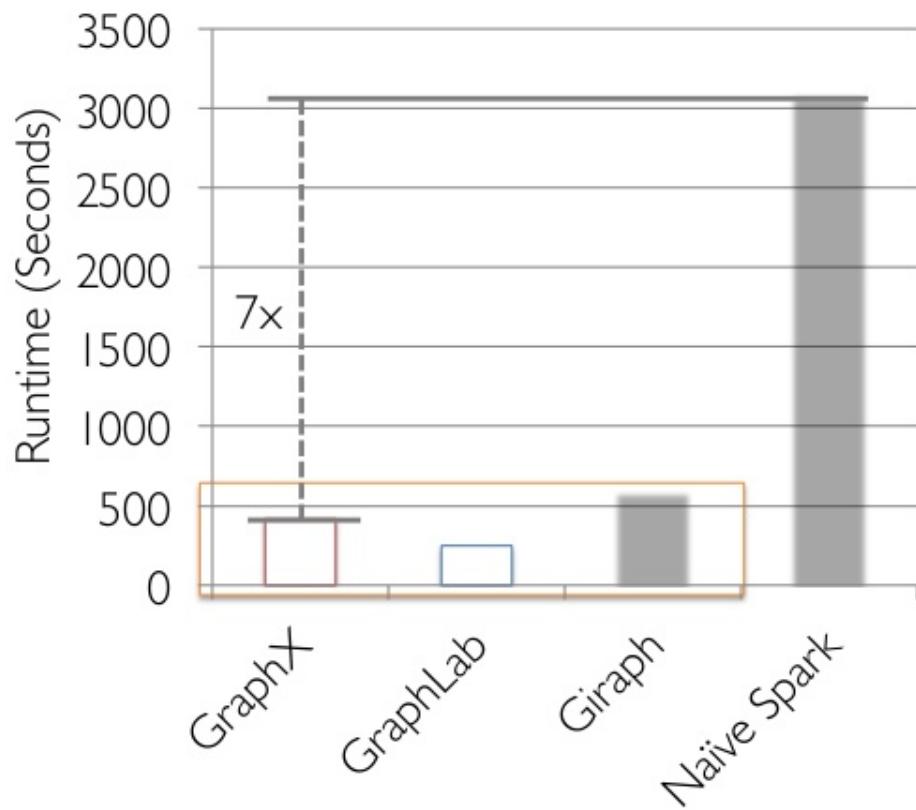
Spark GraphX

- Graph Processing System
- Graph composed by 2 RDDs, one for vertices (nodes), and one for relationships (edges)
- Graphs are immutable
- Perform a transformation to update it
- APIs available only in Scala

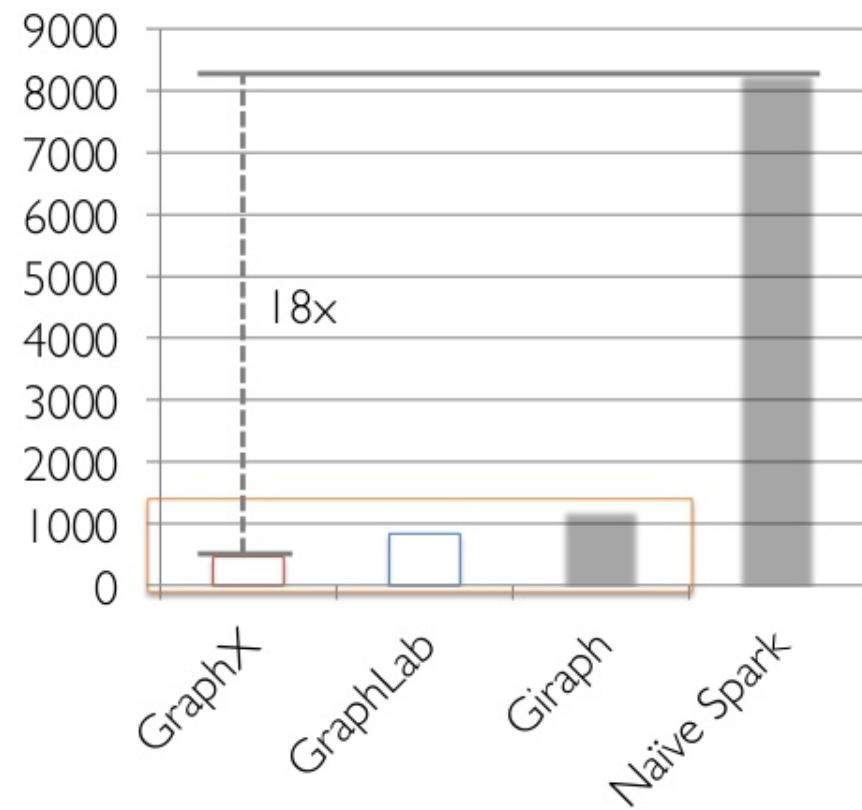
PageRank Benchmark

EC2 Cluster of 16 x m2.4xLarge (8 cores) + 1GigE

Twitter Graph (42M Vertices, 1.5B Edges)

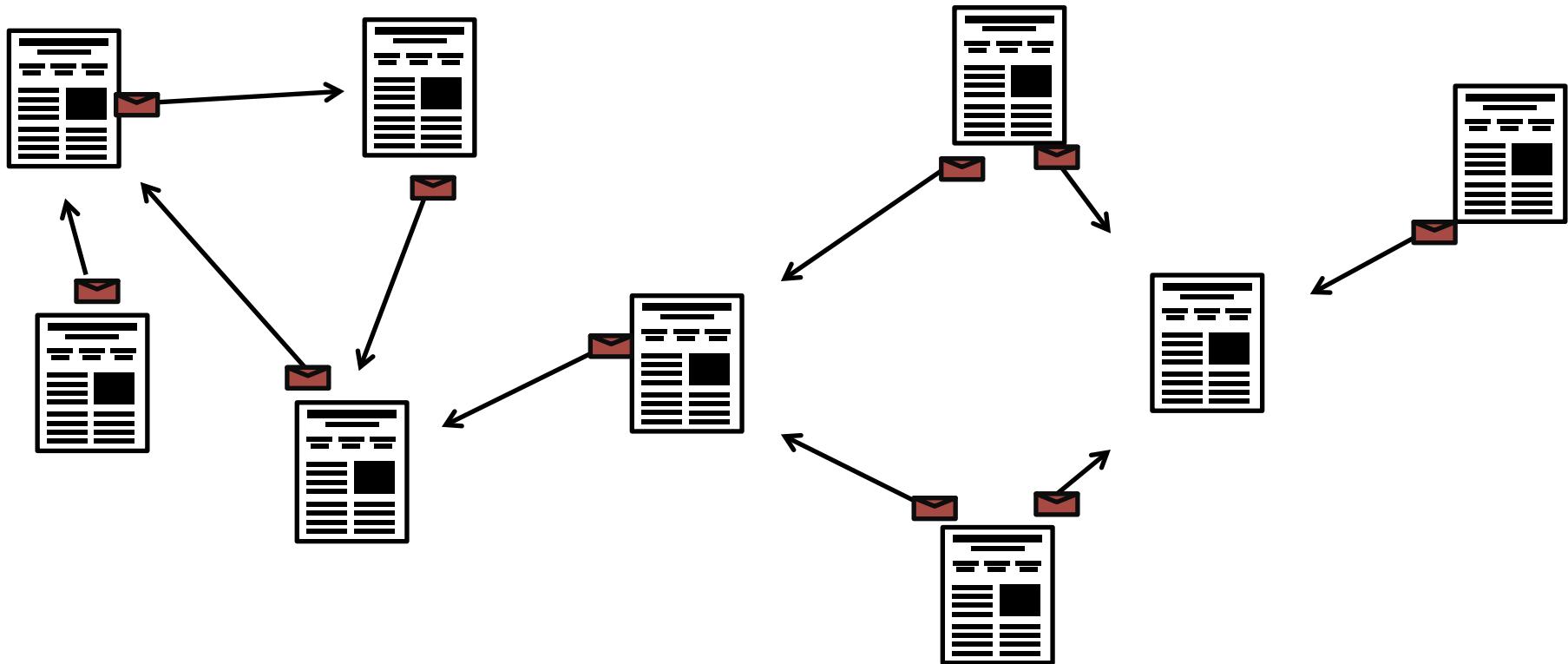


UK-Graph (106M Vertices, 3.7B Edges)

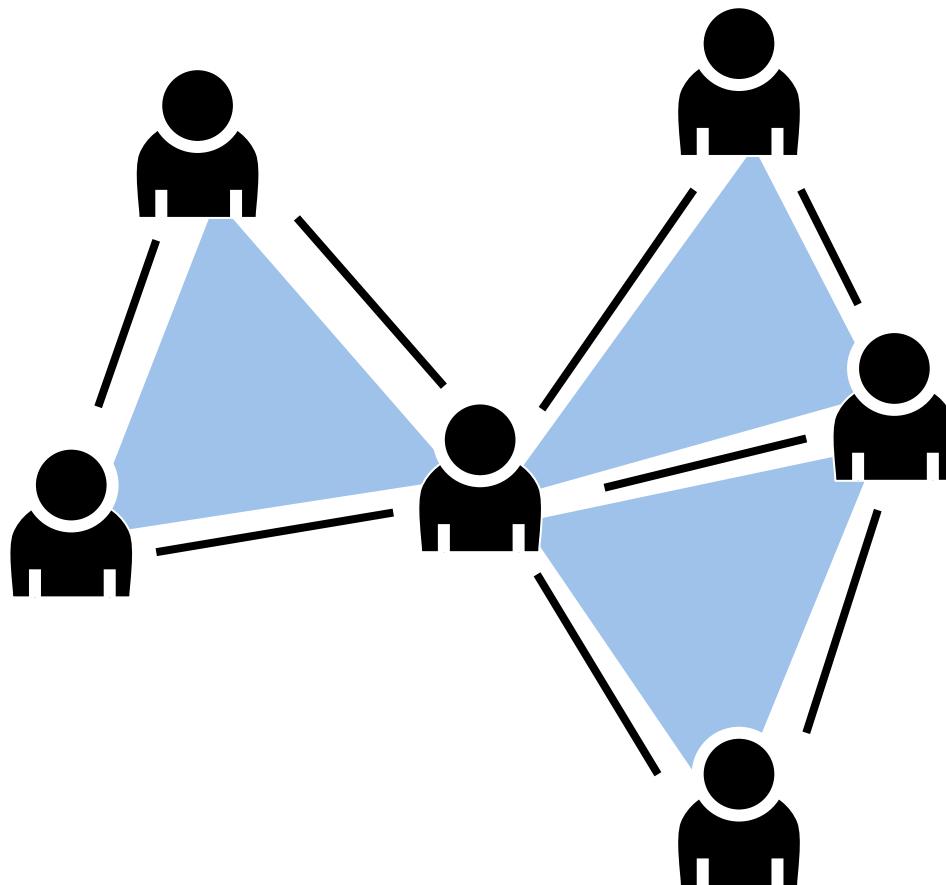


GraphX performs comparably to
state-of-the-art graph processing systems.

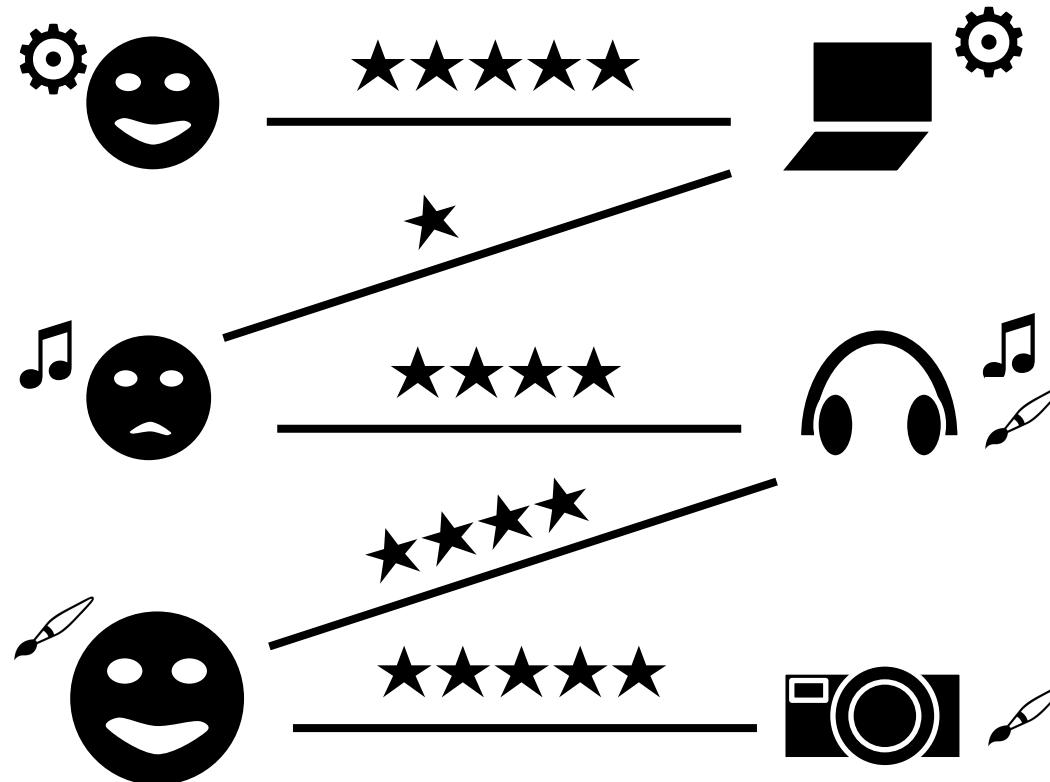
PageRank



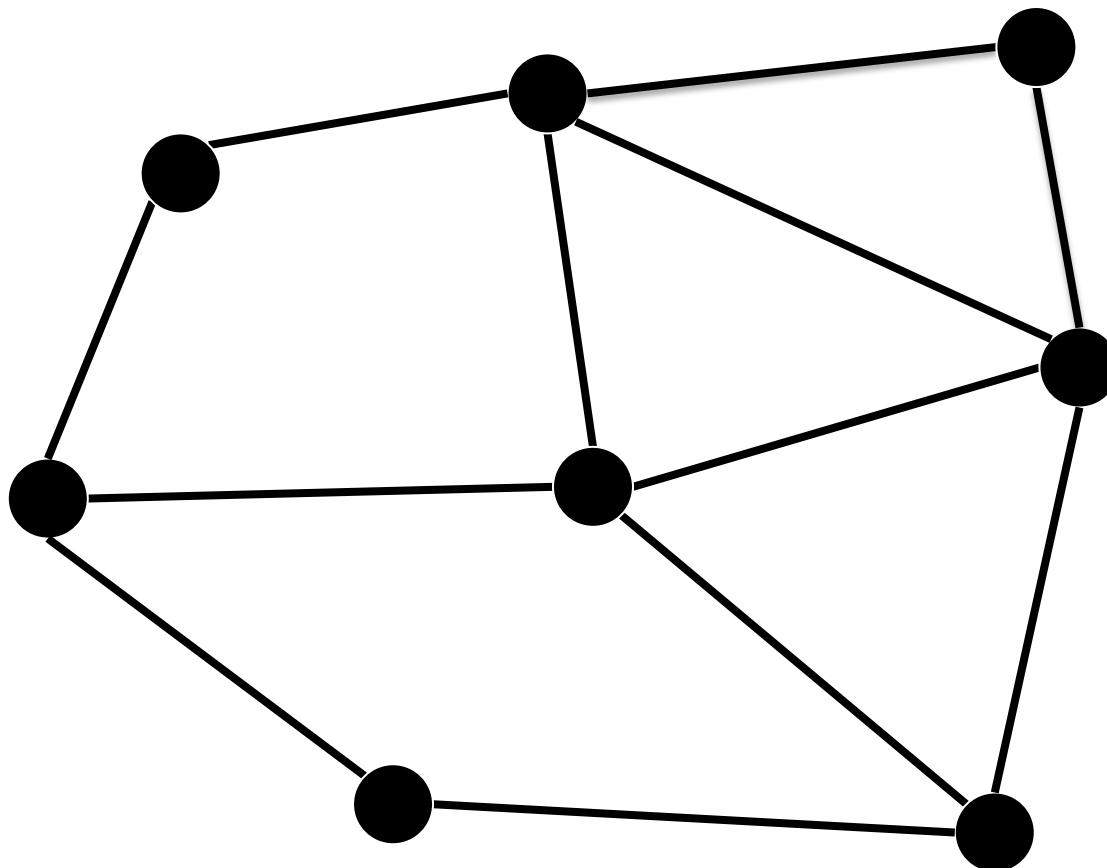
Triangle Counting



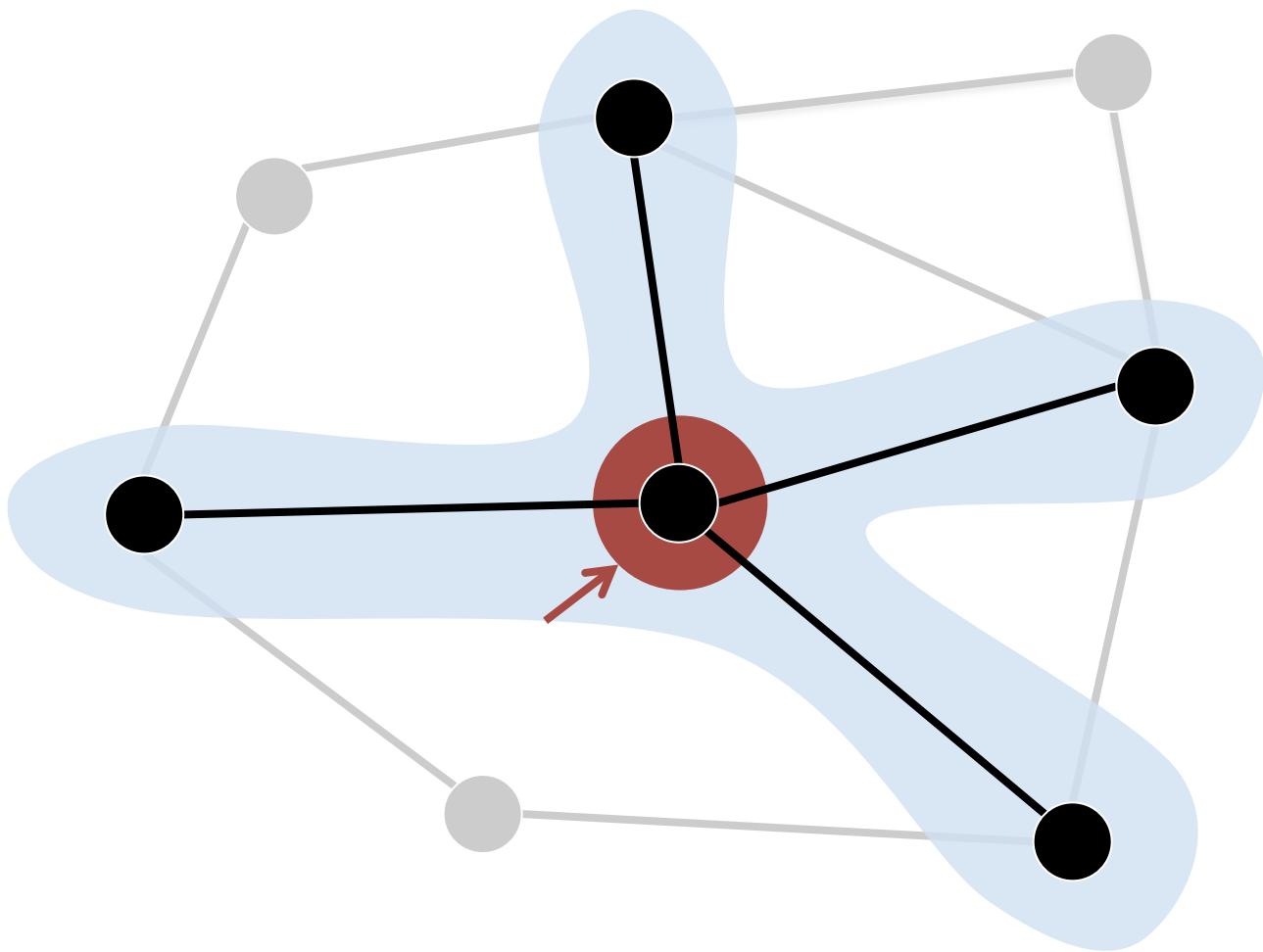
Collaborative Filtering



The Graph-Parallel Pattern



The Graph-Parallel Pattern



Many other algorithms

Collaborative Filtering

- » Alternating Least Squares
- » Stochastic Gradient Descent
- » Tensor Factorization

Structured Prediction

- » Loopy Belief Propagation
- » Max-Product Linear Programs
- » Gibbs Sampling

Semi-supervised ML

- » Graph SSL
- » CoEM

Community Detection

- » Triangle-Counting
- » K-core Decomposition
- » K-Truss

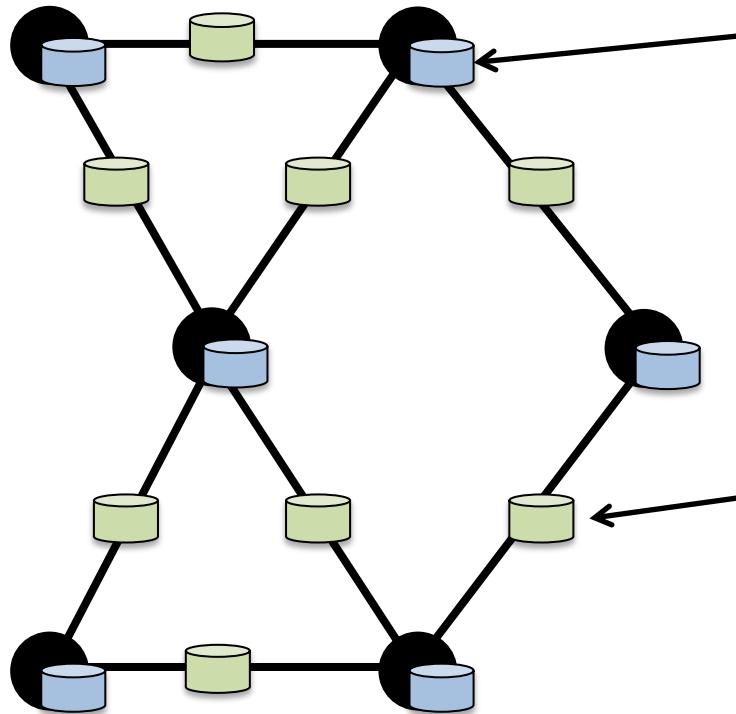
Graph Analytics

- » PageRank
- » Personalized PageRank
- » Shortest Path
- » Graph Coloring

Classification

- » Neural Networks

Property Graphs



Vertex Property:

- User Profile
- Current PageRank Value

Edge Property:

- Weights
- Relationships
- Timestamps

Creating a Graph

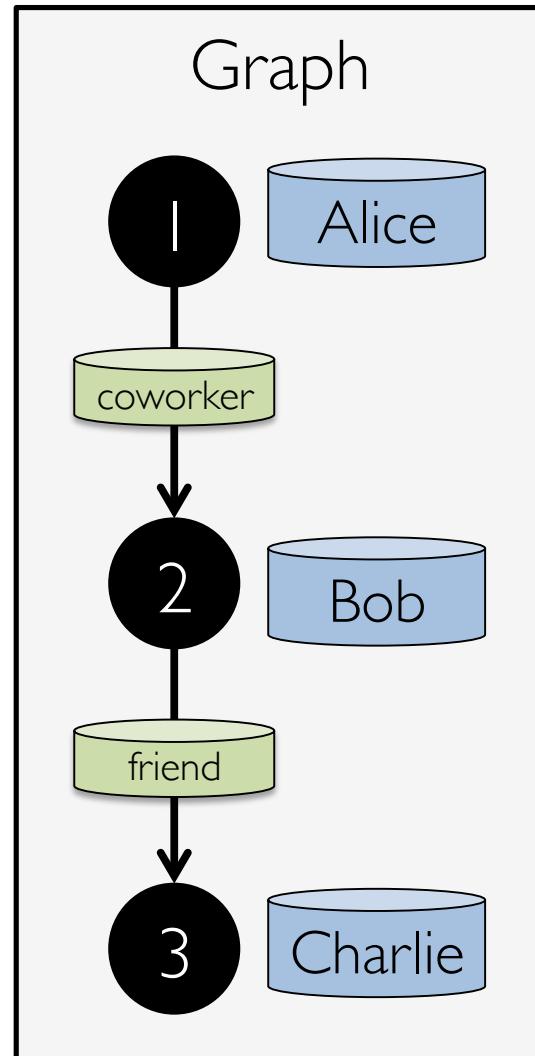
```
type VertexId = Long

val vertices: RDD[(VertexId, String)] =
  sc.parallelize(List(
    (1L, "Alice"),
    (2L, "Bob"),
    (3L, "Charlie")))

class Edge[ED](
  val srcId: VertexId,
  val dstId: VertexId,
  val attr: ED)

val edges: RDD[Edge[String]] =
  sc.parallelize(List(
    Edge(1L, 2L, "coworker"),
    Edge(2L, 3L, "friend")))

val graph = Graph(vertices, edges)
```



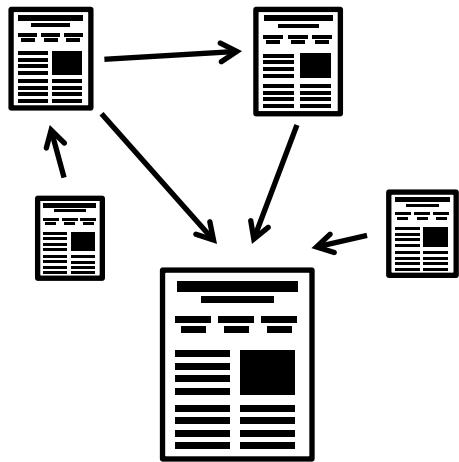
Graph Operations

```
class Graph[VD, ED] {  
    // Table Views -----  
    def vertices: RDD[(VertexId, VD)]  
    def edges: RDD[Edge[ED]]  
    def triplets: RDD[EdgeTriplet[VD, ED]]  
    // Transformations -----  
    def mapVertices[VD2](f: (VertexId, VD) => VD2): Graph[VD2, ED]  
    def mapEdges[ED2](f: Edge[ED] => ED2): Graph[VD2, ED]  
    def reverse: Graph[VD, ED]  
    def subgraph(epred: EdgeTriplet[VD, ED] => Boolean,  
                vpred: (VertexId, VD) => Boolean): Graph[VD, ED]  
    // Joins -----  
    def outerJoinVertices[U, VD2]  
        (tbl: RDD[(VertexId, U)])  
        (f: (VertexId, VD, Option[U]) => VD2): Graph[VD2, ED]  
    // Computation -----  
    def mapReduceTriplets[A] (  
        sendMsg: EdgeTriplet[VD, ED] => Iterator[(VertexId, A)],  
        mergeMsg: (A, A) => A): RDD[(VertexId, A)]
```

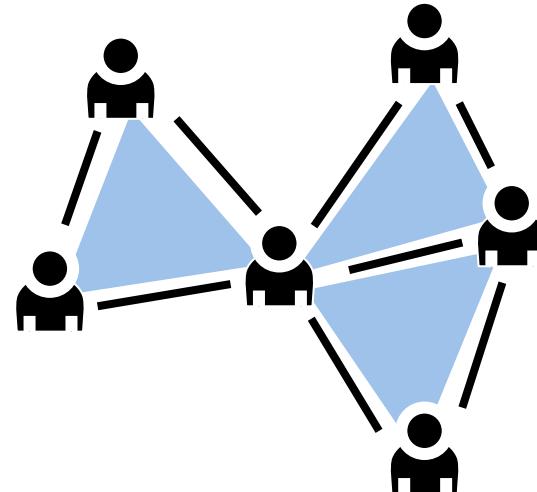
Built-in Algorithms

```
// Continued from previous slide
def pageRank(tol: Double): Graph[Double, Double]
def triangleCount(): Graph[Int, ED]
def connectedComponents(): Graph[VertexId, ED]
// ...and more: org.apache.spark.graphx.lib
}
```

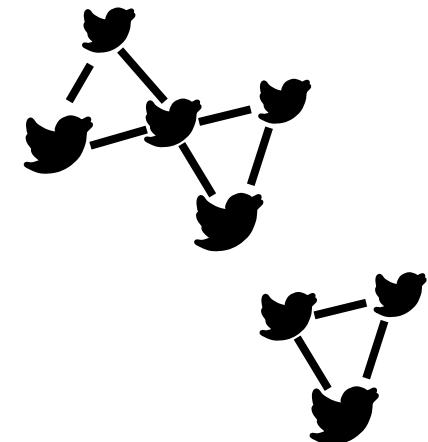
PageRank



Triangle Count



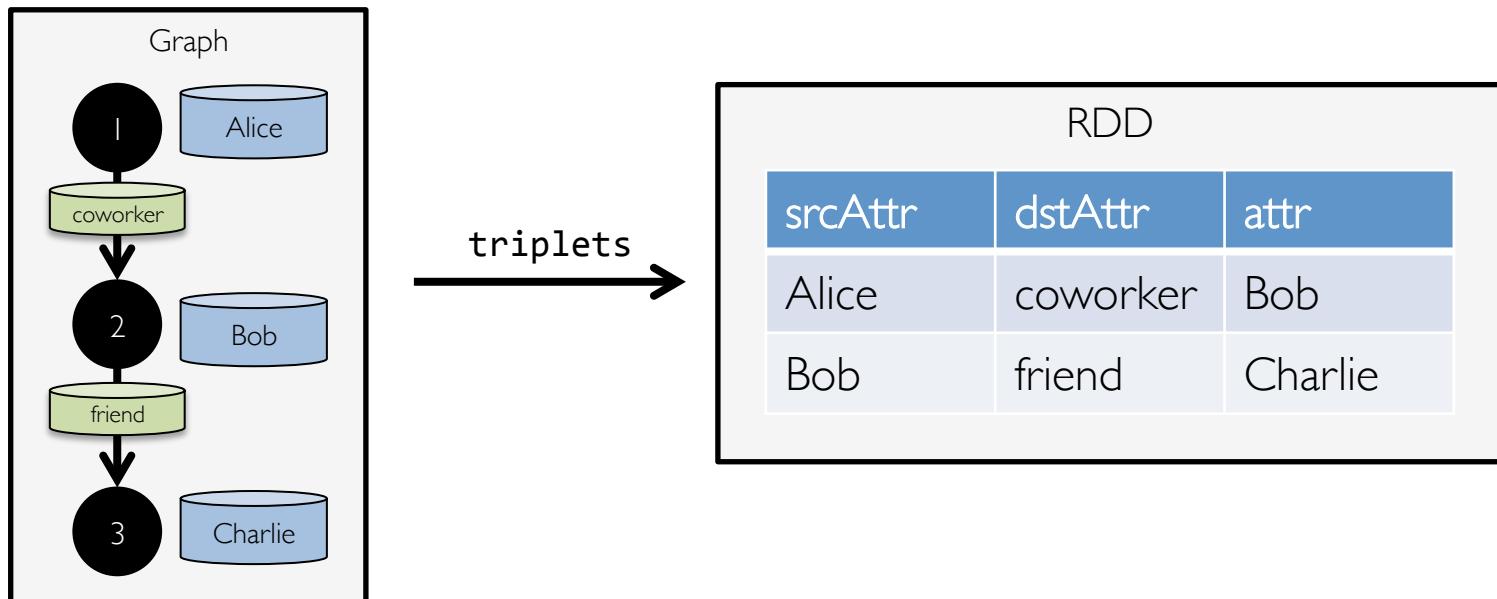
Connected Components



The triplets view

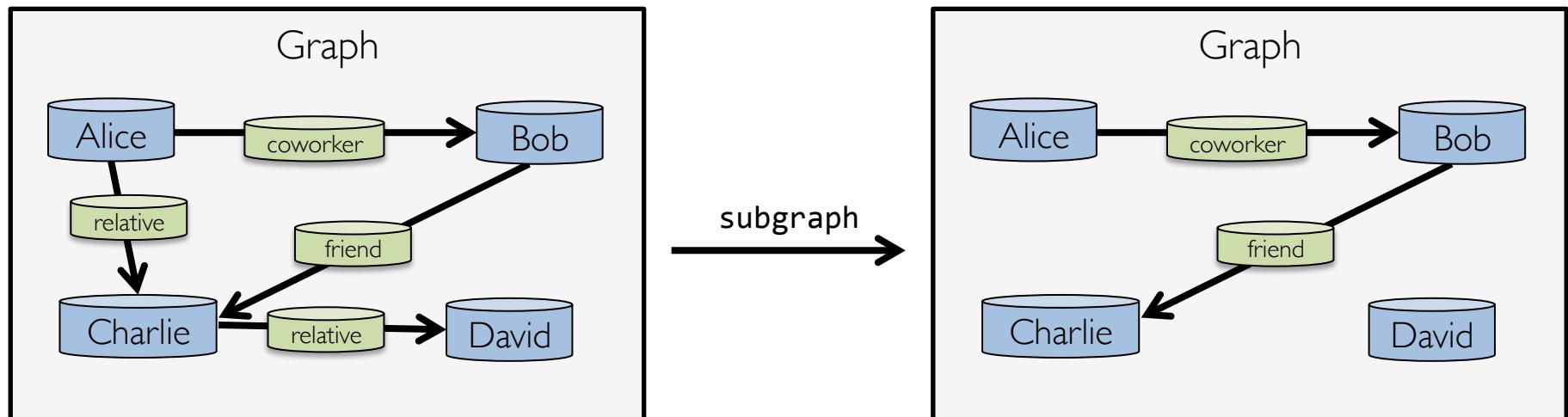
```
class Graph[VD, ED] {  
    def triplets: RDD[EdgeTriplet[VD, ED]]  
}
```

```
class EdgeTriplet[VD, ED](  
    val srcId: VertexId, val dstId: VertexId, val attr: ED,  
    val srcAttr: VD, val dstAttr: VD)
```



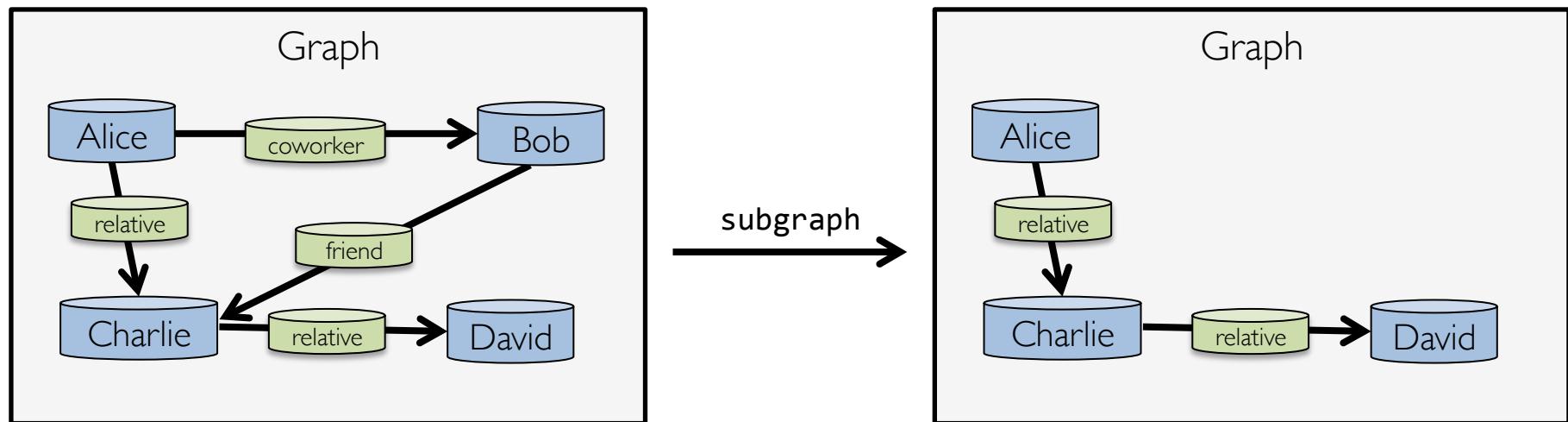
The subgraph transformation

```
class Graph[VD, ED] {  
    def subgraph(epred: EdgeTriplet[VD, ED] => Boolean,  
                vpred: (VertexId, VD) => Boolean): Graph[VD, ED]  
}  
  
graph.subgraph(epred = (edge) => edge.attr != "relative")
```



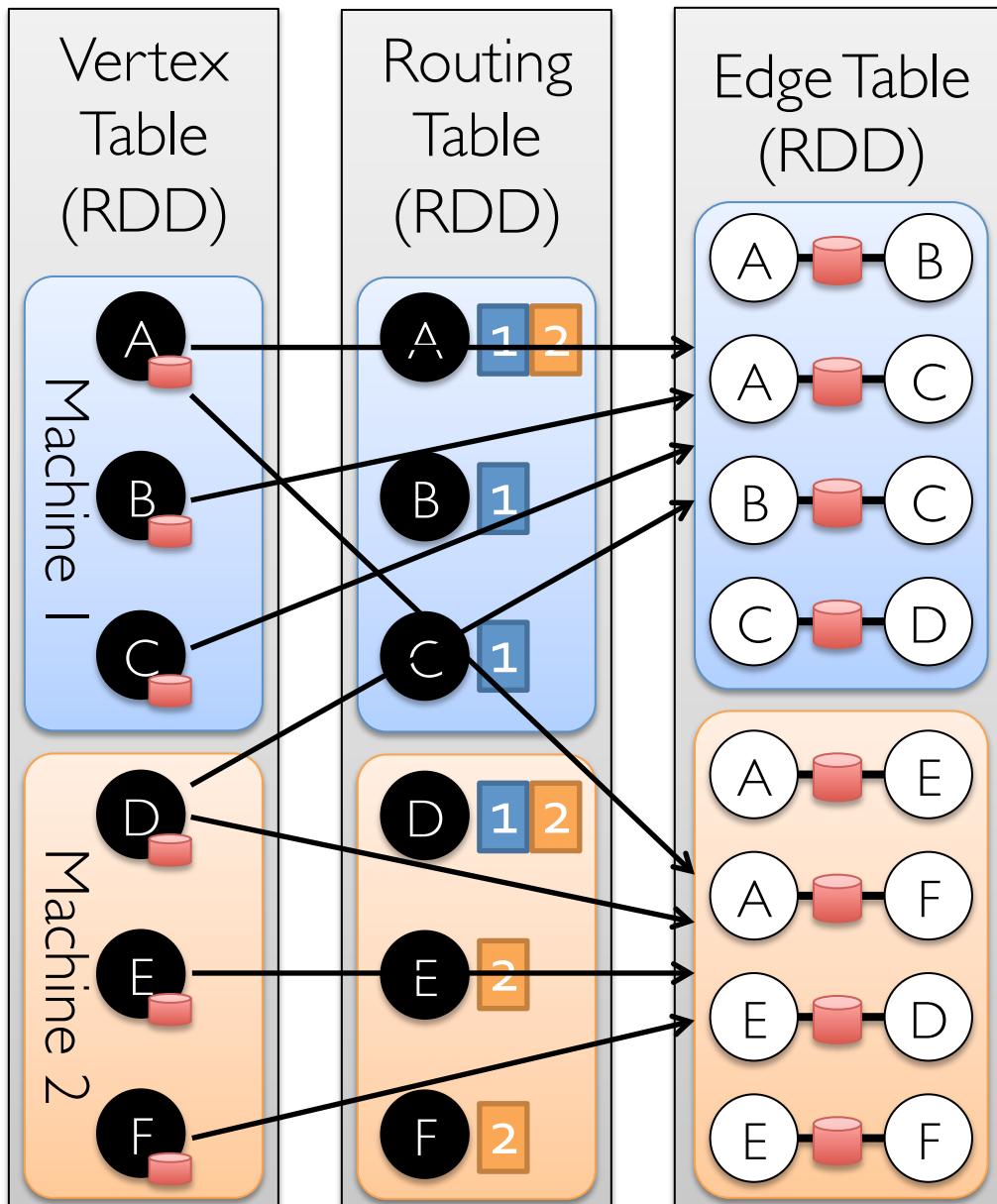
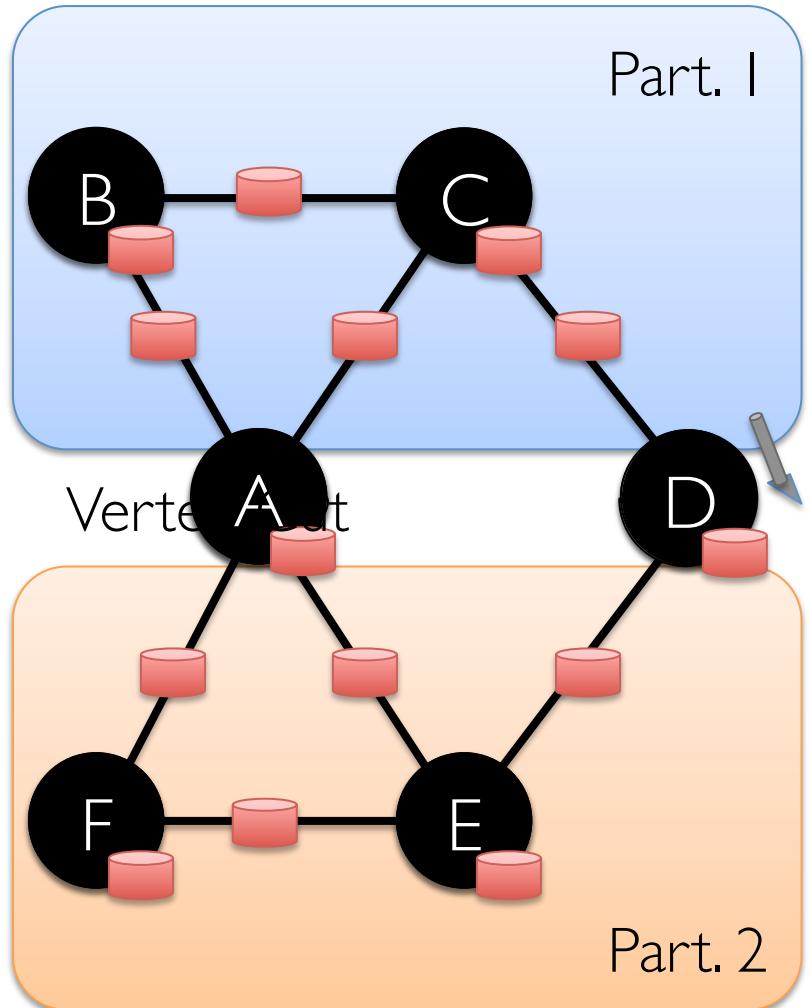
The subgraph transformation

```
class Graph[VD, ED] {  
    def subgraph(epred: EdgeTriplet[VD, ED] => Boolean,  
                vpred: (VertexId, VD) => Boolean): Graph[VD, ED]  
}  
  
graph.subgraph(vpred = (id, name) => name != "Bob")
```



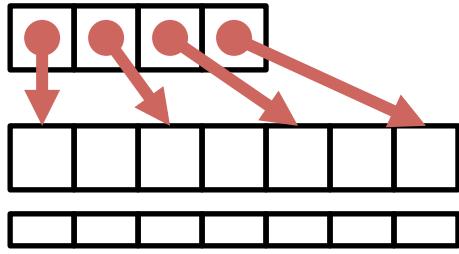
Encoding property Graphs as RDDs

Property Graph

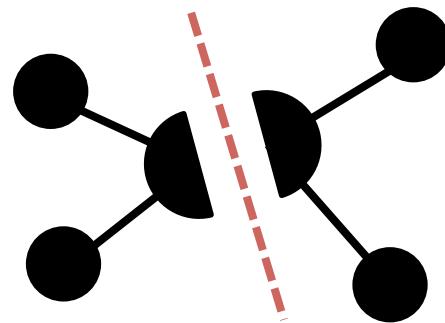


Graph System Optimizations

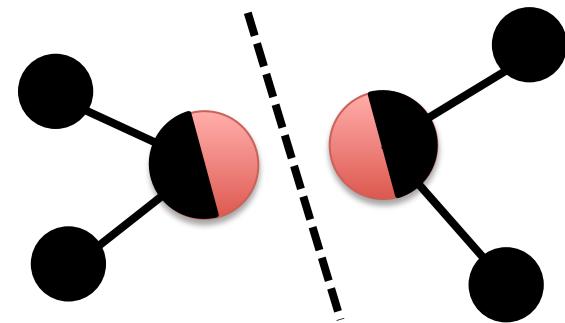
Specialized
Data-Structures



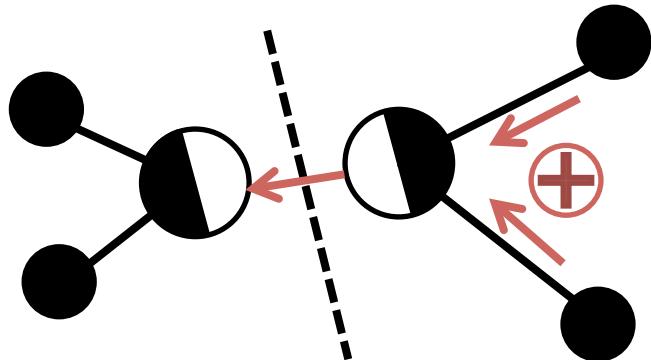
Vertex-Cuts
Partitioning



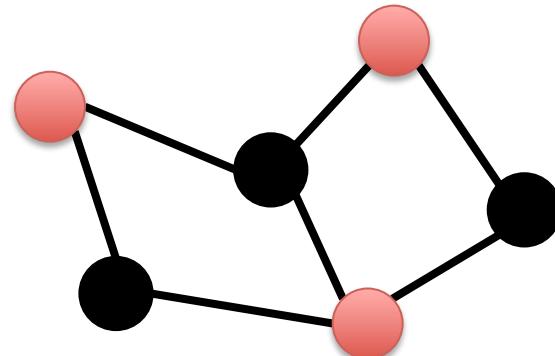
Remote
Caching / Mirroring



Message Combiners



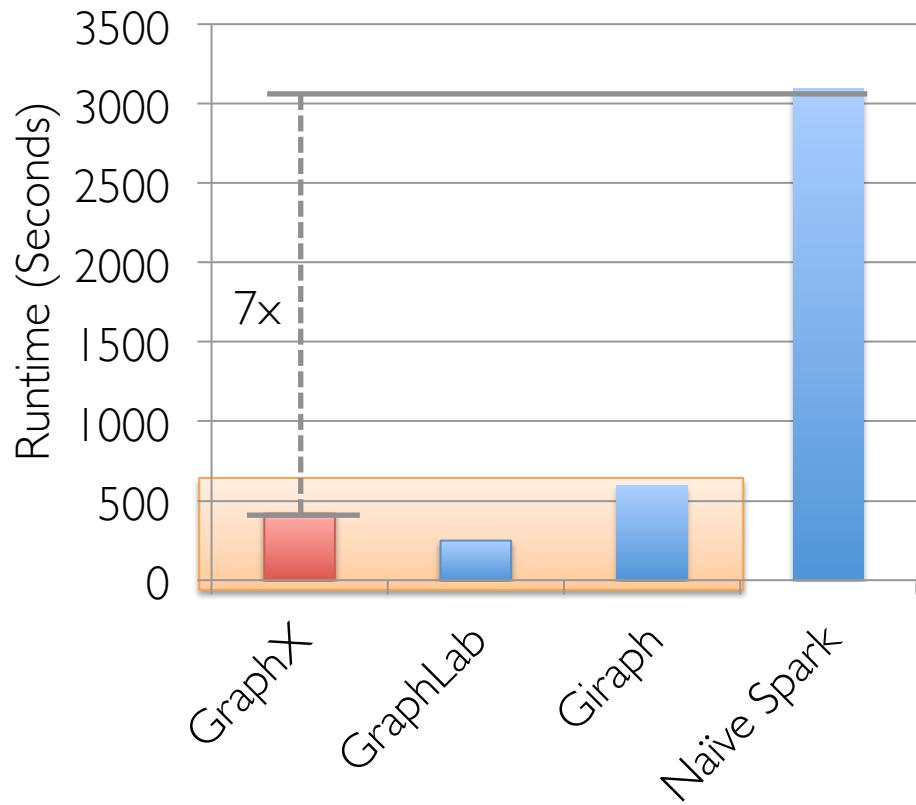
Active Set Tracking



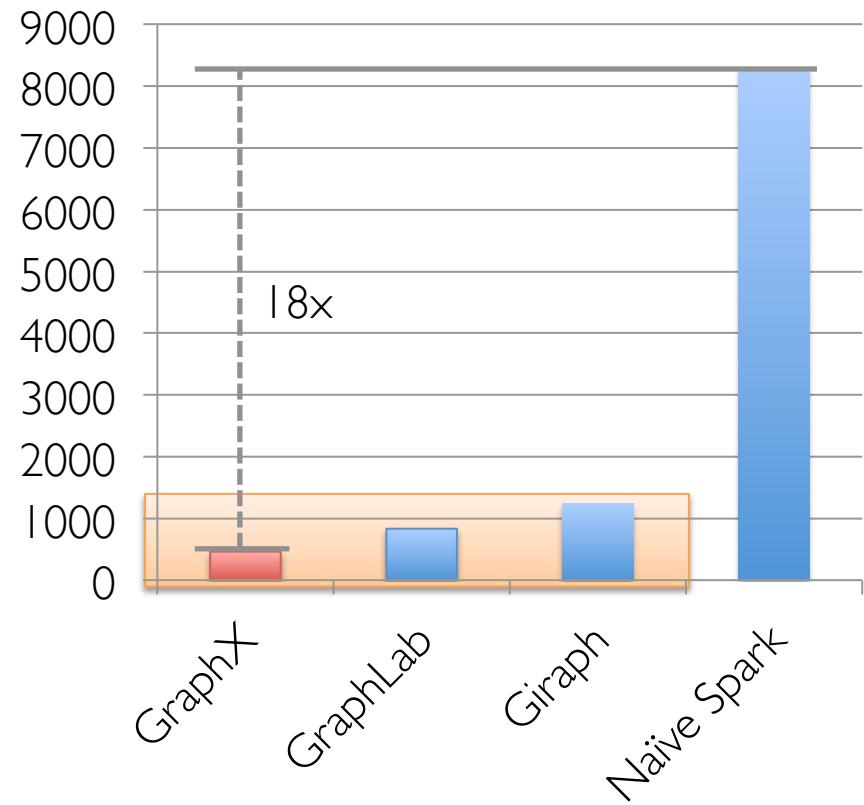
PageRank Benchmark

EC2 Cluster of 16 x m2.4xLarge (8 cores) + 1GigE

Twitter Graph (42M Vertices, 1.5B Edges)



UK-Graph (106M Vertices, 3.7B Edges)



Graph operators

```
val graph: Graph[(String, String), String]
// Use the implicit GraphOps.inDegrees operator
val inDegrees: VertexRDD[Int] = graph.inDegrees
```

```
/** Summary of the functionality in the property graph */
class Graph[VD, ED] {
    // Information about the Graph -----
    val numEdges: Long
    val numVertices: Long
    val inDegrees: VertexRDD[Int]
    val outDegrees: VertexRDD[Int]
    val degrees: VertexRDD[Int]
    // Views of the graph as collections -----
    val vertices: VertexRDD[VD]
    val edges: EdgeRDD[ED]
    val triplets: RDD[EdgeTriplet[VD, ED]]
    // Functions for caching graphs -----
    def persist(newLevel: StorageLevel = StorageLevel.MEMORY_ONLY): Graph[VD, ED]
    def cache(): Graph[VD, ED]
    def unpersistVertices(blocking: Boolean = true): Graph[VD, ED]
    // Change the partitioning heuristic -----
    def partitionBy(partitionStrategy: PartitionStrategy): Graph[VD, ED]
    // Transform vertex and edge attributes -----
    def mapVertices[VD2](map: (VertexId, VD) => VD2): Graph[VD2, ED]
    def mapEdges[ED2](map: Edge[ED] => ED2): Graph[VD, ED2]
    def mapEdges[ED2](map: (PartitionID, Iterator[Edge[ED]]) => Iterator[ED2]): Graph[VD, ED2]
    def mapTriplets[ED2](map: EdgeTriplet[VD, ED] => ED2): Graph[VD, ED2]
    def mapTriplets[ED2](map: (PartitionID, Iterator[EdgeTriplet[VD, ED]]) => Iterator[ED2]):
        Graph[VD, ED2]
    // Modify the graph structure -----
    def reverse: Graph[VD, ED]
    def subgraph(
        opred: EdgeTriplet[VD, ED] => Boolean = (x => true),
        vpred: (VertexId, VD) => Boolean = ((v, d) => true))
        : Graph[VD, ED]
    def mask[VD2, ED2](other: Graph[VD2, ED2]): Graph[VD, ED]
    def groupEdges(merge: (ED, ED) => ED): Graph[VD, ED]
    // Join RDDs with the graph -----
    def joinVertices[U](table: RDD[(VertexId, U)])(mapFunc: (VertexId, VD, U) => VD): Graph[VD, ED]
    def outerJoinVertices[U, VD2](other: RDD[(VertexId, U)])
        (mapFunc: (VertexId, VD, Option[U]) => VD2)
        : Graph[VD2, ED]
    // Aggregate information about adjacent triplets -----
    def collectNeighborIds(edgeDirection: EdgeDirection): VertexRDD[Array[VertexId]]
    def collectNeighbors(edgeDirection: EdgeDirection): VertexRDD[Array[(VertexId, VD)]]
    def aggregateMessages[Msg: ClassTag](
        sendMsg: EdgeContext[VD, ED, Msg] => Unit,
        mergeMsg: (Msg, Msg) => Msg,
        tripletFields: TripletFields = TripletFields.All)
        : VertexRDD[Msg]
    // Iterative graph-parallel computation -----
    def pregel[A](initialMsg: A, maxIterations: Int, activeDirection: EdgeDirection)(
        vprog: (VertexId, VD, A) => VD,
        sendMsg: EdgeTriplet[VD, ED] => Iterator[(VertexId, A)],
        mergeMsg: (A, A) => A)
        : Graph[VD, ED]
    // Basic graph algorithms -----
    def pageRank(tol: Double, resetProb: Double = 0.15): Graph[Double, Double]
    def connectedComponents(): Graph[VertexId, ED]
    def triangleCount(): Graph[Int, ED]
    def stronglyConnectedComponents(numIter: Int): Graph[VertexId, ED]
}
```

Graph operators

```
// Information about the Graph -----
val numEdges: Long
val numVertices: Long
val inDegrees: VertexRDD[Int]
val outDegrees: VertexRDD[Int]
val degrees: VertexRDD[Int]
// Views of the graph as collections -----
val vertices: VertexRDD[VD]
val edges: EdgeRDD[ED]
val triplets: RDD[EdgeTriplet[VD, ED]]
// Functions for caching graphs -----
def persist(newLevel: StorageLevel = StorageLevel.MEMORY_ONLY): Graph[VD, ED]
def cache(): Graph[VD, ED]
def unpersistVertices(blocking: Boolean = true): Graph[VD, ED]
// Change the partitioning heuristic -----
def partitionBy(partitionStrategy: PartitionStrategy): Graph[VD, ED]
// Transform vertex and edge attributes -----
def mapVertices[VD2](map: (VertexId, VD) => VD2): Graph[VD2, ED]
def mapEdges[ED2](map: Edge[ED] => ED2): Graph[VD, ED2]
def mapEdges[ED2](map: (PartitionID, Iterator[Edge[ED]]) => Iterator[ED2]): Graph[VD, ED2]
def mapTriplets[ED2](map: EdgeTriplet[VD, ED] => ED2): Graph[VD, ED2]
def mapTriplets[ED2](map: (PartitionID, Iterator[EdgeTriplet[VD, ED]]) => Iterator[ED2])
: Graph[VD, ED2]
```

Graph operators

```
// Modify the graph structure -----
def reverse: Graph[VD, ED]
def subgraph(
    epred: EdgeTriplet[VD,ED] => Boolean = (x => true),
    vpred: (VertexId, VD) => Boolean = ((v, d) => true))
    : Graph[VD, ED]
def mask[VD2, ED2](other: Graph[VD2, ED2]): Graph[VD, ED]
def groupEdges(merge: (ED, ED) => ED): Graph[VD, ED]
// Join RDDs with the graph -----
def joinVertices[U](table: RDD[(VertexId, U)])(mapFunc: (VertexId, VD, U) => VD): Graph[VD, ED]
def outerJoinVertices[U, VD2](other: RDD[(VertexId, U)])
    (mapFunc: (VertexId, VD, Option[U]) => VD2)
    : Graph[VD2, ED]
// Aggregate information about adjacent triplets -----
def collectNeighborIds(edgeDirection: EdgeDirection): VertexRDD[Array[VertexId]]
def collectNeighbors(edgeDirection: EdgeDirection): VertexRDD[Array[(VertexId, VD)]]
def aggregateMessages[Msg: ClassTag](
    sendMsg: EdgeContext[VD, ED, Msg] => Unit,
    mergeMsg: (Msg, Msg) => Msg,
    tripletFields: TripletFields = TripletFields.All)
    : VertexRDD[A]
```

Graph operators

```
// Iterative graph-parallel computation -----
def pregel[A](initialMsg: A, maxIterations: Int, activeDirection: EdgeDirection)(
    vprog: (VertexId, VD, A) => VD,
    sendMsg: EdgeTriplet[VD, ED] => Iterator[(VertexId,A)],
    mergeMsg: (A, A) => A
  : Graph[VD, ED]
// Basic graph algorithms -----
def pageRank(tol: Double, resetProb: Double = 0.15): Graph[Double, Double]
def connectedComponents(): Graph[VertexId, ED]
def triangleCount(): Graph[Int, ED]
def stronglyConnectedComponents(numIter: Int): Graph[VertexId, ED]
```

Property Operators

```
class Graph[VD, ED] {  
    def mapVertices[VD2](map: (VertexId, VD) => VD2): Graph[VD2, ED]  
    def mapEdges[ED2](map: Edge[ED] => ED2): Graph[VD, ED2]  
    def mapTriplets[ED2](map: EdgeTriplet[VD, ED] => ED2): Graph[VD, ED2]  
}
```

```
val newVertices = graph.vertices.map { case (id, attr) => (id, mapUdf(id, attr)) }  
val newGraph = Graph(newVertices, graph.edges)
```

Instead, use [mapVertices](#) to preserve the indices:

```
val newGraph = graph.mapVertices((id, attr) => mapUdf(id, attr))
```

```
// Given a graph where the vertex property is the out degree  
val inputGraph: Graph[Int, String] =  
    graph.outerJoinVertices(graph.outDegrees)((vid, _, degOpt) => degOpt.getOrElse(0))  
// Construct a graph where each edge contains the weight  
// and each vertex is the initial PageRank  
val outputGraph: Graph[Double, Double] =  
    inputGraph.mapTriplets(triplet => 1.0 / triplet.srcAttr).mapVertices((id, _) => 1.0)
```

Structural Operators

```
class Graph[VD, ED] {  
    def reverse: Graph[VD, ED]  
    def subgraph(epred: EdgeTriplet[VD, ED] => Boolean,  
                vpred: (VertexId, VD) => Boolean): Graph[VD, ED]  
    def mask[VD2, ED2](other: Graph[VD2, ED2]): Graph[VD, ED]  
    def groupEdges(merge: (ED, ED) => ED): Graph[VD, ED]  
}
```

Structural Operations

```
// Create an RDD for the vertices
val users: RDD[(VertexId, (String, String))] =
  sc.parallelize(Array((3L, ("rxin", "student")), (7L, ("jgonzal", "postdoc")),
    (5L, ("franklin", "prof")), (2L, ("istoica", "prof")),
    (4L, ("peter", "student"))))

// Create an RDD for edges
val relationships: RDD[Edge[String]] =
  sc.parallelize(Array(Edge(3L, 7L, "collab"), Edge(5L, 3L, "advisor"),
    Edge(2L, 5L, "colleague"), Edge(5L, 7L, "pi"),
    Edge(4L, 0L, "student"), Edge(5L, 0L, "colleague")))

// Define a default user in case there are relationship with missing user
val defaultUser = ("John Doe", "Missing")

// Build the initial Graph
val graph = Graph(users, relationships, defaultUser)

// Notice that there is a user 0 (for which we have no information) connected to users
// 4 (peter) and 5 (franklin).
graph.triplets.map(
  triplet => triplet.srcAttr._1 + " is the " + triplet.attr + " of " + triplet.dstAttr._1
).collect.foreach(println(_))

// Remove missing vertices as well as the edges to connected to them
val validGraph = graph.subgraph(vpred = (id, attr) => attr._2 != "Missing")
// The valid subgraph will disconnect users 4 and 5 by removing user 0
validGraph.vertices.collect.foreach(println(_))
validGraph.triplets.map(
  triplet => triplet.srcAttr._1 + " is the " + triplet.attr + " of " + triplet.dstAttr._1
).collect.foreach(println(_))
```

Join Operators

```
class Graph[VD, ED] {  
    def joinVertices[U](table: RDD[(VertexId, U)])(map: (VertexId, VD, U) => VD)  
        : Graph[VD, ED]  
    def outerJoinVertices[U, VD2](table: RDD[(VertexId, U)])(map: (VertexId, VD, Option[U]) => VD2)  
        : Graph[VD2, ED]  
}  
  
val nonUniqueCosts: RDD[(VertexId, Double)]  
val uniqueCosts: VertexRDD[Double] =  
    graph.vertices.aggregateUsingIndex(nonUnique, (a,b) => a + b)  
val joinedGraph = graph.joinVertices(uniqueCosts)(  
    (id, oldCost, extraCost) => oldCost + extraCost)  
  
val outDegrees: VertexRDD[Int] = graph.outDegrees  
val degreeGraph = graph.outerJoinVertices(outDegrees) { (id, oldAttr, outDegOpt) =>  
    outDegOpt match {  
        case Some(outDeg) => outDeg  
        case None => 0 // No outDegree means zero outDegree  
    }  
}
```

Aggregate Messages

```
class Graph[VD, ED] {  
    def aggregateMessages[Msg: ClassTag](  
        sendMsg: EdgeContext[VD, ED, Msg] => Unit,  
        mergeMsg: (Msg, Msg) => Msg,  
        tripletFields: TripletFields = TripletFields.All)  
        : VertexRDD[Msg]  
    }  
  
import org.apache.spark.graphx.{Graph, VertexRDD}  
import org.apache.spark.graphx.util.GraphGenerators  
  
// Create a graph with "age" as the vertex property.  
// Here we use a random graph for simplicity.  
val graph: Graph[Double, Int] =  
    GraphGenerators.logNormalGraph(sc, numVertices = 100).mapVertices( (id, _) => id.toDouble )  
// Compute the number of older followers and their total age  
val olderFollowers: VertexRDD[(Int, Double)] = graph.aggregateMessages[(Int, Double)](  
    triplet => { // Map Function  
        if (triplet.srcAttr > triplet.dstAttr) {  
            // Send message to destination vertex containing counter and age  
            triplet.sendToDst(1, triplet.srcAttr)  
        }  
    },  
    // Add counter and age  
    (a, b) => (a._1 + b._1, a._2 + b._2) // Reduce Function  
)  
// Divide total age by number of older followers to get average age of older followers  
val avgAgeOfOlderFollowers: VertexRDD[Double] =  
    olderFollowers.mapValues( (id, value) =>  
        value match { case (count, totalAge) => totalAge / count } )  
// Display the results  
avgAgeOfOlderFollowers.collect.foreach(println(_))
```

Compute Degree information

```
// Define a reduce operation to compute the highest degree vertex
def max(a: (VertexId, Int), b: (VertexId, Int)): (VertexId, Int) = {
  if (a._2 > b._2) a else b
}
// Compute the max degrees
val maxInDegree: (VertexId, Int)  = graph.inDegrees.reduce(max)
val maxOutDegree: (VertexId, Int) = graph.outDegrees.reduce(max)
val maxDegrees: (VertexId, Int)   = graph.degrees.reduce(max)
```

```
class GraphOps[VD, ED] {
  def collectNeighborIds(edgeDirection: EdgeDirection): VertexRDD[Array[VertexId]]
  def collectNeighbors(edgeDirection: EdgeDirection): VertexRDD[ Array[(VertexId, VD)] ]
}
```

PageRank

```
import org.apache.spark.graphx.GraphLoader

// Load the edges as a graph
val graph = GraphLoader.edgeListFile(sc, "data/graphx/followers.txt")
// Run PageRank
val ranks = graph.pageRank(0.0001).vertices
// Join the ranks with the usernames
val users = sc.textFile("data/graphx/users.txt").map { line =>
  val fields = line.split(",")
  (fields(0).toLong, fields(1))
}
val ranksByUsername = users.join(ranks).map {
  case (id, (username, rank)) => (username, rank)
}
// Print the result
println(ranksByUsername.collect().mkString("\n"))
```

Connected Components

```
import org.apache.spark.graphx.GraphLoader

// Load the graph as in the PageRank example
val graph = GraphLoader.edgeListFile(sc, "data/graphx/followers.txt")
// Find the connected components
val cc = graph.connectedComponents().vertices
// Join the connected components with the usernames
val users = sc.textFile("data/graphx/users.txt").map { line =>
    val fields = line.split(",")
    (fields(0).toLong, fields(1))
}
val ccByUsername = users.join(cc).map {
    case (id, (username, cc)) => (username, cc)
}
// Print the result
println(ccByUsername.collect().mkString("\n"))
```

Triangle Counting

```
import org.apache.spark.graphx.{GraphLoader, PartitionStrategy}

// Load the edges in canonical order and partition the graph for triangle count
val graph = GraphLoader.edgeListFile(sc, "data/graphx/followers.txt", true)
  .partitionBy(PartitionStrategy.RandomVertexCut)

// Find the triangle count for each vertex
val triCounts = graph.triangleCount().vertices

// Join the triangle counts with the usernames
val users = sc.textFile("data/graphx/users.txt").map { line =>
  val fields = line.split(",")
  (fields(0).toLong, fields(1))
}

val triCountByUsername = users.join(triCounts).map { case (id, (username, tc)) =>
  (username, tc)
}

// Print the result
println(triCountByUsername.collect().mkString("\n"))
```

Contacts

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