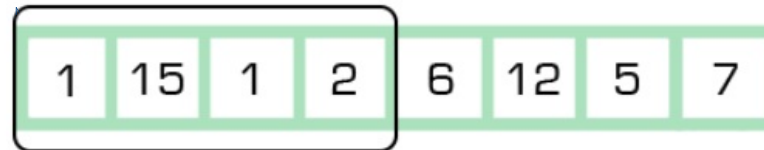
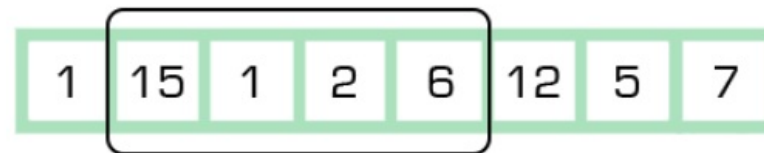


sliding window



slide one element forward



**Sliding Window Technique**

①

Two pointer

[pair | Target | Reverse]

① ②

① same direction  
② opposite direction

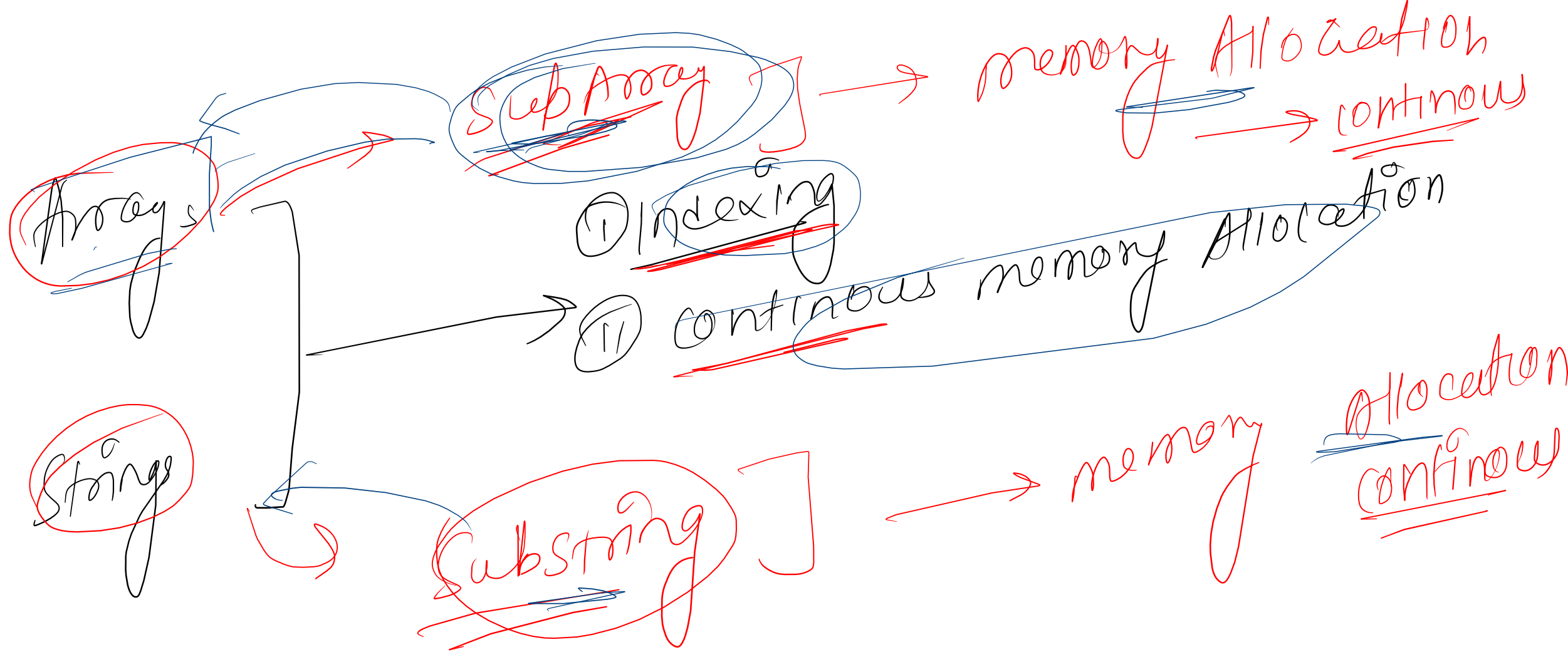
Some case

Array must be sorted

②

Sliding Window

Arrays or Strings



point

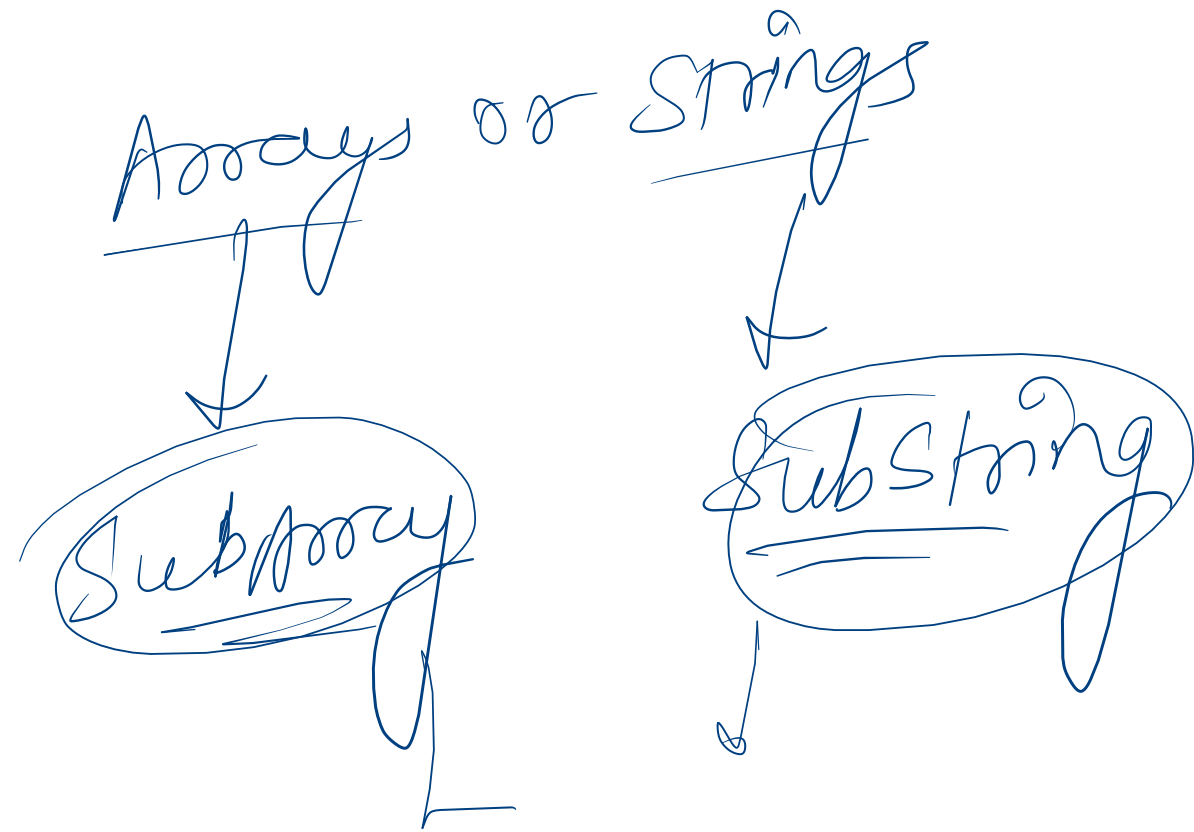
sub

Substring / Subarray → They are just small part of  
array and string in continuous manner.

Arr = [1, 2, 3, 4, 5] → ~~[1, 3, 5]~~

String str = "world" → ~~god~~ world

Sliding Window →



~~Ans~~ [1, 2, 3, 4, 5]  $\rightarrow$  All possible subarrays

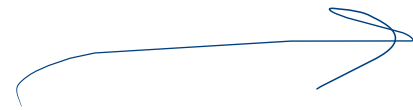
n = 5  
 $\downarrow$  subarrays

{  
[1], [1, 2], [1, 2, 3], [1, 2, 3, 4], [1, 2, 3, 4, 5]  
[2], [2, 3], [2, 3, 4], [2, 3, 4, 5]  
[3], [3, 4], [3, 4, 5]  
[4], [4, 5]  
[5]  
}

$\Rightarrow$   $\frac{n(n+1)}{2}$   
 $\frac{5 \times (5+1)}{2} = 15$   
 $\hookrightarrow$   $(n^2)$

String =

"abc"



n(n+1)

$n=3$

{ "a", "ab", "abc",  
"b", "bc",  
"c" }

$$\frac{n(n+1)}{2}$$

$$\frac{3 \times (3+1)}{2} = 6$$



Arr =

[1, 2, 3]

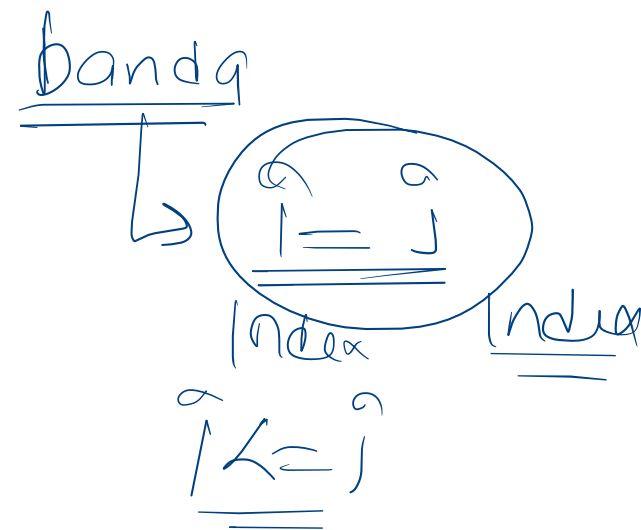
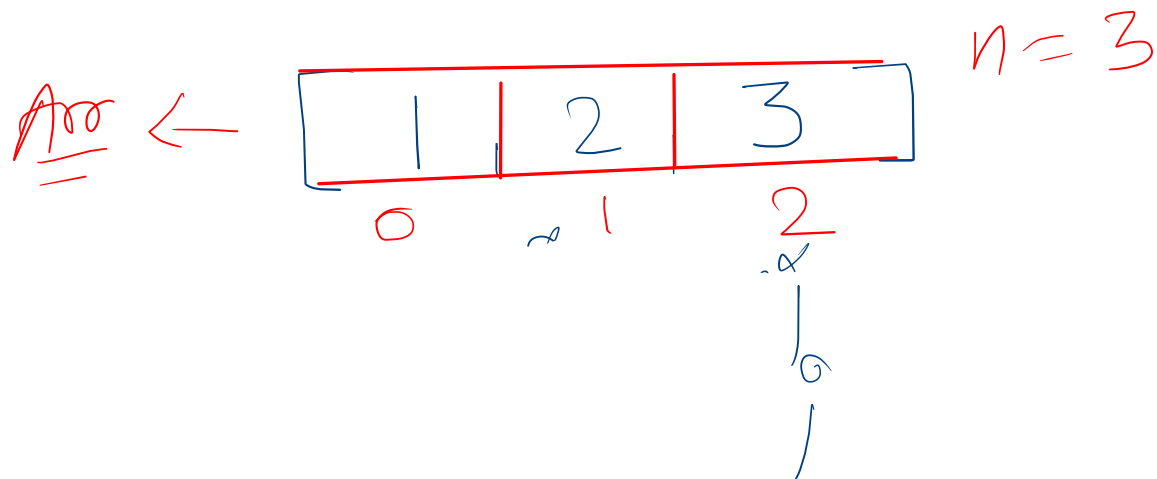
Brute



[print All possible Subarrays]

[  
[1], [1, 2], [1, 2, 3]  
[2], [2, 3]  
[3]  
]

Brute force



$i=0$   
 $j=0$

$\{ [1], [1,2], [1,2,3] \}$   
 $\{ [2], [2,3] \}$   
 $[3]$

Before **Sliding Window**:

map and unordered\_map

<map>

map

<unordered\_map>

unordered\_map

key-value

key-value

→ BST

→ Sorted by key

→ (log n)

→ Insert  
→ delete

→ HashTable

→ O(1)

→ Hashing

→ Not in any specific  
Order

## Feature

### Ordering

`map`

Keys are stored in **sorted order** (ascending by default using `<`).

`unordered_map`

Keys have **no specific order**.

### Underlying Data Structure

Self-balancing BST (usually Red-Black Tree)

Hash Table

### Time Complexity

$O(\log n)$  for insert, delete, find

Average case  $O(1)$ , Worst case  $O(n)$

### Header File

`<map>`

`<unordered_map>`

### Key Requirements

Must be **comparable** (`<` operator)

Must be **hashable** (`std::hash`)

### Traversal

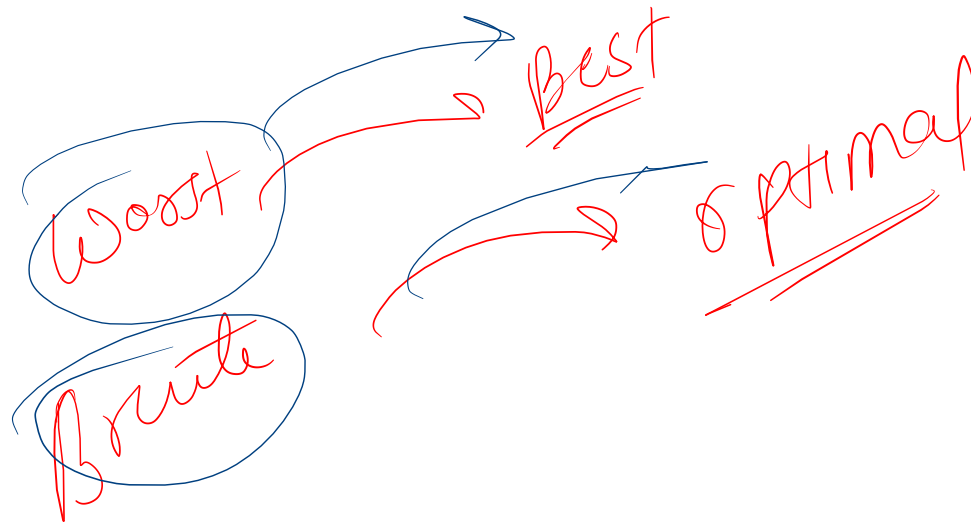
In sorted order by key

In arbitrary (unordered) order

## Sliding Window Technique?

The Sliding Window is a subarray or subset-based technique that is mainly used for problems involving arrays or strings.

Instead of checking every possible subarray (which leads to  $O(n^2)$  time), Sliding Window allows you to move a window of size  $k$  across the array, doing the needed calculation in  $O(n)$  time.



## **When to Use** Sliding Window?

Clue in Problem Statement	Example Phrases
Fixed/Variable-sized Subarray or Substring	"Find max sum of <b>k</b> consecutive elements", "Longest substring with at most <b>k</b> distinct characters"
Need to check or optimize values over subarrays	"Find minimum length of substring", "Count substrings with conditions"
Continuous elements	"Consecutive", "Contiguous", "Subarray"

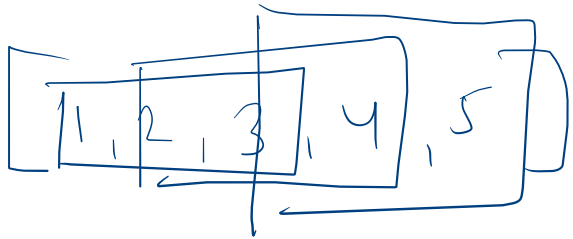
# Sliding Window

Array

object / Hashmap / map  
dictionary

## Model 1

Size of S.W. is **fixed**  
Note: Given in question.



$K = 3$

## Model 2

Size of S.W. is **variable**  
Note: Not Given in question.

Array	1	2	3	4	5	6	7	8	9	10
Index	0	1	2	3	4	5	6	7	8	9
$n-1$										

Size  $\Rightarrow$


$$j - i + 1$$

$$7 - 3 + 1 = 5$$



100 — 98% → Studying Winter

Fixed Sized **Sliding Window**

A red wavy underline line is positioned below the text "Fixed Sized Sliding Window". It starts under the 'F', dips slightly, then rises to end under the 'W'.

## 1. Maximum Sum Subarray of Size K

Given an array of integers and a number  $k$ , find the maximum sum of any contiguous subarray of size  $k$ .

**Input:**  $\text{arr} = [2, 1, 5, 1, 3, 2]$ ,  $k = 3$

**Output:** 9

Brute force  
↓  
Sliding

// [2, 1, 5, 1, 3, 2], k = 3

Sum = 8

Sum = 7

~~Sum = 9~~

Sum = 6

Subarray = k

## Using Brute Force

```
int maxSumK(int arr[], int n, int k) {  
    int maxSum = 0;  
  
    for (int i = 0; i <= n - k; i++) {  
        int currentSum = 0;  
        for (int j = i; j < i + k; j++) {  
            currentSum += arr[j];  
        }  
        maxSum = max(maxSum, currentSum);  
    }  
  
    return maxSum;  
}
```

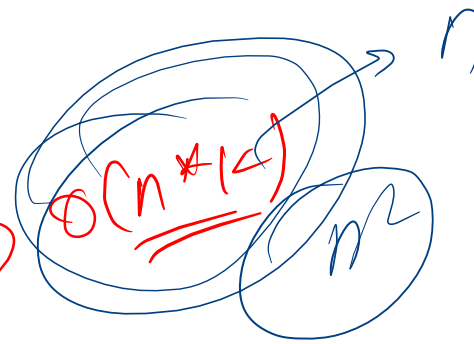
$$n = 6 - 3 = 3$$

$\rightarrow$   
[2, 1, 5, 1, 3, 2], k = 3

0 1 2 3 4 5  
↓  
0  
↓  
0  
↓  
0

$n * k$

$\Rightarrow$

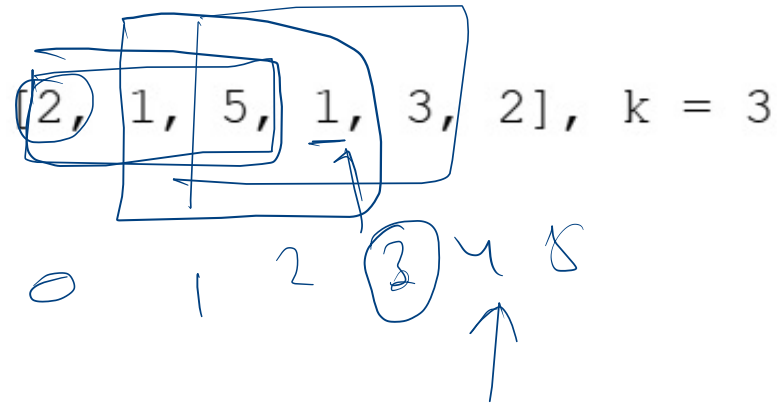


## Using Sliding Window

```
int maxSumK(int arr[], int n, int k) {  
    int maxSum = 0, windowSum = 0;  
  
    for (int i = 0; i < k; i++)  
        windowSum += arr[i];  
  
    maxSum = windowSum;  
    maxSum = max(maxSum, windowSum);  
  
    for (int i = k; i < n; i++) {  
        windowSum += arr[i] - arr[i - k];  
        maxSum = max(maxSum, windowSum);  
    }  
  
    return maxSum;  
}
```

maxSum = 8

WS = 8 + 1  $\Rightarrow$  9 - 2 = 7



$O(n)$

## 2. Count the Number of Vowels in All Substrings of Size k

Given a string `s` and an integer `k`, count the number of vowels in every contiguous substring of size `k`.

**Input:** `s = "abciidef"`, `k = 3`

**Output:**

1 1 2

## Using Brute Force

```
bool isVowel(char c) {  
    c = tolower(c);  
    return c == 'a' || c == 'e' || c == 'i' || c == 'o' || c == 'u';  
}  
  
void countVowelsBrute(string s, int k) {  
    int n = s.length();  
  
    for (int i = 0; i <= n - k; i++) {  
        int count = 0;  
        for (int j = i; j < i + k; j++) {  
            if (isVowel(s[j])) count++;  
        }  
        cout << count << " ";  
    }  
}
```



## Using Sliding Window

```
void countVowelsSliding(string s, int k) {  
    int n = s.length();  
    int count = 0;  
  
    for (int i = 0; i < k; i++) {  
        if (isVowel(s[i])) count++;  
    }  
  
    cout << count << " ";  
  
    for (int i = k; i < n; i++) {  
        if (isVowel(s[i - k])) count--; // remove char going out  
        if (isVowel(s[i])) count++;     // add char coming in  
        cout << count << " ";  
    }  
}
```



Variable Size **Sliding Window**

Find is there any sub-array with the given sum [ return True/ False ]

	0	1	2	3	4	5	$n=6$
arr	1	4	20	3	10	5	sum=33

```

function fun(arr,n,sum) // variable size S.W
{
    windowSum=0, high=0
    for(low=0; low<n; low++)
    {
        while(windowSum<sum && high<n)
        {
            windowSum=windowSum+arr[high]
            high++
        }
        if(windowSum==sum) // happy
        {
            return true
        }
        windowSum=windowSum-arr[low]
    }
    return false
}

```

arr

0	1	2	3	4	5
1	4	20	3	10	5

n=6  
sum=33

Find the size of largest sub-string which doesn't contains any repeated characters in given string

	0	1	2	3	4	5	6	7	8	$n=9$
s	a	b	b	c	d	e	a	b	b	

```

function longestUniqueSubsttr(s,n)
{
    let hm be a hashmap/ object

    maximum_length = 0;

    start = 0;

    for(i= 0; i < n; i++)
    {
        if(hm.containsKey(s[i]))
        {
            start = Math.max(start, hm.get(s[i]) + 1);
        }
        hm.put(s[i], i);
        maximum_length = Math.max(maximum_length, i-start + 1);
    }
    return maximum_length;
}

```

s →

0	1	2	3	4	5	6	7	8
a	b	b	c	d	e	a	b	b

n = 9

Find the Longest Substring which contains K distinct / Unique characters

	0	1	2	3	4	5	6	7	8	9	10	$n = 11$
s →	a	a	b	a	c	b	e	b	e	b	e	$k = 3$

```

int longestKDistinctSubstring(string s, int k) {
    unordered_map<char, int> freq;
    int start = 0, maxLen = 0;
    for (int end = 0; end < s.length(); end++) {
        freq[s[end]]++;

        while (freq.size() > k) {
            freq[s[start]]--;
            if (freq[s[start]] == 0)
                freq.erase(s[start]);
            start++;
        }

        if (freq.size() == k) {
            maxLen = max(maxLen, end - start + 1);
        }
    }

    return maxLen;
}

```

	0	1	2	3	4	5	6	7	8	9	10	n=11
s	0	a	b	a	c	b	e	b	e	b	e	k=3



End