

Minimum Spanning Trees

Hengfeng Wei

Institute of Computer Software
Nanjing University

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Minimum Spanning Trees

- 1 The MST Problem
- 2 The Generic MST Algorithm
- 3 The Algorithms of Kruskal and Prim

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Definition (MST)

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MST: Minimize $w(T)$ over all possible STs

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MST Example

A Wrong Algorithm

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