

Data Structures and Algorithms
with applications in Machine Learning
- Mock MCQ 1 -

NAME: _____

GROUP: _____

Each Question: 1 Mark

Duration: 30 Minutes

Completely fill the circles as shown: ○○●○

Answer sheet

Q1. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q2. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q3. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q4. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q5. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q6. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q7. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q8. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q9. ○ a.
 ○ b.
 ○ c.
 ○ d.

Q10. ○ a.
 ○ b.
 ○ c.
 ○ d.

The Quiz

Q. 1 Complete the missing part of the function to create a `word_index` dictionary from a list of documents.

The input is a list of documents, where each document is a list of tokens. For example:

```
documents = [["the", "cat", "sat"], ["the", "dog", "barked"]]
```

The function should return a dictionary where each unique word is assigned a unique integer starting from 1. For example:

```
{
    "the": 1,
    "cat": 2,
    "sat": 3,
    "dog": 4,
    "barked": 5
}
```

Complete the missing part of the `if` statement to ensure only unique words are added to the dictionary:

```
def create_word_index(documents):
    """
    Creates a word_index dictionary mapping unique tokens to unique integers.

    Parameters:
        documents (list of list of str): List of documents, where each document
        is a list of tokens.

    Returns:
        dict: A dictionary mapping words to unique integers.
    """
    word_index = {}
    current_index = 1

    for document in documents:
        for token in document:
            # Check if the token is already in the dictionary
            if _____: # Fill in the blank
                word_index[token] = current_index
                current_index += 1

    return word_index
```

What should replace the blank in the `if` statement?

- ☐ a. `token in word_index`
- ☐ b. `token not in word_index`
- ☐ c. `current_index in word_index`
- ☐ d. `token == word_index`

Q. 2 What is the expected result of applying the `word_index` dictionary to convert a corpus into sequences of integers?

For example, given the following corpus:

```
documents = [["the", "cat", "sat"], ["the", "dog", "barked"]]
```

And the `word_index` dictionary:

```
{
  "the": 1,
  "cat": 2,
  "sat": 3,
  "dog": 4,
  "barked": 5
}
```

What would the resulting sequences look like?

- ☐ a. `[[1, 2, 3], [1, 4, 5]]`
- ☐ b. `[["the", "cat", "sat"], ["the", "dog", "barked"]]`
- ☐ c. `[[2, 3, 1], [4, 5, 1]]`
- ☐ d. `[1, 2, 3, 4, 5]`

Q. 3 Below is the algorithm for computing the co-occurrence matrix:

Algorithm 1 Getting the Co-occurrence Matrix

Require: sequences (list of lists of integers), context_size

Ensure: X (the co-occurrence matrix)

```
1: Initialize matrix  $X \in \mathbb{M}_{V,V}(\mathbb{R})$  with zeros
2: for all sequence in sequences do
3:   for all center_word with index  $i$  in sequence do
4:     for all context_word with index  $j$  in context of center_word do
5:       if  $i \neq j$  then
6:          $X[\text{center\_word}, \text{context\_word}] \leftarrow X[\text{center\_word}, \text{context\_word}] + 1$ 
7:       end if
8:     end for
9:   end for
10: end for
11: return  $X$ 
```

The task is to implement this algorithm in Python. Complete the missing part of the following function to handle the update of the co-occurrence matrix.

```
def get_cooccurrence_matrix(sequences, context_size, vocab_size):
    """
    Creates a co-occurrence matrix from sequences of word indices.

    Parameters:
        sequences (list of list of int): List of sentences represented
        as lists of word indices.
        context_size (int): The size of the context window.
        vocab_size (int): The size of the vocabulary.
```

Returns:

```
numpy.ndarray: A co-occurrence matrix of shape (vocab_size, vocab_size).
"""
import numpy as np
X = np.zeros((vocab_size, vocab_size), dtype=np.float32)

for sequence in sequences:
    for i, center_word in enumerate(sequence):
        # Define start and end of the context window
        start = max(0, i - context_size)
        end = min(len(sequence), i + context_size + 1)

        for j in range(start, end):
            if i != j:
                # Update the co-occurrence matrix
                X[center_word, sequence[j]] = _____ # Fill in the blank

return X
```

What should replace the blank to correctly implement the algorithm?

- ☐ a. $X[\text{center_word}, \text{sequence}[j]] - 1$
- ☐ b. $X[\text{center_word}, \text{sequence}[j]] + 1$
- ☐ c. $X[\text{sequence}[j], \text{center_word}] + 1$
- ☐ d. $X[\text{center_word}, \text{center_word}] + 1$

Q. 4 What does the element X_{ij} in the co-occurrence matrix represent based on the algorithm for constructing the matrix?

- ☐ a. The number of times the word represented by index j appears in the context of the word represented by index i within the specified context window
- ☐ b. The frequency of the word represented by index i in the entire corpus
- ☐ c. The cosine similarity between the words represented by indices i and j
- ☐ d. The total number of words in the sentence containing i and j

Q. 5 Given the following small corpus and word_index:

```
corpus = [["cat", "sat", "on", "the", "mat"],
          ["the", "cat", "is", "cute"]]
```

```
word_index = {"cat": 0, "sat": 1, "on": 2, "the": 3, "mat": 4, "is": 5, "cute": 6}
```

Suppose the context window size is 1. Calculate $X_{0,3}$, where X_{ij} is the number of times the word corresponding to index j ("the") appears in the context of the word corresponding to index i ("cat").

- ☐ a. $X_{0,3} = 2$, because the word "the" appears twice in the context of "cat" in the corpus
- ☐ b. $X_{0,3} = 1$, because the word "the" appears only once in the context of "cat" in the corpus
- ☐ c. $X_{0,3} = 0$, because the word "the" does not appear in the context of "cat"
- ☐ d. $X_{0,3} = 3$, because the word "the" appears three times in the corpus

Q. 6 Recall the desired approximation:

$$\log X_{ij} \approx W_i^T \tilde{W}_j + b_i + \tilde{b}_j$$

The term $W_i^T \tilde{W}_j$ represents the relationship between the word indexed by i and the word indexed by j through their embeddings.

If we manage to achieve this approximation, what would we expect regarding the following comparisons of the dot products for the words "king", "queen", and "apple" with embeddings $W_{\text{king}}, W_{\text{queen}}, W_{\text{apple}}$?

- ☐ a. $W_{\text{king}}^T W_{\text{queen}} > W_{\text{king}}^T W_{\text{apple}}$
- ☐ b. $W_{\text{king}}^T W_{\text{queen}} < W_{\text{king}}^T W_{\text{apple}}$
- ☐ c. $W_{\text{king}}^T W_{\text{queen}} = W_{\text{king}}^T W_{\text{apple}}$
- ☐ d. $W_{\text{king}}^T W_{\text{queen}} = 0$

Q. 7 Recall the cost function J :

$$J(\theta) = \sum_{i=1}^V \sum_{j=1}^V f(X_{ij})(\log X_{ij} - W_i^T \tilde{W}_j - b_i - \tilde{b}_j)^2$$

The parameters to optimize are:

- $W \in \mathcal{M}_{V,D}(\mathbb{R})$, the first embedding matrix,
- $\tilde{W} \in \mathcal{M}_{V,D}(\mathbb{R})$, the second embedding matrix,
- $b \in \mathbb{R}^V$, the bias vector for W ,
- $\tilde{b} \in \mathbb{R}^V$, the bias vector for \tilde{W} .

What is the total number of parameters to train in the model, assuming the vocabulary size is V and the embedding dimension is D ?

- ☐ a. $2VD + 2V$
- ☐ b. $VD + V$
- ☐ c. $V^2 + D^2$
- ☐ d. $2V + D$

Q. 8 Consider the gradient of the cost function J with respect to W_i , given by:

$$\nabla_{W_i} J(W_i) = -2 \sum_{j'=1}^V f(X_{ij'}) \left(\log X_{ij'} - W_i^T \tilde{W}_{j'} - b_i - \tilde{b}_{j'} \right) \tilde{W}_{j'}.$$

What is the shape of $\nabla_{W_i} J(W_i)$?

- ☐ a. \mathbb{R}^D
- ☐ b. \mathbb{R}^V

- ☐ c. $\mathbb{R}^{V \times D}$
- ☐ d. \mathbb{R}

Q. 9 The following pseudo-code implements gradient descent for optimizing the loss function J . Fill in the blank to correctly update the embedding matrix W during training.

Algorithm 2 Optimizing the Loss Function with Gradient Descent

Require: $\log X$, $f(X)$, learning rate η , number of epochs N_{epochs}

Ensure: $W^{(N_{\text{epochs}}-1)}, \tilde{W}^{(N_{\text{epochs}}-1)}, b^{(N_{\text{epochs}}-1)}, \tilde{b}^{(N_{\text{epochs}}-1)}$ (The trained parameters)

```

1: Initialize parameters  $W^{(0)}, \tilde{W}^{(0)}, b^{(0)}, \tilde{b}^{(0)}$ 
2: for  $t = 0$  to  $N_{\text{epochs}} - 1$  do
3:   Compute the cost  $J(W^{(t)}, \tilde{W}^{(t)}, b^{(t)}, \tilde{b}^{(t)})$ 
4:   for  $i = 0$  to  $V - 1$  do
5:      $W_i^{(t+1)} \leftarrow \dots$  ▷ Update  $W_i$  using gradient descent
6:   end for
7:   for  $j = 0$  to  $V - 1$  do
8:      $\tilde{W}_j^{(t+1)} \leftarrow \tilde{W}_j^{(t)} - \eta \cdot \nabla_{\tilde{W}_j} J(\tilde{W}_j^{(t)})$ 
9:   end for
10:  for  $i = 0$  to  $V - 1$  do
11:     $b_i^{(t+1)} \leftarrow b_i^{(t)} - \eta \cdot \nabla_{b_i} J(b_i^{(t)})$ 
12:  end for
13:  for  $j = 0$  to  $V - 1$  do
14:     $\tilde{b}_j^{(t+1)} \leftarrow \tilde{b}_j^{(t)} - \eta \cdot \nabla_{\tilde{b}_j} J(\tilde{b}_j^{(t)})$ 
15:  end for
16: end for

```

What should replace the blank in the update step for $W_i^{(t+1)}$?

- ☐ a. $W_i^{(t)} - \eta \cdot \nabla_{W_i} J(W_i^{(t)})$
- ☐ b. $W_i^{(t)} + \eta \cdot \nabla_{W_i} J(W_i^{(t)})$
- ☐ c. $W_i^{(t)} - \nabla_{W_i} J(W_i^{(t)})$
- ☐ d. $W_i^{(t)} + \nabla_{W_i} J(W_i^{(t)})$

Q. 10 After training the model using gradient descent, the algorithm outputs the embedding matrices W and \tilde{W} .

What do these embedding matrices represent?

- ☐ a. W and \tilde{W} are matrices of word embeddings where each row corresponds to a vector representation of a word, capturing its semantic relationships with other words in the vocabulary.
- ☐ b. W and \tilde{W} are co-occurrence matrices where each element represents the number of times two words co-occur in the corpus.
- ☐ c. W and \tilde{W} are matrices of random values, used only for initializing the optimization process.
- ☐ d. W and \tilde{W} are matrices of word frequencies where each row corresponds to the total number of occurrences of a word in the corpus.