

Data-driven Modelling, Forecasting and Control for Buildings in the Future Low Carbon Society



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<https://www.flexibleenergydenmark.dk/>

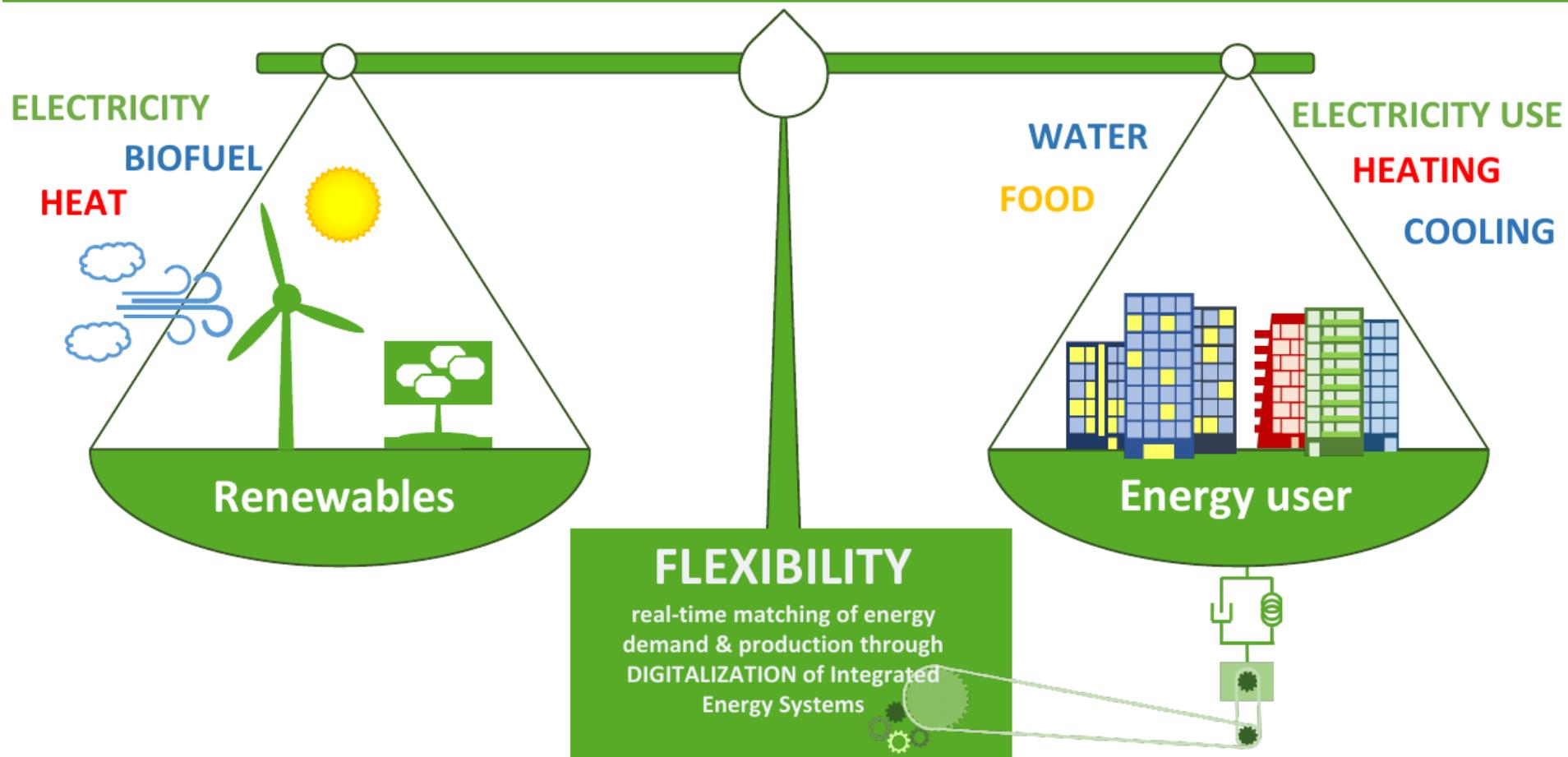
<http://www.smart-cities-centre.org>

<http://www.henrikmadsen.org>

The Challenges



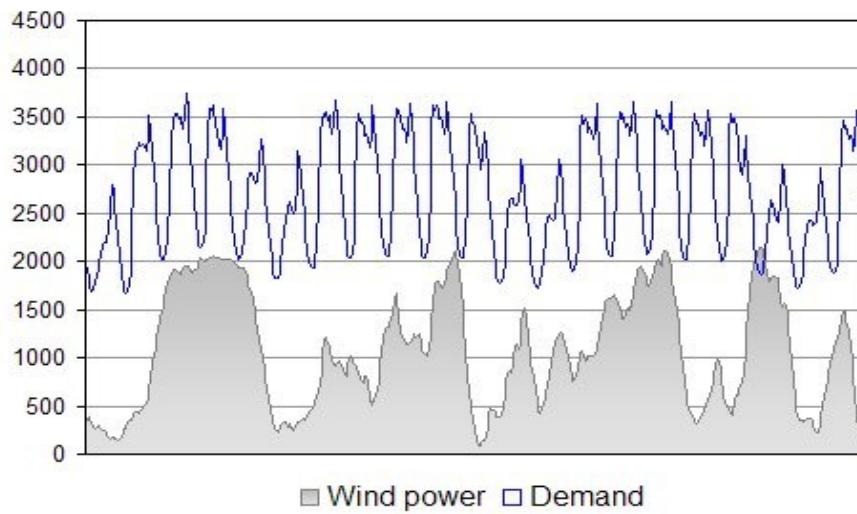
The Challenge: Denmark Fossil Free 2050



The Danish Wind Power Case

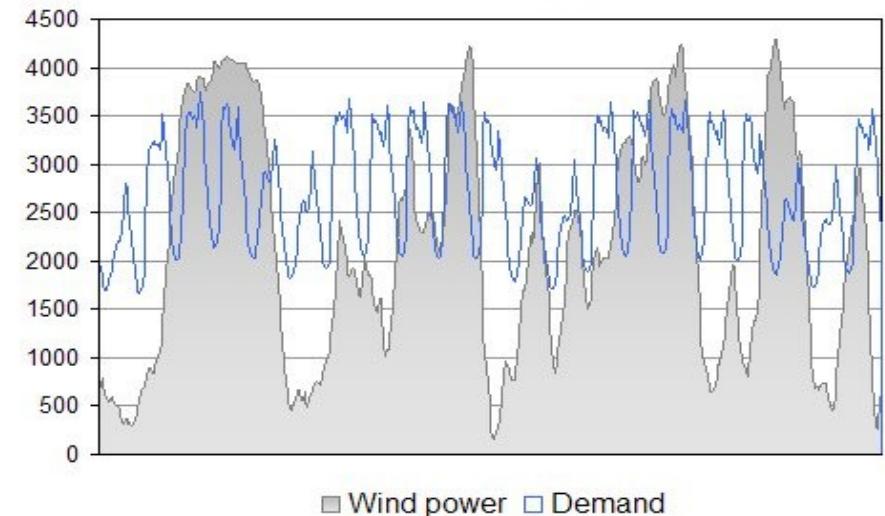
.... balancing of the power system

25 % wind energy (West Denmark January 2008)



In 2008 wind power did cover the entire demand of electricity in 200 hours (West DK)

50 % wind energy



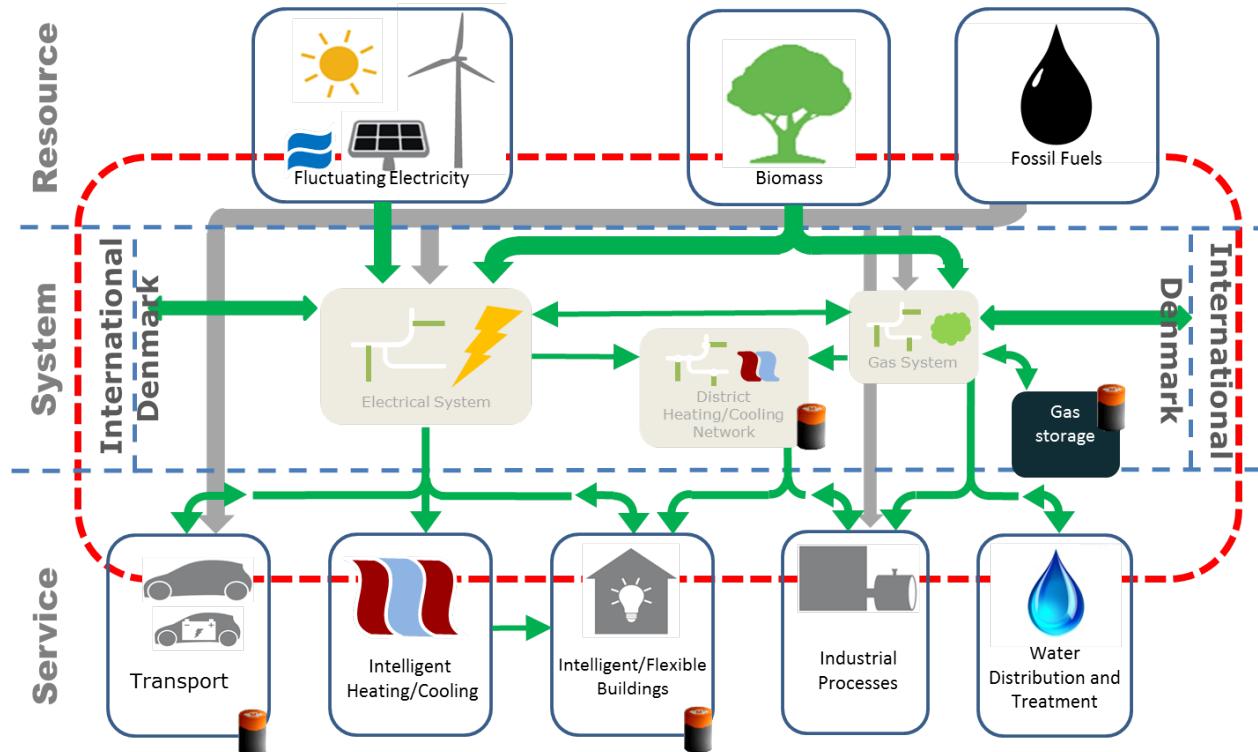
**In 2020 Flexibility and End-user Engagement is Important (→ Need for Smart Buildings)
That's the topic of 'Flexible Energy Denmark'**
(For several days the wind power production is more than 100 pct of the power load)

Combining grey-box modelling, forecasting and control (Smart-Energy OS)



Energy System Models for Real Time Applications and Data Assimilation

Grey-box models are simplified models for the individual components facilitating system integration and use of sensor data

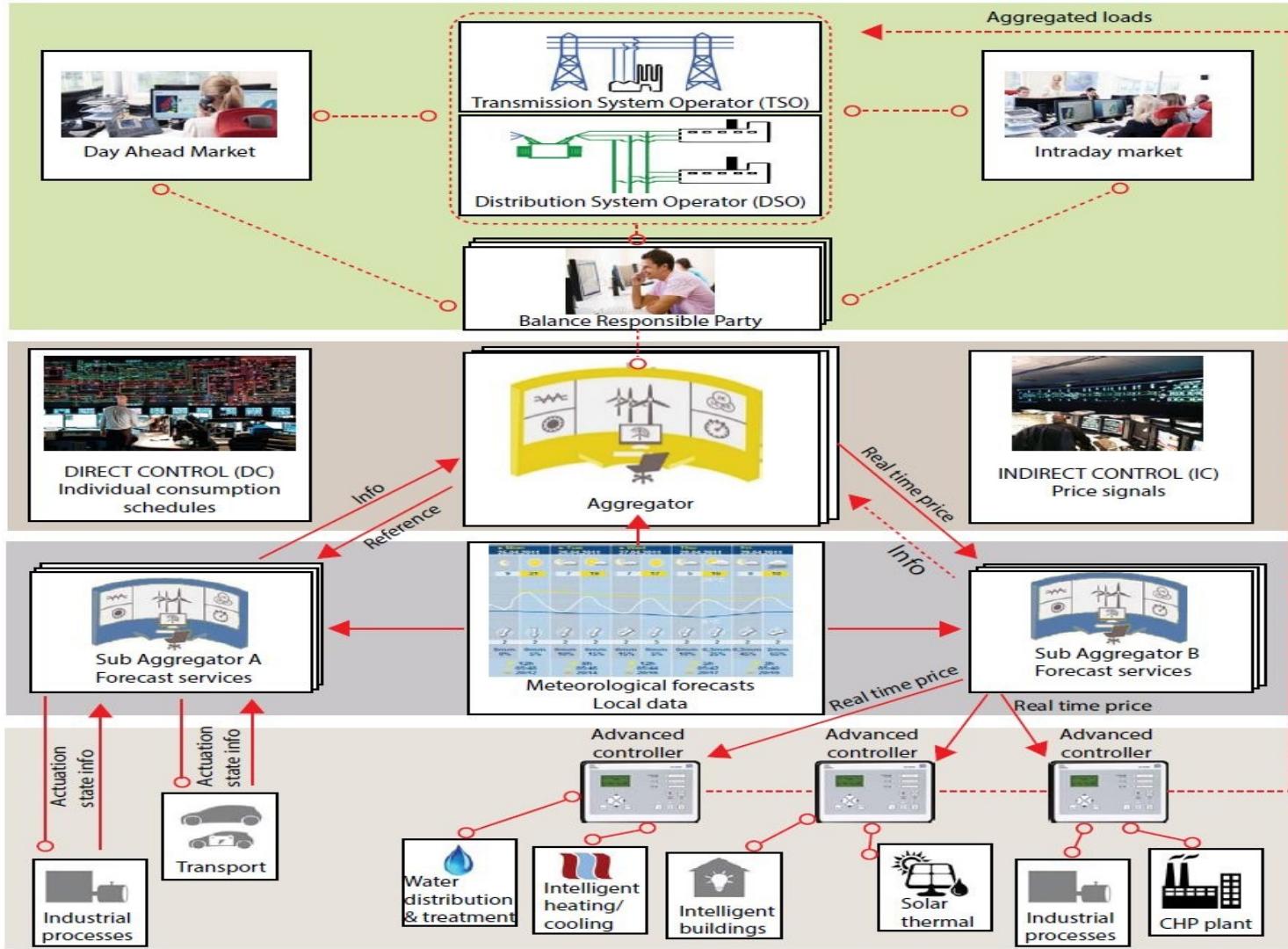


Temporal and Spatial Scales

The **Smart-Energy Operating-System (SE-OS)** is used to develop, implement and test of solutions (layers: data, models, optimization, control, aggregation, communication) for **operating flexible electrical energy systems at all scales**.

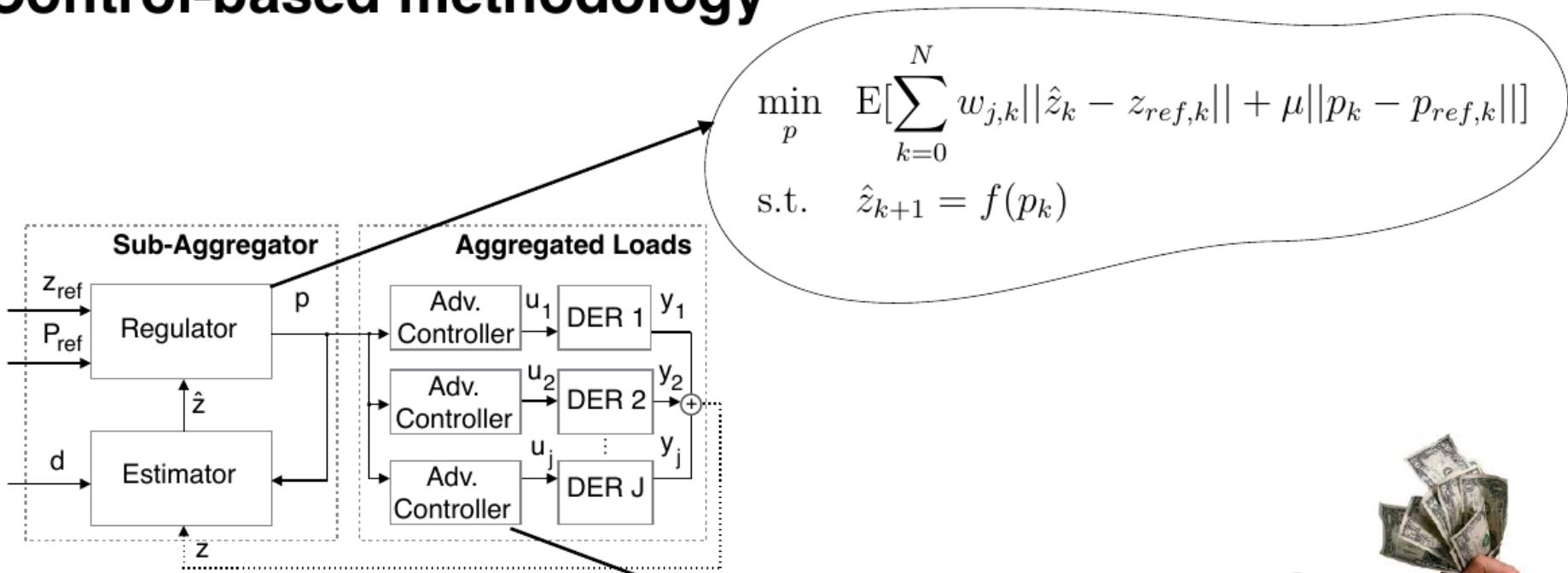


Smart-Energy OS



Proposed methodology

Control-based methodology



We adopt a control-based approach where the **price** becomes the driver to **manipulate** the behaviour of a certain pool flexible prosumers.

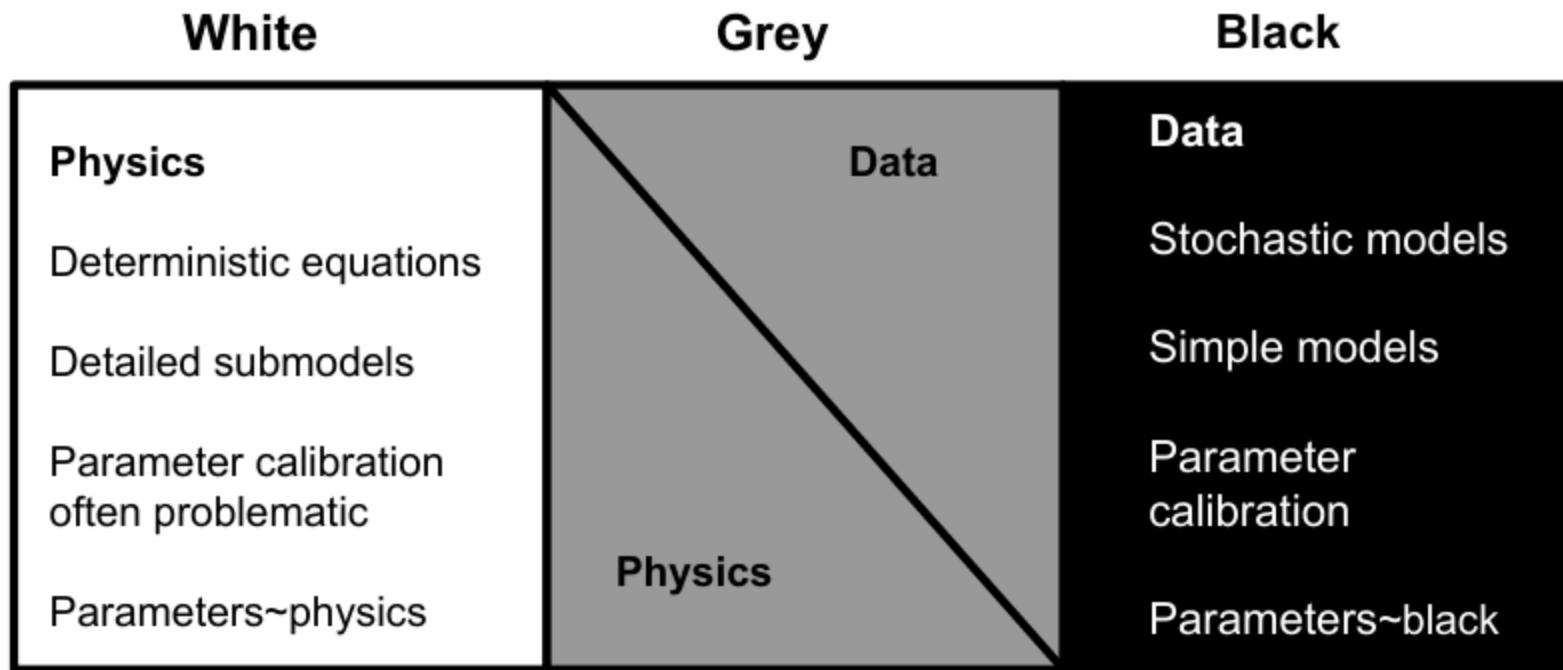


$$\begin{aligned} \min_u \quad & E\left[\sum_{k=0}^N \sum_{j=1}^J \phi_j(x_{j,k}, u_{j,k}, p_k)\right] \\ \text{s.t.} \quad & x_{k+1} = Ax_k + Bu_k + Ed_k, \\ & y_k = Cx_k, \\ & y_k^{min} \leq y_k \leq y_k^{max}, \\ & u_k^{min} \leq u_k \leq u_k^{max} \end{aligned}$$

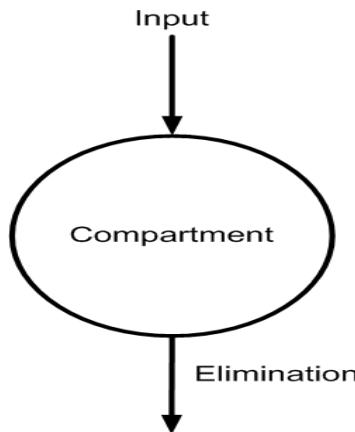
Grey-box Modelling



Grey-box Modelling



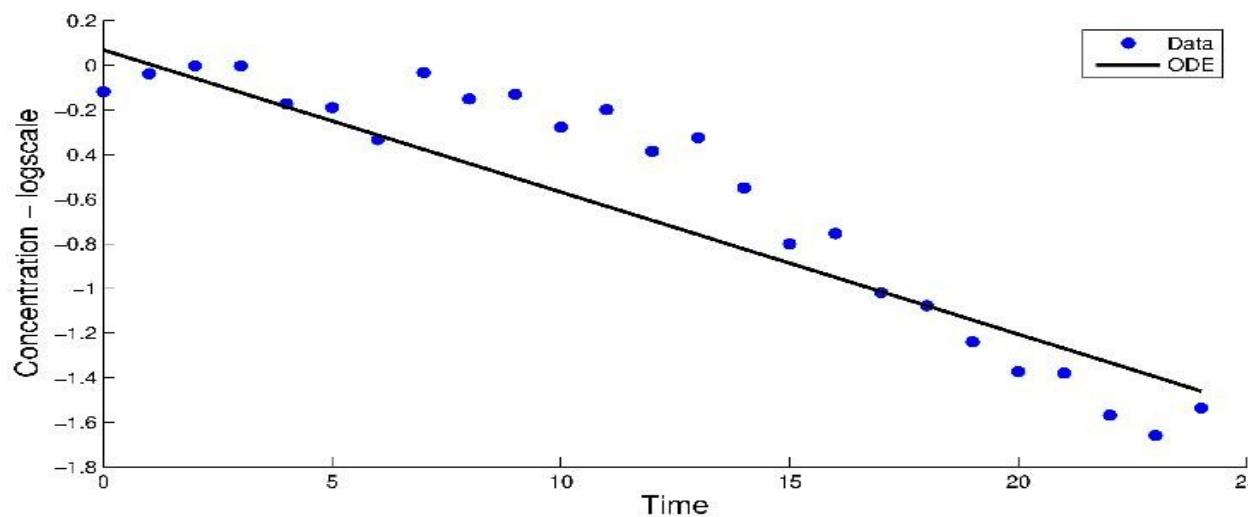
Traditional Dynamical Model



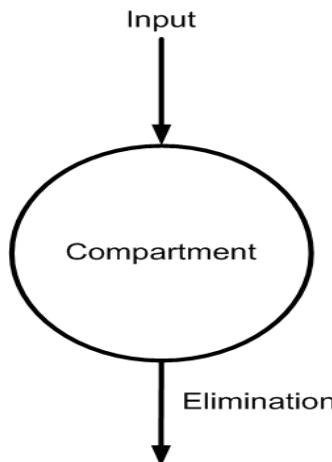
- Ordinary Differential Equation:

$$dA = -K A dt$$

$$Y = A + \epsilon$$



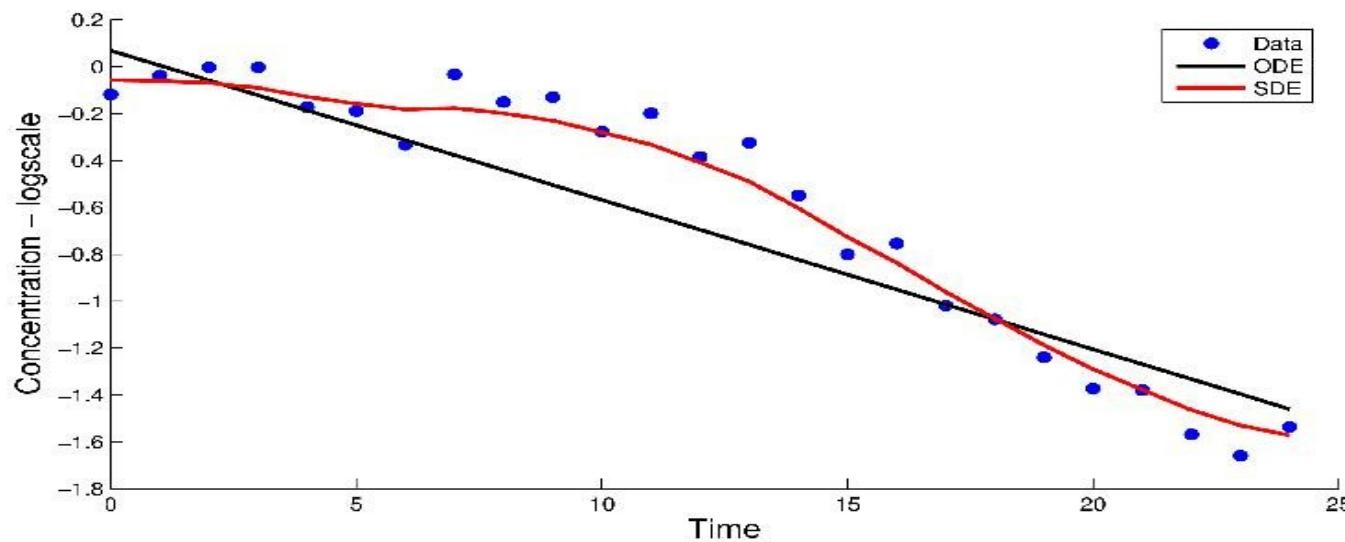
Stochastic Dynamical Model



- Stochastic Differential Equation:

$$dA = -K A dt + \sigma dw$$

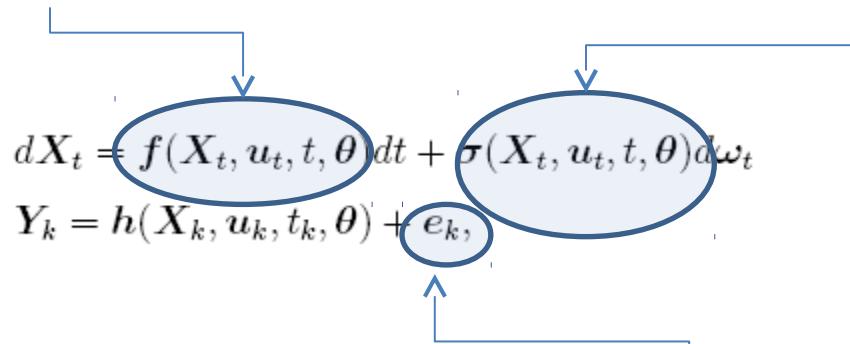
$$Y = A + e$$



The Grey-Box model

Drift term

$$dX_t = f(X_t, u_t, t, \theta) dt + \sigma(X_t, u_t, t, \theta) d\omega_t$$

$$Y_k = h(X_k, u_k, t_k, \theta) + e_k,$$


Diffusion term

System equation

Observation equation

Observation
noise

Notation:

- X_t : State variables
- u_t : Input variables
- θ : Parameters
- Y_k : Output variables
- t : Time
- ω_t : Standard Wiener process
- e_k : White noise process with $N(0, S)$

Grey-Box Modeling

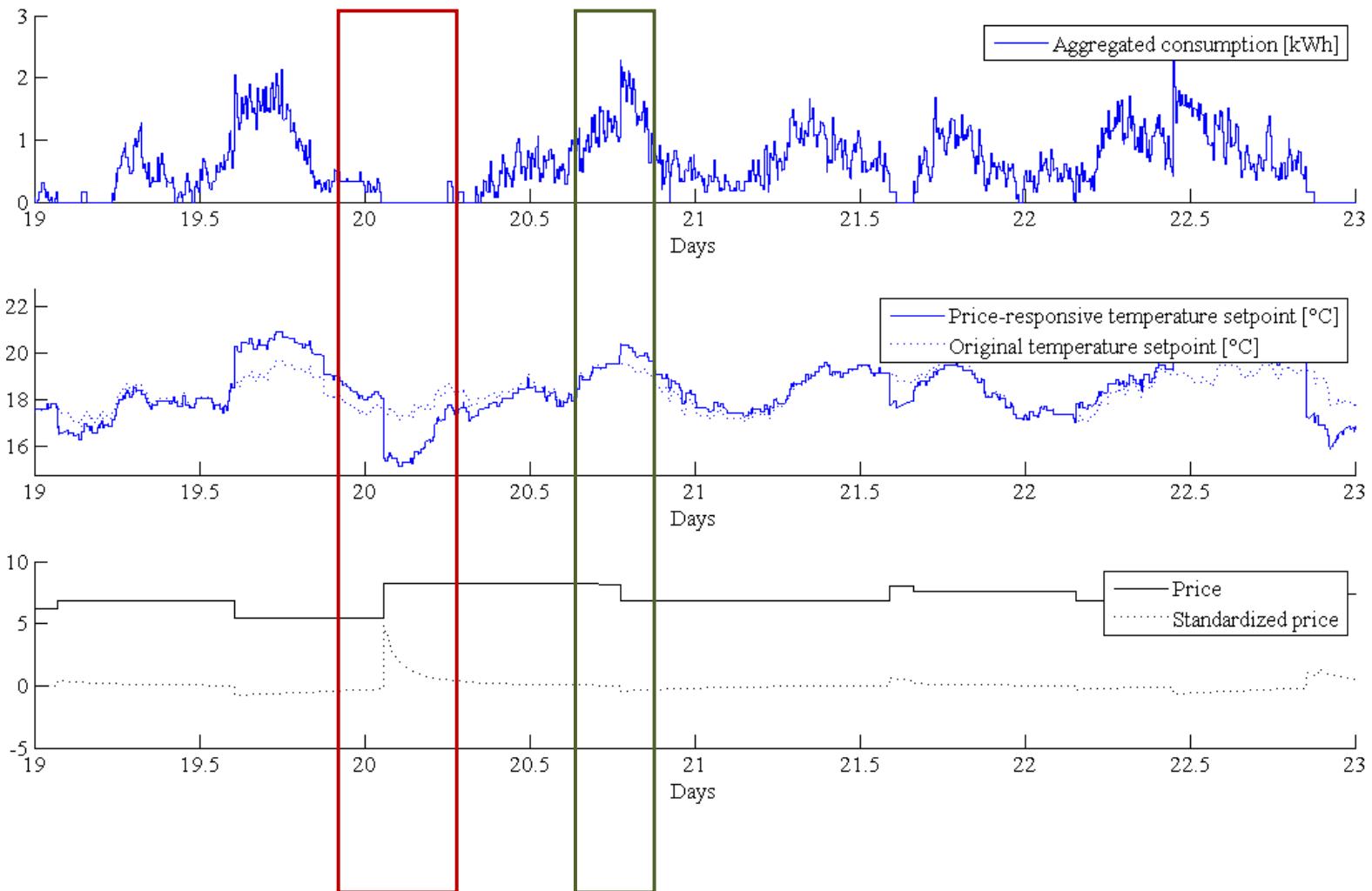
- **Bridges the gap between physical and statistical modeling**
- Provides methods for **model identification**
- Provides methods for **model validation**
- Provides methods for **pinpointing model deficiencies**
- Enables methods for a reliable description of the uncertainties, which implies that the same model can be used for **k-step forecasting, simulation** and **control**

Case study (Level III)

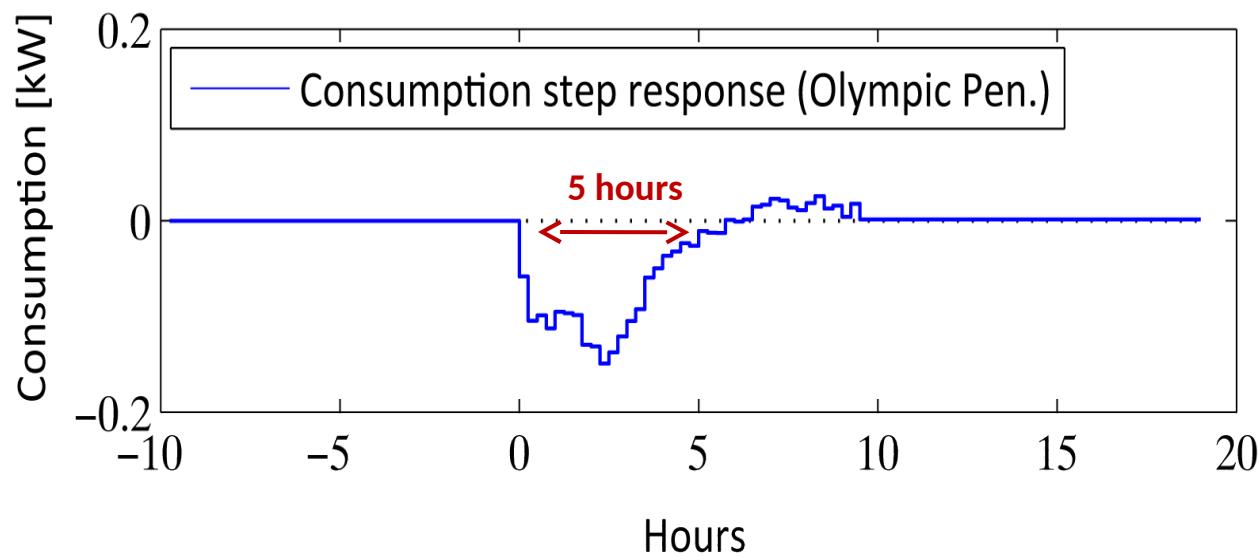
Price-based Control of Power Consumption (Peak Shaving)



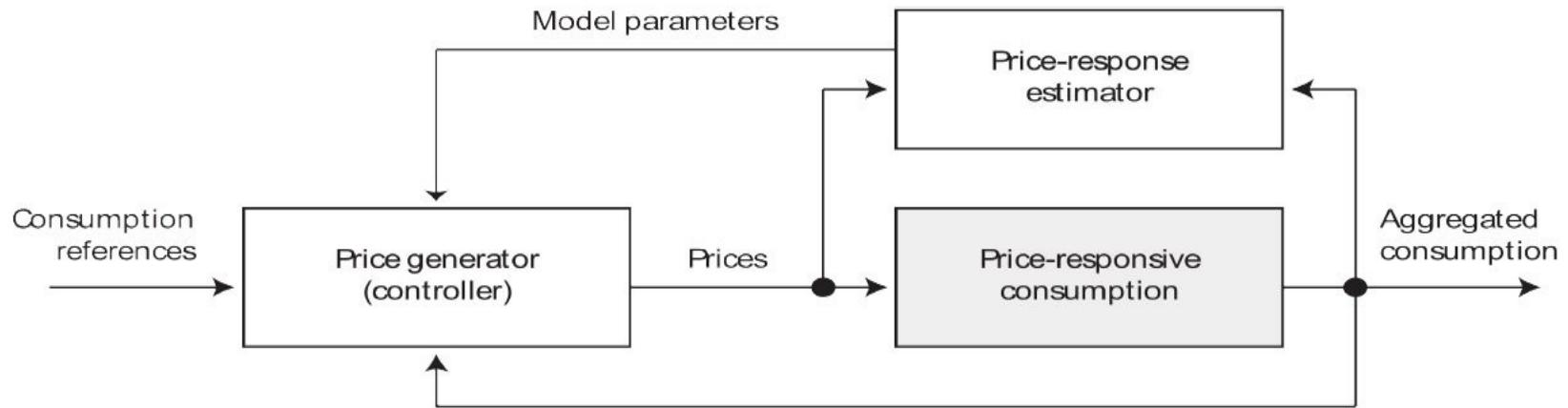
Aggregation (over 20 houses)



Response on Price Step Change

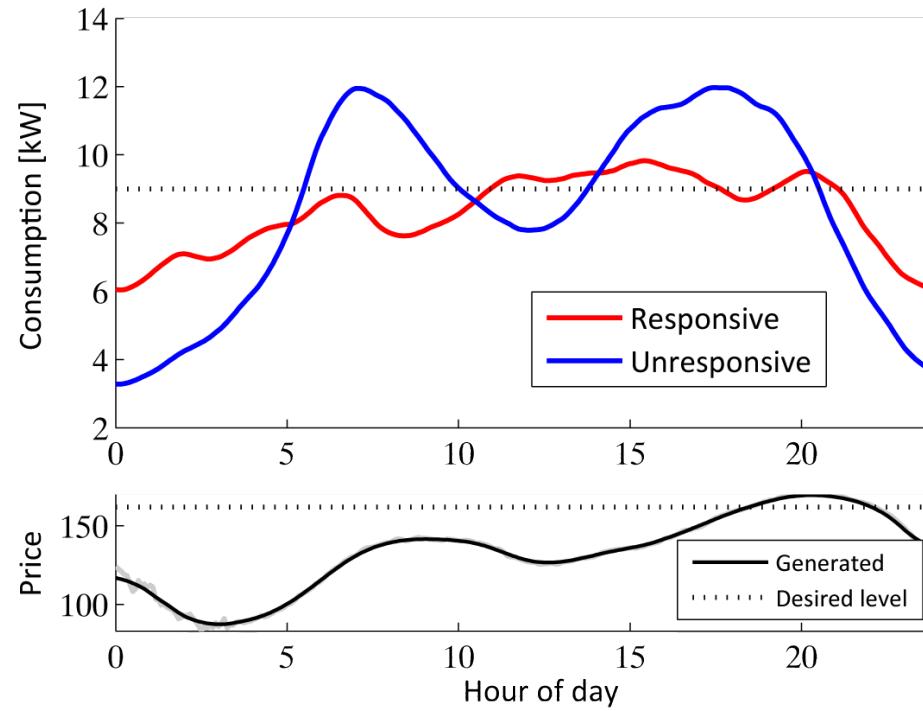


Control of Power Consumption



Control performance

Considerable reduction in peak consumption



Flexibility Function

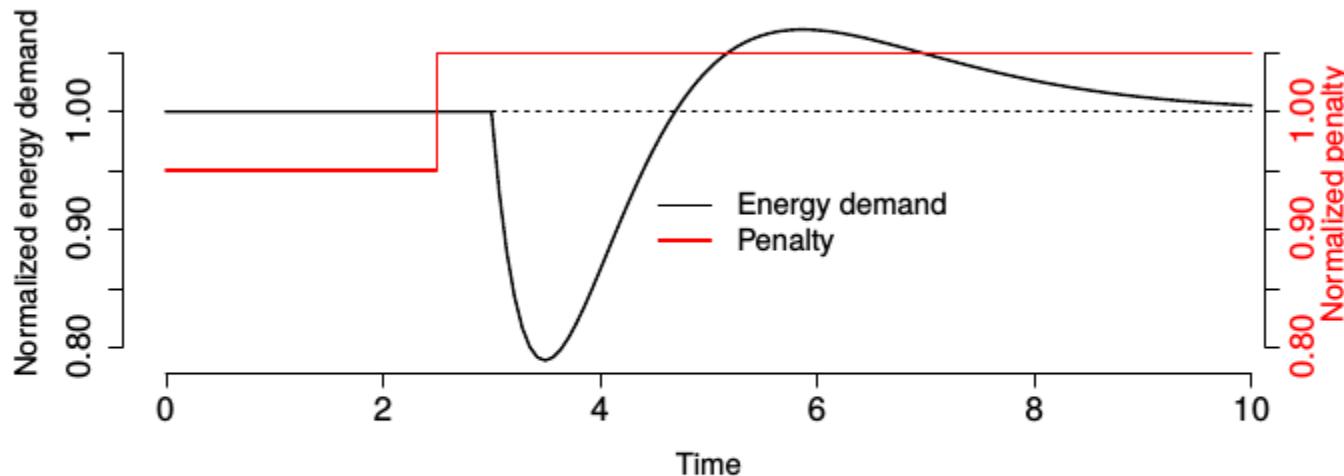
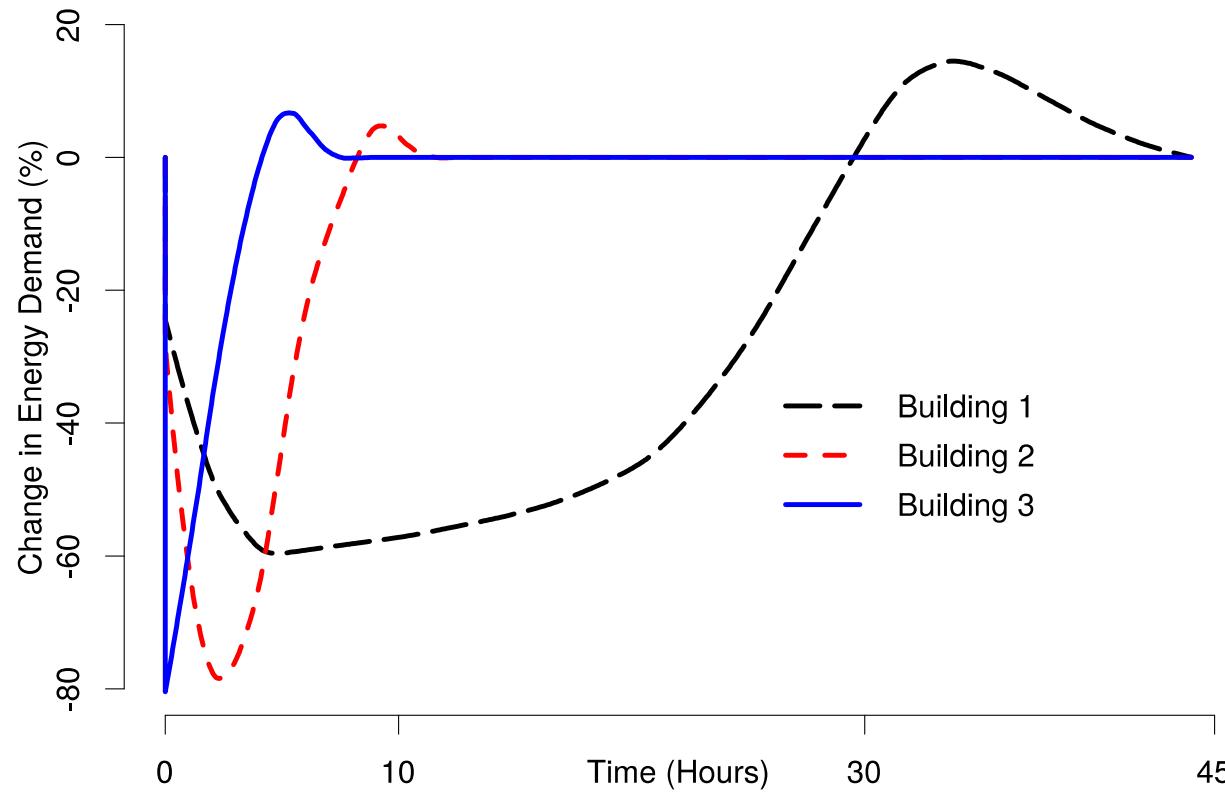


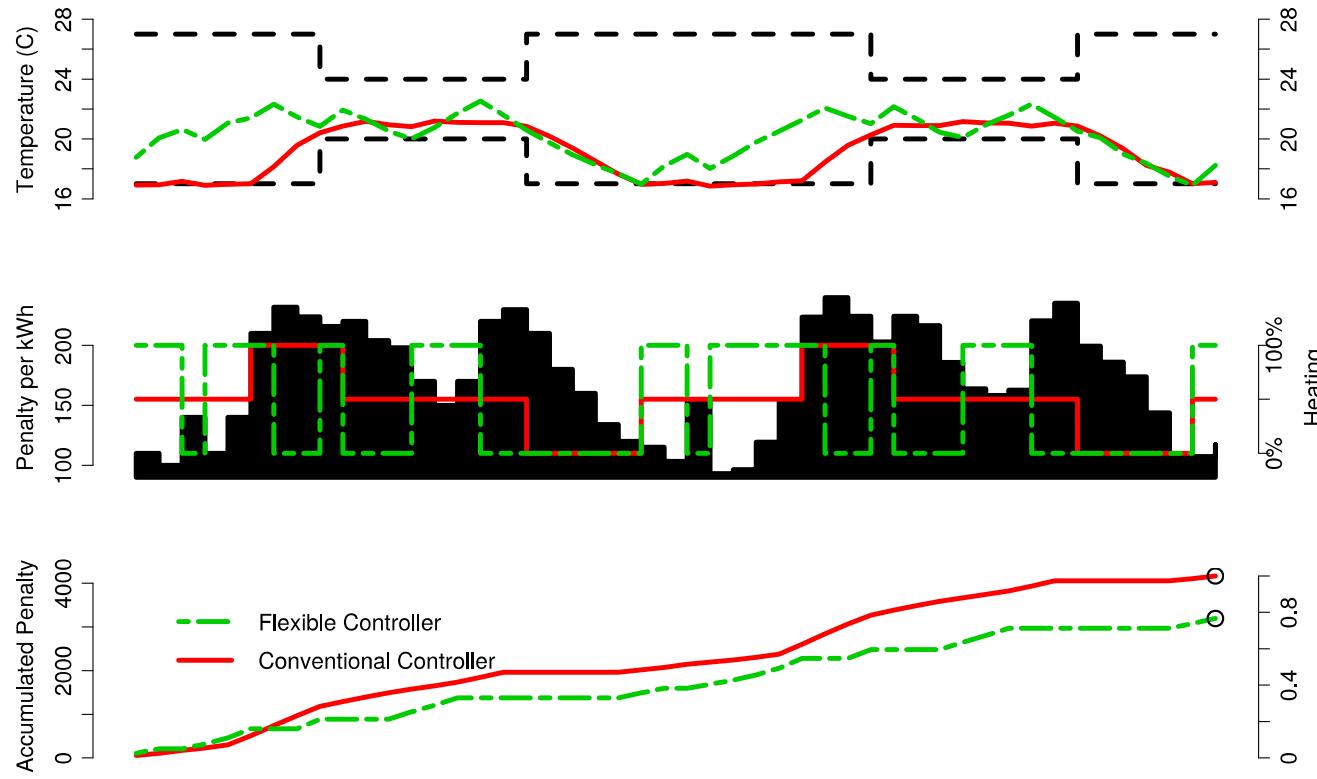
Figure 2: The energy consumption before and after an increase in penalty. The red line shows the normalized penalty while the black line shows the normalized energy consumption. The time scale could be very short with the units being seconds or longer with units of hours. At time 2.5 the penalty is increased,

Examples of Flexibility Functions



Flexibility Index

(Penalty based control setup)



Penalty Function (examples)

- **Real time CO₂.** If the real time (marginal) CO₂ emission related to the actual electricity production is used as penalty, then, a smart building will minimize the total carbon emission related to the power consumption. Hence, the building will be *emission efficient*.
- **Real time price.** If a real time price is used as penalty, the objective is obviously to minimize the total cost. Hence, the building is *cost efficient*.
- **Constant.** If a constant penalty is used, then, the controllers would simply minimize the total energy consumption. The smart building is, then, *energy efficient*.

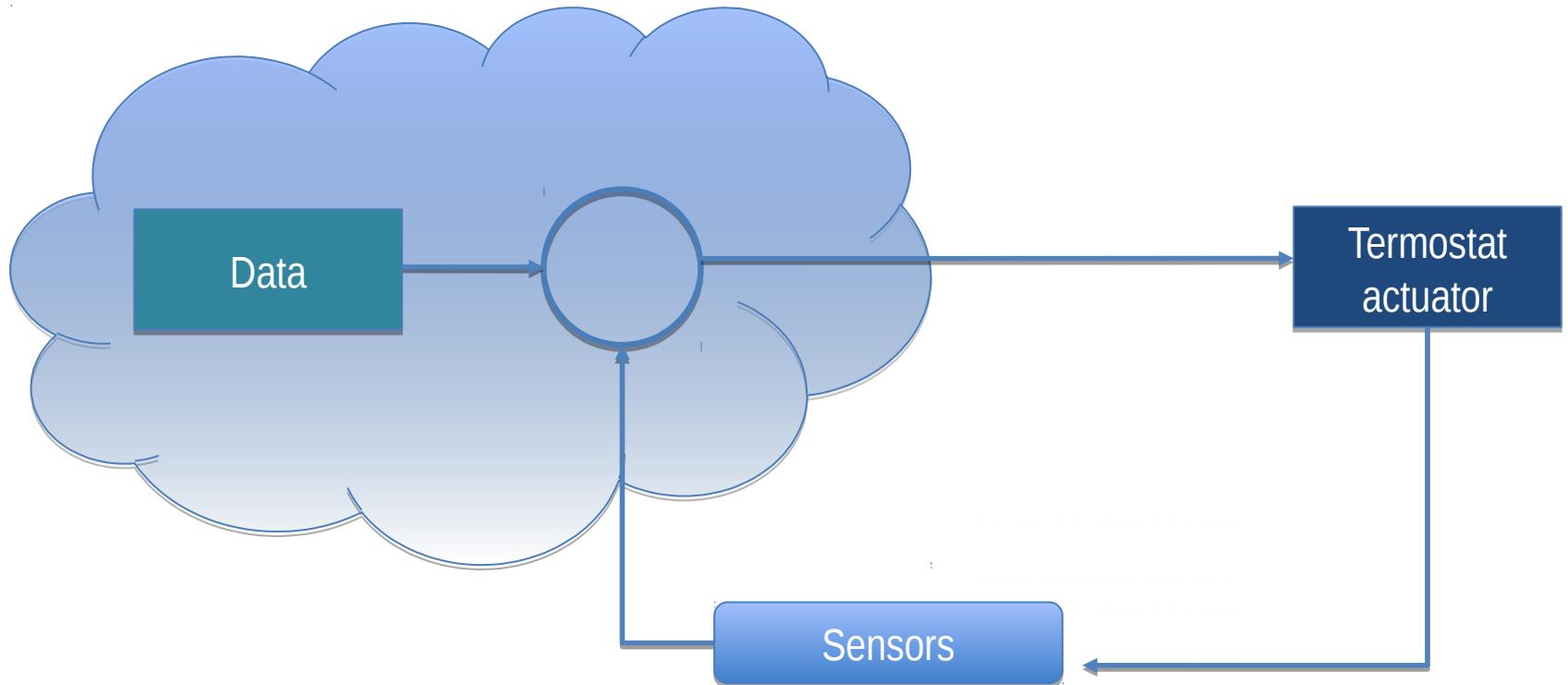
Case study (Level IV – Indirect Control)

Control of HVAC Systems (based on varying prices from Level III)

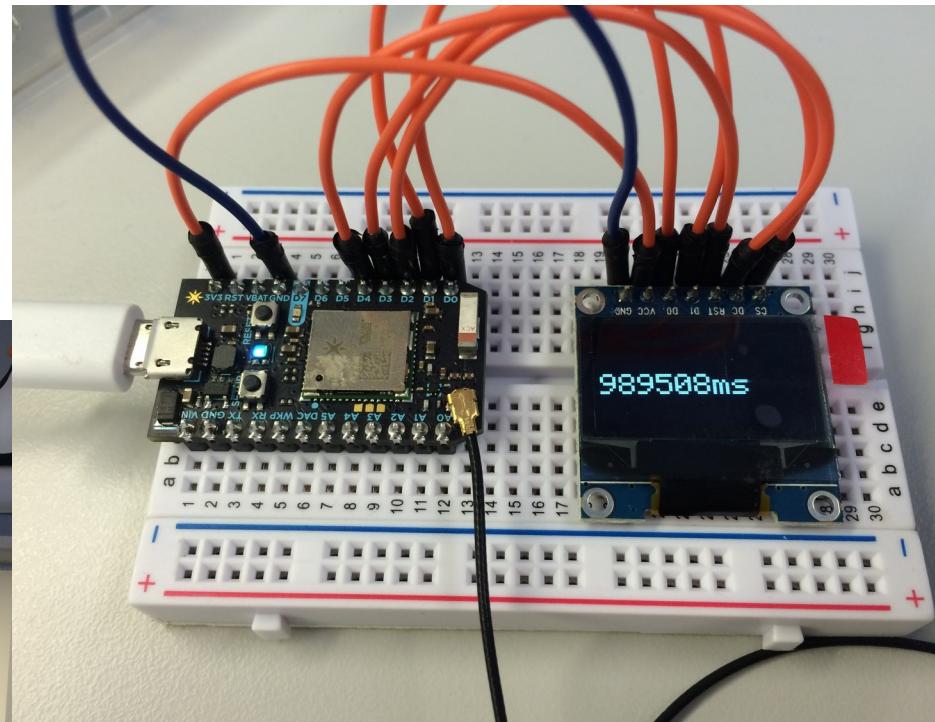
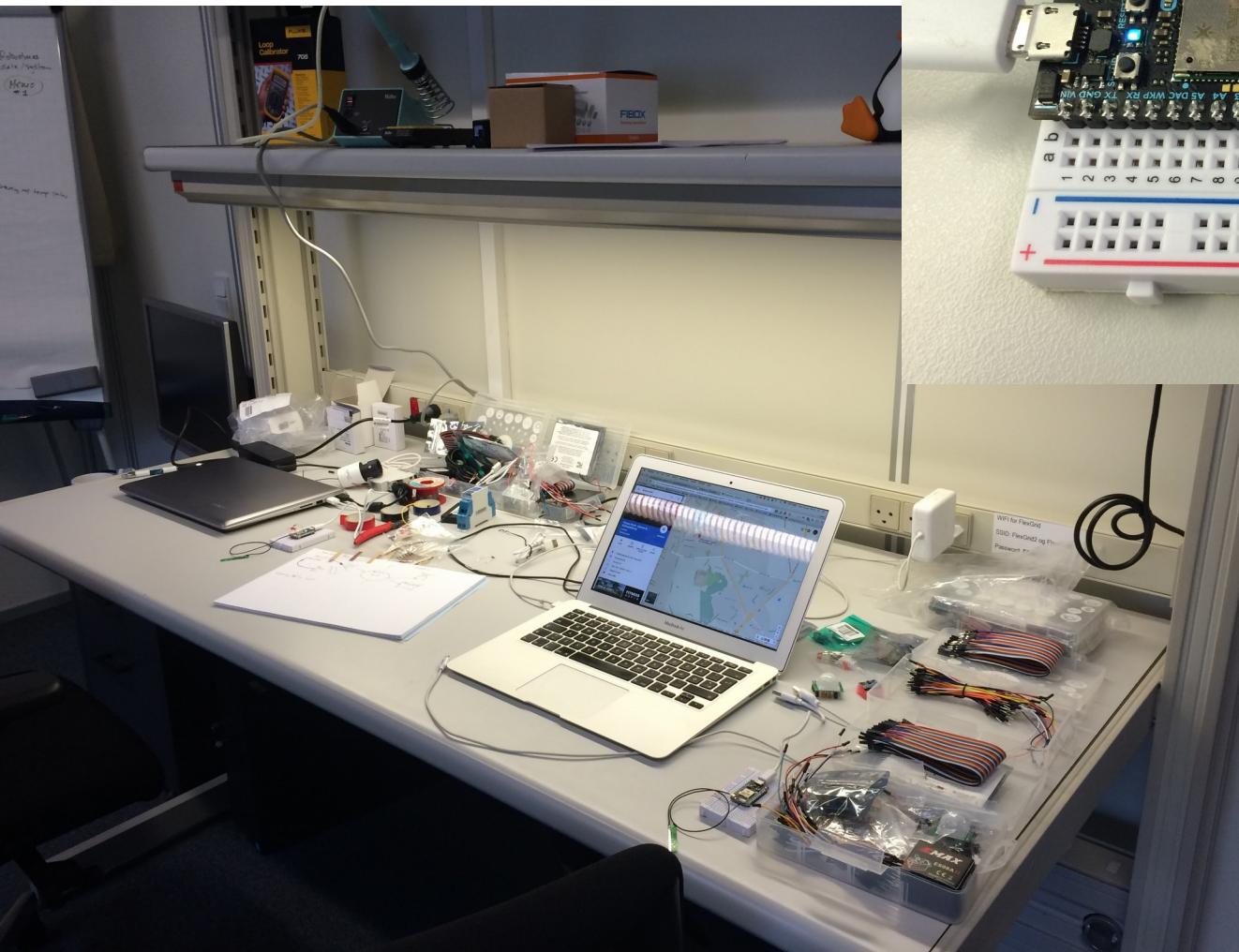


SE-OS – Low level controllers

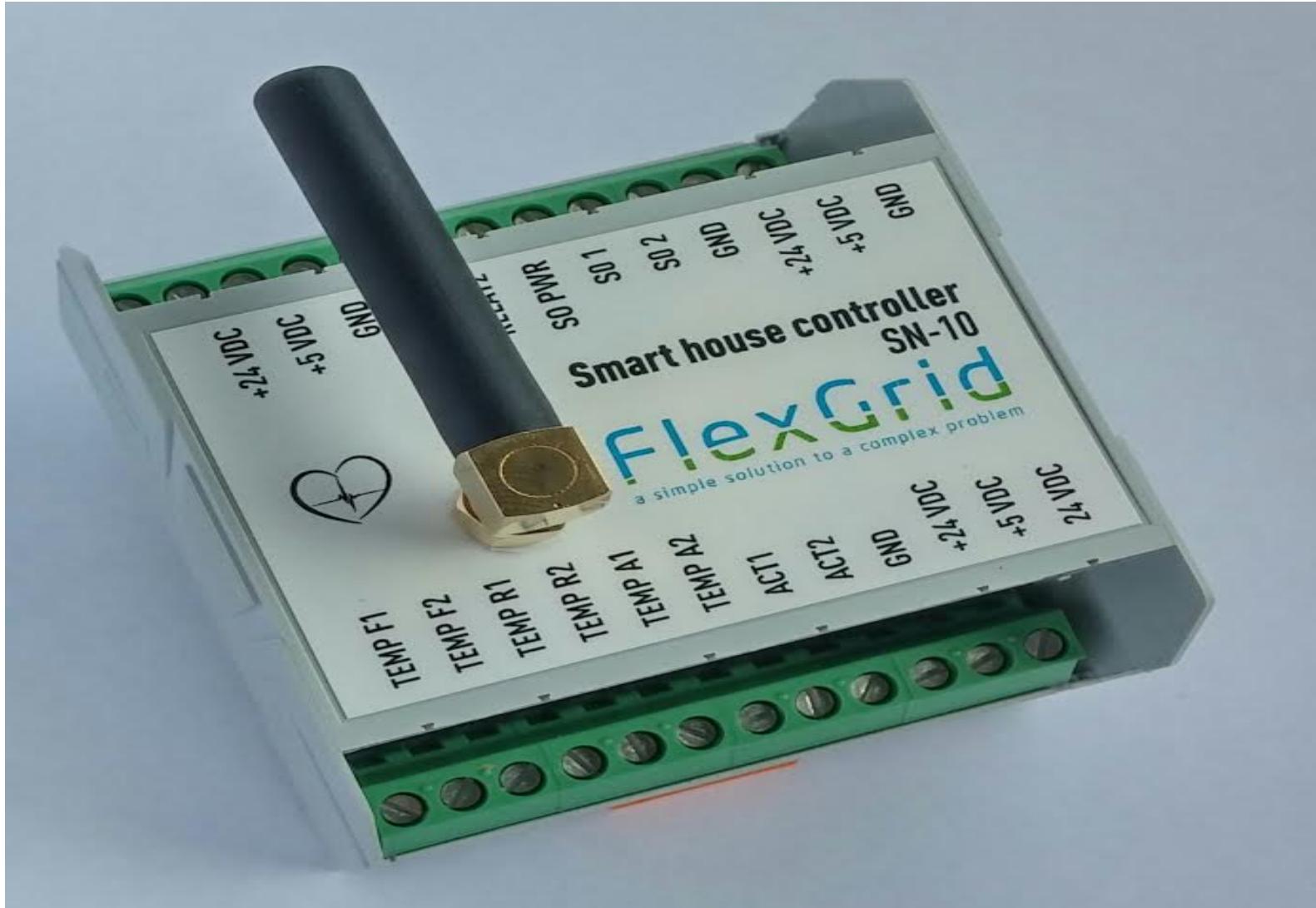
Control loop design – **logical drawing**



Lab testing



SN-10 Smart House Prototype



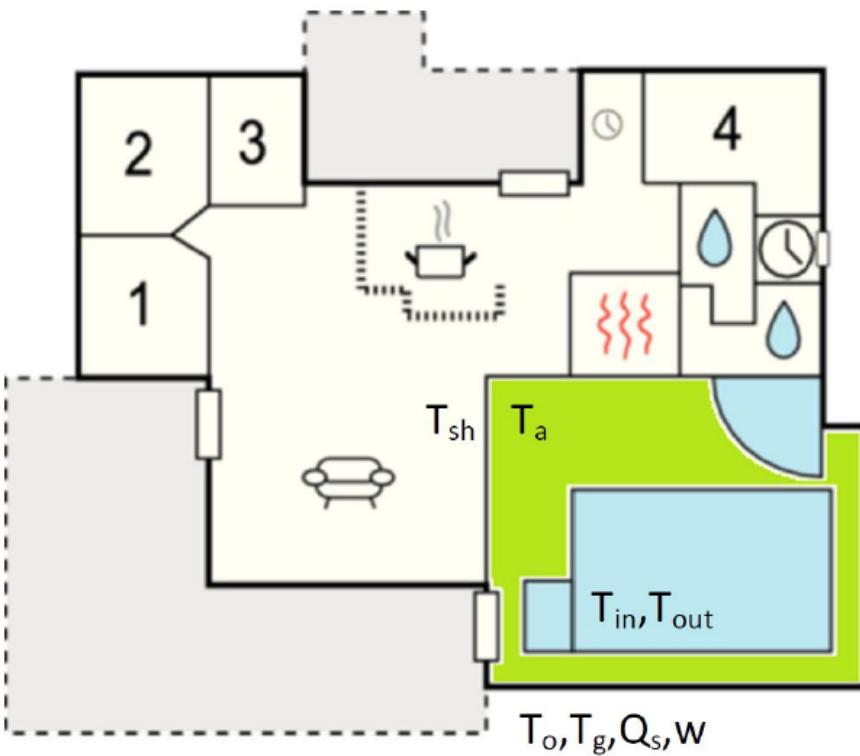
Case study

Control of heat pumps (Energy or/and CO₂ efficient control)



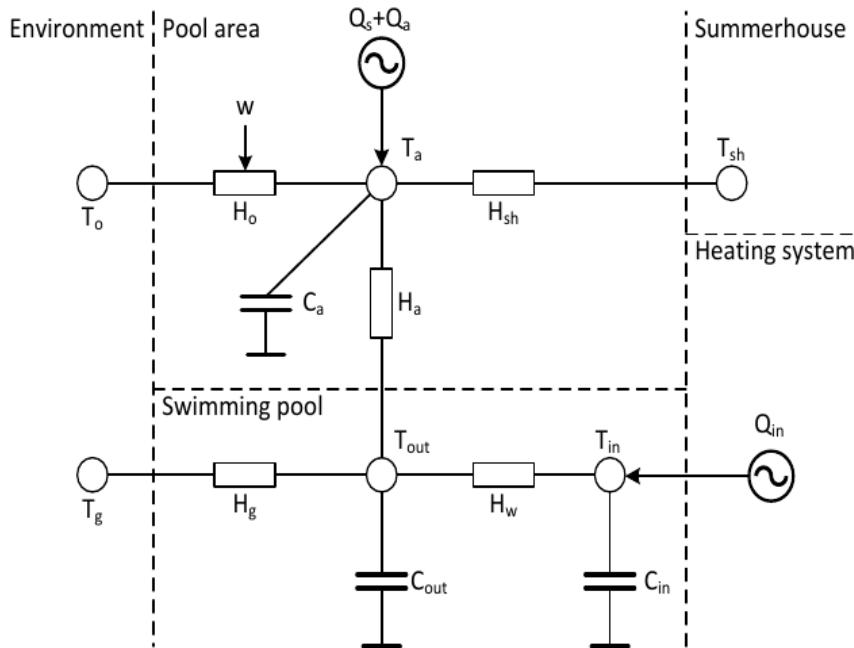


The considered house



- T_{sh} – summerhouse temperature
- T_a – temperature of air in the pool area
- T_{in} – water temperature into the swimming pool
- T_{out} – water temperature out of the swimming pool (controlled)
- T_o – outdoor temperature
- T_g – ground temperature
- Q_s – solar heat gain
- w – wind speed

Grey-box model (lumped parameter model)



- Based on equivalent thermal parameters model

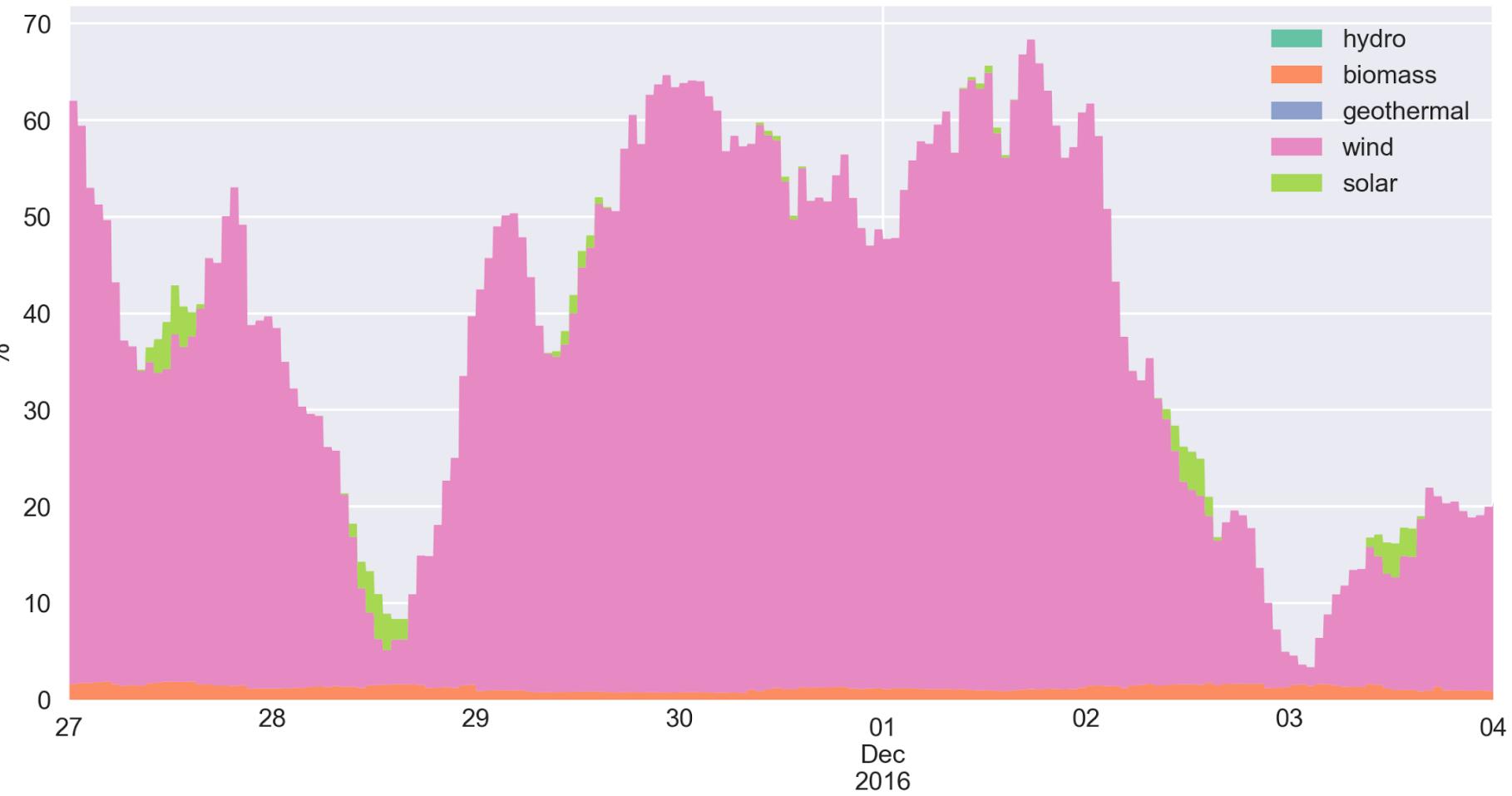
- Dynamics:

$$\frac{dT_{in}}{dt} = \frac{1}{C_{in}} [H_w(T_{out} - T_{in}) + Q_{in}]$$

$$\frac{dT_{out}}{dt} = \frac{1}{C_{out}} [H_w(T_{in} - T_{out}) + H_g(T_g - T_{out}) + H_a(T_a - T_{out})]$$

$$\frac{dT_a}{dt} = \frac{1}{C_a} [H_o(w)(T_0 - T_a) + H_a(T_{out} - T_a) + H_{sh}(T_{sh} - T_a) + Q_s + Q_a]$$

Share of electricity originating from renewables in Denmark Late Nov 2016 - Start Dec 2016

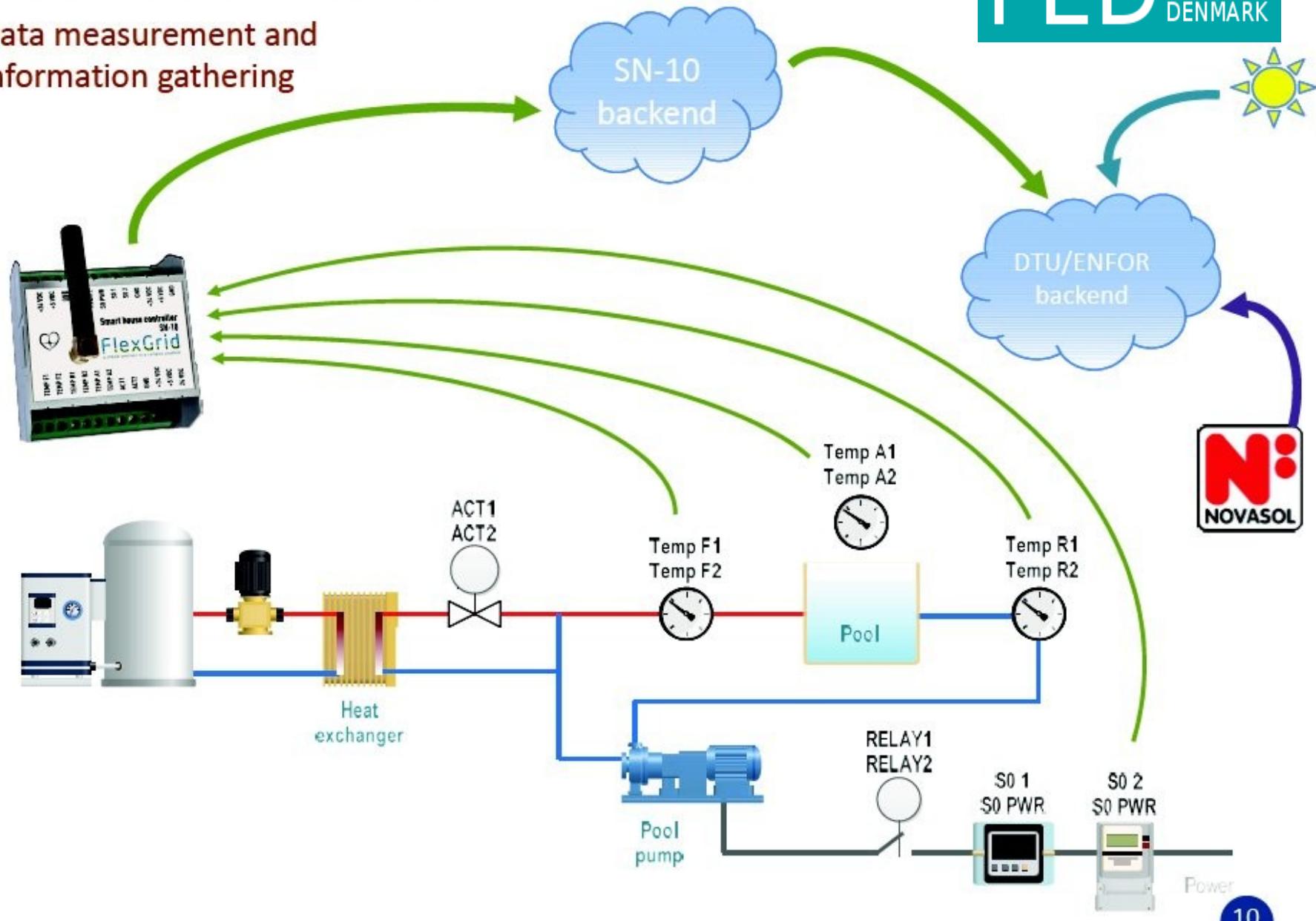


Source: pro.electricitymap.org

How does it work?

Data measurement and information gathering

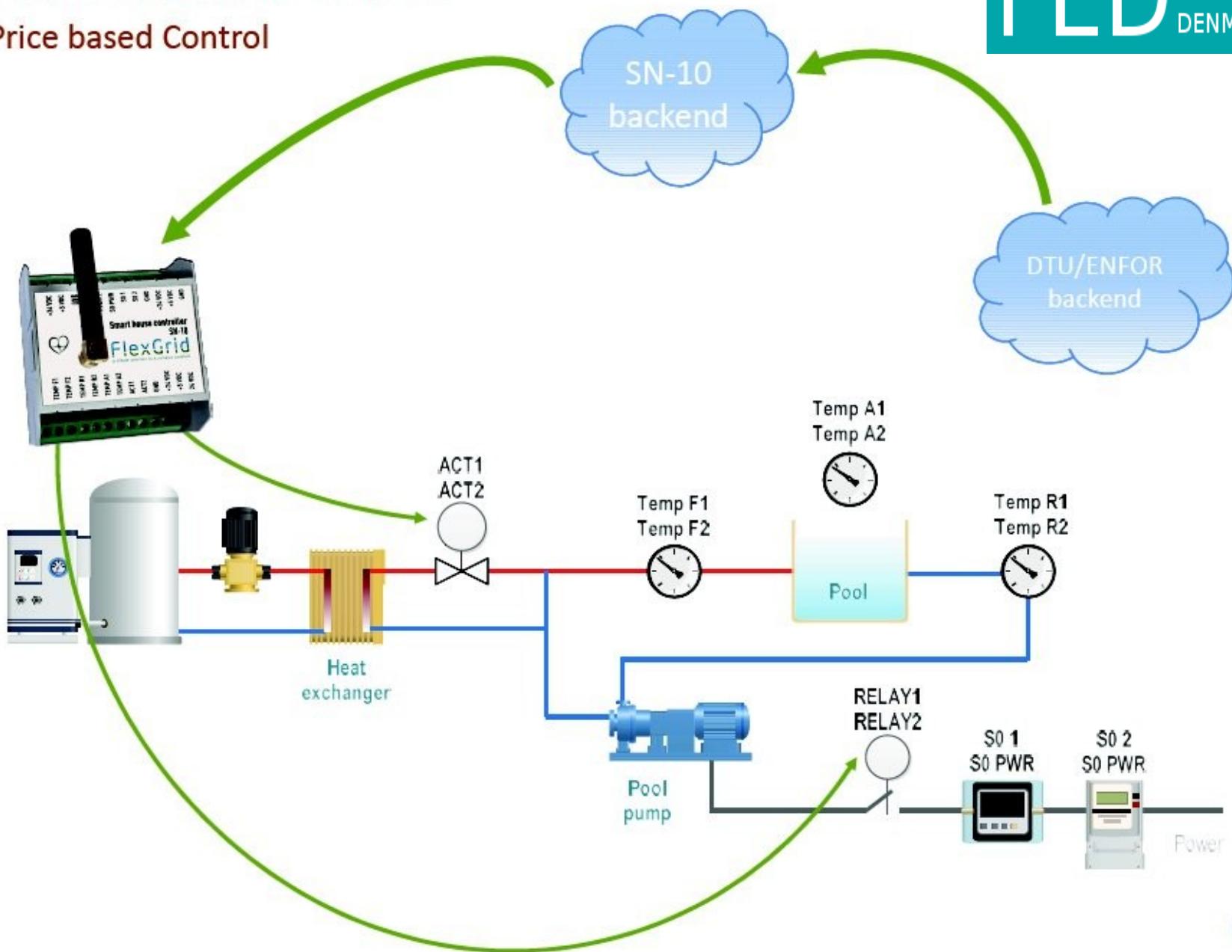
FED FLEXIBLE ENERGY DENMARK



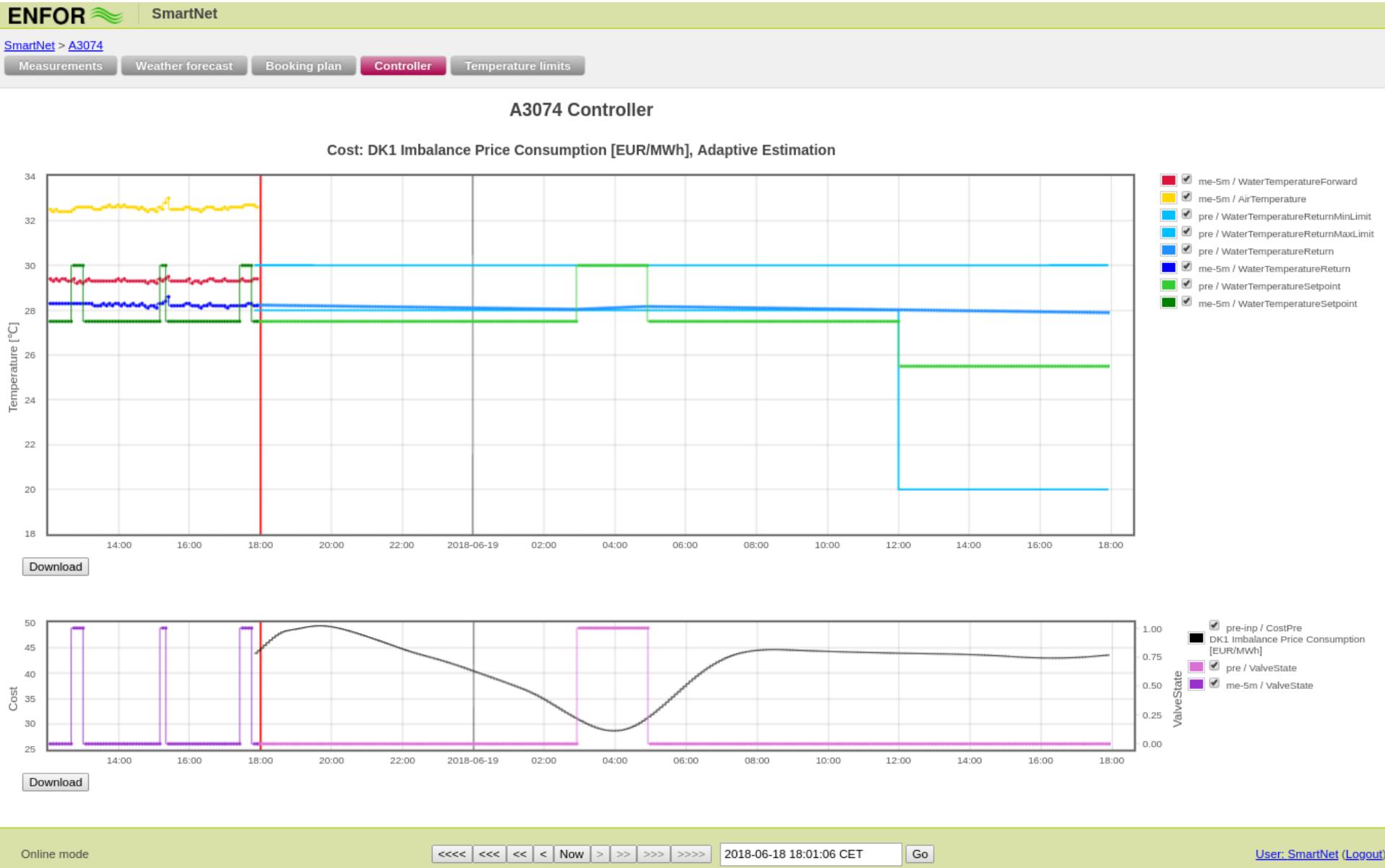
How does it work?

Price based Control

FED FLEXIBLE ENERGY DENMARK



Example: Price-based control (using embedded forecasts)



Example: CO2-based control (using embedded forecasts) (10-15 pct savings in CO2 emission)

ENFOR  SmartNet

[SmartNet > D7811](#)

Measurements

Weather forecast

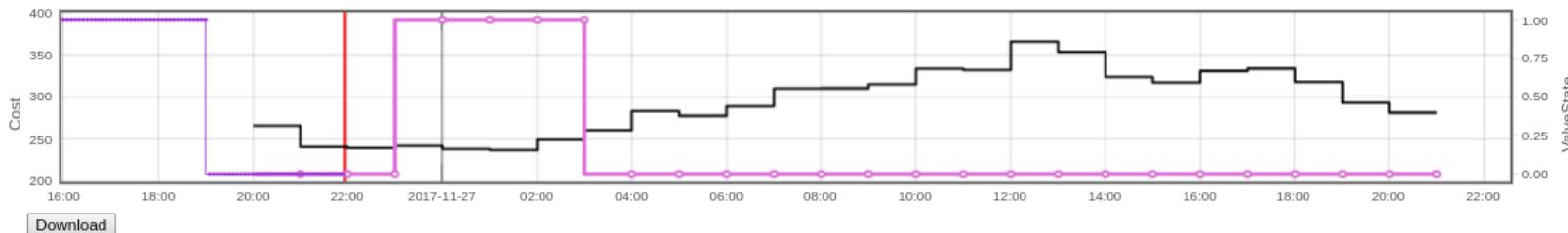
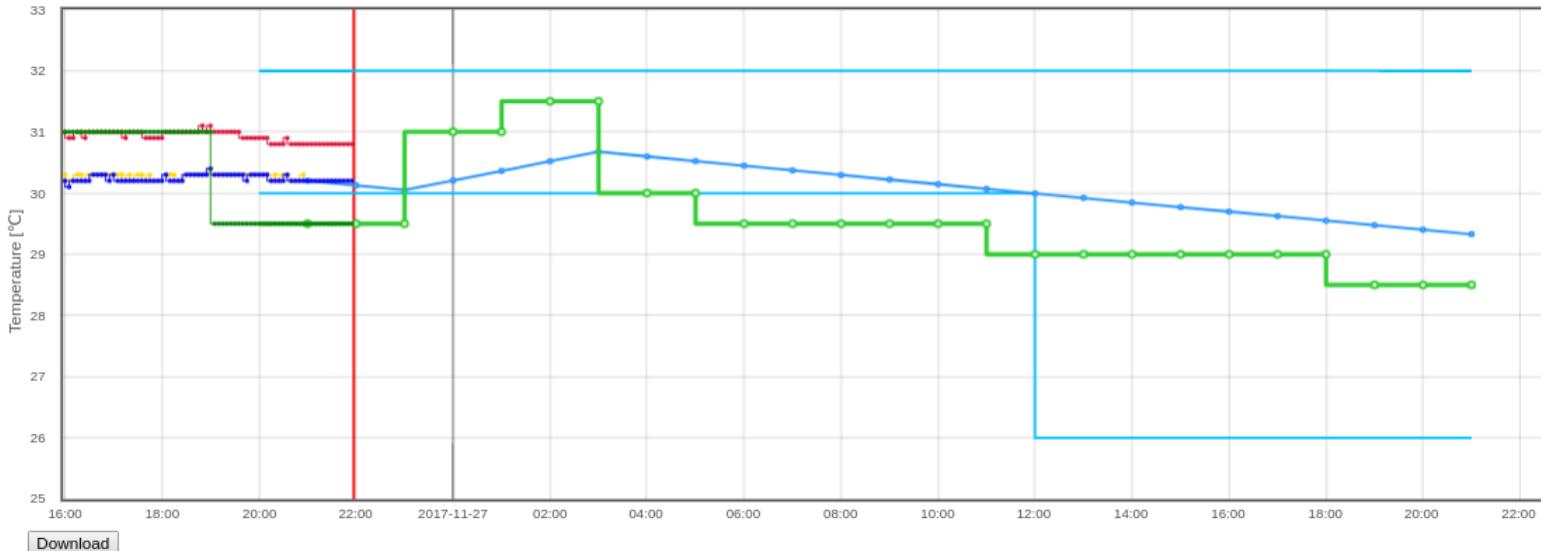
Booking plan

Controller

Temperature limits

D7811 Controller

Cost: co2intensity [g/kWh]



Integrated Forecasting and Control for Smart Buildings



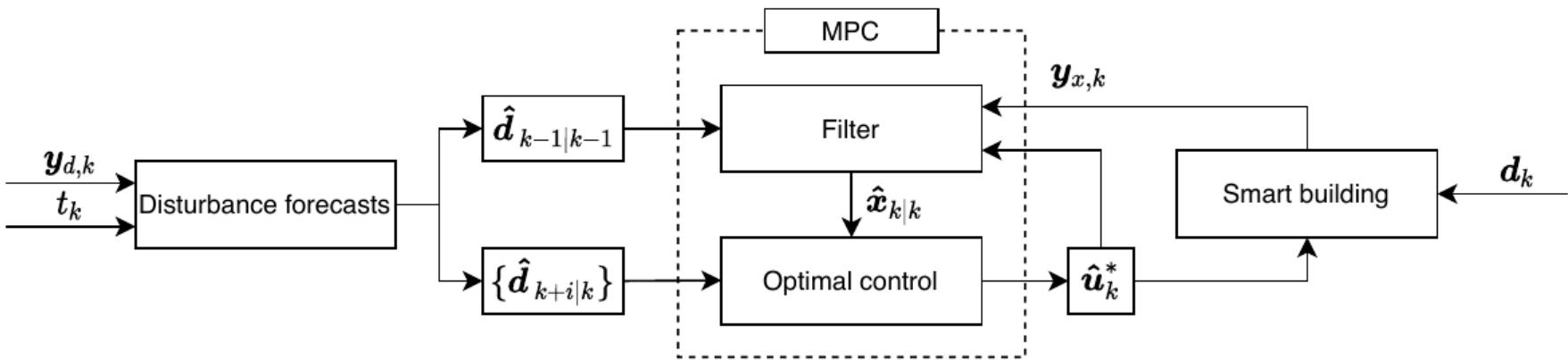
Grey-box model for Forecasting

(Cloud cover, solar radiation, ambient air temperature)

$$\begin{aligned}
 & \text{Disturbance model} \quad \left\{ \begin{array}{l} dZ_\kappa = f_\psi(Z_\kappa)dt + \sigma_\psi d\omega_\kappa \\ \kappa = \psi^{-1}(Z_\kappa) \\ \phi = I_N(\kappa, t) + I_D(\kappa, t) \\ R_n = R_n(\kappa, \phi, t) \\ dT_s = f_{T_s}(T_l, T_s)dt + \sigma_s d\omega_s \\ dT_l = f_{T_l}(T_l, T_s, R_n)dt + \sigma_l d\omega_a \\ \mathbf{d} = [T_a, \phi]^T \end{array} \right. \\
 & \text{Observation equation} \quad \left\{ \begin{array}{l} d_\phi = \phi + v_\phi, \quad v_\phi \sim N_{iid}(0, R_\phi) \\ d_{T_a} = T_l + v_{T_a}, \quad v_{T_a} \sim N_{iid}(0, R_{T_a}) \\ \mathbf{y}_d = [d_{T_a}, d_\phi]^T, \end{array} \right. \\
 & \qquad \qquad \qquad (13)
 \end{aligned}$$

Integrated Forecasting and Control

The MPC framework for smart house control and how disturbance forecasts are incorporated



$$\begin{aligned} d\mathbf{x}(t) &= f_s(\mathbf{x}(t), \mathbf{u}(t), \mathbf{d}(t))dt \\ &\quad + g_s(\mathbf{x}(t), \mathbf{u}(t), \mathbf{d}(t))d\boldsymbol{\omega}_s(t), \end{aligned} \quad (1a)$$

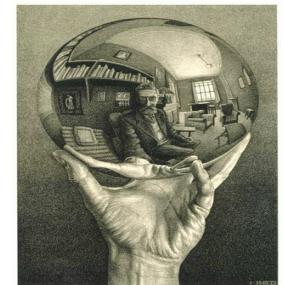
$$d\mathbf{d}(t) = f_d(\mathbf{d}(t))dt + g_d(\mathbf{d}(t))d\boldsymbol{\omega}_d(t), \quad (1b)$$

$$\mathbf{y}_s(t_k) = h_s(\mathbf{x}(t_k)) + \mathbf{v}_{s,k}, \quad (1c)$$

$$\mathbf{y}_d(t_k) = h_d(\mathbf{d}(t_k)) + \mathbf{v}_{d,k}, \quad (1d)$$

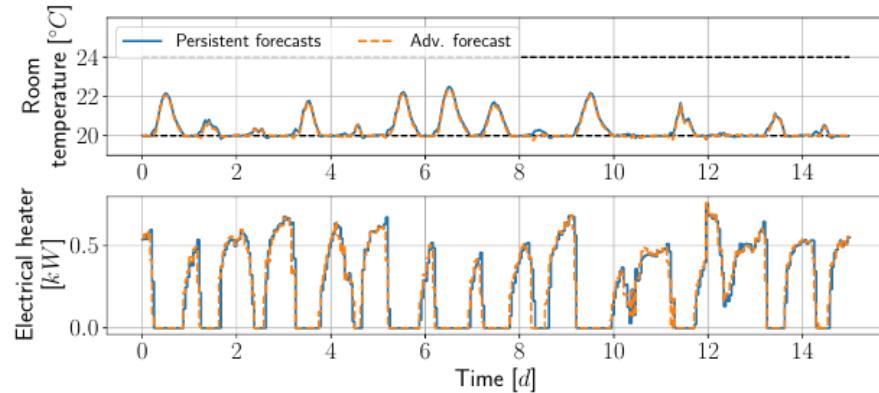
Heating strategies

- Strategy No. 1: Electrical heaters
- Strategy No. 2: Heat pump
- Strategy No. 3: Heat pump and electrical heaters
- Strategy No. 4: Heat pump plus electrical heaters and cooling

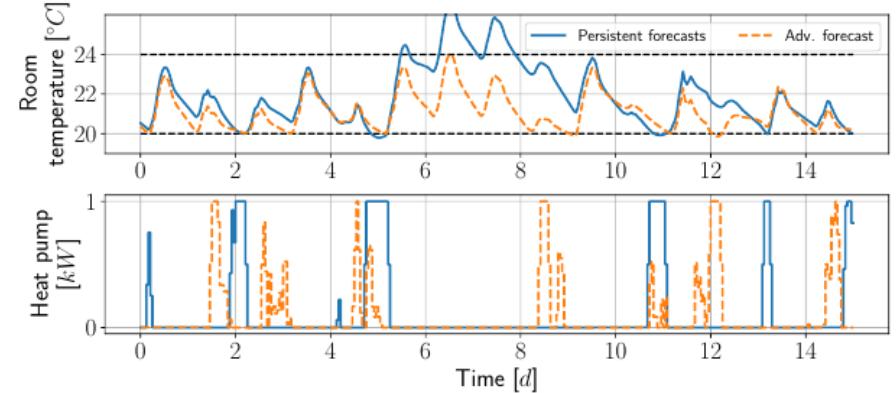


15 days out of 7 months simulation

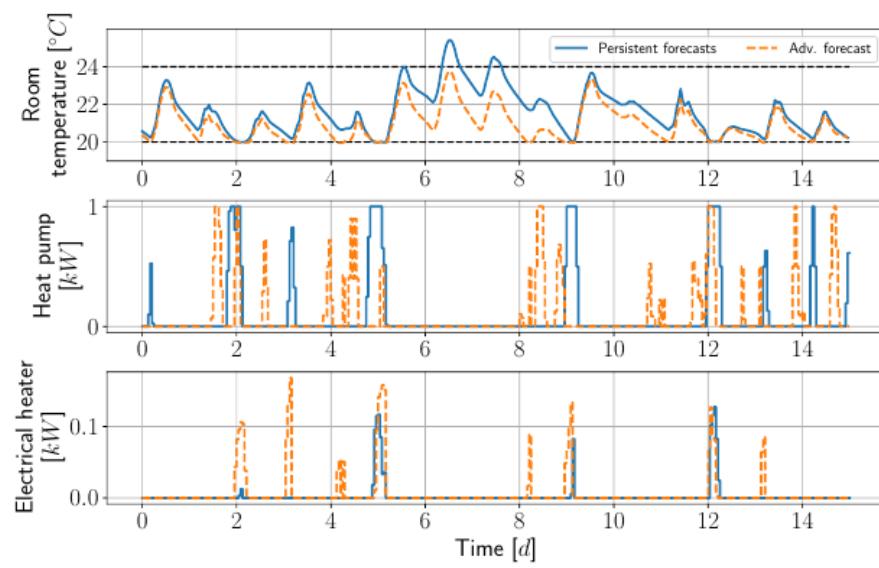
Strategy 1: Electrical Heaters



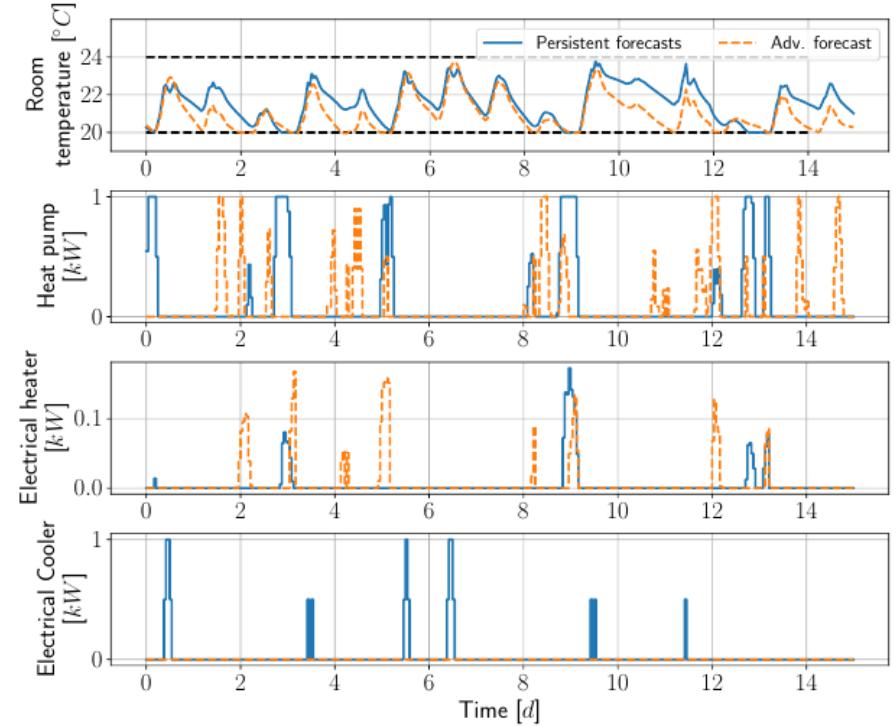
Strategy 2: Heat Pump



Strategy 3: Heat Pump & Electrical Heaters



Strategy 4: Heat Pump & Electrical Heaters & Coolers



Electricity cost in EUR

Electricity cost of the simulations

Heating strategy	Persistent	Advanced disturbances	Perfect
Electrical heaters, u_1	303.2	302.2	302.0
Heat pump, u_2	117.3	110.4	107.7
Heat pump plus electrical heaters, u_3	113.0	108.2	107.5
Heat pump plus electrical heaters and coolers, u_4	117.9	108.3	107.5

Constraint violations

Constraint violation of the control simulations

Heating strategy	Persistent	Advanced disturbances	Perfect
Electrical heaters, u_1	48.5	39.6	25.1
Heat pump, u_2	157.9	12.3	1.7
Heat pump plus electrical heaters, u_3	48.0	6.7	1.2
Heat pump plus electrical heaters and coolers, u_4	4.4	2.4	0

Summary

- We have demonstrated how to use grey-box models for integrated forecasting and control for smart buildings
- We have suggested the use of Flexibility Functions (and Flexibility Indexes)
- We have described the hierarchy of Smart-Energy OS Controllers with embedded aggregation, modelling, and forecasting
- The Smart-Energy OS can focus eg. on
 - ★ Peak Shaving
 - ★ Smart Grid demand (like ancillary services needs, ...)
 - ★ Energy Efficiency
 - ★ Cost Minimization
 - ★ Emission Efficiency
- Center Denmark is established as a National Digitalization Hub for Smart Energy and related systems (eg. water). Main purpose is to unlock the flexibility needed for the green transition

For more information ...

See for instance

www.smart-cities-centre.org

...or contact

- Henrik Madsen (DTU Compute)
hmad@dtu.dk

Acknowledgement:

Innovation Fund Denmark (DSF 1305-00027B) and EU H2020 (No. 691405)

Center Denmark - Control Room



Some 'randomly picked' books on modeling and renewable integration

