

ROUTING

make evil go away.

verse 1

there is a world
that is virtual and different
it can be so cold
makes us stand up for what's right
our hope through our life
if we reset it to the start

verse 3

we'll do our best
to never let you down
we're up to the test
to turn this world around

mini-chorus ...

chorus

here we are, going far
to save all that we love
if we give, all we've got
we will make it through
here we are, like a star
shining bright on your world
today (make evil go away)
code lyoko we'll, reset it all

mini-chorus ...

mini-chorus

code lyoko be there when you call
code lyoko eve, will stand real tall
code lyoko stronger after all

by Noam Kaniel (vocals)

written by

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Franck Keller

verse 2

a world of machines
it can shadow human nature
all that we need
is the way to find the answer
and one thing is for sure
you can count on us for good.

A WORLD WITHOUT DANGER

CODE LYOKO (June 6, 2004)

chorus ...

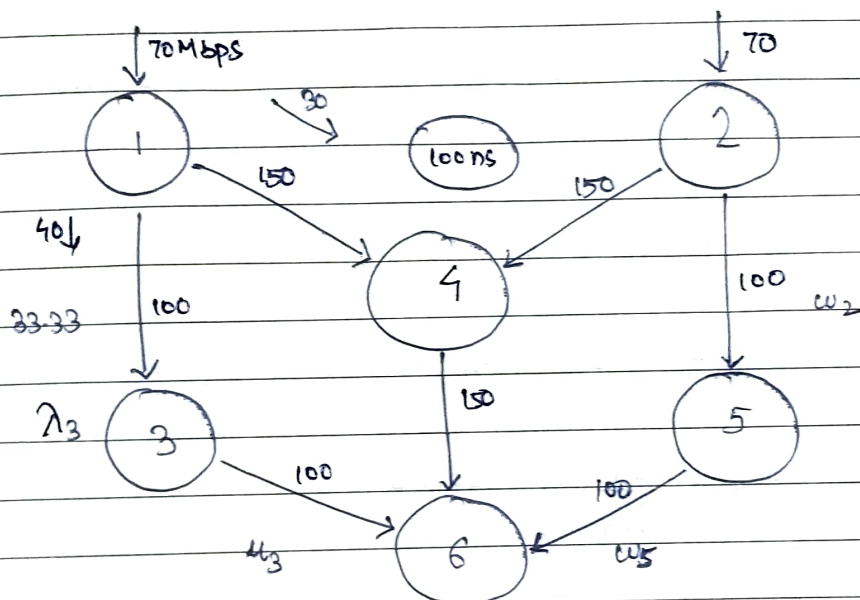
RECAP

$M/M/m$
 $M/M/m/m$
 $M/G/1$
 $M/D/1$

} queuing system

$M/M/1$

L, W, W_s, L_q, W_q, L_s tabular summary

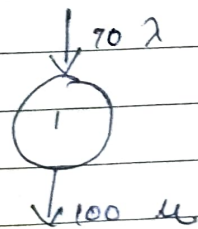


routing 1 1-3-6 & 2-5-6
 2 1-4-6 & 2-4-6
 2

routing 1

$$\rho = \frac{70}{100} = 0.7$$

w_1 : delay from 1 \rightarrow 3



$$w_1 = \frac{L_1}{\lambda_1} = \frac{\rho_1}{\lambda_1(1-\rho_1)} = \frac{7}{3 \times 70 \times 10^6} = \frac{10^{-6}}{30} = \frac{100}{3} \text{ ns} = 33.3 \text{ ns}$$

$$\lambda_3 = 70 \times 10^6$$

$$\rho_3 =$$

$$w_3 = 33.33 \text{ ns}$$

$$w_2 = w_5 = 33.33 \text{ ns}$$

routing 2

1-4-6

2-4-6

$$\lambda_1 = 70$$

$$\mu_1 = 150$$

$$\rho_1 = \frac{70}{150}$$

$$1-4 \quad w_1 = \frac{L_1}{\lambda_1} = \frac{70}{70 (80) \times 10^6} = 12.5 \text{ ns}$$

$$2-4 \quad w_2 = 12.5 \text{ ns}$$

4-6

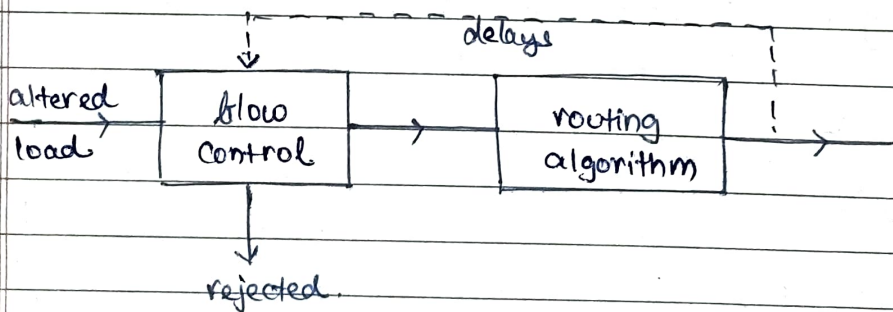
$$\lambda_4 = 140$$

$$\mu_4 = 150$$

$$\rho_4 = \frac{140}{150}$$

$$w_4 = \frac{L_4}{\lambda_4} = 100 \text{ ns}$$

$$\text{Net delay } w_1 + w_4 \text{ or } w_2 + w_4 = \underline{112.5 \text{ ns}}$$

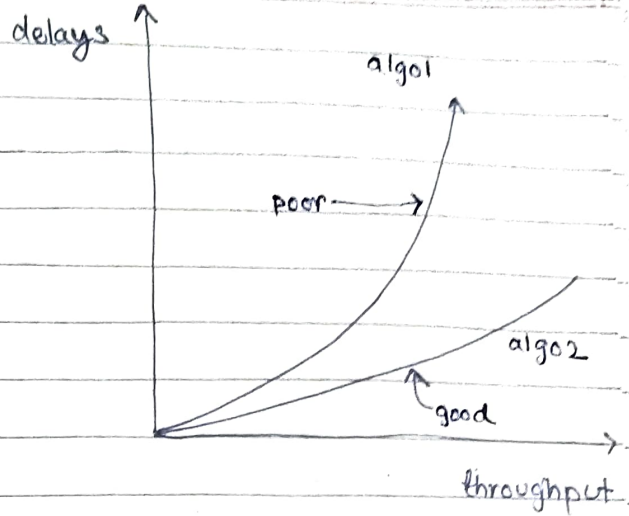


$$\underline{\text{throughput} = \text{offered load} - \text{rejected load}}$$

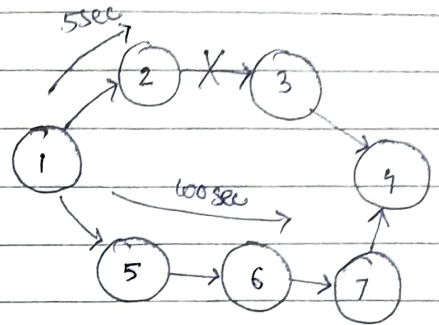
ROUTING

ensure delays are minimized
maximize throughputs

routing $\begin{cases} \text{protocols} \\ \text{algorithms} \end{cases}$



- (i) static vs. dynamic
- (ii) flat vs. hierarchical
- (iii) ~~flat~~ intra-domain vs. inter-domain
- (iv) distributed vs. centralized
- (v) single vs. multipath
- (vi) link state vs. distance vector



need to know whole network (bellman-ford, dijkstra)

ROUTING ALGORITHMS

DIJKSTRA

(Shortest-path algorithms)

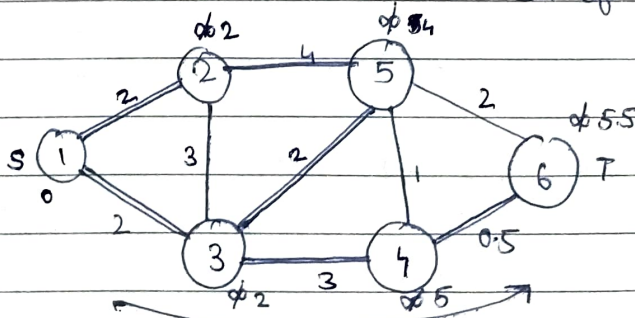
$$G = (V, E)$$

V set of vertices

E set of edges

- (i) dijkstra
- (ii) bellman-ford
- (iii) Floyd-warshall

$$s = \{1\}$$



every step we add 1 node to our shortest path tree

$$S = \{1\}$$

$$\text{initialization } D_1 = 0 \quad D_j = d_{ji} \quad \forall j \neq 1$$

$$P = \{1\}$$

ALGORITHM

$$\textcircled{1} \quad D_i = \min_{j \notin P} D_j \quad i \notin P$$

$$P = P \cup \{i\}$$

$$\textcircled{2} \quad D_j = \min \{D_j, D_i + d_{ij}\} \quad \forall j \notin P$$

2 + 3

goto $\textcircled{1}$ until $P = G$

$$\text{initialization } D_1 = 0 \quad D_2 = 2 \quad D_3 = 2 \quad D_4 = \infty \quad D_5 = \infty \quad D_6 = \infty$$

$$P = \{1\}$$

$$\textcircled{1} \quad P = \{1, 2\}$$

$$D_2 = 2, \quad D_3 = 2 \quad D_4 = \infty \quad D_5 = 6 \quad D_6 = \infty$$

$$\textcircled{2} \quad P = \{1, 2, 3\}$$

$$D_2 = 2 \quad D_3 = 2 \quad \underline{D_4 = 5} \quad \underline{D_5 = 4} \quad D_6 = \infty$$

$$\textcircled{3} \quad P = \{1, 2, 3, 5\}$$

$$D_2 = 2 \quad D_3 = 2 \quad D_5 = 4 \quad D_4 = 5 \quad D_6 = 5.5$$

$$\textcircled{4} \quad P = \{1, 2, 3, 4, 5, 6\}$$

done,

running time $|V| = N$

iterations = $N-1$

$O(N)$ in each iteration

$O(N^2) \rightarrow O(N \log N)$ $O(|E| + |V| \log |V|)$

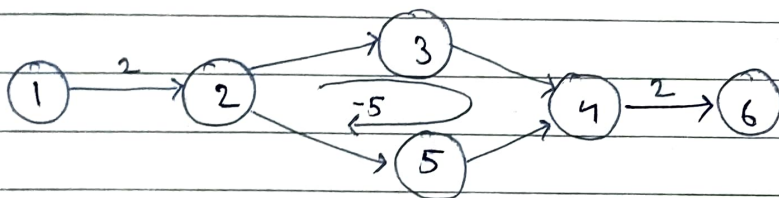
dijkstra disadvantage

(i) -ve edges are not allowed.

BELLMAN-FORD

-ve edges are allowed
but, no -ve wt. cycles.

shortest path is not defined



init. $D_i^0 = 0$ $i = 1 \dots n$

$D_i^0 = \infty$ $\forall i = 2 \dots n$ $i \neq 1$

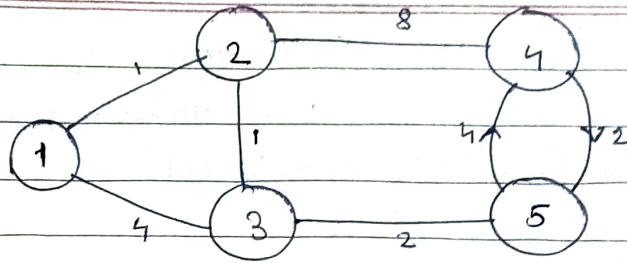
algorithm $D_i^{n+1} = \min \{ d_{ij} + D_j^n \} \quad \forall i \neq 1$

terminate if $D_i^n = D_i^{n-1} \quad \forall i$

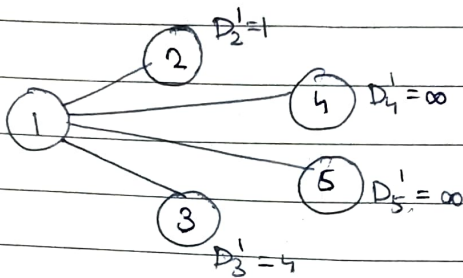
(D_j^n min. cost of reaching j using atmost n edges)

$D_i^{n+1} \leq \min_{j \neq i} \{ d_{ij} + D_j^n, D_i^n \}$

every step, shortest path with n edges to each node is calculated.



$$D_1^1 = 0 \quad D_2^0 = D_3^0 = D_4^0 = D_5^0 = \infty$$



running time

$$O(|V||E|) \quad O(N^3)$$

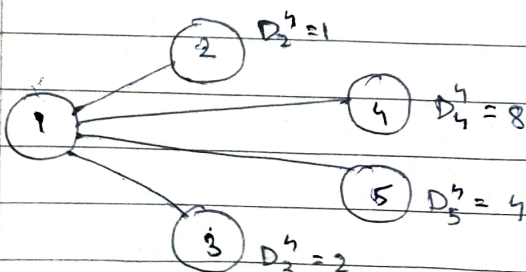
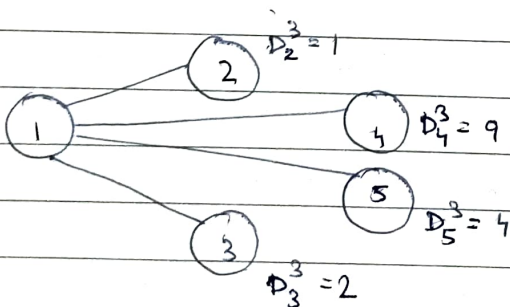
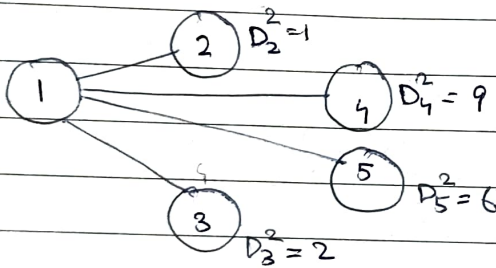
$$|V| = N$$

$$O(m|E|)$$

iteration required.

$$m \ll N$$

$$|E| \ll N^2$$



PROPOSITION

- (a) D_i^h 's are generated by the algorithm are equal to the shortest path from i to l of # edges $\leq h$.
- (b) the algorithm terminates iff all cycles not containing node l are having non-neg. costs. if algo terminates, it so in $h \leq N$ & at termination, D_i^h is the cost of shortest path from i to l (or l to i).

HW $K \leq h$ prove $h+1$

$$D_i^{K+1} \leq D_i^K \quad \forall K \leq h.$$

FLOYD - WARSHALL

(all-pair shortest path)

$$D_{ij}^0 = d_{ij} \quad \forall i, j \quad \text{for } h = 0 \dots N-1$$

$$D_{ij}^{h+1} = \min_k [D_{ij}^h, D_{ik}^h + D_{kj}^h]$$

iteration - h:

We have the shortest path cost from i to j using nodes $1, 2, \dots, h$ ($h=0$, w/o any node)

$$O(N^3) \quad O(|V|^3)$$