## What is Your Estimand?

Defining the Target Quantity Connects Statistical Evidence to Theory



Ian Lundberg

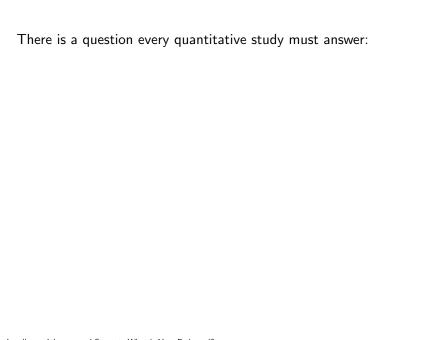
UCLA Sociology ianlundberg.org Rebecca Johnson

Dartmouth Quantitative Social Science rebeccajohnson.io Brandon M. Stewart

Princeton Sociology brandonstewart.org

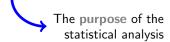
#### 23 September 2021.

Paper in *American Sociological Review*. Preprint on SocArxiv. Replication code on Dataverse. Research reported in this publication was supported by The Eunice Kennedy Shriver National Institute of Child Health & Human Development of the National Institutes of Health under Award Number P2CHD047879



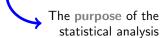
What is your estimand?

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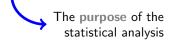
A common answer:



### What is your estimand?

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— We took [data source]



#### What is your estimand?

A common answer:

- We took [data source]
- We estimated  $\beta_1$

$$Y = \beta_0 + X_1 \beta_1 + X_2 \beta_2 + \epsilon$$



The purpose of the statistical analysis

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 $\beta_1$  is an estimand that assumes a model

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What if the model is wrong?

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The purpose of the statistical analysis

What if the model is wrong?

The model is an approximation

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Is it a good approximation?

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Epistemological crisis

### What is your estimand?

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**\** 

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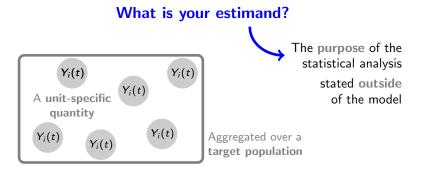


A unit-specific quantity

### What is your estimand?

 $Y_i(t)$ 

A unit-specific quantity

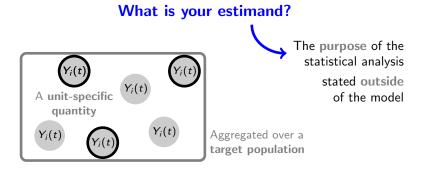


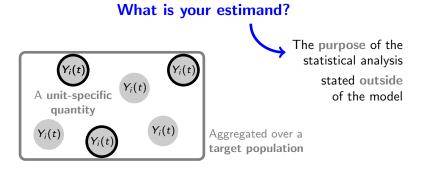


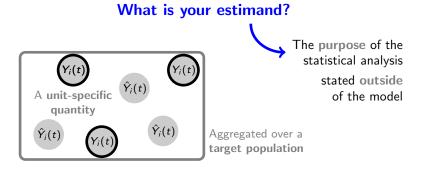


Our framework expands <u>theory</u>, links to transparent <u>evidence</u>, and unlocks computational <u>tools</u>









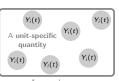


#### What is Your Estimand?

Defining the Target Quantity Connects Statistical Evidence to Theory

Introduce a framework for quantitative social science
Illustrate through three examples where something went wrong
Document that these issues are everywhere
Demonstrate how our framework can help
Extend to answer new theoretical questions

Discuss Every quantitative study should define the estimand



Averaged over a target population



#### What is Your Estimand?

Defining the Target Quantity Connects Statistical Evidence to Theory

→ Introduce a framework for quantitative social science

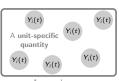
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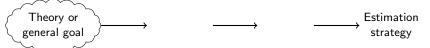
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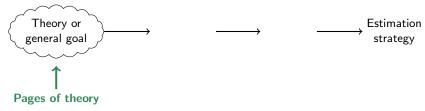
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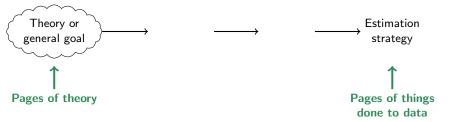
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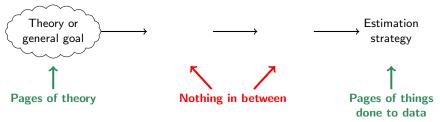


Averaged over a target population

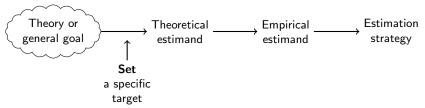


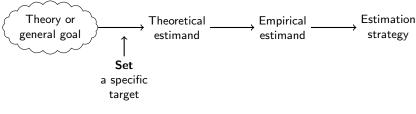






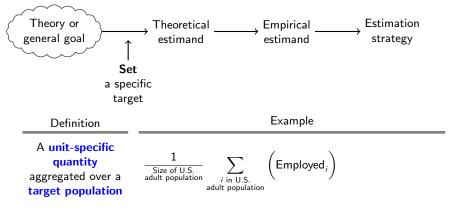


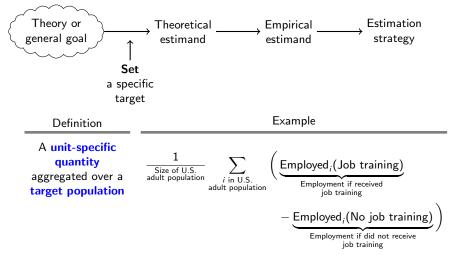


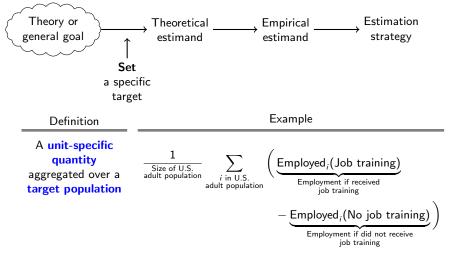


#### Definition

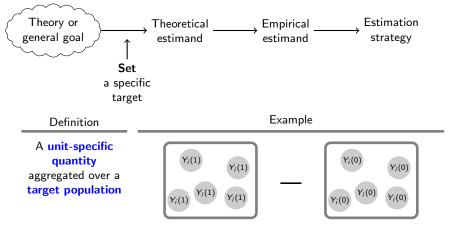
A unit-specific quantity aggregated over a target population



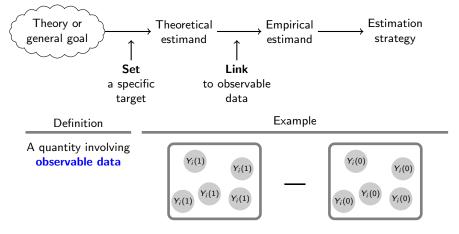


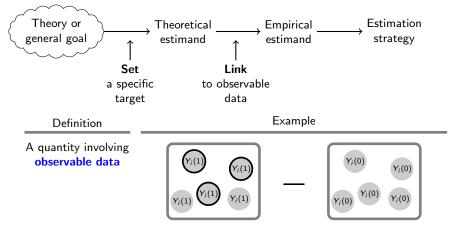


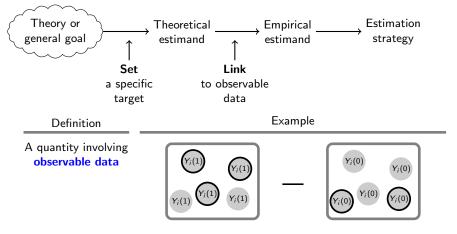
Lieberson 1987, Abbott 1988, Freedman 1991, Xie 2013, Hernán 2018

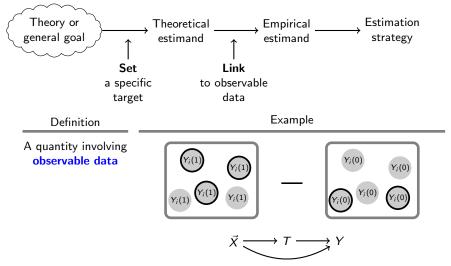


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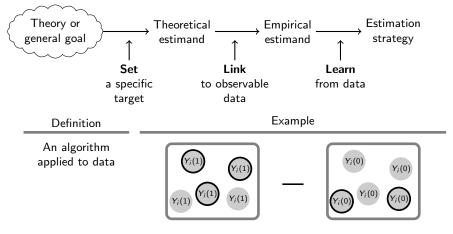


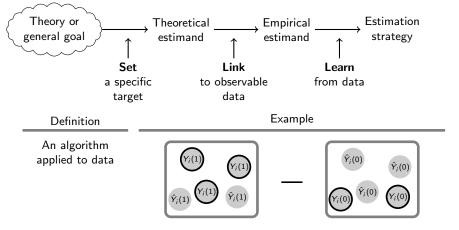




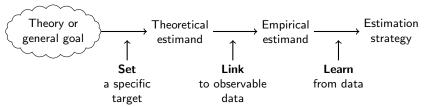


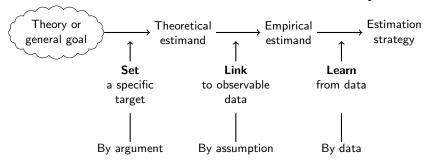
Pearl 2009, Imbens and Rubin 2015, Morgan and Winship 2015, Elwert and Winship 2014





Young 2009, Watts 2014, Berk et al. 2019, Molina and Garip 2019







### What is Your Estimand?

Defining the Target Quantity Connects Statistical Evidence to Theory

→ Introduce a framework for quantitative social science

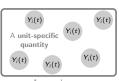
Illustrate through three examples where something went wrong

Document that these issues are everywhere

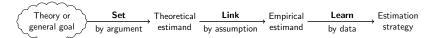
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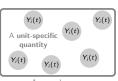
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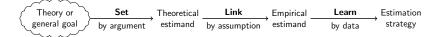
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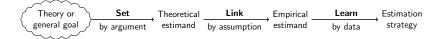
Example 1: An influential study with a narrow theoretical estimand

Theory or general goal by argument estimand by assumption estimand by data Estimation

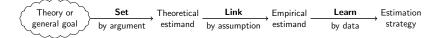




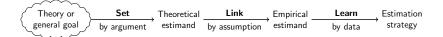
First two births are the same sex



First two births are the same sex Third birth

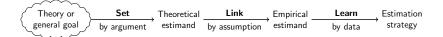


First two births are the same sex 
$$\longrightarrow$$
 Third birth  $\longrightarrow$  Employed



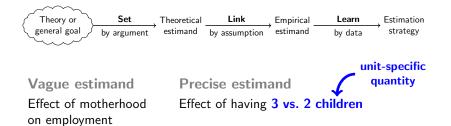
Vague estimand Effect of motherhood on employment

First two births are the same sex 
$$\longrightarrow$$
 Third birth  $\longrightarrow$  Employed

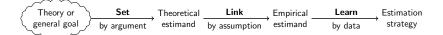


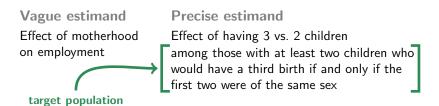
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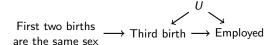
First two births are the same sex 
$$\longrightarrow$$
 Third birth  $\longrightarrow$  Employed



First two births are the same sex  $\longrightarrow$  Third birth  $\longrightarrow$  Employed







Theory or general goal by argument estimand Link by assumption estimand by data Estimation strategy

### Precise estimand

Effect of having 3 vs. 2 children among those with at least two children who would have a third birth if and only if the first two were of the same sex

 $\approx$  4% of all mothers

Theory or general goal by argument estimand by assumption Empirical by data Estimation estimated by data

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You have to argue for one of two things:

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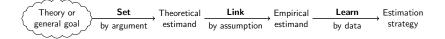
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### You have to argue for one of two things:

- 1) That estimand matters for theory, or
- 2) It speaks to some broader estimand



Example 2: An influential study with a misleading link to evidence



### An Empirical Analysis of Racial Differences in Police Use of Force

Roland G. Fryer Jr.

Harvard University and National Bureau of Economic Research

This paper explores racial differences in police use of force. On nonlethal uses of force, blacks and Hispanics are more than 50 percent more likely to experience some form of force in interactions with police. Adding controls that account for important context and civilian behavior reduces, but cannot fully explain, these disparities. On the most extreme use of force—officer-involved shootings—we find no racial differences either in the raw data or when contextual factors are taken into account. We arrue that the patterns in the data are consistent with a model in which police officers are utility maximizers, a fraction of whom have a preference for discrimination, who incur relatively high expected costs of officer-involved shootings.

We can never be satisfied as long as the Negro is the victim of the unspeakable horrors of police brutality. (Martin Luther King Jr., August 28, 1963)

#### I. Introduction

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This work has benefited greatly from discussions and debate with Chief William Exans Chief Charles McClelland, Chief Martha Montalvo, Sergrant Stephen Morrison, Jon Murad, Lynn Overmann, Chief Bud Riley, and Chief Scott Thomson. I am grateful to David Card, Kersein Charles, Christian Dustmann, Michael Greenstone, James Heckman, Richard Holden, Lasorence Katz, Steven Levitt, Jens Ludwig, Glenn Loury, Kevin Murphy, Derek Neal, John Overdeck, Jose Shapiro, Andrei Shleifer, Jory Spenkuch, Max Stone, John Van Roman, Christopher Winship, and seminar participants at Brown University, University of Chicago, London

Electronically published April 22, 2019 [Journal of Policial Economy, 2019, vol. 127, no. 5] © 2019 by The University of Chicago, All (solts reserved, 0022-0009-2019/12705-0006510.00



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Lundberg, Johnson, and Stewart. What is Your Estimand?

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: The Upshot

Surprising New Evidence Shows Bias in Police Use of Force but Not in Shootings

Theory or Set Learn  $\mathsf{Theoretical}$ Empirical Estimation general goal estimand strategy by argument by assumption estimand by data

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OPINION / COMMENTAR The Myth of Systemic Police Racism Hold officers accountable who use excessive force. But there's no evidence of widespread racial bias. By Heather Mac Donald June 2, 2020 144 gm FT

Set Theory or general goal by argument

 $\mathsf{Theoretical}$ estimand

by assumption

Empirical estimand

Learn by data Estimation strategy

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Reality check: study finds no racial bias in police shootings

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Evidence: Police use lethal force at the same rate against black and white civilians who are stopped.

Theory or general goal by argument estimand by assumption estimand by data Estimation

**Evidence:** Police use lethal force at the same rate against

black and white civilians who are stopped.

Claim: Police are unbiased











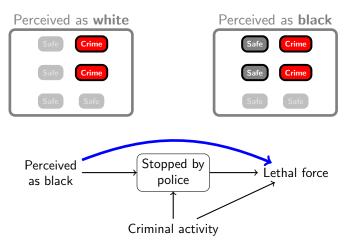












Fryer 2019. Fuller critique by Knox et al. 2020 and Durlauf and Heckman 2020.

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Fryer responds:

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Evidence: Police use lethal force at the same rate against

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Claim: Police are unbiased

Fryer responds:



Evidence: Police use lethal force at the same rate against

black and white civilians who are stopped.

Claim: Police are unbiased

Fryer responds:

"We use the term 'racial differences' 114 times in lieu of the more prescriptive wording—'racial discrimination.' We use the phrase 'conditional on an interaction' 20 times...I am not sure how many more ways we would have needed to caveat our results to satisfy [the critics]."



Example 3: An influential study where estimation led to confusion

Theory or general goal by argument Set of the stimand by assumption strategy

The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

	β	(SE)	
Birth Cohort 1966+ (vs. 1938–1965)	.318	(.285)	
Female	136	(.133)	
Later Cohorts × Female	107	(.272)	
Mother Some College	.737**	(.134)	
Later Cohorts × Mother Some College	.079	(.218)	
No Father Present	031	(.129)	
Father Some College	1.285**	(.113)	
Later Cohorts × No Father	107	(.226)	
Later Cohorts × Father Some College	390	(.211)	
Mother Some College × Female	.120	(.147)	
No Father Present × Female			
Father Some College × Female			
Mother Some College × No Father	.108	(.208)	
Mother Some College × Father Some College	.150	(.138)	
No Father or Father ≤HS × Male	.303*	(.143)	
No Father or Father ≤HS × Male × Later Cohorts	801**	(.293)	
Mother Some College × Female × Later Cohorts	.221	(.295)	
No Father × Female × Later Cohorts			
Father Some College $\times$ Male $\times$ Later Cohorts			
Age Main Effects	(omitted)		
2- and 3-way Interactions between			
Age and (Gender, Cohort)	(omitted)		
Constant	1.695**	(.140)	
N	7,024		
df	15		

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Theory or general goal by argument Theoretical estimand by assumption Empirical estimation strategy

Coefficient: Gender  $\times$  Cohort  $\times$  Father status The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

Theory or general goal by argument Theoretical estimand by assumption Empirical estimation strategy

Coefficient:
Gender × Cohort
× Father status

The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

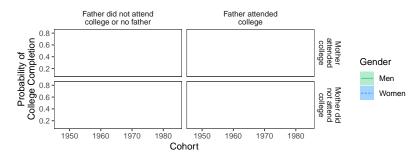
— Buchmann and DiPrete 2006

**Descriptive** Proportion completing college estimand: within subgroups of the predictors

Lundberg, Johnson, and Stewart. What is Your Estimand?

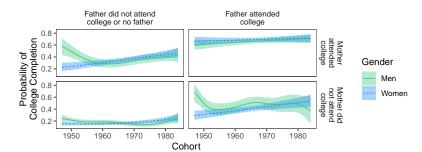


The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.



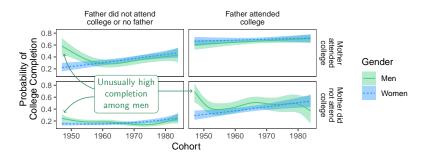


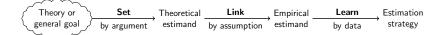
The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.





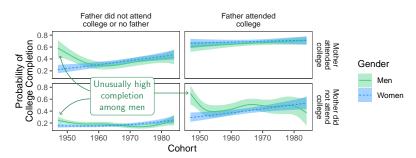
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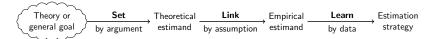


The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

— Buchmann and DiPrete 2006



Alternate theory: The Vietnam War



### What is Your Estimand?

Defining the Target Quantity Connects Statistical Evidence to Theory

Introduce a framework for quantitative social science

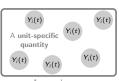
→ Illustrate through three examples where something went wrong

Document that these issues are everywhere

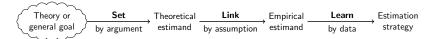
Demonstrate how our framework can help

**Extend** to answer new theoretical questions

Discuss Every quantitative study should define the estimand



Averaged over a target population



### What is Your Estimand?

Defining the Target Quantity Connects Statistical Evidence to Theory

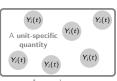
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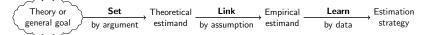
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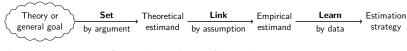


Review
All 32 articles
in ASR 2018
using
quantitative
data

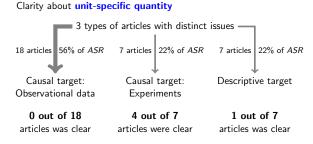


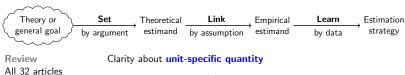
Experiments

Observational data

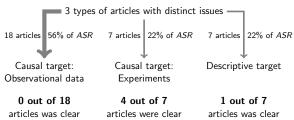


Review
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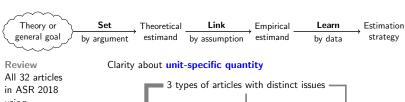


All 32 articles in ASR 2018 using quantitative data



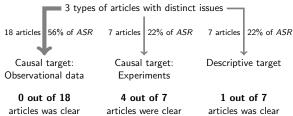
#### Clarity about the target population



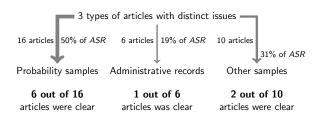


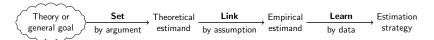
in ASR 2018
using
quantitative
data

3 typ
18 articles
56% of AS



Clarity about the target population





#### What is Your Estimand?

Defining the Target Quantity Connects Statistical Evidence to Theory

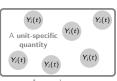
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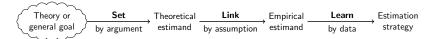
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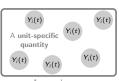
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Averaged over a target population

Theory or general goal by argument Theoretical Link by assumption estimand by data Estimation strategy

Pal and Waldfogel (2016) estimate the family gap in pay.



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Is the theoretical estimand descriptive?



Pal and Waldfogel (2016) estimate the family gap in pay.

Is the theoretical estimand descriptive?

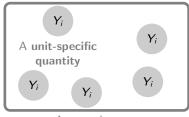
"the differential in hourly wages between women with children and women without children"



Pal and Waldfogel (2016) estimate the family gap in pay.

Is the theoretical estimand descriptive?

"the differential in hourly wages between women with children and women without children"



Averaged over a target population of mothers



Averaged over a target population of non-mothers





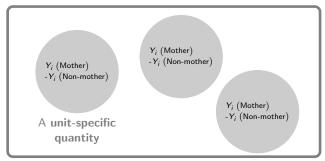
Pal and Waldfogel (2016) estimate the family gap in pay.

Is the theoretical estimand descriptive? Is it causal?

"causal estimation techniques"



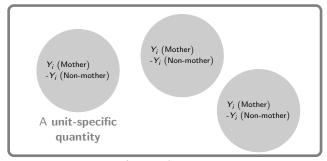
"causal estimation techniques"



Averaged over a target population of mothers



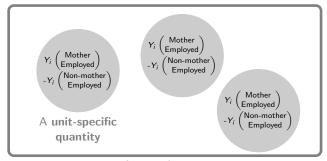
Added complexity: Wages are undefined for the non-employed.



Averaged over a target population of mothers



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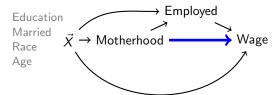


Averaged over a target population of mothers Theory or general goal by argument by argument by assumption Estimation strategy

Unit-specific quantity:  $Y_i \begin{pmatrix} Mother, \\ Employed \end{pmatrix} - Y_i \begin{pmatrix} Non-mother, \\ Employed \end{pmatrix}$ 

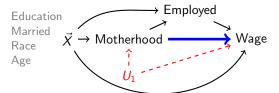
Theory or general goal by argument by argument by argument estimand by assumption estimand by data Estimation strategy

Unit-specific quantity: 
$$Y_i \begin{pmatrix} Mother, \\ Employed \end{pmatrix} - Y_i \begin{pmatrix} Non-mother, \\ Employed \end{pmatrix}$$



Theory or general goal by argument by argument by argument estimand by assumption estimand by data Estimation strategy

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Theory or general goal by argument by argument by assumption testimand by data Estimation strategy

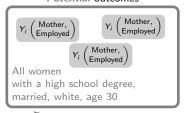
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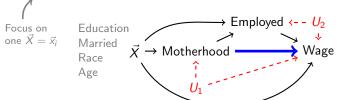


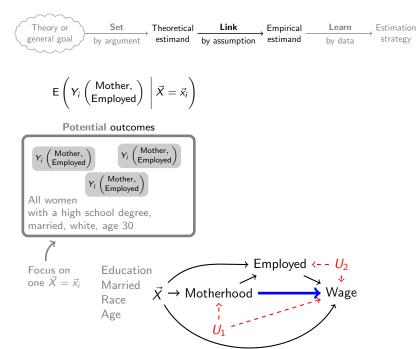


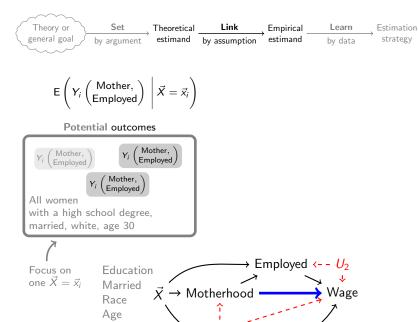
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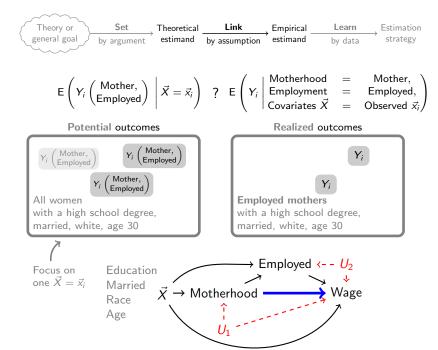
#### Potential outcomes

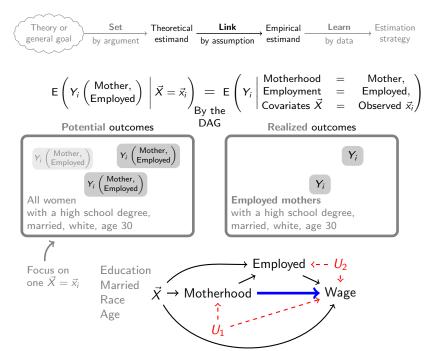












Theory or general goal by argument estimand Link by assumption estimand by data Estimation strategy

$$\mathsf{E}\left(Y_i \middle| \begin{array}{lll} \mathsf{Motherhood} & = & \mathsf{Mother}, \\ \mathsf{Employment} & = & \mathsf{Employed}, \\ \mathsf{Covariates} \ \vec{X} & = & \mathsf{Observed} \ \vec{x_{ij}}, \end{array} \right)$$

#### Realized outcomes



 $Y_i$ 

Employed mothers with a high school degree, married, white, age 30



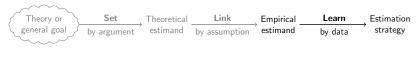
This can be estimated by machine learning!  $\rightarrow$  E  $\left(Y_i \middle| \begin{array}{ccc} \text{Motherhood} & = & \text{Mother,} \\ \text{Employment} & = & \text{Employed,} \\ \text{Covariates } \vec{X} & = & \text{Observed } \vec{x_i} \end{array}\right)$ 

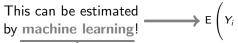
#### Realized outcomes



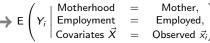
 $Y_i$ 

**Employed mothers** with a high school degree, married, white, age 30





Any prediction algorithm that minimizes squared errors

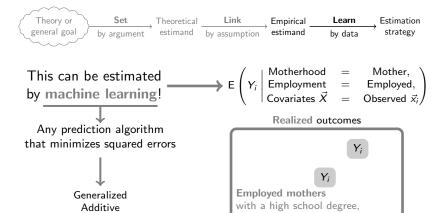






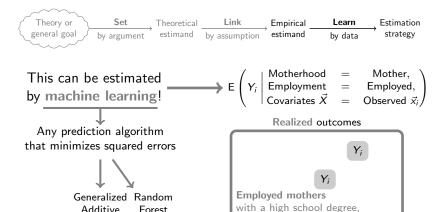


Employed mothers
with a high school degree,
married, white, age 30



married, white, age 30

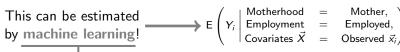
Model



married, white, age 30

Model





Any prediction algorithm that minimizes squared errors



Ordinary Generalized Random Least Additive Forest Squares Model







Employed mothers
with a high school degree,
married, white, age 30

Theory or general goal by argument Set estimand by assumption by data Estimation strategy



1) Learn an algorithm to predict the outcome

Theory or general goal by argument estimand by assumption Empirical estimation strategy

- 1) Learn an algorithm to predict the outcome
- 2) Predict for every unit at each treatment value

$$\hat{\mathsf{E}}\left(Y_i \middle| \begin{array}{ll} \mathsf{Motherhood} &=& \mathsf{Mother}, \\ \mathsf{Employment} &=& \mathsf{Employed}, \\ \mathsf{Covariates} \ \vec{X} &=& \mathsf{Observed} \ \vec{x_i} \end{array}\right)$$

- 1) Learn an algorithm to predict the outcome
- 2) Predict for every unit at each treatment value

$$\hat{Y}_i \begin{pmatrix} \text{Mother}, \\ \text{Employed} \end{pmatrix} = \hat{E} \begin{pmatrix} Y_i & \text{Motherhood} & = & \text{Mother}, \\ \text{Employment} & = & \text{Employed}, \\ \text{Covariates } \vec{X} & = & \text{Observed } \vec{x_i} \end{pmatrix}$$

- 1) Learn an algorithm to predict the outcome
- 2) Predict for every unit at each treatment value

$$\hat{Y}_i egin{pmatrix} ext{Non-mother}, \ ext{Employed} \end{pmatrix} = \hat{\mathsf{E}} \left( Y_i \middle| egin{pmatrix} ext{Motherhood} &= & ext{Non-mother}, \ ext{Employment} &= & ext{Employed}, \ ext{Covariates } \vec{X} &= & ext{Observed } \vec{x_i} \end{pmatrix}$$

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$$\hat{Y}_i \begin{pmatrix} \text{Non-mother}, \\ \text{Employed} \end{pmatrix} = \hat{E} \begin{pmatrix} Y_i & \text{Motherhood} & = & \text{Non-mother}, \\ \text{Employment} & = & \text{Employed}, \\ \text{Covariates } \vec{X} & = & \text{Observed } \vec{x_i} \end{pmatrix}$$

$$\hat{Y}_i \begin{pmatrix} \text{Mother}, \\ \text{Employed} \end{pmatrix} - \hat{Y}_i \begin{pmatrix} \text{Non-mother}, \\ \text{Employed} \end{pmatrix}$$

- 1) Learn an algorithm to predict the outcome
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3) Average over the target population

$$\frac{1}{n} \sum_{i=1}^{n} \left( \hat{Y}_{i} \begin{pmatrix} \text{Mother,} \\ \text{Employed} \end{pmatrix} - \hat{Y}_{i} \begin{pmatrix} \text{Non-mother,} \\ \text{Employed} \end{pmatrix} \right)$$

- 1) Learn an algorithm to predict the outcome
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$$\hat{Y}_i inom{ ext{Non-mother},}{ ext{Employed}} = \hat{\mathsf{E}} igg( Y_i igg| egin{array}{cccc} ext{Motherhood} &= & ext{Non-mother}, \\ ext{Employment} &= & ext{Employed}, \\ ext{Covariates } \vec{X} &= & ext{Observed } \vec{x_i} \end{array}$$

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This is called an imputation estimator

Hahn, 1998 Abadie & Imbens 2006

Also called the parametric g-formula in biostatistics, Hernán & Robins 2020



Outcome Log hourly wage

Predictors Motherhood, age, race, education, marital status



Outcome Log hourly wage

Predictors Motherhood, age, race, education, marital status

Candidate algorithms

Least flexible



Outcome Log hourly wage

Predictors Motherhood, age, race, education, marital status

Candidate algorithms

Least flexible OLS with a quadratic for age



Outcome Log hourly wage

Predictors Motherhood, age, race, education, marital status

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Least flexible OLS with a quadratic for age

+ Interaction between age and motherhood



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Outcome Log hourly wage

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Least flexible OLS with a quadratic for age

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+ Include each age as a separate indicator variable



Outcome Log hourly wage

Predictors Motherhood, age, race, education, marital status

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Least flexible OLS with a quadratic for age

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Most flexible + Include all interactions among all predictors



Outcome Log hourly wage

Predictors Motherhood, age, race, education, marital status

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Least flexible OLS with a quadratic for age

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#### Choices about functional form



Outcome Log hourly wage

Predictors Motherhood, age, race, education, marital status

**Candidate algorithms** 

Least flexible OLS with a quadratic for age

+ Interaction between age and motherhood

+ Allow a smooth curve for age rather than quadratic

+ Include each age as a separate indicator variable

Most flexible + Include all interactions among all predictors

Choices about functional form are best decided by the data



Outcome Log hourly wage

Predictors Motherhood, age, race, education, marital status

**Candidate algorithms** 

Least flexible OLS with a quadratic for age

Best predictions + Interaction between age and motherhood

+ Allow a smooth curve for age rather than quadratic

+ Include each age as a separate indicator variable

Most flexible + Include all interactions among all predictors

Choices about functional form are best decided by the data



#### Our framework partitions research choices

#### Some choices must be theory-driven

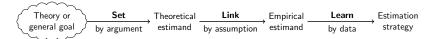
— What question is important? theoretical estimand

— What variables should I adjust? empirical estimand

#### Some choices can be data-driven

— Do I include a squared term? estimation strategy

— Do I need an interaction?



#### What is Your Estimand?

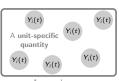
Defining the Target Quantity Connects Statistical Evidence to Theory

Introduce a framework for quantitative social science
Illustrate through three examples where something went wrong
Document that these issues are everywhere

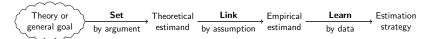
→ Demonstrate how our framework can help

Extend to answer new theoretical questions

Discuss Every quantitative study should define the estimand



Averaged over a target population



#### What is Your Estimand?

Defining the Target Quantity Connects Statistical Evidence to Theory

Introduce a framework for quantitative social science

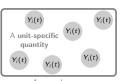
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The Gap-Closing Estimand:

A Causal Approach to Study Interventions

That Close Disparities Across Social Categories

Lundberg, lan Working paper

On SocArxiv

**Standard practice:** Report the coefficient on race, gender, or class.

**The Gap-Closing Estimand:**A Causal Approach to Study Interventions

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Lundberg, Ian Working paper On SocArxiv Standard practice: Report the coefficient on race, gender, or class.

But is "treatment" the right role for these complex constructs?

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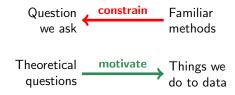
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That Close Disparities Across Social Categories

**Standard practice:** Report the coefficient on race, gender, or class.

But is "treatment" the right role for these complex constructs?



The Gap-Closing Estimand:
A Causal Approach to Study Interventions
That Close Disparities Across Social Categories

Gap-Defining	
Category	
X = x	

Gap-Defining Category X = x'

Race Class Origin Gender





Collections of units

The Gap-Closing Estimand:

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Gap-Defining Category X = x'

Race Class Origin Gender



Collections of units

Incarceration College Occupation

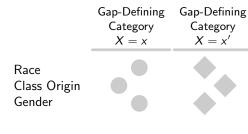




Exposed to the gap-closing treatment T = t

The Gap-Closing Estimand:

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Collections of units

Exposed to the gap-closing treatment T = t



To yield a counterfactual disparity

The Gap-Closing Estimand:
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Defining the Target Quantity Connects Statistical Evidence to Theory

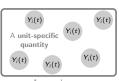
Introduce a framework for quantitative social science
Illustrate through three examples where something went wrong

Document that these issues are everywhere

Demonstrate how our framework can help

→ Extend to answer new theoretical questions

Discuss Every quantitative study should define the estimand



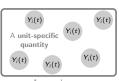
Averaged over a target population



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Averaged over a target population



Every quantitative study should answer this question



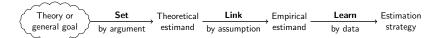
Averaged over a target population



 Every quantitative study should answer this question



Averaged over a target population



Every quantitative study should answer this question

When you **write** a quantitative paper, the estimand allows you to

— Motivate the question

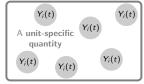


Averaged over a target population



 Every quantitative study should answer this question

- Motivate the question
- Address selection

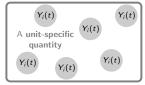


Averaged over a target population



Every quantitative study should answer this question

- Motivate the question
- Address selection
- Unlock computational tools

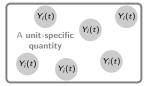


Averaged over a target population



Every quantitative study should answer this question

- Motivate the question
- Address selection
- Unlock computational tools
- Speak to a broad audience



Averaged over a target population

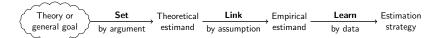


Every quantitative study should answer this question

- Understand the author's aim
- Pinpoint your concerns



Averaged over a target population



In the future, estimands will only become more important

Every quantitative study should answer this question



Averaged over a target population

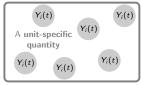


**In the future,** estimands will only become more important

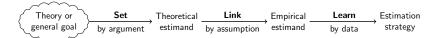
New data have missing values

- Non-probability samples
- Administrative records

Every quantitative study should answer this question



Averaged over a target population



Every quantitative study should answer this question

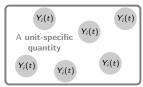
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New methods flourish with a clear goal

— Machine learning



Averaged over a target population



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 $\begin{array}{c|c} Y_i(t) & Y_i(t) \\ \text{A unit-specific quantity} & Y_i(t) \\ Y_i(t) & Y_i(t) \end{array}$ 

Averaged over a target population

New methods flourish with a clear goal

— Machine learning

New questions can be found beyond coefficients

- Describe counterfactual disparities
- Predict the effects of targeted interventions



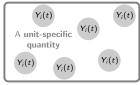
Defining the Target Quantity Connects Statistical Evidence to Theory

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Draft on SocArxiv Code on Dataverse Forthcoming, American Sociological Review