

What is Your Estimand?

Defining the Target Quantity
Connects Statistical Evidence
to Theory



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There is a question every quantitative study must answer:

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The **purpose** of the
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A common answer:




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There is a question every quantitative study must answer:

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A common answer:

- We took [data source]
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**Epistemological
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A **unit-specific**
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$$Y_i(t)$$

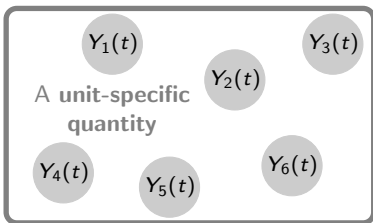
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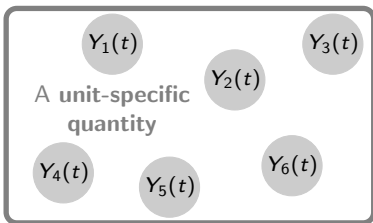
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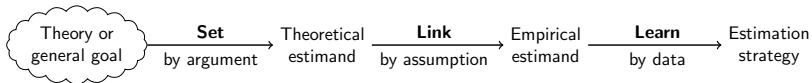


Aggregated over a
target population

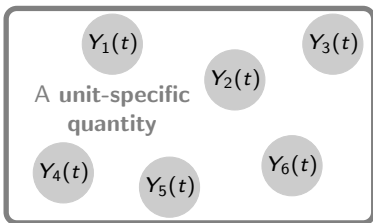
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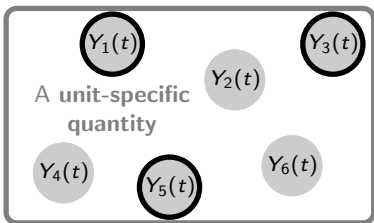
Set



Aggregated over a
target population



Set

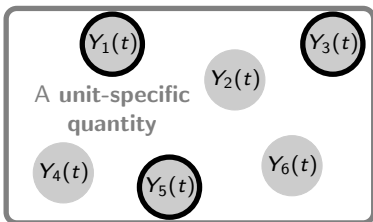


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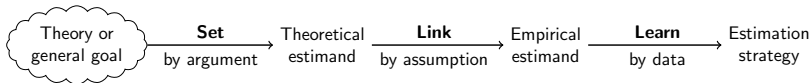
Set

Link



$$\vec{X} \xrightarrow{\quad} T \xrightarrow{\quad} Y$$

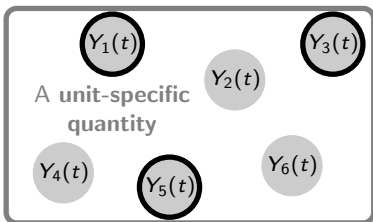
Aggregated over a
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Set

Link

Learn



Aggregated over a
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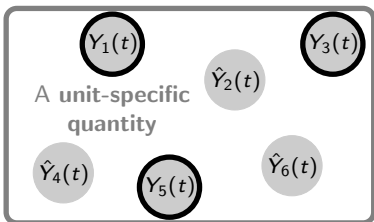
$$\hat{Y}_i(t) = \hat{f}(\vec{X}_i, t)$$



Set

Link

Learn



Aggregated over a
target population

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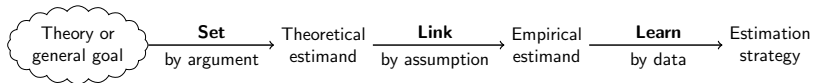


Roadmap of the talk:

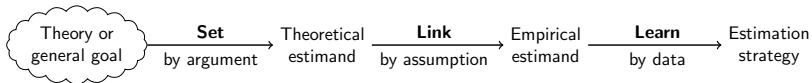
- 1) Examples of how things can go wrong
- 2) An example that follows our framework from top to bottom



Example 1: An influential study with a narrow theoretical estimand



Angrist and Evans 1998



Effect of motherhood
on employment

Angrist and Evans 1998



Effect of motherhood
on employment

First two births
are the same sex

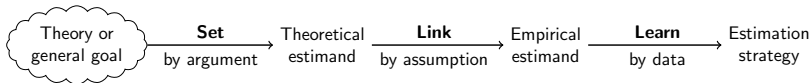
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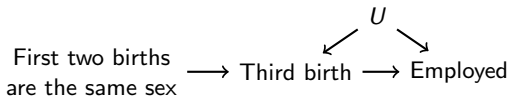
Effect of motherhood
on employment

First two births are the same sex \longrightarrow Third birth

Angrist and Evans 1998



Effect of motherhood
on employment

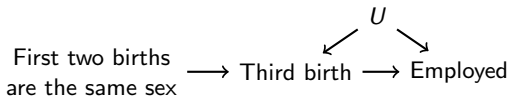


Angrist and Evans 1998



Vague estimand

Effect of motherhood
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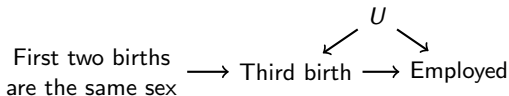
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Vague estimand

Effect of motherhood
on employment

Precise estimand



Angrist and Evans 1998



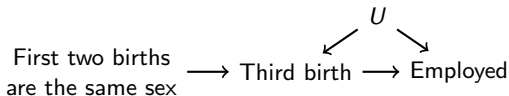
Vague estimand

Effect of motherhood
on employment

Precise estimand

Effect of having **3 vs. 2 children**

**unit-specific
quantity**



Angrist and Evans 1998



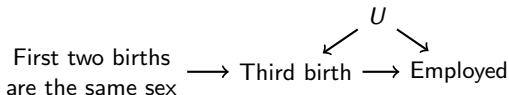
Vague estimand

Effect of motherhood
on employment

target population

Precise estimand

Effect of having 3 vs. 2 children
among those with at least two children who
would have a third birth if and only if the
first two were of the same sex



Angrist and Evans 1998



Precise estimand

Effect of having 3 vs. 2 children
among those with at least two children who
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$\approx 4\%$ of all mothers

Angrist and Evans 1998



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You have to argue either:

- 1)
- 2)

Angrist and Evans 1998



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You have to argue either:

- 1) That estimand matters for theory, or
- 2)

Angrist and Evans 1998



Precise estimand

Effect of having 3 vs. 2 children
among those with at least two children who
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$\approx 4\%$ of all mothers

You have to argue either:

- 1) That estimand matters for theory, or
- 2) It speaks to some broader estimand

Angrist and Evans 1998



Example 2: An influential study with a misleading link to evidence



An Empirical Analysis of Racial Differences in Police Use of Force

Roland G. Fryer Jr.

Harvard University and National Bureau of Economic Research

This paper explores racial differences in police use of force. On non-lethal uses of force, blacks and Hispanics are more than 50 percent more likely to experience some form of force in interactions with police. Adding controls that account for important context and civilian behavior reduces, but cannot fully explain, these disparities. On the most extreme use of force—officer-involved shootings—we find no racial differences either in the raw data or when contextual factors are taken into account. We argue that the patterns in the data are consistent with a model in which police officers are utility maximizers, a fraction of whom have a preference for discrimination, who incur relatively high expected costs of officer-involved shootings.

We can never be satisfied as long as the Negro is the victim of the unspeakable horrors of police brutality. (Martin Luther King Jr., August 28, 1963)

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TheUpshot
DATA DIVE

Surprising New Evidence Shows Bias in Police Use of Force but Not in Shootings



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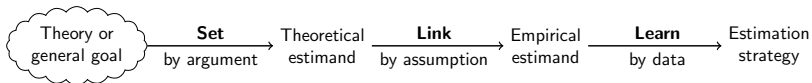
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Reality check: study finds no racial bias in police shootings

The Guardian

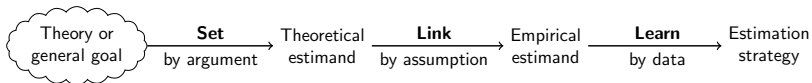


Evidence:

Claim:

Why wrong:

Fryer 2019. Fuller critique by Knox et al. 2020 and Durlauf and Heckman 2020.

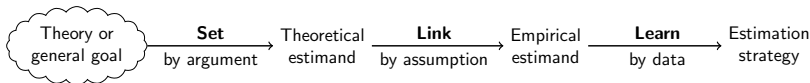


Evidence: Police use lethal force at the same rate against black and white civilians who are stopped.

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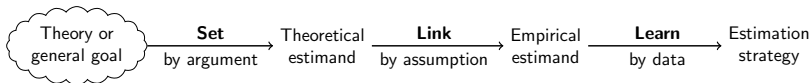
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Lundberg, Johnson, and Stewart. What is Your Estimand?



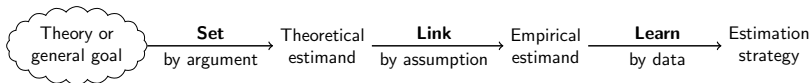
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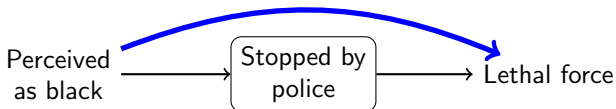
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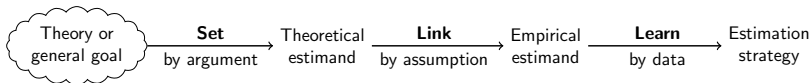
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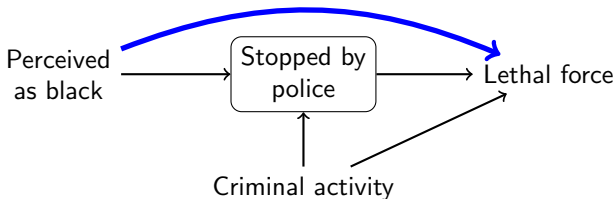
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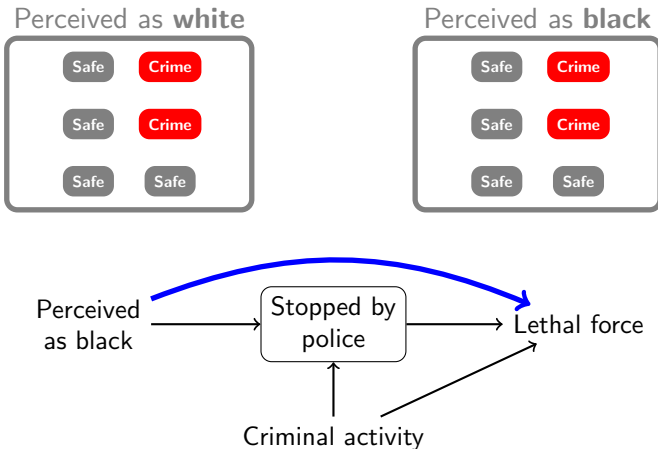
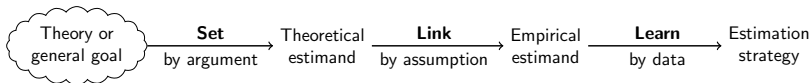
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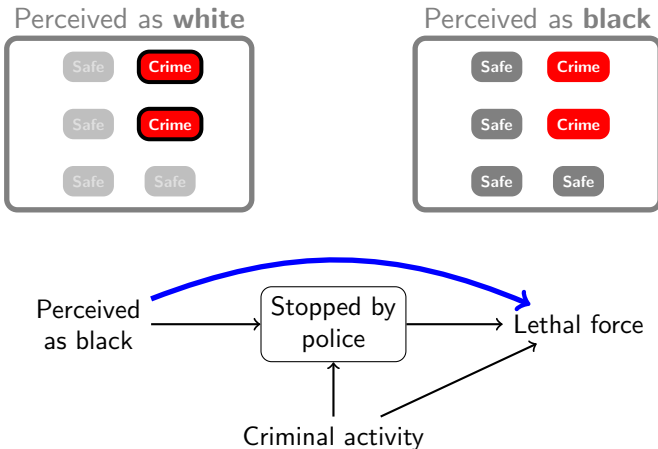
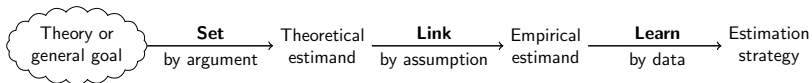
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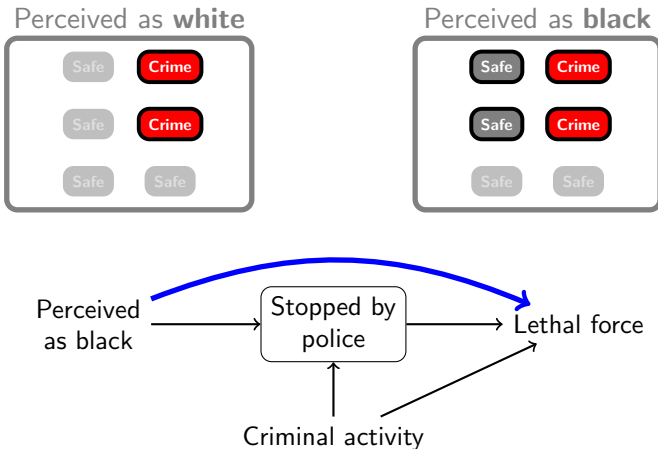
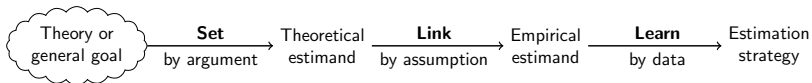
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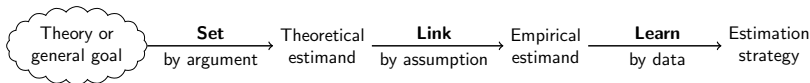
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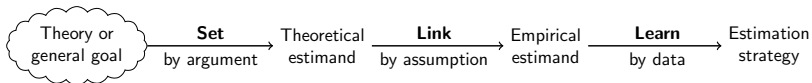


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Claim: Police are unbiased

Why wrong: Causal sample selection. Among those stopped, the white civilians may be more dangerous.

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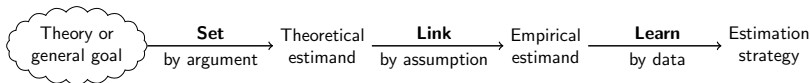
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Claim: Police are unbiased

Why wrong: Causal sample selection. Among those stopped, the white civilians may be more dangerous.

**Fryer
responds:**

Fryer 2019. Fuller critique by Knox et al. 2020 and Durlauf and Heckman 2020.



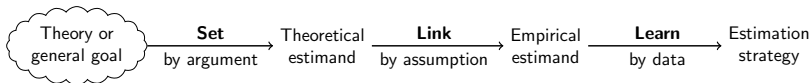
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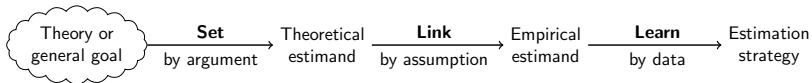
Fryer responds:

“We use the term ‘racial differences’ 114 times in lieu of the more prescriptive wording—‘racial discrimination.’ We use the phrase ‘conditional on an interaction’ 20 times...I am not sure how many more ways we would have needed to caveat our results to satisfy [the critics].”

Fryer 2019. Fuller critique by Knox et al. 2020 and Durlauf and Heckman 2020.



Example 3: An influential study where estimation led to confusion



The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

— Buchmann and DiPrete 2006

	β	(SE)
Birth Cohort 1966+ (vs. 1938–1965)	.318	(.285)
Female	–.136	(.133)
Later Cohorts \times Female	–.107	(.272)
Mother Some College	.737**	(.134)
Later Cohorts \times Mother Some College	.079	(.218)
No Father Present	–.031	(.129)
Father Some College	1.285**	(.113)
Later Cohorts \times No Father	–.107	(.226)
Later Cohorts \times Father Some College	–.390	(.211)
Mother Some College \times Female	.120	(.147)
No Father Present \times Female		
Father Some College \times Female		
Mother Some College \times No Father	.108	(.208)
Mother Some College \times Father Some College	.150	(.138)
No Father or Father \leq HS \times Male	.303*	(.143)
No Father or Father \leq HS \times Male \times Later Cohorts	–.801**	(.293)
Mother Some College \times Female \times Later Cohorts	.221	(.295)
No Father \times Female \times Later Cohorts		
Father Some College \times Male \times Later Cohorts		
Age Main Effects	(omitted)	
2- and 3-way Interactions between Age and (Gender, Cohort)	(omitted)	
Constant	1.695**	(.140)
N	7,024	
df	15	

	β	(SE)
Birth Cohort 1966+ (vs. 1938–1965)	.318	(.285)
Female	-.136	(.133)
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→ No Father or Father \leq HS \times Male \times Later Cohorts →	-.801**	(.293)
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No Father \times Female \times Later Cohorts		
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Age Main Effects	(omitted)	
2- and 3-way Interactions between		
Age and (Gender, Cohort)	(omitted)	
Constant	1.695**	(.140)
N	7,024	
df	15	

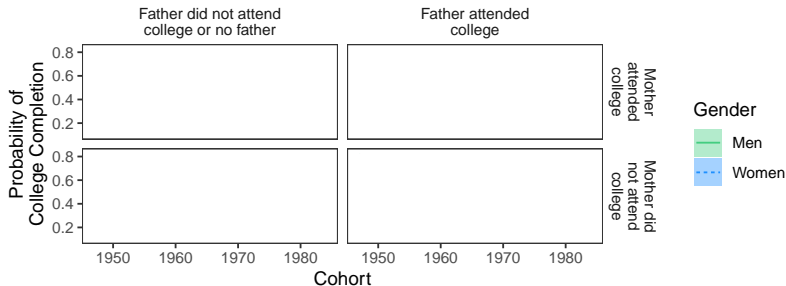


Coefficient:

Gender \times Cohort
 \times Father status

The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

— Buchmann and DiPrete 2006



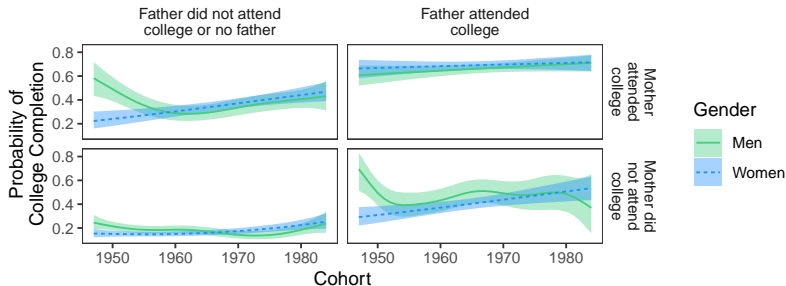


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The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

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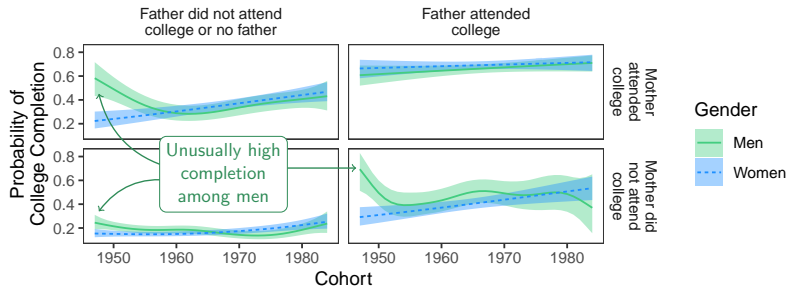


Coefficient:

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The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

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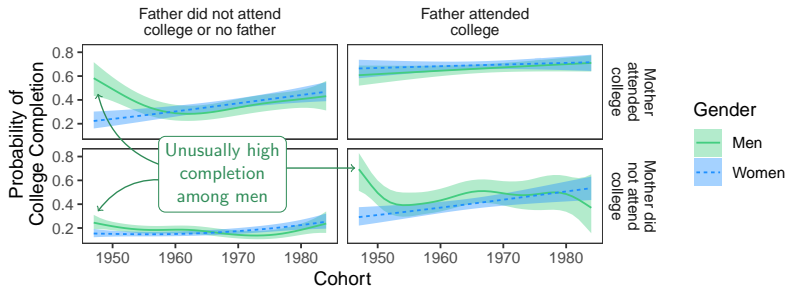


Coefficient:

Gender \times Cohort
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The emergence of a female advantage in education is attributable to a reversal in the gender-specific effects of father status.

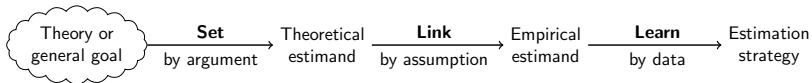
— Buchmann and DiPrete 2006



Alternate theory: The Vietnam War



Meta-example: Vague estimands are widespread



Review

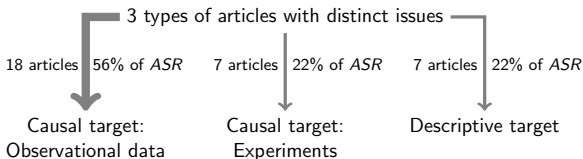
All 32 articles
in ASR 2018
using
quantitative
data



Review

All 32 articles
in ASR 2018
using
quantitative
data

Clarity about **unit-specific quantity**

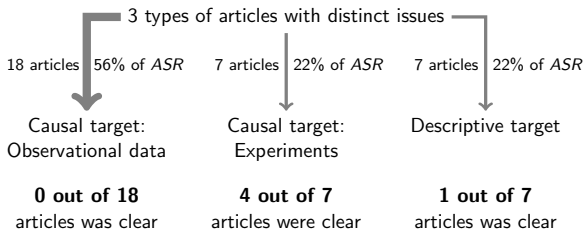


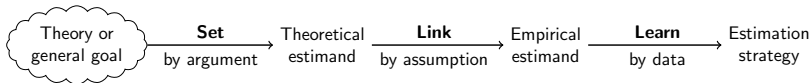


Review

All 32 articles in ASR 2018 using quantitative data

Clarity about **unit-specific quantity**

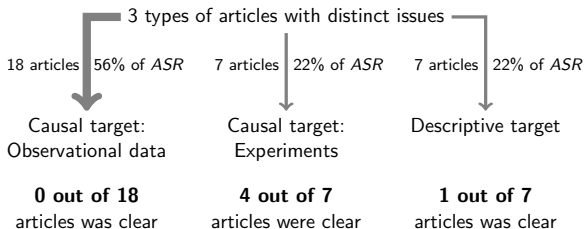




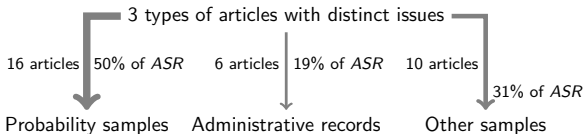
Review

All 32 articles in ASR 2018 using quantitative data

Clarity about **unit-specific quantity**



Clarity about the **target population**

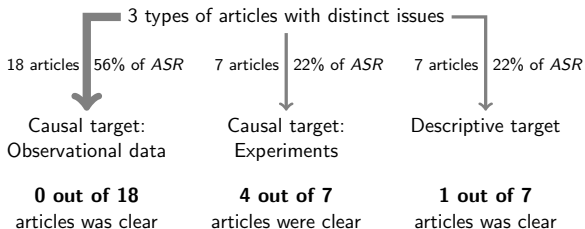




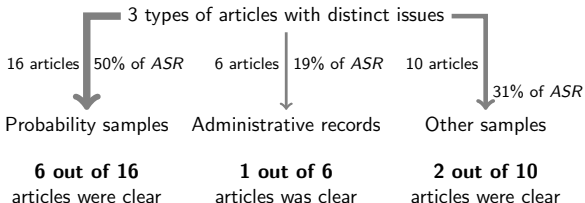
Review

All 32 articles in ASR 2018 using quantitative data

Clarity about **unit-specific quantity**



Clarity about the **target population**





Roadmap of the talk:

- 1) Examples of how things can go wrong
- 2) An example that follows our framework from top to bottom



Roadmap of the talk:

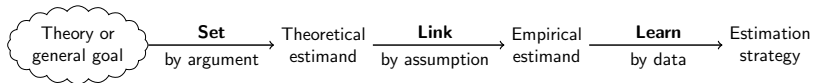
- 1) Examples of how things can go wrong
- 2) An example that follows our framework from top to bottom

General Method

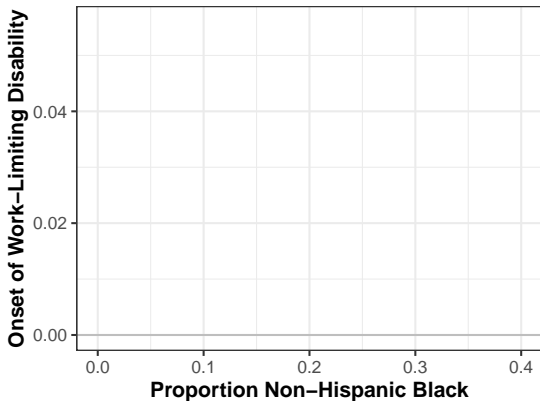
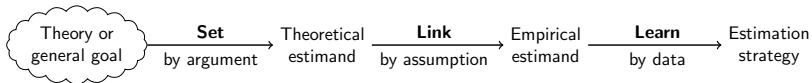
The Gap-Closing Estimand:
The Disparity Across Social Categories
That Would Persist if We Equalized a Treatment

Specific Example

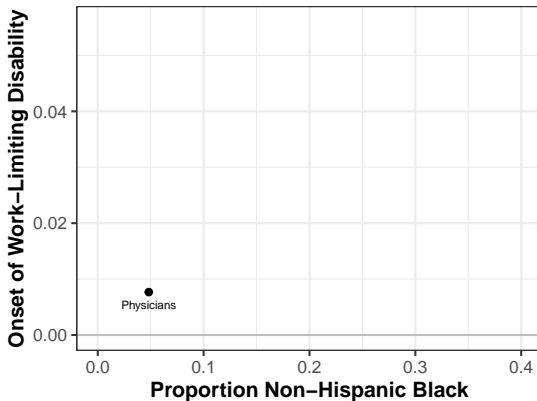
Quantifying the Contribution of Occupational
Segregation to Racial Disparities in Health:
A Gap-Closing Perspective



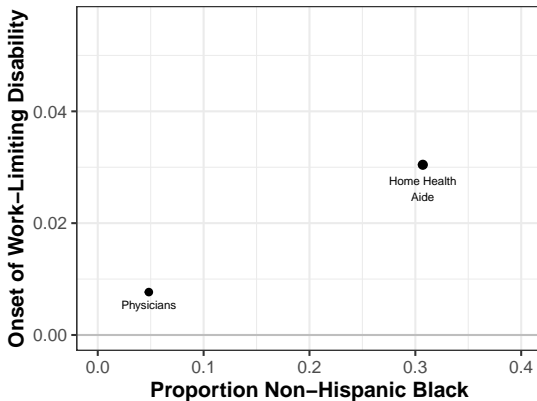
Current
Population Survey
Annual Social and
Economic Supplement
Ages 25–60
2005–2020



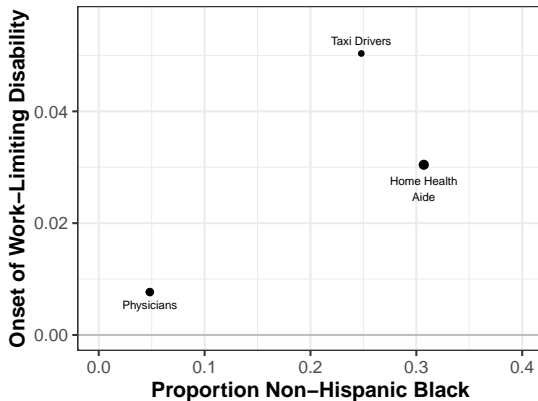
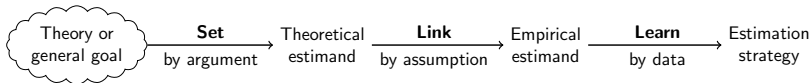
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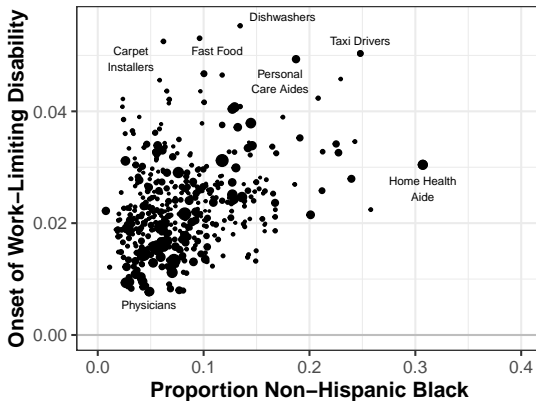
Current
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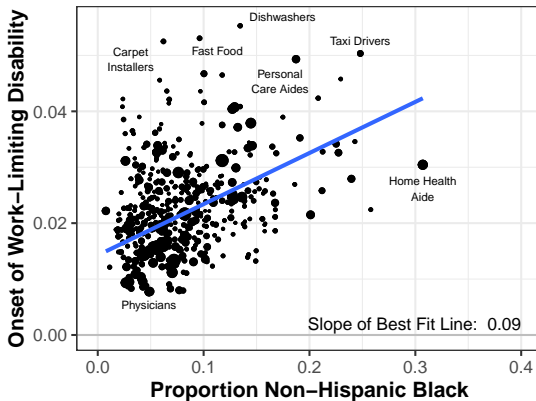
Current
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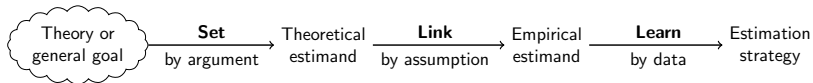
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Current
Population Survey
Annual Social and
Economic Supplement
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Current
Population Survey
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Theoretical estimand



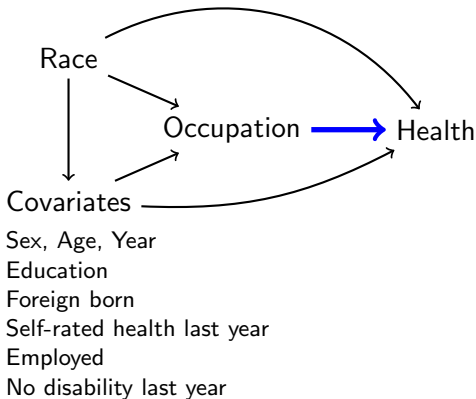
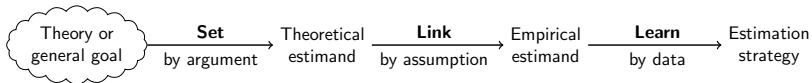
Theoretical estimand

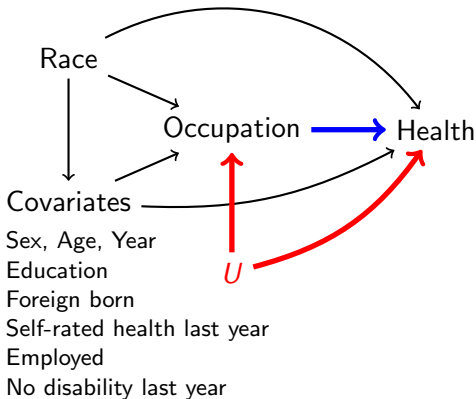
- ▶ **Unit-specific quantity:**

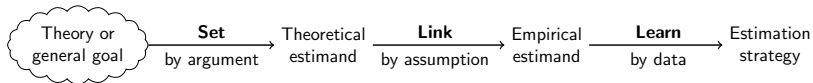
Onset of work-limiting disability
if occupations were randomly shuffled
within educational strata

- ▶ Target population

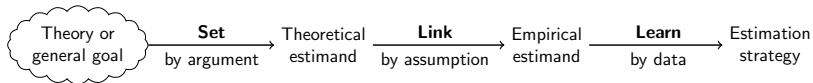
- ▶ U.S. Ages 25–60
- ▶ Employed at baseline survey
- ▶ No work-limiting disability at baseline survey
- ▶ Never previously quit a job for health reasons







		Administrative Assistant	Home Health Aid	Sales Supervisor
White	Person 1	<i>y</i>		
	Person 2			<i>y</i>
	Person 3		<i>y</i>	
	Person 4		<i>y</i>	
Black	Person 5			<i>y</i>
	Person 6	<i>y</i>		
	Person 7	<i>y</i>		
	Person 8			<i>y</i>



		Administrative Assistant	Home Health Aid	Sales Supervisor
White	Person 1	y	•	•
	Person 2	•	•	y
	Person 3	•	y	•
	Person 4	•	y	•
Black	Person 5	•	•	y
	Person 6	y	•	•
	Person 7	y	•	•
	Person 8	•	•	y



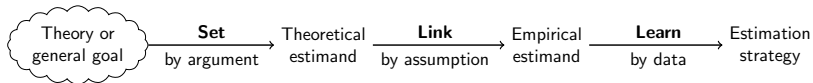
		Administrative Assistant	Home Health Aid	Sales Supervisor	Average outcome if occupations were shuffled ↓
White	Person 1	y	•	•	•
	Person 2	•	•	y	
	Person 3	•	y	•	
	Person 4	•	y	•	
Black	Person 5	•	•	y	
	Person 6	y	•	•	
	Person 7	y	•	•	
	Person 8	•	•	y	



$$\hat{y}_i(t) = \hat{f}(\vec{X}_i, t)$$

Average outcome
if occupations
were shuffled

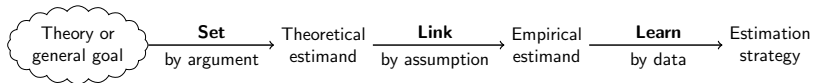
		Administrative Assistant	Home Health Aid	Sales Supervisor	
White	Person 1	y	•	•	•
	Person 2	•	•	y	
	Person 3	•	y	•	
	Person 4	•	y	•	
Black	Person 5	•	•	y	
	Person 6	y	•	•	
	Person 7	y	•	•	
	Person 8	•	•	y	



$$\hat{y}_i(t) = \hat{f}(\vec{X}_i, t)$$

Average outcome
if occupations
were shuffled

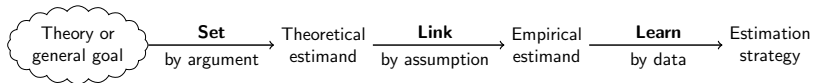
		Administrative Assistant	Home Health Aid	Sales Supervisor	were sh
White	Person 1	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 2	•	•	y	
	Person 3	•	y	•	
	Person 4	•	y	•	
<hr style="border-top: 1px dashed black;"/>					
Black	Person 5	•	•	y	
	Person 6	y	•	•	
	Person 7	y	•	•	
	Person 8	•	•	y	



$$\hat{y}_i(t) = \hat{f}(\vec{X}_i, t)$$

Average outcome
if occupations
were shuffled

		Administrative Assistant	Home Health Aid	Sales Supervisor	↓
White	Person 1	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 2	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 3	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 4	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
Black	Person 5	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 6	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 7	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 8	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$

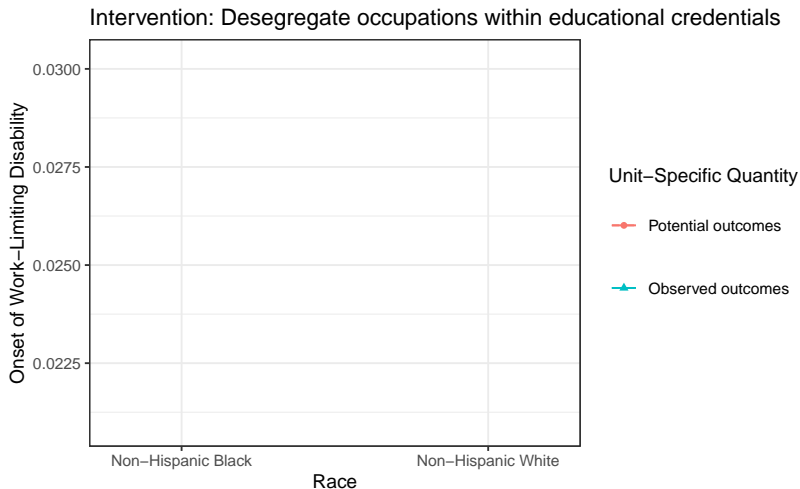
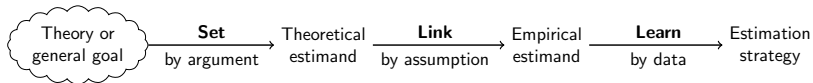


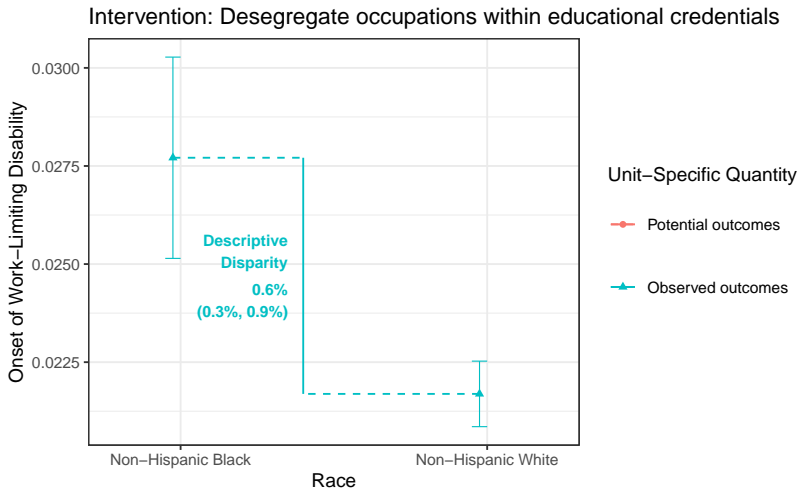
$$\hat{y}_i(t) = \hat{f}(\vec{X}_i, t)$$

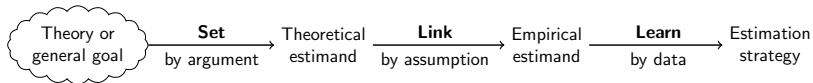
Average outcome
if occupations
were shuffled

		Administrative Assistant	Home Health Aid	Sales Supervisor	
White	Person 1	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 2	\hat{y}	\hat{y}	\hat{y}	
	Person 3	\hat{y}	\hat{y}	\hat{y}	
	Person 4	\hat{y}	\hat{y}	\hat{y}	
Black	Person 5	\hat{y}	\hat{y}	\hat{y}	$\hat{\bar{y}}$
	Person 6	\hat{y}	\hat{y}	\hat{y}	
	Person 7	\hat{y}	\hat{y}	\hat{y}	
	Person 8	\hat{y}	\hat{y}	\hat{y}	

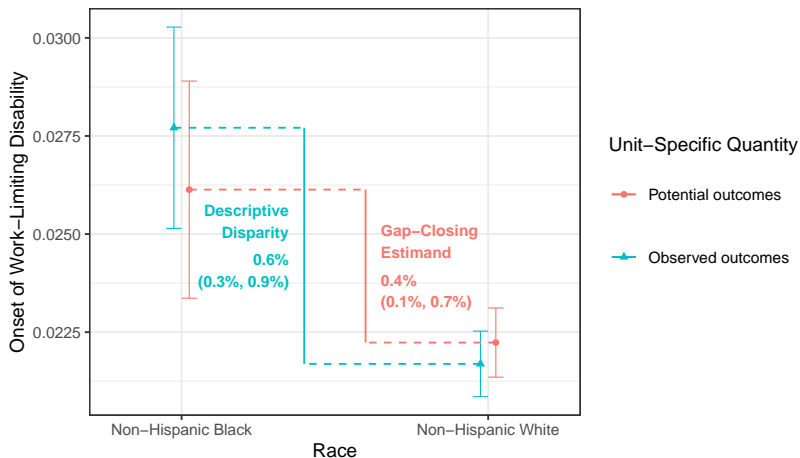
Gap-Closing
Estimand





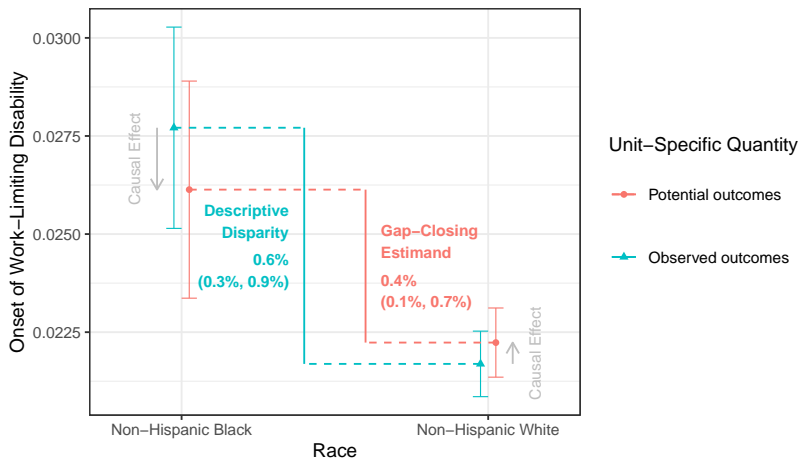


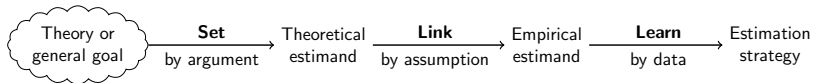
Intervention: Desegregate occupations within educational credentials





Intervention: Desegregate occupations within educational credentials





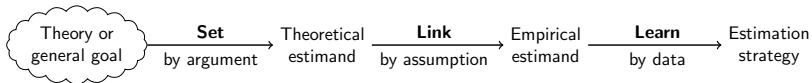
		Treatment Condition	
		Black	White
Population	Person 1	$Y_1(\text{Black})$	$Y_1(\text{White})$
	Person 2	$Y_2(\text{Black})$	$Y_2(\text{White})$
	Person 3	$Y_3(\text{Black})$	$Y_3(\text{White})$
	Person 4	$Y_4(\text{Black})$	$Y_4(\text{White})$
	Person 5	$Y_5(\text{Black})$	$Y_5(\text{White})$
	Person 6	$Y_6(\text{Black})$	$Y_6(\text{White})$



Black	Person 1
	Person 2
	Person 3
White	Person 4
	Person 5
	Person 6



		As observed
Black	Person 1	Y_1
	Person 2	Y_2
	Person 3	Y_3
White	Person 4	Y_4
	Person 5	Y_5
	Person 6	Y_6

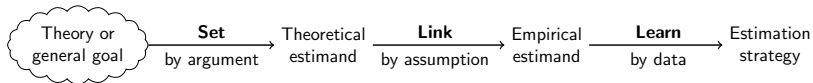


		As observed
Black	Person 1	Y_1
	Person 2	Y_2
	Person 3	Y_3
White	Person 4	Y_4
	Person 5	Y_5
	Person 6	Y_6

Descriptive
Disparity



		As observed	Under intervention
Black	Person 1	Y_1	$Y_1(t)$
	Person 2	Y_2	$Y_2(t)$
	Person 3	Y_3	$Y_3(t)$
White	Person 4	Y_4	$Y_4(t)$
	Person 5	Y_5	$Y_5(t)$
	Person 6	Y_6	$Y_6(t)$
		Descriptive Disparity	Gap-Closing Estimand

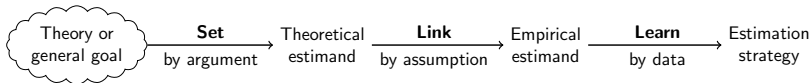


		As observed	Under intervention
Black	Person 1	Y_1	$Y_1(t)$
	Person 2	Y_2	$Y_2(t)$
	Person 3	Y_3	$Y_3(t)$
White	Person 4	Y_4	$Y_4(t)$
	Person 5	Y_5	$Y_5(t)$
	Person 6	Y_6	$Y_6(t)$
		Descriptive Disparity	Gap-Closing Estimand

Vanderweele & Robinson 2014

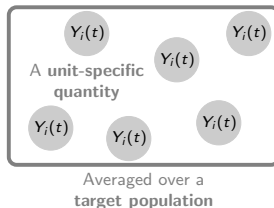
Jackson & Vanderweele 2018

Lundberg 2021



What is your estimand?

← Every quantitative study should answer this question

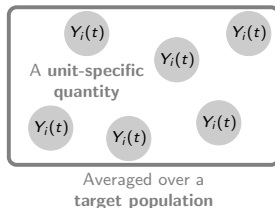


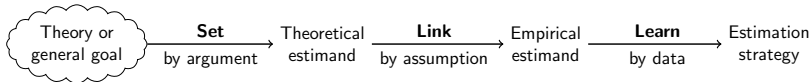


What is your estimand?

← Every quantitative study should answer this question

When you **write** a quantitative paper, the estimand allows you to



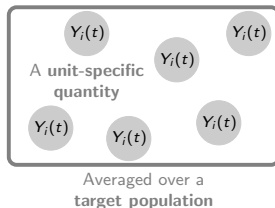


What is your estimand?

← Every quantitative study should answer this question

When you **write** a quantitative paper, the estimand allows you to

- Motivate the question
- Address selection
- Use machine learning
- Speak to a broad audience

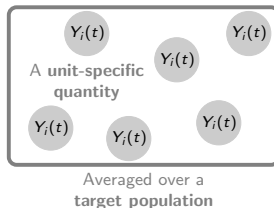


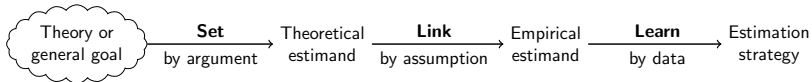


What is your estimand?

← Every quantitative study should answer this question

When you **read** a quantitative paper, the estimand allows you to



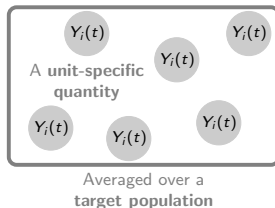


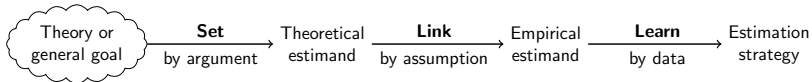
What is your estimand?

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When you **read** a quantitative paper, the estimand allows you to

- Understand the author's aim
- Pinpoint your concerns

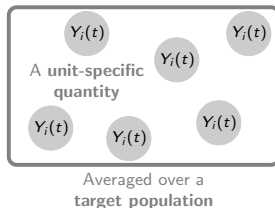


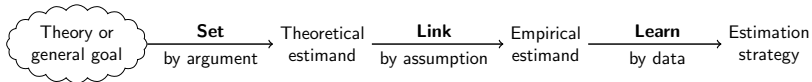


What is your estimand?

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In the future, estimands will only become more important





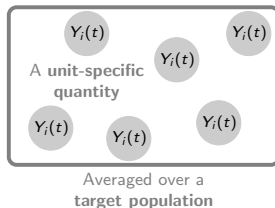
What is your estimand?

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In the future, estimands will only become more important

New data have missing values

- Non-probability samples
- Administrative records





What is your estimand?

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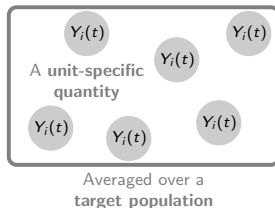
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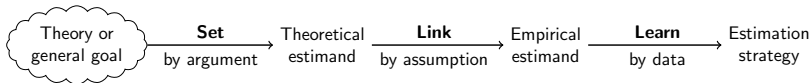
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New methods flourish with a clear goal

- Machine learning





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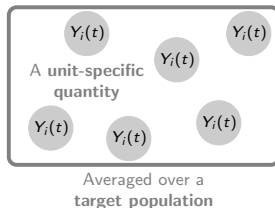
- Non-probability samples
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New methods flourish with a clear goal

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New questions can be found beyond coefficients

- Describe counterfactual disparities
- Predict the effects of targeted interventions





What is your estimand?

← Every quantitative study should answer this question

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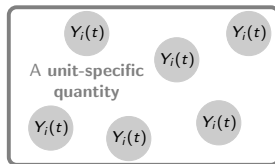
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Averaged over a
target population

American Sociological Review, 2021.

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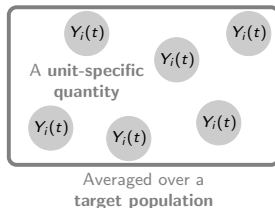
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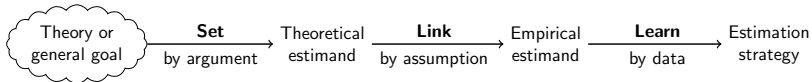
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Defining the Target Quantity
Connects Statistical Evidence
to Theory

Ian Lundberg

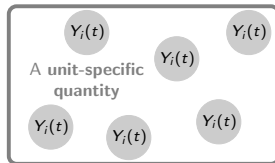
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