

Chain Transition Helper Functions

$\text{getGKeys} \in \text{NewEpochState} \rightarrow \mathbb{P} \text{ KeyHash}_G$
 $\text{getGKeys } nes = \text{dom } \text{genDelegs}$
where
 $(_, _, _, es, _, _) = nes$
 $(_, _, ls, _, _) = es$
 $(_, ((_, _, _, _, _, _, _), _), _) = ls$

$\text{updateNES} \in \text{NewEpochState} \rightarrow \text{BlocksMade} \rightarrow \text{LState} \rightarrow \text{NewEpochState}$
 $\text{updateNES } (e_\ell, b_{prev}, _, (acnt, ss, _, prevPp, pp), ru, pd) b_{cur} ls =$
 $(e_\ell, b_{prev}, b_{cur}, (acnt, ss, ls, prevPp, pp), ru, pd)$

$\text{chainChecks} \in \mathbb{N} \rightarrow (\mathbb{N}, \mathbb{N}, \text{ProtVer}) \rightarrow \text{BHeader} \rightarrow \text{Bool}$
 $\text{chainChecks } maxpv (maxBHSIZE, maxBBSIZE, protocolVersion) bh =$
 $m \leq maxpv$
 $\wedge \text{bHeaderSize } bh \leq maxBHSIZE$
 $\wedge \text{hBbsize } (\text{bhbody } bh) \leq maxBBSIZE$
where $(m, _) := protocolVersion$

$\text{lastAppliedHash} \in \text{LastAppliedBlock}^? \rightarrow \text{HashHeader}^?$
 $\text{lastAppliedHash } lab = \begin{cases} \diamond & lab = \diamond \\ h & lab = (_, _, h) \end{cases}$

$\text{prtISeqChecks} \rightarrow \text{LastAppliedBlock}^? \rightarrow \text{BHeader} \rightarrow \text{Bool}$
 $\text{prtISeqChecks } lab bh = \begin{cases} \text{True} & lab = \diamond \\ s_\ell < slot \wedge b_\ell + 1 = bn \wedge ph = \text{bprev } bhb & lab = (b_\ell, s_\ell, _) \end{cases}$
where
 $bhb := \text{bhbody } bh$
 $bn := \text{bblockno } bhb$
 $slot := \text{bslot } bhb$
 $ph := \text{lastAppliedHash } lab$

Figure 74: Helper Functions used in the CHAIN transition

$bh := \text{bheader } block$ $bhb := \text{bhbody } bh$ $s := \text{bslot } bhb$ $\text{prtSeqChecks } lab \ bh$ $\vdash nes \xrightarrow[\text{TICK}]{s} nes'$ $(e_1, _, _, _, _, _) := nes$ $(e_2, _, b_{cur}, es, _, _, pd) := nes'$ $(acnt, _, ls, _, pp) := es$ $(_, ((_, _, _, _, genDelegs, _), (_, _, _))) := ls$ $ne := e_1 \neq e_2$ $\eta_{ph} := \text{prevHashToNonce (lastAppliedHash } lab)$ $\text{chainChecks MaxMajorPV (maxHeaderSize } pp, \text{ maxBlockSize } pp, \text{ pv } pp) bh$ $\frac{pp}{\eta_c} \vdash \begin{pmatrix} \eta_0 \\ \eta_h \end{pmatrix} \xrightarrow[\text{TICKN}]{ne} \begin{pmatrix} \eta'_0 \\ \eta'_h \end{pmatrix}$ $\frac{\begin{matrix} (d \ pp) \\ pd \\ genDelegs \end{matrix}}{\eta'_0} \vdash \begin{pmatrix} cs \\ \eta_v \\ \eta_c \end{pmatrix} \xrightarrow[\text{PRTCL}]{bh} \begin{pmatrix} cs' \\ \eta'_v \\ \eta'_c \end{pmatrix}$ $\frac{pp}{acnt} \vdash \begin{pmatrix} ls \\ b_{cur} \end{pmatrix} \xrightarrow[\text{BBODY}]{block} \begin{pmatrix} ls' \\ b'_{cur} \end{pmatrix}$ $nes'' := \text{updateNES } nes' \ b'_{cur}, \ ls'$ $lab' := (\text{bblockno } bhb, s, \text{ bhash } bh)$	
<p style="margin: 0;">Chain</p> <hr style="border: 0.5px solid black; margin: 5px 0;"/> $\vdash \begin{pmatrix} nes \\ cs \\ \eta_0 \\ \eta_v \\ \eta_c \\ \eta_h \\ lab \end{pmatrix} \xrightarrow[\text{CHAIN}]{block} \begin{pmatrix} nes'' \\ cs' \\ \eta'_0 \\ \eta'_v \\ \eta'_c \\ \eta'_{h'} \\ lab' \end{pmatrix}$	(43)

Figure 75: Chain rules

12.14 Byron to Shelley Transition

This section defines the valid initial Shelley ledger states and describes how to transition the state held by the Byron ledger to Shelley. The Byron ledger state `CEState` is defined in [BC-D1]. The valid initial Shelley ledger states are exactly the range of the function `initialShelleyState` defined in Figure 76. Figure 77 defines the transition function from Byron. Note that we use the hash of the final Byron header as the first evolving and candidate nonces for Shelley.

Shelley Initial States

$\text{initialShelleyState} \in \text{LastAppliedBlock}^? \rightarrow \text{Epoch} \rightarrow \text{UTxO} \rightarrow \text{Coin} \rightarrow \text{GenesisDelegation}$
 $\rightarrow (\text{Slot} \mapsto \text{KeyHash}_G^?) \rightarrow \text{PParams} \rightarrow \text{Seed} \rightarrow \text{ChainState}$

$$\text{initialShelleyState} \begin{pmatrix} \text{lab} \\ e \\ \text{utxo} \\ \text{reserves} \\ \text{genDelegs} \\ \text{pp} \\ \text{initNonce} \end{pmatrix} = \left(\begin{array}{c} \left(\begin{array}{c} e \\ \emptyset \\ \emptyset \\ \left(\begin{array}{c} 0 \\ \text{reserves} \\ (\emptyset, \emptyset) \\ (\emptyset, \emptyset) \\ (\emptyset, \emptyset) \\ \emptyset \\ \emptyset \\ 0 \end{array} \right) \\ \left(\begin{array}{c} \text{utxo} \\ 0 \\ 0 \\ (\emptyset, \emptyset) \\ \emptyset \\ \emptyset \\ \emptyset \\ \text{genDelegs} \\ \emptyset \\ \left(\begin{array}{c} \emptyset \\ \emptyset \\ \emptyset \end{array} \right) \\ \text{pp} \\ \text{pp} \end{array} \right) \\ \diamond \\ \emptyset \\ cs \\ \text{initNonce} \\ \text{initNonce} \\ \text{initNonce} \\ 0_{\text{seed}} \\ \text{lab} \end{array} \right) \end{array} \right)$$

where $cs = \{hk \mapsto 0 \mid (hk, _) \in \text{range genDelegs}\}$

Figure 76: Initial Shelley States

Byron to Shelley Transition

$\text{toShelley} \in \text{CEState} \rightarrow \text{GenesisDelegation} \rightarrow \text{BlockNo} \rightarrow \text{ChainState}$

$$\text{toShelley} \left(\begin{array}{c} s_{last} \\ \bar{h} \\ (utxo, reserves) \\ - \\ us \end{array} \right) gd\ bn = \text{initialShelleyState} \left(\begin{array}{c} (s_{last}\ bn, \text{prevHashToNonce } h) \\ e \\ \text{hash } h \\ utxo \\ reserves \\ gd \\ \text{overlaySchedule } e (\text{dom } gd) pp \\ pp \\ \text{prevHashToNonce } h \end{array} \right)$$

where

$$e = \text{epoch } s_{last}$$

$$pp = \text{pps } us$$

Figure 77: Byron to Shelley State Transition