

BPL_IEC_operation

Authors: Karl Johan Brink and Jan Peter Axelsson

In this notebook we show operation of a typical ion-exchange chromatography step. The impact of pH is also illustrated.

The model is based on the simplified model [1].

```
In [1]: run -i BPL_IEC_fmpy_explore.py
```

Linux - run FMU pre-compiled OpenModelica

Model for the process has been setup. Key commands:

- par() - change of parameters and initial values
- init() - change initial values only
- simu() - simulate and plot
- newplot() - make a new plot
- show() - show plot from previous simulation
- disp() - display parameters and initial values from the last simulation
- describe() - describe culture, broth, parameters, variables with value s/units

Note that both disp() and describe() takes values from the last simulation and the command process_diagram() brings up the main configuration

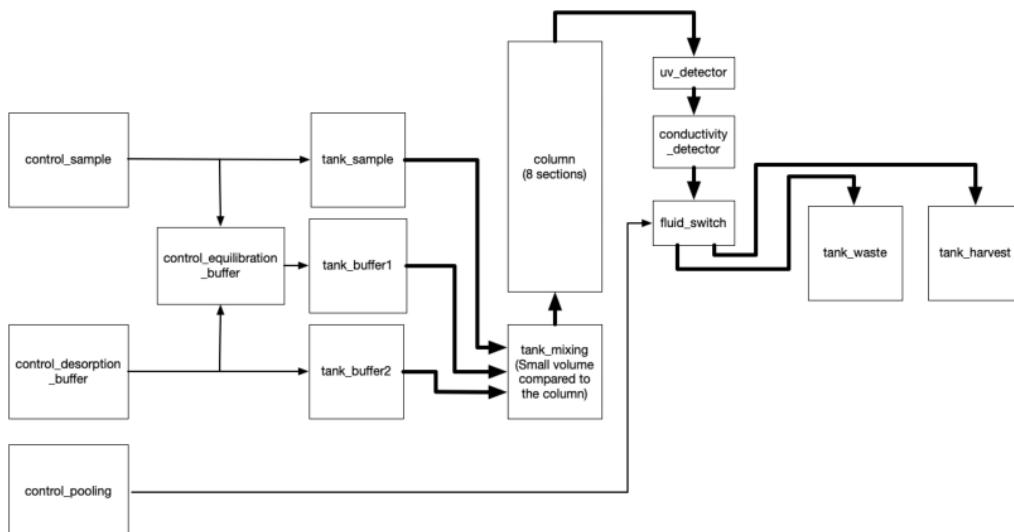
Brief information about a command by help(), eg help(simu)

Key system information is listed with the command system_info()

```
In [2]: plt.rcParams['figure.figsize'] = [30/2.54, 24/2.54]
```

```
In [3]: # The process diagram is made outside Modelica to illustrate the configuration
process_diagram()
```

No processDiagram.png file in the FMU, but try the file on disk.



1 Typical parameters an ion exchange

chromatography column step

```
In [4]: # From given column height (h) diameter (d) and linear flow rate (lfr)
# actual column volume (V) and volume flow rate (VFR) are calculated below

from numpy import pi
h = 20.0
d = 1.261
a = pi*(d/2)**2
V = h*a
print('V =', np.round(V,1), '[mL]')

lfr = 48
VFR = a*lfr/60
print('VFR =', np.round(VFR,1), '[mL/min]')

V = 25.0 [mL]
VFR = 1.0 [mL/min]
```

In []:

```
In [5]: # Sample concentration product P_in and antagonist A_in
par(P_in = 1.0)
par(A_in = 1.0)
par(E_in = 0.0)

# Column properties are described by the size and binding capacity of the
par(height = h)
par(diameter = d)
par(Q_av = 6.0)

# Resin parameters - default values used

# Remaining salt koncentration in the column from prvious batch and elimi
init(E_start = 50)

# Salt concentration of the desorption buffer
par(E_in_desorption_buffer = 8.0)

# Flow rate rate through the
par(LFR=lfr)

# Switching points during operation are conveniently described in terms o
CV_ekv = 1.0
CV_ads = 0.5
CV_wash = 1.0
CV_desorb = 3.0
CV_start_pool = 1.2
CV_stop_pool = 4.5
CV_wash2 = 2.5
par(scale_volume=True, start_adsorption=CV_ekv*V, stop_adsorption=(CV_ekv
par(start_desorption=(CV_ekv+CV_ads+CV_wash)*V, stationary_desorption=(CV_
par(stop_desorption=7.5*V)
par(start_pooling=(CV_ekv+CV_ads+CV_wash+CV_start_pool)*V, stop_pooling=(

# Simulation and plot of results
newplot(title='Illustration of operation of the chromatgraphy step', plot
simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)
```

```
- RuntimeError                                     Traceback (most recent call last)
t)
Cell In[5], line 37
    35 # Simulation and plot of results
    36 newplot(title='Illustration of operation of the chromatography ste
p', plotType='Elution-conductivity-vs-CV-combined-all')
--> 37 simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)

File /media/sf_Modelica/GitHub/Colab/BPL_IEC_operation/BPL_IEC_fmpy_explor
e.py:1233, in simu(simulationTime, mode, options, diagrams)
  1230     start_values = {parLocation[k]:parDict[k] for k in parDict.keys
()}
  1232     # Simulate
-> 1233     sim res = simulate fmu(
  1234         filename = fmu model,
  1235         validate = False,
  1236         start time = 0,
  1237         stop time = simulationTime,
  1238         output interval = simulationTime/options['ncp'],
  1239         record events = True,
  1240         start values = start values,
  1241         fmi call logger = None,
  1242         output = list(set(extract_variables(diagrams) + list(stateDi
ct.keys()) + key_variables))
  1243     )
  1245     simulationDone = True
  1247 elif mode in ['Continued', 'continued', 'cont']:

File ~/miniconda3/envs/fmpy/lib/python3.12/site-packages/fmpy/simulation.p
y:787, in simulate_fmu(filename, validate, start_time, stop_time, solver,
step_size, relative_tolerance, output_interval, record_events, fmi_type, s
tart_values, apply_default_start_values, input, output, timeout, debug_log
ging, visible, logger, fmi_call_logger, step_finished, model_description,
fmu_instance, set_input_derivatives, remote_platform, early_return_allowed
, use_event_mode, initialize, terminate, fmu_state, set_stop_time)
  785 # simulate_fmu the FMU
  786 if fmi_type == 'ModelExchange':
--> 787     result = simulateME(model description, fmu, start time, stop t
ime, solver, step size, relative tolerance, start values, apply default st
art values, input, output, output_interval, record_events, timeout, step_f
inished, validate, set_stop_time)
  788 elif fmi_type == 'CoSimulation':
  789     result = simulateCS(model description, fmu, start_time, stop_t
ime, relative_tolerance, start_values, apply_default_start_values, input,
output, output_interval, timeout, step_finished, set_input_derivatives, us
e_event_mode, early_return_allowed, validate, initialize, terminate, set_s
top_time)

File ~/miniconda3/envs/fmpy/lib/python3.12/site-packages/fmpy/simulation.p
y:1085, in simulateME(model_description, fmu, start_time, stop_time, solve
r_name, step_size, relative_tolerance, start_values, apply_default_start_v
alues, input_signals, output, output_interval, record_events, timeout, ste
p_finished, validate, set_stop_time)
  1081 input_event = isclose(next_communication_point, next_input_event_t
ime)
  1083 time_event = next_event_time_defined and isclose(next_communicatio
n_point, next_event_time)
-> 1085 state_event, roots_found, time = solver.step(time, next_communicat
```

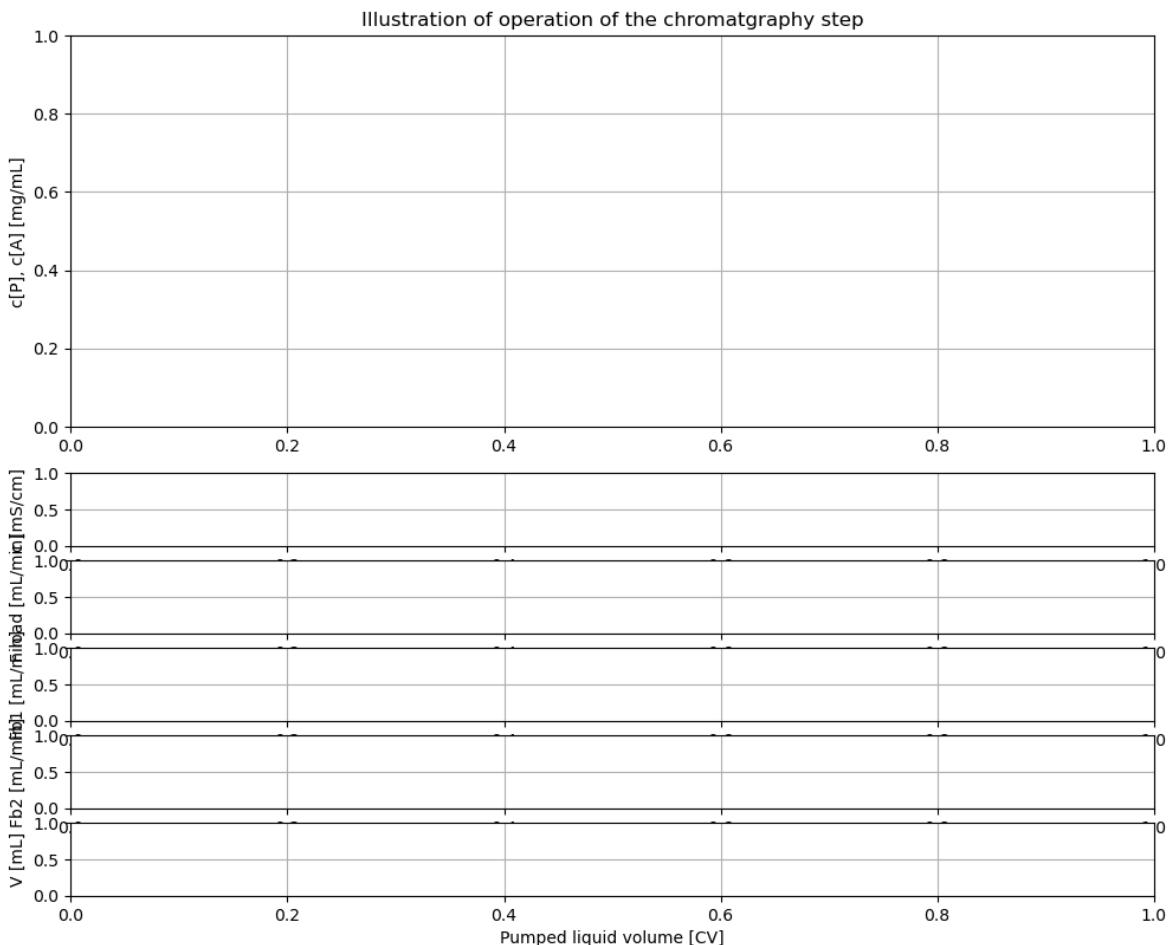
```

    ion_point)
1087 fmu.setTime(time)
1089 input.apply(time, discrete=False)

File ~/miniconda3/envs/fmpy/lib/python3.12/site-packages/fmpy/sundials/__i
nit__.py:178, in CVodeSolver.step(self, t, tNext)
    176     _assert_cv_success(CVodeGetRootInfo(self.cvode_mem, p_roots_fo
und))
177 elif flag < 0:
--> 178     raise RuntimeError("CVode error (code %s) in module %s, functi
on %s: %s" % self.error_info)
180 return flag > 0, roots_found, tret.value

```

RuntimeError: CVode error (code -3) in module CVODE, function CVode: At $t = 188.786$ and $h = 8.85619e-06$, the error test failed repeatedly or with $|h| = hmin$.



Comments of steps of operations:

1. Time: 0-1 hours - equilibration. Just to illustrate the equilibration process the first part of the column is given an initial value of salt concentration.
2. Time: 1-1.5 hours - sample is loaded on the column. The product P is adsorbed to the column and just a small amount passes through and goes to the waste. The antagonist A is much less adsorbed.
3. Time: 1.5-2.5 hours - washing 1. The column comes to equilibrium and both antagonist and product comes down to low levels.
4. Time: 2.5-5.5 hours - desorption. A linear gradient of increasing salt concentration is applied. First the antagonist and later the product comes out.
5. Time: 5.5-7.5 hours - washing 2 The column has constant salt concentration and

stationary desorption.

6. Time: 3.7-7.0 hours - pooling of product. The start- and stop of pooling are chosen with trade-off between maximizing the product pooled and minimize the amount of antagonist in the pooling.
7. Time: 7.5-8.0 hours - desorption stopped and salt is washed out and preparation of the next batch to come.

Note that step 4 and 5 is parallel to step 6.

```
In [ ]: describe_general('V', decimals=3)
```

```
parLoc = parLocation['V'] par_var = model_description.modelVariables for k in range(len(par_var)): if par_var[k].name == parLoc: try: if par_var[k].name in start_values.keys(): value = start_values[par_var[k].name] elif par_var[k].variability in ['constant', 'fixed']: value = float(par_var[k].start) elif par_var[k].variability == 'continuous': try: timeSeries = sim_res[par_var[k].name] value = timeSeries[-1] except (AttributeError, ValueError): value = None print('Variable not logged') else: value = None except NameError: print('Error: Information available after first simulation') value = None print(value)
```

```
In [ ]: model_get(parLocation['V'])
```

```
In [ ]: # Check mass-balance of P and A
P_mass = model_get('tank_harvest.m[1]') + model_get('tank_waste.m[1]')
A_mass = model_get('tank_harvest.m[2]') + model_get('tank_waste.m[2]')
print('P_mass [mg] =', P_mass)
print('A_mass [mg] =', A_mass)
```

2 The impact of the slope of the desorption gradient

```
In [ ]: # Simulations showing the impact of change of slope of the desorption gradient
newplot(title='Impact of the slope of the gradient', plotType='Elution-column')

# Same gradient as before
par(start_desorption=(CV_ekv+CV_ads+CV_wash)*V, stationary_desorption=(CV_ekv+CV_ads+CV_wash)*V)
par(stop_desorption=7.5*V)
simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)

# Gradient finishes after 0.5 of the volume
par(stationary_desorption = (CV_ekv + CV_ads + CV_wash + 0.5*CV_desorb)*V)
simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)

# Gradient finishes after 0.25 of the volume
par(stationary_desorption = (CV_ekv + CV_ads + CV_wash + 0.25*CV_desorb)*V)
simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)
```

3 The impact of salt concentration in the sample

These values should be compared with the expected value 12.5 mg, i.e. half a column volume with sample concentration 1 mg/L. The difference is due to numerical errors during simulation.

```
In [ ]: # Let us investigate the impact of increasing salt concentration in the sample

# Simulate and plot the results
newplot(title='Adsorption to the column - E_in increased', plotType='Elution')

for value in [0, 10, 20]:
    par(E_in=value)
    simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)

# Restore default values
par(k2=0.05, k4=0.3, E_in=0)
```

Note, that increased salt concentration in the sample affect binding of both proteins. During adsorption less is bound. During desorption less product P can be harvested but the fraction of antagonist A may be lowered. Thus, some product is lost but the quality in terms of purity is improved.

4 The impact of change of binding strength due to pH

There are many factors that contribute to the binding strength. A most important factor is the pH-value of the resin and the characteristic iso-electric point of the protein. The binding strength can be seen as proportional to the difference.

The binding strength of the resin is described by the quotient $K_P = k_1/k_2$ for the protein P and similarly $K_A = k_3/k_4$ for the protein A.

Below a few help-functions that describe this idea of the pH difference and its impact on binding strength in terms of the parameters k_1, k_2, k_3 , and k_4 of the protein-resin interaction.

```
In [ ]: # Define function that describe the proportionality of binding strength on
# the pH difference of the iso-electric point and the resin

def KP_pH_sensitivity(pI_P=8.0, pH_resin=7.0):
    K_P_nom = 0.0
    coeff_pH = 6.0
    return K_P_nom + coeff_pH*(pI_P-pH_resin)

def KA_pH_sensitivity(pI_A=7.1667, pH_resin=7.0):
    K_A_nom = 0.0
    coeff_pH = 1.0
    return K_A_nom + coeff_pH*(pI_A-pH_resin)

def par_pH(pI_P=8.0, pI_A=7.1667, pH_resin=7.0, TP=3.33, TA=20.0):
    if (pI_P > pH_resin) & (pI_A > pH_resin):
        par(k2 = 1/(TP*KP_pH_sensitivity(pI_P=pI_P, pH_resin=pH_resin)))
        par(k4 = 1/(TA*KA_pH_sensitivity(pI_A=pI_A, pH_resin=pH_resin)))
    else:
```

```
    print('Both pI_P > pH_resin and pI_A > pH_resin must hold - no pa
```

```
In [ ]: # The default parameters of the column
disp('column')
```

```
In [ ]: # Let us investigate the impact of change of the iso-electric pH for prot

# Simulate and plot the results
newplot(title='Adsorption to the column - increasing pI_P', plotType='Elu')

for value in [7.2, 7.6, 8.0]:
    par_pH(pI_P=value, pI_A=7.1667, pH_resin=7.0)
    simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)

# Restore default values
par(k2 = 0.05, k4 = 0.3)
```

Note, with increasing pI_P the binding of P increase which leads less loss of product during adsorption. During desorption the peak height is lower with increasing binding strength, but the total amoiumt of product P that can be harvested is higher, due to the smaller loss during adsorption.

```
In [ ]: # Let us investigate the impact of pI_P close to pH_resin

# Simulate and plot the results
newplot(title='Adsorption to the column - pI_P close to pH_resin', plotType='Elu')

for value in [7.0001]:
    par_pH(pI_P=value, pI_A=8)
    simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)

# Restore default values
par(k2=0.05, k4=0.3)
```

```
In [ ]: # Let us investigate the impact of pI_A close to pH_resin

# Simulate and plot the results
newplot(title='Adsorption to the column - pI_A close to pH_resin', plotType='Elu')

for value in [7.001]:
    par_pH(pI_P=8.0, pI_A=value)
    simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)

# Restore default values
par(k2=0.05, k4=0.3)
```

```
In [ ]: # Let us also investigate the impact of salt concentration of the desorpt

# Simulate and plot the results
newplot(title='Adsorption to the column - desorption buffer salt conc var', plotType='Elu')

for value in [8.0, 16.0]:
    par(E_in_desorption_buffer=value)
    par_pH(pI_P=8.0, pI_A=7.001, pH_resin=7.0)
    simu((CV_ekv+CV_ads+CV_wash+CV_desorb+CV_wash2)*V/VFR)

# Restore default values
```

```
par(E_in_desorption_buffer=8.0)
par(k2=0.05, k4=0.3)
```

5 Breakthrough curve often used during process development

```
In [ ]: # Experiment to check column capacity Q_av often called breakthrough curve
par(P_in=1, A_in=0, E_in=0)
init(E_start = 0)
par(Q_av=6.0)

par(scale_volume=True, start_adsorption=1*V, stop_adsorption=4.01*V)
par(start_desorption=10*V, stationary_desorption=10.5*V, stop_desorption=
par(start_pooling=11*V, stop_pooling=12*V)

newplot(title='Impact of variation in column capacity Q_av', plotType='El'
for value in [1, 2, 3, 6]: par(Q_av=value); simu(4.0*V/VFR)

# Linje för 10% UV
ax1.plot([0,4], [0.1,0.1], 'k--')

# Restore default parameters
par(Q_av=6.0, A_in=1.0)
```

With greater column capacity Q_{av} the longer it takes before the concentration of protein start to increase. Note, that the salt concenration increase initially during adsorption but then go back to low levels. This phenomenon ia also seen experimentally.

6 Summary

The simplified simulation model was found useful to describe operational aspects of ion exchange chromatography.

- The model describe qualitatively well the impact of typical operational changes in the flow rate.
- The model also describe qualtively well the impact of changes in iso-electric point of the proteins relative the pH of the resin.
- The small deviations in salt concentration from linear increase during the gradient in the salt buffer is also what you see in reality.

References

1. Månnsson, Jonas, "Control of chromatography comlumn in production scale", Master thesis TFRT-5599, Department of Automatic Control, LTH, Lund Sweden, 1998.
2. Pharmacia LKB Biotechnology. "Ion Exchange chromatography. Principles and Methods.", 3rd edition, 1991.
3. Jungbauer, Alois and Giorgio Carta, "Protein Chromatography: Process Development and Scale-Up", Wiley 2nd edition, 2020.

Appendix

```
In [6]: describe('MSL')
```

```
MSL: 4.1.0 - used components: RealInput, RealOutput, CombiTimeTable, Types
```

```
In [7]: system_info()
```

```
System information
```

```
-OS: Linux  
-Python: 3.12.11  
-Scipy: not installed in the notebook  
-FMPy: 0.3.26  
-FMU by: OpenModelica Compiler OpenModelica 1.26.0~dev-200-gcb3254b  
-FMI: 2.0  
-Type: ME  
-Name: BPL_IEC.Column_system  
-Generated: 2025-07-25T20:05:46Z  
-MSL: 4.1.0  
-Description: Bioprocess Library version 2.3.1  
-Interaction: FMU-explore for FMPy version 1.0.1
```

```
In [8]: !lsb_release -a
```

```
No LSB modules are available.  
Distributor ID: Ubuntu  
Description:    Ubuntu 24.04.3 LTS  
Release:        24.04  
Codename:       noble
```

```
In [ ]:
```