

CUDA C: RACE CONDITIONS AND ATOMICS

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OUTLINE

- Overview of race conditions and atomics
- CUDA C built-in atomic functions
- Locks and mutex
- Warps
- Appendix: the atomic dot product

Featured examples:

- `dot_product_atomic_builtin.cu`
- `dot_product_atomic_lock.cu`
- `race_condition.cu`
- `race_condition_fixed.cu`
- `blockCounter.cu`

RACE CONDITIONS AND ATOMICS

Consider the following GPU operation on integer **x**, which is stored in global memory:

x++;

which tells the GPU to do 3 things...

`x++;`

1. Read the value stored in `x`.
2. Add 1 to the value read in step 1.
3. Write the result back to `x`.

Say we need threads A and B to increment x. We want:

STEP	EXAMPLE
1. Thread A reads the value in x.	A reads 7 from x.
2. Thread A adds 1 to the value it read.	A computes 8.
3. Thread A writes the result back to x.	$x \leftarrow 8$.
4. Thread B reads the value in x.	B reads 8 from x.
5. Thread B adds 1 to the value it read.	B computes 9.
6. Thread B writes the result back to x.	$x \leftarrow 9$.

but we might get:

STEP	EXAMPLE
Thread A reads the value in x .	A reads 7 from x .
Thread B reads the value in x .	B reads 7 from x .
Thread A adds 1 to the value it read.	A computes 8.
Thread B adds 1 to the value it read.	B computes 8.
Thread A writes the result back to x .	$x \leftarrow 8$.
Thread B writes the result back to x .	$x \leftarrow 8$.

EXAMPLE: race_condition.cu

```
#include <stdio.h>
#include <stdlib.h>
#include <cuda.h>
#include <cuda_runtime.h>

__global__ void colonel( int *a_d ) {
    *a_d += 1;
}

int main() {

    int a = 0, *a_d;

    cudaMalloc(( void **) &a_d, sizeof(int));
    cudaMemcpy(a_d, &a, sizeof(int), cudaMemcpyHostToDevice);

    float elapsedTime;
    cudaEvent_t start, stop;
    cudaEventCreate(&start);
    cudaEventCreate(&stop);
```

```
    cudaEventRecord( start , 0 ) ;

    colonel<<<1000,1000>>>(a_d) ;

    cudaEventRecord( stop , 0 ) ;
    cudaEventSynchronize( stop ) ;
    cudaEventElapsedTime( &elapsedTime , start , stop ) ;
    cudaEventDestroy( start ) ;
    cudaEventDestroy( stop ) ;
    printf("GPU Time elapsed: %f seconds\n" , elapsedTime/1000.0) ;

    cudaMemcpy(&a , a_d , sizeof( int ) , cudaMemcpyDeviceToHost) ;

    printf("a = %d\n" , a) ;
    cudaFree( a_d ) ;

}
```

```
[landau@impact1 race_condition]$ make  
nvcc race_condition.cu -o race_condition  
[landau@impact1 race_condition]$ ./race_condition  
GPU Time elapsed: 0.000148 seconds  
a = 88  
[landau@impact1 race_condition]$ |
```

Since we started with **a** at 0, we should have gotten **a** $= 1000 \cdot 1000 = 1,000,000$.

Race Condition: A computational hazard that arises when the results of a program depend on the timing of uncontrollable events, such as threads.

Atomic Operation: A command that is executed one thread at a time, thus avoiding a race condition.

To avoid the race condition in our example, we atomically add 1 to `*a_d`:

```
atomicAdd( a_d, 1 );
```

instead of using `*a_d += 1;`

EXAMPLE: race_condition_fixed.cu

```
#include <stdio.h>
#include <stdlib.h>
#include <cuda.h>
#include <cuda_runtime.h>

__global__ void colonel( int *a_d ){
    atomicAdd( a_d , 1 );
}

int main( ){

    int a = 0 , *a_d ;

    cudaMalloc(( void **) &a_d , sizeof(int));
    cudaMemcpy(a_d , &a , sizeof(int) , cudaMemcpyHostToDevice);

    float elapsedTime;
    cudaEvent_t start , stop ;
    cudaEventCreate(&start);
    cudaEventCreate(&stop);
```

```
    cudaEventRecord( start , 0 ) ;

    colonel<<<1000,1000>>>(a_d) ;

    cudaEventRecord( stop , 0 ) ;
    cudaEventSynchronize( stop ) ;
    cudaEventElapsedTime( &elapsedTime , start , stop ) ;
    cudaEventDestroy( start ) ;
    cudaEventDestroy( stop ) ;
    printf("GPU Time elapsed: %f seconds\n" , elapsedTime/1000.0) ;

    cudaMemcpy(&a , a_d , sizeof( int ) , cudaMemcpyDeviceToHost) ;

    printf("a = %d\n" , a) ;
    cudaFree( a_d ) ;

}
```

```
[landau@impact1 race_condition_fixed]$ make
nvcc race_condition_fixed.cu -arch sm_20 -o race_condition_fixed
[landau@impact1 race_condition_fixed]$ ./race_condition_fixed
GPU Time elapsed: 0.014850 seconds
a = 1000000
[landau@impact1 race_condition_fixed]$
```

We got the right answer, but the execution time was far longer?
Why?

THINGS TO NOTE

- The code slowed down because that the additions happened sequentially instead of simultaneously.
- If you're using any of the above functions in your code, compile with the flag, `-arch sm_20` as above. (Atomics support floating point operations only for CUDA “compute capability” 2.0. and above.)

LIST OF CUDA C BUILT-IN ATOMIC FUNCTIONS

atomicAdd()

atomicSub()

atomicMin()

atomicMax()

atomicInc()

atomicDec()

atomicExch()

atomicCAS()

For documentation, refer to the CUDA C Programming Guide

(http://developer.download.nvidia.com/compute/DevZone/docs/html/C/doc/CUDA_C_Programming_Guide.pdf).

```
int atomicAdd(int* address, int val);
unsigned int atomicAdd(unsigned int* address,
                      unsigned int val);
unsigned long long int atomicAdd(unsigned long long int* address,
                                 unsigned long long int val);
float atomicAdd(float* address, float val);
```

reads the 32-bit or 64-bit word **old** located at the address **address** in global or shared memory, computes **(old + val)**, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

```
--  
int atomicSub(int* address, int val);  
unsigned int atomicSub(unsigned int* address,  
                      unsigned int val);
```

reads the 32-bit word **old** located at the address **address** in global or shared memory, computes **(old - val)**, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

```
int atomicExch(int* address, int val);
unsigned int atomicExch(unsigned int* address,
                      unsigned int val);
unsigned long long int atomicExch(unsigned long long int* address,
                                  unsigned long long int val);
float atomicExch(float* address, float val);
```

reads the 32-bit or 64-bit word **old** located at the address **address** in global or shared memory and stores **val** back to memory at the same address. These two operations are performed in one atomic transaction. The function returns **old**.

```
--  
int atomicMin(int* address, int val);  
unsigned int atomicMin(unsigned int* address,  
                      unsigned int val);
```

reads the 32-bit word **old** located at the address **address** in global or shared memory, computes the minimum of **old** and **val**, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

```
--  
int atomicMax(int* address, int val);  
unsigned int atomicMax(unsigned int* address,  
                      unsigned int val);
```

reads the 32-bit word **old** located at the address **address** in global or shared memory, computes the maximum of **old** and **val**, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

```
--  
unsigned int atomicInc(unsigned int* address,  
                      unsigned int val);
```

reads the 32-bit word **old** located at the address **address** in global or shared memory, computes $((\text{old} \geq \text{val}) ? 0 : (\text{old}+1))$, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

```
unsigned int atomicDec(unsigned int* address,  
                      unsigned int val);
```

reads the 32-bit word **old** located at the address **address** in global or shared memory, computes $((\text{old} == 0) \mid (\text{old} > \text{val})) ? \text{val} : (\text{old}-1)$, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

```
int atomicCAS(int* address, int compare, int val);
unsigned int atomicCAS(unsigned int* address,
                      unsigned int compare,
                      unsigned int val);
unsigned long long int atomicCAS(unsigned long long int* address,
                                 unsigned long long int compare,
                                 unsigned long long int val);
```

reads the 32-bit or 64-bit word **old** located at the address **address** in global or shared memory, computes (**old == compare ? val : old**), and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old** (Compare And Swap).

```
int atomicAnd(int* address, int val);
unsigned int atomicAnd(unsigned int* address,
                      unsigned int val);
```

reads the 32-bit word **old** located at the address **address** in global or shared memory, computes **(old & val)**, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

```
int atomicOr(int* address, int val);
unsigned int atomicOr(unsigned int* address,
                     unsigned int val);
```

reads the 32-bit word **old** located at the address **address** in global or shared memory, computes **(old | val)**, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

```
int atomicXor(int* address, int val);
unsigned int atomicXor(unsigned int* address,
                      unsigned int val);
```

reads the 32-bit word **old** located at the address **address** in global or shared memory, computes **(old ^ val)**, and stores the result back to memory at the same address. These three operations are performed in one atomic transaction. The function returns **old**.

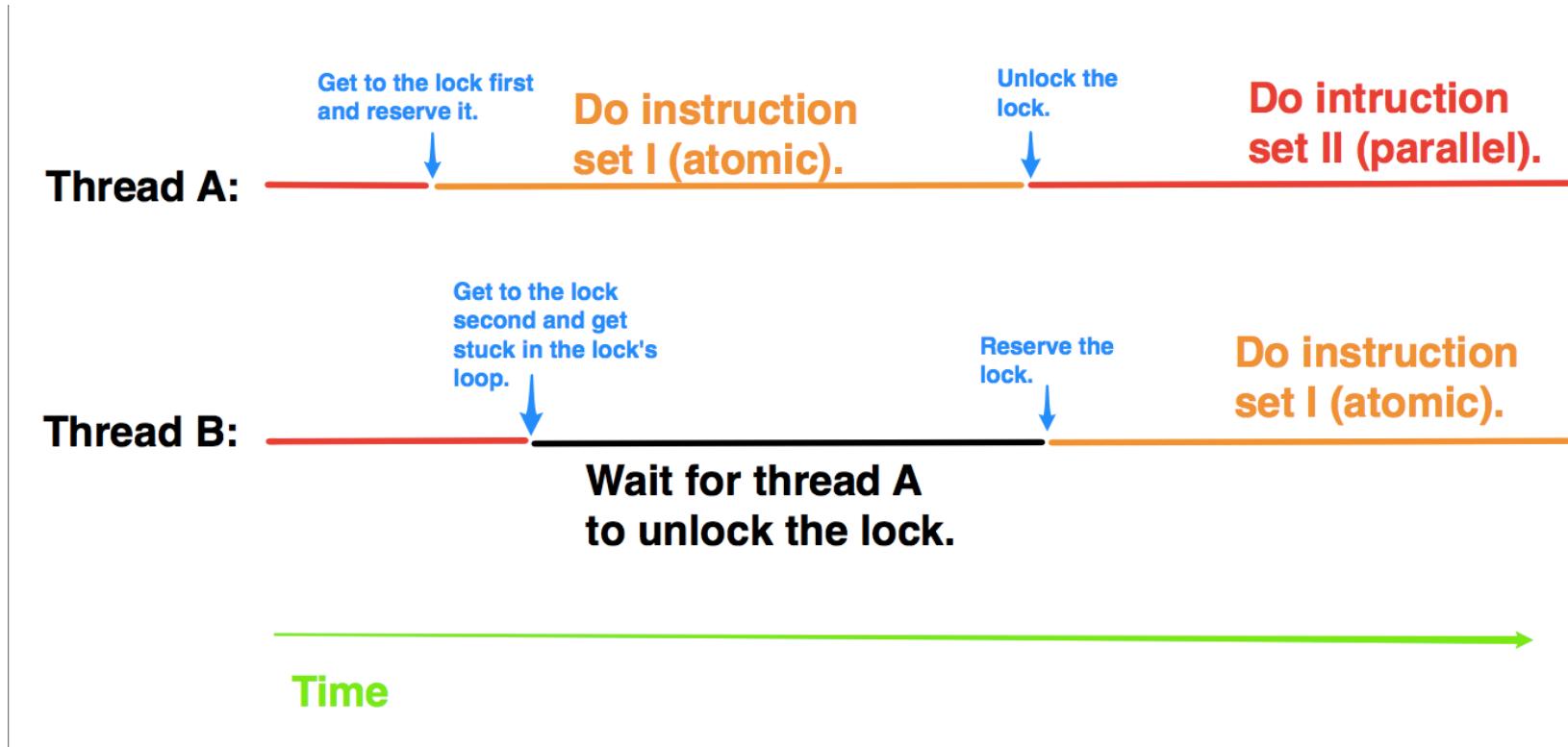
LOCKS

Lock: a mechanism in parallel computing that forces an entire segment of code to be executed atomically.

mutex: short for “mutual exclusion”, the idea behind locks: while a thread is running code inside a lock, it blocks all other threads from running the code.

THE CONCEPT

```
--global-- void someKernel( void ){  
    // some parallel code  
  
    Lock mylock;  
    mylock.lock();  
  
    // some sequential code  
  
    mylock.unlock();  
  
    // some parallel code  
}
```



lock.h:

```
struct Lock {
    int *mutex;
    Lock( void ) {
        int state = 0;
        HANDLE_ERROR( cudaMalloc( (void**)& mutex,
                                sizeof(int) ) );
        HANDLE_ERROR( cudaMemcpy( mutex, &state, sizeof(int),
                                cudaMemcpyHostToDevice ) );
    }

    ~Lock( void ) {
        cudaFree( mutex );
    }

    __device__ void lock( void ) {
        while( atomicCAS( mutex, 0, 1 ) != 0 );
    }

    __device__ void unlock( void ) {
        atomicExch( mutex, 0 );
    }
};
```

Now, let's look at the lock function:

```
--device__ void lock( void ) {
    while( atomicCAS( mutex, 0, 1 ) != 0 );
}
```

In pseudo-code:

```
--device__ void lock( void ) {
repeat{
    do atomically{

        if(mutex == 0){
            mutex = 1;
            return_value = 0;
        }

        else if(mutex == 1){
            return_value = 1;
        }

    } // do atomically

    if(return_value = 0)
        exit loop;

} // repeat
}// lock
```

EXAMPLE: COUNTING THE NUMBER OF BLOCKS

Compare these two kernels, both of which attempt to count the number of spawned blocks:

```
--global__ void blockCounterUnlocked( int *nblocks ){
    if(threadIdx.x == 0){
        *nblocks = *nblocks + 1;
    }
}

--global__ void blockCounter1( Lock lock , int *nblocks ){
    if(threadIdx.x == 0){
        lock.lock();
        *nblocks = *nblocks + 1;
        lock.unlock();
    }
}
```

Which one gives us the correct answer?

Which one is faster?

blockCounter.cu

```
#include "../common/lock.h"
#define NBLOCKS_TRUE 512
#define NTHREADS_TRUE 512 * 2

__global__ void blockCounterUnlocked( int *nbblocks ){
    if(threadIdx.x == 0){
        *nbblocks = *nbblocks + 1;
    }
}

__global__ void blockCounter1( Lock lock, int *nbblocks ){
    if(threadIdx.x == 0){
        lock.lock();
        *nbblocks = *nbblocks + 1;
        lock.unlock();
    }
}
```

```
int main(){
    int nblocks_host, *nblocks_dev;
    Lock lock;
    float elapsedTime;
    cudaEvent_t start, stop;

    cudaMalloc((void**) &nblocks_dev, sizeof(int));

    //blockCounterUnlocked:

    nblocks_host = 0;
    cudaMemcpy( nblocks_dev, &nblocks_host, sizeof(int), cudaMemcpyHostToDevice );

    cudaEventCreate(&start);
    cudaEventCreate(&stop);
    cudaEventRecord( start, 0 );

    blockCounterUnlocked<<<NBLOCKS_TRUE, NTHREADS_TRUE>>>(nblocks_dev);

    cudaEventRecord( stop, 0 );
    cudaEventSynchronize( stop );
    cudaEventElapsedTime( &elapsedTime, start, stop );
```

```
cudaEventDestroy( start );
cudaEventDestroy( stop );

cudaMemcpy( &nblocks_host, nblocks_dev, sizeof(int), cudaMemcpyDeviceToHost );
printf("blockCounterUnlocked <<< %d, %d >>> () counted %d blocks in %f ms.\n",
       NBLOCKS_TRUE,
       NTHREADS_TRUE,
       nblocks_host,
       elapsedTime);

//blockCounter1:

nblocks_host = 0;
cudaMemcpy( nblocks_dev, &nblocks_host, sizeof(int), cudaMemcpyHostToDevice );

cudaEventCreate(&start);
cudaEventCreate(&stop);
cudaEventRecord( start, 0 );

blockCounter1<<<NBLOCKS_TRUE, NTHREADS_TRUE>>>(lock, nblocks_dev);

cudaEventRecord( stop, 0 );
cudaEventSynchronize( stop );
```

```
cudaEventElapsedTime( &elapsedTime, start, stop );

cudaEventDestroy( start );
cudaEventDestroy( stop );

cudaMemcpy( &nblocks_host, nblocks_dev, sizeof(int), cudaMemcpyDeviceToHost );
printf("blockCounter1 <<< %d, %d >>> () counted %d blocks in %f ms.\n",
       NBLOCKS_TRUE,
       NTHREADS_TRUE,
       nblocks_host,
       elapsedTime);

cudaFree(nblocks_dev);
}
```

```
[landau@impact1 blockCounter]$ nvcc blockCounter.cu -arch sm_20 -o blockCounter
[landau@impact1 blockCounter]$ ./blockCounter
blockCounterUnlocked <<< 512, 1024 >>> () counted 47 blocks in 0.057920 ms.
blockCounter1 <<< 512, 1024 >>> () counted 512 blocks in 0.636864 ms.
[landau@impact1 blockCounter]$
[landau@impact1 blockCounter]$ ./blockCounter
blockCounterUnlocked <<< 512, 1024 >>> () counted 51 blocks in 0.052288 ms.
blockCounter1 <<< 512, 1024 >>> () counted 512 blocks in 0.638304 ms.
[landau@impact1 blockCounter]$
[landau@impact1 blockCounter]$ ./blockCounter
blockCounterUnlocked <<< 512, 1024 >>> () counted 47 blocks in 0.052096 ms.
blockCounter1 <<< 512, 1024 >>> () counted 512 blocks in 0.640768 ms.
[landau@impact1 blockCounter]$ |
```

**WITH MORE THAN 1 THREAD PER BLOCK,
THIS KERNEL WILL MAKE YOUR PROGRAM
PAUSE INDEFINITELY**

```
--global__ void blockCounter2( Lock lock, int *nblocks ){
    lock.lock();
    if(threadIdx.x == 0){
        *nblocks = *nblocks + 1 ;
    }
    lock.unlock();
}
```

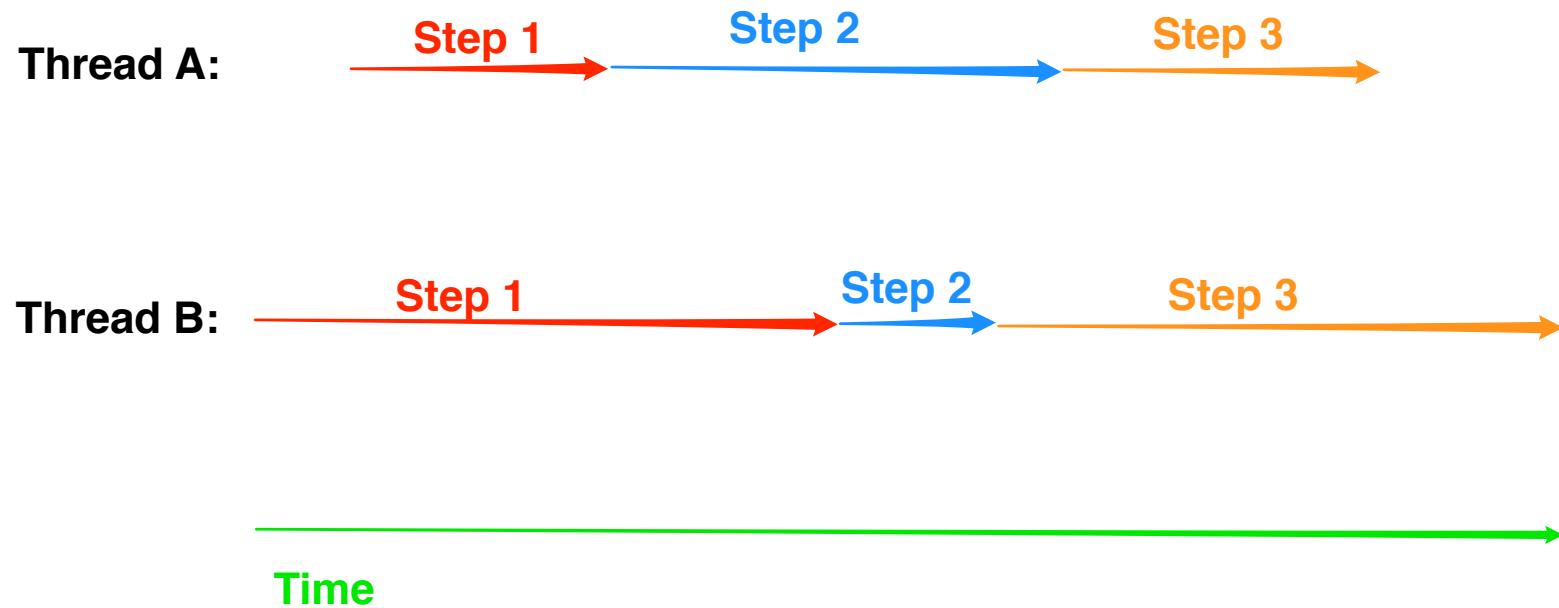
WHY? BECAUSE OF WARPS!

Each block is divided into groups of 32 threads called warps.

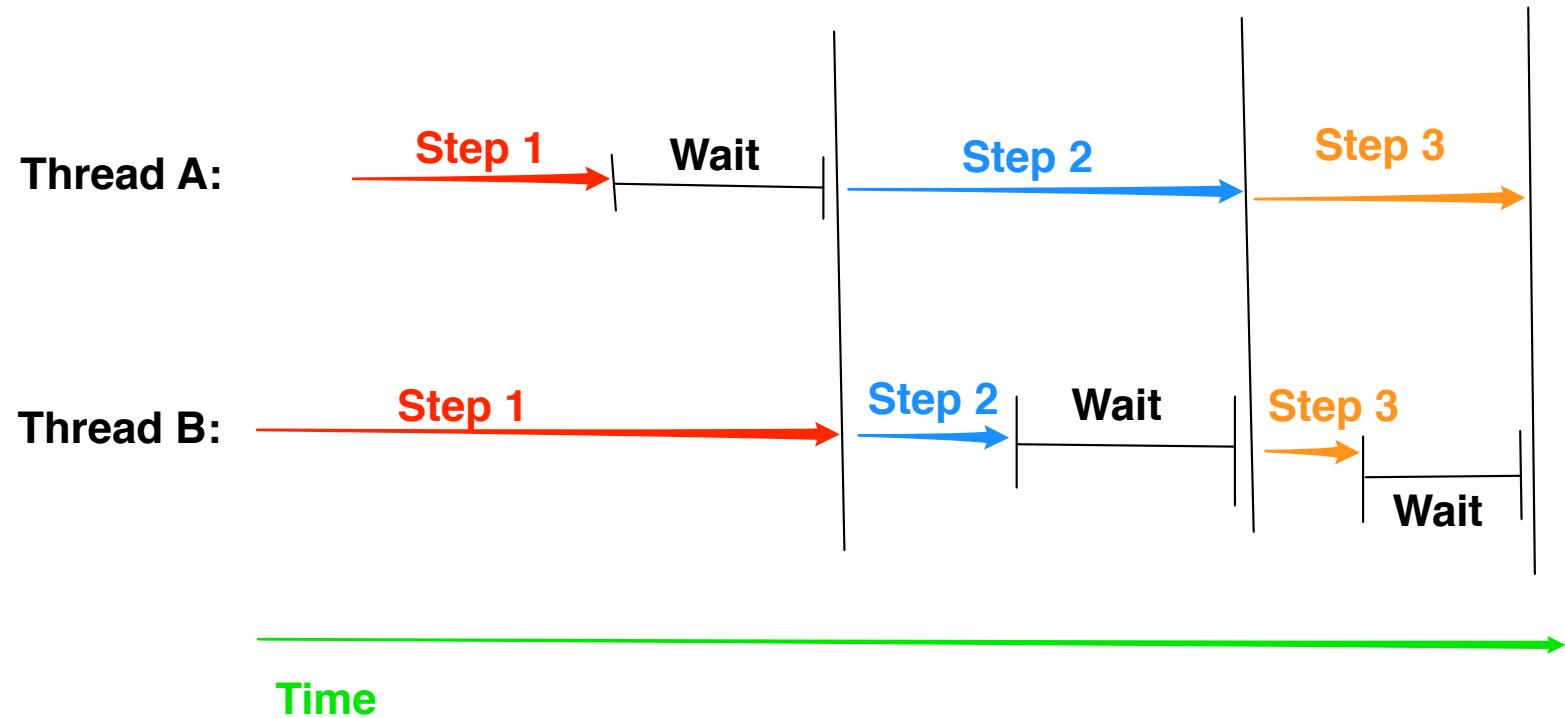
Warp: a group of 32 threads that execute together in lockstep: that is, all threads in the warp synchronize after every single step.

Imagine that a warp is saturated with calls to `__synchThreads()`.

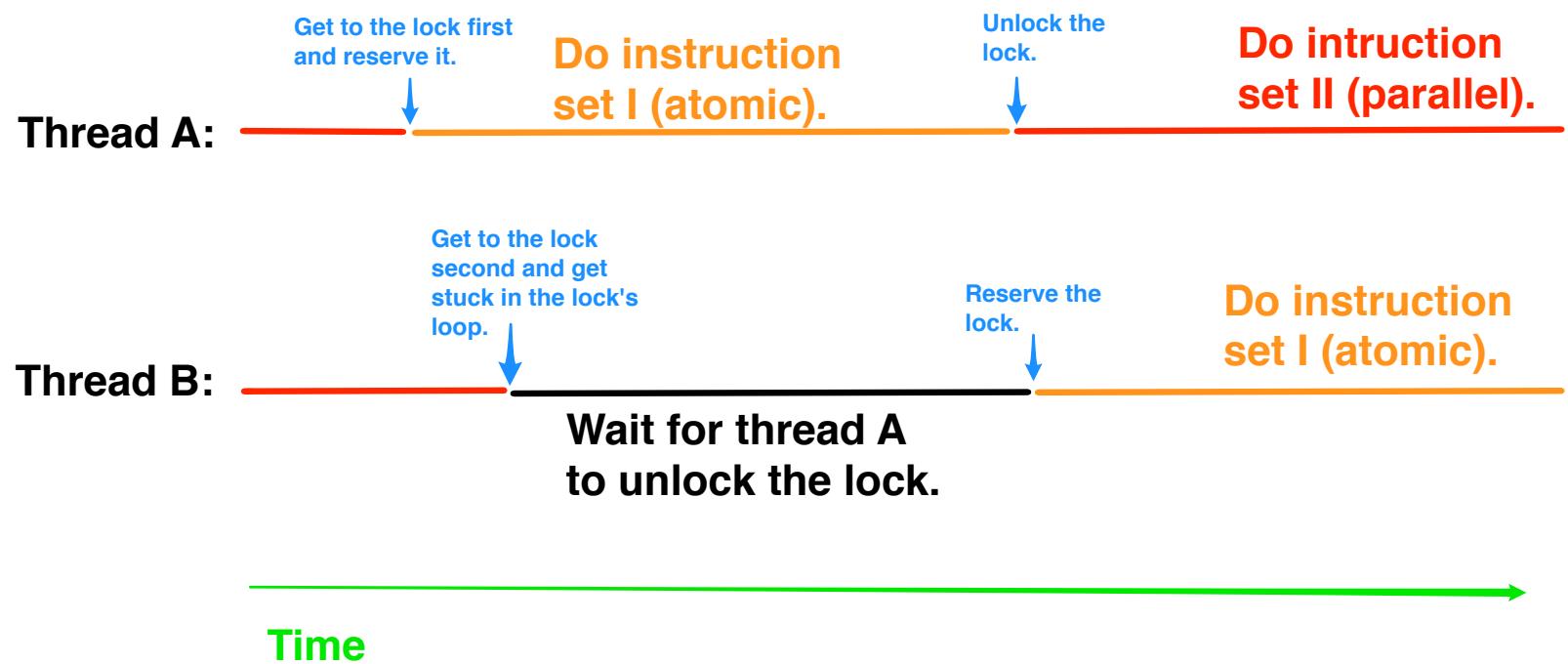
Threads in different warps:



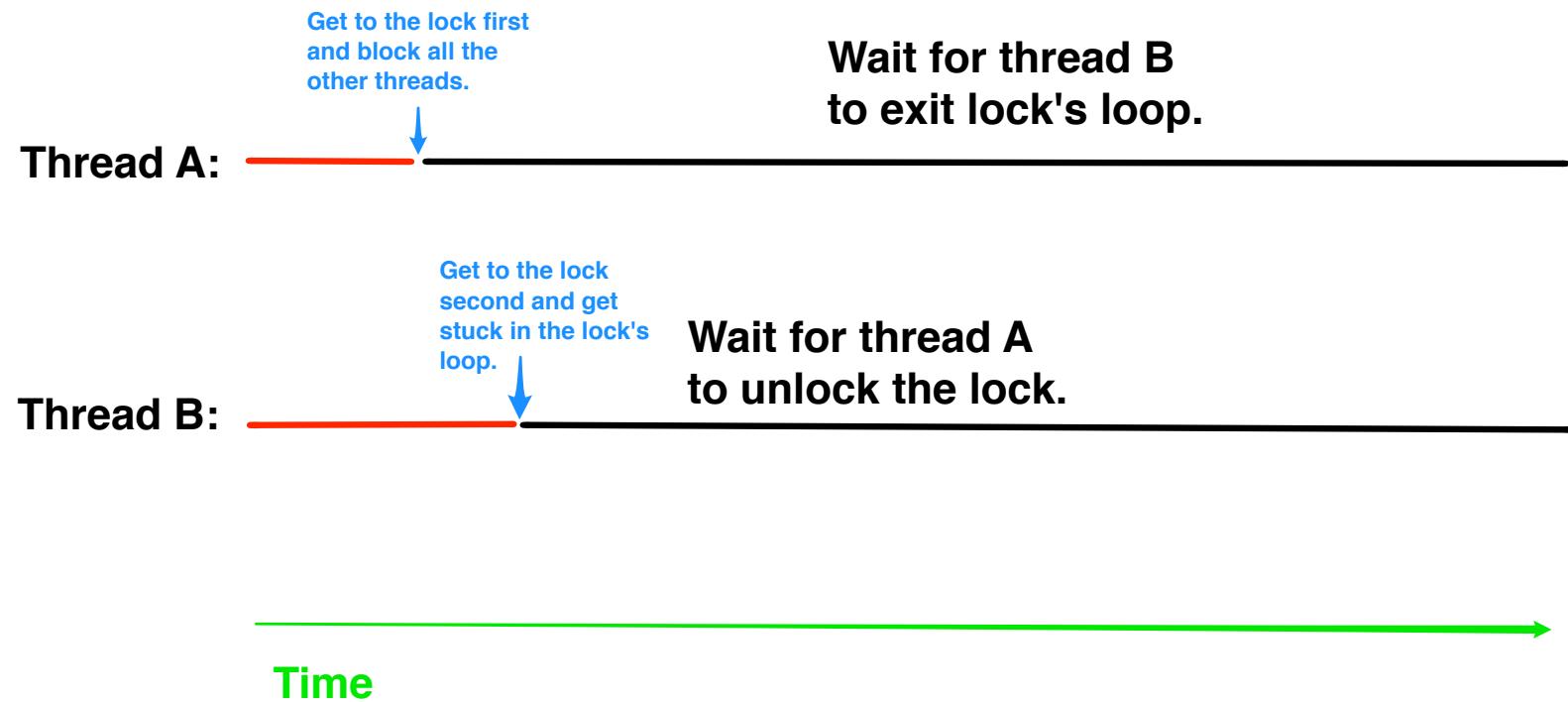
Threads in the same warp:



Threads in different warps:



Threads in the same warp:



KEEP TO THE SINGLE INSTRUCTION MULTIPLE DATA PARADIGM AS MUCH AS POSSIBLE

- Race conditions are difficult to debug.
- Atomics are sequential, and therefore slow.
- Locks are tricky, and may cause your programs to pause indefinitely.

OUTLINE

- Race conditions and atomics
- CUDA C built-in atomic functions
- Locks and mutex
- Warps
- Appendix: the atomic dot product

Featured examples:

- `dot_product_atomic_builtin.cu`
- `dot_product_atomic_lock.cu`
- `race_condition.cu`
- `race_condition_fixed.cu`
- `blockCounter.cu`

LECTURE SERIES MATERIALS

These lecture slides, a tentative syllabus for the whole lecture series, and code are available at:

<https://github.com/wlandau/gpu>.

After logging into you home directory on impact1, type:

```
git clone https://github.com/wlandau/gpu
```

into the command line to download all the course materials.

REFERENCES

NVIDIA CUDA C Programming Guide. Version 3.2.
2010.

J. Sanders and E. Kandrot. *CUDA by Example*.
Addison-Wesley, 2010.

APPENDIX: THE ATOMIC DOT PRODUCT

$$(a_0, a_1, \dots, a_{15}) \bullet (b_0, b_1, \dots, b_{15}) = a_0b_0 + a_1b_1 + \dots + a_{15}b_{15}$$

The basic workflow is:

- Pass vectors **a** and **b** to the GPU.
- Give each block a sub vector of **a** and the analogous subvector of **b**.

For the case of 16-element vectors, let there be 2 blocks and 4 threads per block.

Block 0 works on:

$$\begin{aligned}(a_0, a_1, a_2, a_3, a_8, a_9, a_{10}, a_{11}) \\ (b_0, b_1, b_2, b_3, b_8, b_9, b_{10}, b_{11})\end{aligned}$$

Block 1 works on:

$$\begin{aligned}(a_4, a_5, a_6, a_7, a_{12}, a_{13}, a_{14}, a_{15}) \\ (b_4, b_5, b_6, b_7, b_{12}, b_{13}, b_{14}, b_{15})\end{aligned}$$

- Within each block, compute a vector of partial sums of pairwise products:

Block 0:

$$\text{cache} = (a_0 \cdot b_0 + a_8 \cdot b_8, a_1 \cdot b_1 + a_9 \cdot b_9, \dots, a_3 \cdot b_3 + a_{11} \cdot b_{11})$$

Block 1:

$$\text{cache} = (a_4 \cdot b_4 + a_{12} \cdot b_{12}, a_5 \cdot b_5 + a_{13} \cdot b_{13}, \dots, a_7 \cdot b_7 + a_{15} \cdot b_{15})$$

where `cache` is an array in shared memory.

- Within each block, compute the pairwise sum of `cache` and write it to `cache[0]`. In our example:

Block 0:

$$\text{cache}[0] = a_0 \cdot b_0 + \cdots + a_3 \cdot b_3 + a_8 \cdot b_8 + \cdots + a_{11} \cdot b_{11}$$

Block 1:

$$\text{cache}[0] = a_4 \cdot b_4 + \cdots + a_7 \cdot b_7 + a_{12} \cdot b_{12} + \cdots + a_{15} \cdot b_{15}$$

SKIP THESE STEPS:

- Fill a new vector in global memory, `partial_c`, with these partial dot products:

$$\text{partial_c} = (\text{block 0 cache}[0], \text{block 1 cache}[0])$$

- Return to the CPU and compute the linear sum of `partial_c` and write it to `partial_c[0]`. Then:

$$\text{partial_c}[0] = a_0 \cdot b_0 + a_1 \cdot b_1 + \cdots + a_{15} \cdot b_{15}$$

INSTEAD:

- Within `dot()`, ATOMICALLY ADD each block's copy of `cache[0]` to the integer `c`. Then:

$$c = a_0 \cdot b_0 + a_1 \cdot b_1 + \cdots + a_{15} \cdot b_{15}$$

dot_product_atomic_builtin.cu

```
#include "../common/book.h"
#include "../common/lock.h"

#define imin(a,b) (a<b?a:b)

// NOTE: COMPILE LIKE THIS:
//nvcc dot_product_atomic.cu -arch sm_20 -o dot_product_atomic

const int N = 32 * 1024 * 1024;
const int threadsPerBlock = 256;
const int blocksPerGrid =
    imin( 32, (N+threadsPerBlock-1) / threadsPerBlock );

__global__ void dot( Lock lock, float *a,
                     float *b, float *c ) {

    __shared__ float cache[threadsPerBlock];
    int tid = threadIdx.x + blockIdx.x * blockDim.x;
    int cacheIndex = threadIdx.x;

    float temp = 0;
    while (tid < N) {
```

```

        temp += a[ tid ] * b[ tid ];
        tid += blockDim.x * gridDim.x;
    }

    // set the cache values
    cache[ cacheIndex ] = temp;

    // synchronize threads in this block
    __syncthreads();

    // for reductions, threadsPerBlock must be a power of 2
    // because of the following code
    int i = blockDim.x/2;
    while ( i != 0 ) {
        if ( cacheIndex < i )
            cache[ cacheIndex ] += cache[ cacheIndex + i ];
        __syncthreads();
        i /= 2;
    }

    // Here's where we use atomic addition:
    if ( cacheIndex == 0 ) {
        atomicAdd( c, cache[ 0 ] );
    }
}

```

```
}
```

```
int main( void ) {
    float *a, *b, c = 0;
    float *dev_a, *dev_b, *dev_c;

    // allocate memory on the CPU side
    a = ( float * ) malloc( N * sizeof( float ) );
    b = ( float * ) malloc( N * sizeof( float ) );

    // allocate the memory on the GPU
    HANDLEERROR( cudaMalloc( ( void ** ) & dev_a,
                           N * sizeof( float ) ) );
    HANDLEERROR( cudaMalloc( ( void ** ) & dev_b,
                           N * sizeof( float ) ) );
    HANDLEERROR( cudaMalloc( ( void ** ) & dev_c,
                           sizeof( float ) ) );

    // fill in the host memory with data
    for ( int i = 0; i < N; i++ ) {
        a[ i ] = i;
        b[ i ] = i * 2;
    }
```

```

// copy the arrays 'a' and 'b' to the GPU
HANDLEERROR( cudaMemcpy( dev_a , a , N*sizeof( float ) ,
                      cudaMemcpyHostToDevice ) );
HANDLEERROR( cudaMemcpy( dev_b , b , N*sizeof( float ) ,
                      cudaMemcpyHostToDevice ) );
HANDLEERROR( cudaMemcpy( dev_c , &c , sizeof( float ) ,
                      cudaMemcpyHostToDevice ) );

Lock lock;
dot<<<blocksPerGrid , threadsPerBlock>>>( lock , dev_a ,
                                              dev_b , dev_c ) ;

// copy c back from the GPU to the CPU
HANDLEERROR( cudaMemcpy( &c , dev_c ,
                      sizeof( float ) ,
                      cudaMemcpyDeviceToHost ) );

#define sum_squares(x) (x*(x+1)*(2*x+1)/6)
printf( "Does GPU value %.6g = %.6g?\n" , c ,
        2 * sum_squares( (float)(N - 1) ) ) ;

// free memory on the GPU side
cudaFree( dev_a );
cudaFree( dev_b );

```

```
    cudaFree( dev_c ) ;

    // free memory on the CPU side
    free( a );
    free( b );
}
```

OUTPUT

```
[landau@impact1 dot_product_atomic_builtin]$ nvcc  
dot_product_atomic_builtin.cu -arch sm_20 -o dot  
[landau@impact1 dot_product_atomic_builtin]$ ./dot  
Does GPU value 2.76217e+22 = 2.76217e+22?  
[landau@impact1 dot_product_atomic_builtin]$
```

Again, if you're using any of the above functions in your code, compile with the flag, **-arch sm_20** as above.

dot_product_atomic_lock.cu: THE ATOMIC DOT PRODUCT WITH LOCKS

```
#include "common/book.h"
#include "common/lock.h"

#define imin(a,b) (a<b?a:b)

// NOTE: COMPILE LIKE THIS:
//nvcc dot_product_atomic.cu -arch sm_20 -o dot_product_atomic

const int N = 32 * 1024 * 1024;
const int threadsPerBlock = 256;
const int blocksPerGrid =
    imin( 32, (N+threadsPerBlock-1) / threadsPerBlock );

__global__ void dot( Lock lock , float *a,
                     float *b, float *c ) {

    __shared__ float cache[threadsPerBlock];
    int tid = threadIdx.x + blockIdx.x * blockDim.x;
    int cacheIndex = threadIdx.x;
```

```

float temp = 0;
while (tid < N) {
    temp += a[tid] * b[tid];
    tid += blockDim.x * gridDim.x;
}

// set the cache values
cache[cacheIndex] = temp;

// synchronize threads in this block
__syncthreads();

// for reductions, threadsPerBlock must be a power of 2
// because of the following code
int i = blockDim.x/2;
while (i != 0) {
    if (cacheIndex < i)
        cache[cacheIndex] += cache[cacheIndex + i];
    __syncthreads();
    i /= 2;
}

// Here's where locks come in:

```

```

    if (cacheIndex == 0) { lock.lock();
        *c += cache[0];
        lock.unlock();
    }
}

int main( void ) {
    float *a, *b, c = 0;
    float *dev_a, *dev_b, *dev_c;

    // allocate memory on the CPU side
    a = (float*)malloc( N*sizeof(float) );
    b = (float*)malloc( N*sizeof(float) );

    // allocate the memory on the GPU
    HANDLEERROR( cudaMalloc( (void**)&dev_a,
                            N*sizeof(float) ) );
    HANDLEERROR( cudaMalloc( (void**)&dev_b,
                            N*sizeof(float) ) );
    HANDLEERROR( cudaMalloc( (void**)&dev_c,
                            sizeof(float) ) );

    // fill in the host memory with data
    for (int i=0; i<N; i++) {

```

```

    a[ i ] = i ;
    b[ i ] = i *2;
}

// copy the arrays 'a' and 'b' to the GPU
HANDLEERROR( cudaMemcpy( dev_a , a, N*sizeof( float ) ,
                        cudaMemcpyHostToDevice ) );
HANDLEERROR( cudaMemcpy( dev_b , b, N*sizeof( float ) ,
                        cudaMemcpyHostToDevice ) );
HANDLEERROR( cudaMemcpy( dev_c , &c , sizeof( float ) ,
                        cudaMemcpyHostToDevice ) );

Lock lock;
dot<<<blocksPerGrid , threadsPerBlock>>>( lock , dev_a ,
                                                dev_b , dev_c ) ;

// copy c back from the GPU to the CPU
HANDLEERROR( cudaMemcpy( &c , dev_c ,
                        sizeof( float ) ,
                        cudaMemcpyDeviceToHost ) ) ;

#define sum_squares(x) (x*(x+1)*(2*x+1)/6)
printf( "Does GPU value %.6g = %.6g?\n" , c ,
        2 * sum_squares( ( float )(N - 1) ) );

```

```
// free memory on the GPU side
cudaFree( dev_a );
cudaFree( dev_b );
cudaFree( dev_c );

// free memory on the CPU side
free( a );
free( b );
}
```

OUTPUT

```
[landau@impact1 dot_product_atomic_lock]$ nvcc  
dot_product_atomic_lock.cu -arch sm_20 -o dot  
[landau@impact1 dot_product_atomic_lock]$ ./dot  
Does GPU value 2.76217e+22 = 2.76217e+22?  
[landau@impact1 dot_product_atomic_lock]$
```

NOTE: we still need **-arch sm_20** because the lock relies on built-in atomic functions.