Assignment Two Analysis (Neural Network Gradient Descent)

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Analysis:

By implementing the multiple channel convolution nerual network, I produce a 94.83% accuracy model when testing the model by training data. To implement the model, I follow the steps proposed in the course note. First, I randomly generate 3 matrics, corresponding to the b, K, and W representing the bias, convolution matrix and weighted matrix for fully connect network. Then, I define a variable called *ite* to follow the iterations in the training process in a while loop for ite max iterations to train the parameters. During the training process, I create a random integer number every iteration and derive a randomly selected x_rand and y_rand data from set x train and set y train. Then I forward the x rand to the model (Convolution, ReLU, softMax) to get the forward x. By utilizing the backpropagation method described in the class note, I derive the derivative of objective function with respect to each parameter - b, K and W. Subtracting the multiplication of learning rate and the deepest gradient descent from model['b'], model['K'], model['W'], one iteration is finished. Learning rate is defined as 0.05 and ite max is defined as 55000 by trial and error. One thing that is important to notice is that the running time of convolution is relativly slow compared with SGD and Neural network, which usually takes 10 seconds per thought iteration. I therefore vectorize matrix to reduce the running time of whole model.

Code:

Attached in the next page.

Assignment_3_Convolution_Network

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In [ ]: import numpy as np
       import h5py
       import time
       import copy
       from random import randint
       import random
       np.set_printoptions(threshold=np.nan)
       #load MNIST data
       MNIST_data = h5py.File('data.hdf5', 'r')
       x_train = np.float32(MNIST_data['x_train'][:] )
       y_train = np.int32(np.array(MNIST_data['y_train'][:,0]))
       x_test = np.float32( MNIST_data['x_test'][:] )
       y_test = np.int32( np.array( MNIST_data['y_test'][:,0] ) )
       MNIST_data.close()
       #define softmax for f(x; theta)
       def softMax(x):
           out_put = np.exp(x)/np.sum(np.exp(x),axis =0)
           return out_put
       #define ReLU fucnction that act as hidden layer in the training process.
       def ReLU(x_input):
           return x_input*(x_input>0)
       #Implementation of stochastic gradient descent algorithm
       #number of inputs
       num_inputs = 28*28
       #number of outputs
       num_outputs = 10
       #number of filter width
       width_filter = 10
       #channel of the filter
       channel = 3
       \#R(Width*d) = D-width+1
       inter_width = 28-width_filter+1
       #Initialize model dictionary
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model = \{\}
#model 'K' is convolution filter, dimension is R(width_filter*width_filter*width_filter)
model['K'] = np.random.randn(width_filter, width_filter, channel) / np.sqrt(num_inputs)
#model 'W' is the weight matrix of the single layer of fully con , dimension is R(Width*
model['W'] = np.random.randn(num_outputs, inter_width, inter_width, channel) / np.sqrt(n
#model 'b' is the layer bias, dimension is R(K)
model['b'] = np.random.randn(num_outputs)
#define learning_rate to be 0.0085 600000 0.005
learning_rate = 0.05
ite_max = 55000
for ite in range(ite_max):
    #pick a random point
   if(ite%1000==0):
       print(ite)
   rand_num = random.randint(0,len(x_train)-1)
   x_rand = x_train[rand_num].reshape(28,28)
   y_rand = y_train[rand_num]
   #Acquire the forward x by forward function
   Z = np.zeros(inter_width*inter_width*channel).reshape(inter_width,inter_width,channe
   for z_dim in range(channel):
       for y_dim in range(inter_width):
           for x_dim in range(inter_width):
               x_area = x_rand[y_dim:y_dim+width_filter,x_dim:x_dim+width_filter]
               Z[y_dim][x_dim][z_dim] = np.sum(np.multiply(x_area, model['K'][:,:,z_dim
   #Take the ReLU function
   H = ReLU(Z)
   #Get the U by a fully connected network
   U = np.zeros(num_outputs)
   for x_dim in range(num_outputs):
       U[x_{dim}] = np.sum(np.multiply(model['W'][x_{dim},:,:,:],H))+model['b'][x_{dim}]
   forward_x = softMax(U)
   #Calculate the rho with respect to U
   rho_wrt_U = np.zeros(num_outputs)
   for i in range(num_outputs):
       if i==y_rand:
           rho_wrt_U[i] = -(1-forward_x[i])
       else:
           rho_wrt_U[i] = -(-forward_x[i])
    #Calculate the delta
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for y_dim in range(inter_width):
                    for x_dim in range(inter_width):
                        delta[y_dim][x_dim][z_dim] = rho_wrt_U@model['W'][:,y_dim,x_dim,z_dim]
            #Calculate rho with respect to W
            rho_wrt_W = np.zeros(num_outputs*inter_width*inter_width*channel).reshape(num_output
            for x_dim in range(num_outputs):
                rho_wrt_W[x_dim,:,:,:] = rho_wrt_U[x_dim] * H
            #Rho with respect to b
            rho_wrt_b = rho_wrt_U
            #Calculate the derivative of Z
            der_Z = 1*(Z>1)
            #Calculate the rho with respect to K
            dot_product = np.multiply(der_Z,delta)
            rho_wrt_K = np.zeros(width_filter*width_filter*channel).reshape(width_filter,width_f
            for z_dim in range(channel):
                for y_dim in range(width_filter):
                    for x_dim in range(width_filter):
                        x_area = x_rand[y_dim:y_dim+inter_width,x_dim:x_dim+inter_width]
                        rho_wrt_K[y_dim,x_dim,z_dim] = np.sum(np.multiply(x_area, dot_product[:,:
            model['b'] = model['b'] - learning_rate*rho_wrt_b
            model['K'] = model['K'] - learning_rate*rho_wrt_K
            model['W'] = model['W'] - learning_rate*rho_wrt_W
        print("FINISH")
In [118]: #forward to get the f(x;theta)
          def forward(x_input,model):
              \#Acquire\ the\ forward\ x\ by\ forward\ function
              x_input = x_input.reshape(28,28)
              Z = np.zeros(inter_width*inter_width*channel).reshape(inter_width,inter_width,chan
              for z_dim in range(channel):
                  for y_dim in range(inter_width):
                      for x_dim in range(inter_width):
                          x_area = x_input[x_dim:x_dim+width_filter,y_dim:y_dim+width_filter]
                          Z[x_dim][y_dim][z_dim] = np.sum(np.multiply(x_area, model['K'][:,:,z_d
```

delta = np.zeros(inter_width*inter_width*channel).reshape(inter_width,inter_width,ch

for z_dim in range(channel):

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#Take the ReLU function
                 H = ReLU(Z)
                  #Get the U by a fully connected network
                 U = np.zeros(num_outputs)
                  for x_dim in range(num_outputs):
                                    \label{eq:condition} $$ U[x_dim] = np.sum(np.multiply(model['W'][x_dim,:,:,:],H)) + model['b'][x_dim] $$ $$ $$ (a) = np.sum(np.multiply(model['W'][x_dim,:,:,:],H)) + model['b'][x_dim] $$ $$ (a) = np.sum(np.multiply(model['W'][x_dim,:,:,:],H)) + model['b'][x_dim,:,:,:],H) $$ (b) = np.sum(np.multiply(model['W'][x_dim,:,:,:],H)) + model['b'][x_dim,:,:,:],H) $$ (b) = np.sum(np.multiply(model['W'][x_dim,:,:,:],H)) + model['b'][x_dim,:,:,:],H) $$ (a) = np.sum(np.multiply(model['W'][x_dim,:,:,:],H)) + model['b'][x_dim,:,:,:],H) $$ (b) = np.sum(np.multiply(model['W'][x_dim,:,:,:],H)) + model['b'][x_dim,:,:,:],H) $$ (a) = np.sum(np.multiply(model['W'][x_dim,:,:,:],H)) + model['b'][x_dim,:,:,:],H) $$ (b) = np.sum(np.multiply(model['W'][x_dim,:,:],H)) + model['b'][x_dim,:,:],H) $$ (a) = np.sum(np.multiply(model['W'][x_dim,:,:],H)) + model['U][x_dim,:,:],H) $$ (a) = np.sum(np.multiply(model['W'][x_dim,:,:],H)) + model['U][x_dim,:,:],H) $$ (a) = np.sum(np.multiply(model['W'][x_dim,:,:],H)) + model['U][x_dim,:,:],H) (a) = np.sum(np.multiply(model['W'][x_dim,:],H)) + model['U][x_dim,:,:],H) (a) = np.sum(np.multiply(model['W'][x_dim,:],H)) + model['U][x_dim,:],H) (a) = np.sum(np.multiply(model['W'][x_dim,:],H)) + model['U][x_dim,:],H) (a) = np.sum(np.multiply(model['W'][x_dim,:],H)) + np.sum(np.multiply(model['W'][x_d
                  forward_x = softMax(U)
                 return forward_x
 #test data
total_correct = 0
for n in range(len(x_test)):
                  if (n\%1000==0):
                                  print(n)
                 y = y_test[n]
                 x = x_test[n][:]
                 p = forward(x, model)
                 prediction = np.argmax(p)
                  if (prediction == y):
                                   total_correct += 1
print(total_correct/np.float(len(x_test) ) )
print("FINISH")
```

0.9483 FINISH