Data Analysis and Unsupervised Learning A tour of the tidyverse

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École Polytechnique, Autumn semester, 2020-2021

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Outline

- 1 Introduction
- 2 Structures and types: tibble, forcats, stringr
- 3 data wrangling: readr, tidyr, dplyr
- 4 Manipulation: magrittr, purrr
- **5** Visualization: ggplot2

References

Many ideas/examples inspired/stolen there:

R for data science (Wickham & Grolemund, 2017), http://r4ds.had.co.nz



Tidyverse website, https://www.tidyverse.org/

Core packages



Prerequisites

Data Structures in base R

- 1 Atomic vector (integer, double, logical, character)
- Recursive vector (list)
- § Factor
- Matrix and array
- 6 Data Frame

R base programming

- Control Statements (if/then/else, while, for)
- ② Functions
- § Functionals ([x]apply)
- Input/output (read.[x]/write.[x])
- 6 Rstudio IDE

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- 5 Visualization: ggplot2

Tidy data: motivation

Collected data are (never) under a proper canonical format

"Happy families are all alike; every unhappy family is unhappy in its own way." – Leo Tolstoy

"Tidy datasets are all alike, but every messy dataset is messy in its own way." - Hadley Wickham 1

¹Rstudio's chief scientific advisor

Tidy data: what?

First, a subjective question

What is the observation/statistical unit in your data?

Definition

Tidy data is a standard way of mapping the meaning of a dataset to its structure. A dataset is messy or tidy depending on how rows, columns and tables are matched up with observations, variables and types.

In tidy data,

- 1 each variable forms a column,
- 2 each observation forms a row,
- 3 each observational unit have its own cell

Tidy data: why?

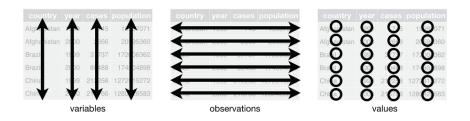


Figure 1: Tidy data

- make manipulation, visualization and modelling easier
- a common structure for all packages
- a philosophy for data representation (beyond the R framework)

Tidy or not?

tidyr::table3

Tidy or not?

tidyr::table2

```
# A tibble: 12 x 4
##
     country
                 year type
##
      <chr>
                 <int> <chr>
                                        <int>
    1 Afghanistan 1999 cases
                                          745
   2 Afghanistan 1999 population
                                   19987071
##
##
    3 Afghanistan 2000 cases
                                         2666
   4 Afghanistan 2000 population 20595360
##
##
   5 Brazil
                   1999 cases
                                        37737
##
    6 Brazil
                   1999 population
                                   172006362
                                        80488
##
  7 Brazil
                   2000 cases
   8 Brazil
                   2000 population
                                   174504898
   9 China
                   1999 cases
                                       212258
  10 China
                   1999 population 1272915272
  11 China
                   2000 cases
                                       213766
## 12 China
                   2000 population 1280428583
```

Tidy or not?

tidyr::table1

```
## # A tibble: 6 x 4
##
    country year cases population
    <chr>
               <int> <int>
##
                           <int>
## 1 Afghanistan
               1999 745
                           19987071
  2 Afghanistan
                2000 2666 20595360
  3 Brazil
                1999 37737
                           172006362
## 4 Brazil
                2000
                     80488
                           174504898
               1999 212258 1272915272
## 5 China
## 6 China
                2000 213766 1280428583
```

The process of data analysis

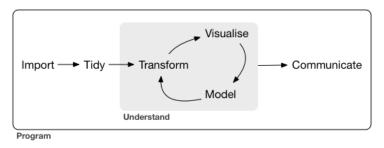


Figure 2: scheme for data analysis process

- import: read/load the data
- tidy: formating (individuals/variables data frame)
- transform: suppression/creation/filtering/selection
- visualization: representation and validation
- model: statistical fits
- communication: diffusion (web/talk/article)

The tidyverse

Definition

- contraction of 'tidy' ("well arranged) and 'universe'.
- an opinionated collection of R packages designed for data science.
- all packages share an underlying design philosophy, grammar, and data structures

Phylosophy

allows the user to focus on the important statistical questions rather than focusing on the technical aspects of data analysis

Let's have a look

The core tidyverse loads ggplot2, tibble, tidyr, readr, purrr, stringr, forecats, dplyr and others in a fancy and unconflicted way.

Tidyverse dependencies: a lot

tidyverse:::tidyverse_deps() %>% knitr::kable()

package	cran	local	behind
broom	0.7.0	0.7.0	FALSE
dbplyr	1.4.4	1.4.4	FALSE
dplyr	1.0.2	1.0.2	FALSE
forcats	0.5.0	0.5.0	FALSE
ggplot2	3.3.2	3.3.2	FALSE
haven	2.3.1	2.3.1	FALSE
hms	0.5.3	0.5.3	FALSE
httr	1.4.2	1.4.2	FALSE
jsonlite	1.7.1	1.7.1	FALSE
lubridate	1.7.9	1.7.9	FALSE
magrittr	1.5	1.5	FALSE
modelr	0.1.8	0.1.8	FALSE
pillar	1.4.6	1.4.6	FALSE
purrr	0.3.4	0.3.4	FALSE
readr	1.3.1	1.3.1	FALSE
read×l	1.3.1	1.3.1	FALSE
reprex	0.3.0	0.3.0	FALSE
rlang	0.4.7	0.4.7	FALSE
rvest	0.3.6	0.3.6	FALSE
stringr	1.4.0	1.4.0	FALSE
tibble	3.0.3	3.0.3	FALSE
tidyr	1.1.2	1.1.2	FALSE
xml2	1.3.2	1.3.2	FALSE

Packages roles and overview: types



a modern re-imagining of the data frame



a cohesive set of functions designed to make working with strings as easy as possible



a suite of useful tools that solve common problems with factors

Packages roles and overview: wrangling



a fast and friendly way to read rectangular data (like csv, tsv, ...)



a set of functions that help you get to tidy data



a consistent set of verbs that solve the most common data manipulation challenges

Packages roles and overview: manipulation



a system for declaratively creating graphics, based on The Grammar of Graphics



enhances R's functional programming (FP) toolkit



offers a set of operators which make your code more readable

Data analysis with the tidyverse (v1)

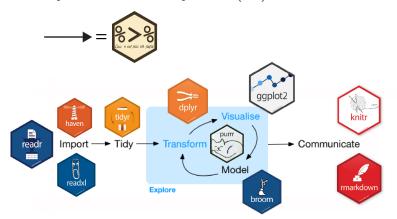




Figure 3: Updated scheme for data analysis process

Data analysis with the tidyverse (v2)

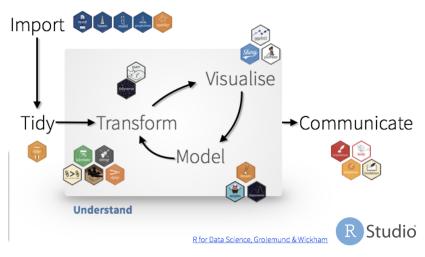


Figure 4: Updated scheme for data analysis process (v2)

Getting help

Rstudio's cheatsheets https://www.rstudio.com/resources/cheatsheets/

For a quick overview of the main features

Stackoverflow https://stackoverflow.com/

For all your specific questions



Tidyverse.org https://www.tidyverse.org

For an exhaustive documentation



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{tibble}



Figure 5: a modern re-imagining of the data frame

tibble versus data.frame

tibbles (or tbl_df) are modern reimagining of the data.frame,

- lazy: do less (e.g. do not change variable names, types, no partial matching)
- surly: complain more (e.g. when a variable does not exist)
- \leadsto smarter output, no row-name, no partial matching, more flexible column names, etc.
- → 100% compatible with data.frame

Conversion from a data.frame

head(iris)

```
Sepal.Length Sepal.Width Petal.Length Petal.Width Species
##
## 1
              5.1
                          3.5
                                        1.4
                                                    0.2
                                                         setosa
## 2
              4.9
                          3.0
                                                    0.2
                                                         setosa
## 3
              4.7
                          3.2
                                       1.3
                                                    0.2 setosa
                          3.1
## 4
              4.6
                                       1.5
                                                    0.2 setosa
## 5
             5.0
                          3.6
                                       1.4
                                                    0.2 setosa
              5.4
## 6
                          3.9
                                       1.7
                                                    0.4 setosa
```

as_tibble(iris)

Conversion from a data.frame

head(iris)

```
Sepal.Length Sepal.Width Petal.Length Petal.Width Species
##
## 1
             5.1
                        3.5
                                     1.4
                                                0.2 setosa
## 2
             4.9
                        3.0
                                     1.4
                                                0.2 setosa
## 3
             4.7
                        3.2
                                     1.3
                                                0.2 setosa
            4.6
                        3.1
                                    1.5
## 4
                                                0.2 setosa
## 5
            5.0
                        3.6
                                     1.4
                                                0.2 setosa
            5.4
## 6
                        3.9
                                     1.7
                                                 0.4 setosa
```

as_tibble(iris)

```
## # A tibble: 150 x 5
##
     Sepal.Length Sepal.Width Petal.Length Petal.Width Species
##
            <dbl>
                       <dbl>
                                   <dbl>
                                              <dbl> <fct>
              5.1
                         3.5
                                     1.4
                                                0.2 setosa
##
             4.9
##
                                     1.4
                                                0.2 setosa
##
             4.7
                        3.2
                                     1.3
                                                0.2 setosa
##
              4.6
                         3.1
                                     1.5
                                                0.2 setosa
##
              5
                         3.6
                                     1.4
                                                0.2 setosa
              5.4
                         3.9
                                     1.7
                                                0.4 setosa
##
             4.6
                        3.4
                                     1.4
                                                0.3 setosa
##
              5
                         3.4
                                     1.5
                                                0.2 setosa
##
              4.4
                         2.9
                                     1.4
                                                0.2 setosa
              4.9
                         3.1
                                     1.5
                                                0.1 setosa
    ... with 140 more rows
```

Creating a tibble

```
tibble(
  x = 1:5,
  y = 1,
  z = x ^ 2 + y
)
```

A tibble: 5 x 3

Column names of a tibble

Names can start by any character. To refer such variables, use the backticks tibble(\hat{1:})^ = "smile", \hat{1} = "space", \hat{2000} = "number")

```
## # A tibble: 1 x 3
## ':)' ' '2000'
## <chr> <chr> <chr> ## 1 smile space number
```

Creating a tibble

```
tibble(

x = 1:5,

y = 1,

z = x^2 + y
)
```

1 smile space number

A tibble: 5 x 3

Column names of a tibble

Names can start by any character. To refer such variables, use the backticks

```
tibble(':)' = "smile", ' = "space", '2000' = "number")
## # A tibble: 1 x 3
## ':)' ' '2000'
## <chr> <chr> <chr>
```

Row names I

Row do not have names in a tibble

Solution

- one can use name by adding a specfic column
- rownames_to_column () can help

Example

```
as tibble(swiss, rownames = "Province")
  # A tibble: 47 x 7
##
     Province Fertility Agriculture Examination Education Catholic
##
     <chr>>
                   <dbl>
                               <dbl>
                                           <int>
                                                     <int>
                                                               <dbl>
    1 Courtel~
                    80.2
                                17
                                              15
                                                         12
                                                               9.96
    2 Delemont
                    83.1
                                45.1
                                                               84.8
##
                                               6
                 92.5
##
   3 Franche~
                                39.7
                                                              93.4
  4 Moutier
                  85.8
                                36.5
                                              12
                                                              33.8
##
                76.9
##
   5 Neuvevi~
                                43.5
                                              17
                                                         15
                                                              5.16
   6 Porrent~
                76.1
                                35.3
                                                               90.6
##
   7 Brove
                    83.8
                                70.2
                                              16
                                                              92.8
##
   8 Glane
                    92.4
                                67.8
                                              14
                                                              97.2
##
    9 Gruvere
                    82.4
                                53.3
                                              12
                                                              97.7
  10 Sarine
                    82.9
                                45.2
                                              16
                                                         13
                                                               91.4
##
  # ... with 37 more rows, and 1 more variable: Infant.Mortality <dbl>
```

Row names II

Example 2

```
as_tibble(rownames_to_column(swiss))
```

```
## # A tibble: 47 x 7
##
      rowname Fertility Agriculture Examination Education Catholic Infant. Mortality
##
      <chr>>
                  <dh1>
                              <dbl>
                                           <int>
                                                     <int>
                                                              <dbl>
                                                                               <dh1>
    1 Courte~
                   80.2
                               17
                                             15
                                                               9.96
                                                                                22.2
##
                                                        12
   2 Delemo~
##
                   83.1
                               45.1
                                              6
                                                              84.8
                                                                                22.2
##
   3 Franch~
               92.5
                               39.7
                                              5
                                                         5
                                                              93.4
                                                                                20.2
                                             12
##
   4 Moutier
               85.8
                               36.5
                                                              33.8
                                                                                20.3
   5 Neuvev~
##
               76.9
                               43.5
                                             17
                                                        15
                                                            5.16
                                                                                20.6
##
  6 Porren~
                76.1
                               35.3
                                              9
                                                             90.6
                                                                                26.6
##
  7 Brove
                  83.8
                               70.2
                                             16
                                                             92.8
                                                                                23.6
##
   8 Glane
                   92.4
                               67.8
                                             14
                                                         8
                                                            97.2
                                                                                24.9
    9 Gruyere
                   82.4
                               53.3
                                             12
                                                        7
                                                              97.7
                                                                                21
  10 Sarine
                   82.9
                               45.2
                                             16
                                                        13
                                                              91.4
                                                                                24.4
## # ... with 37 more rows
```

Example 3

Row names III

```
my_tibble <- as_tibble(swiss, rownames = "Province")</pre>
head(as.data.frame(column_to_rownames(my_tibble, "Province")))
##
                Fertility Agriculture Examination Education Catholic
## Courtelary
                     80.2
                                  17.0
                                                           12
                                                                  9.96
## Delemont
                     83.1
                                  45.1
                                                                 84.84
## Franches-Mnt
                     92.5
                                  39.7
                                                               93.40
                                  36.5
## Moutier
                     85.8
                                                12
                                                                33.77
## Neuveville
                     76.9
                                  43.5
                                                17
                                                           15
                                                                5.16
## Porrentruy
                     76.1
                                  35.3
                                                                 90.57
##
                Infant.Mortality
## Courtelary
                             22.2
## Delemont
                             22.2
## Franches-Mnt.
                            20.2
## Moutier
                            20.3
## Neuveville
                            20.6
## Porrentruv
                            26.6
```

Consistency in subsetting

```
df \leftarrow data.frame(x = 1:9, y = LETTERS[1:9])
tbl <- tibble(x = 1:9, y = LETTERS[1:9])
```

Consistency in subsetting

```
df <- data.frame(x = 1:9, y = LETTERS[1:9])
tbl <- tibble(x = 1:9, y = LETTERS[1:9])

class(df[, 1:2])

## [1] "data.frame"

class(tbl[, 1:2])

## [1] "tbl_df" "tbl" "data.frame"

class(df[, 4])</pre>
```

Consistency in subsetting

"tbl"

[1] "tbl_df"

```
df \leftarrow data.frame(x = 1:9, y = LETTERS[1:9])
tbl <- tibble(x = 1:9, y = LETTERS[1:9])
class(df[, 1:2])
## [1] "data.frame"
class(tbl[, 1:2])
## [1] "tbl_df"
                                  "data.frame"
                    "tbl"
class(df[, 1])
## [1] "integer"
class(tbl[, 1])
```

"data.frame"

List-column

The type list is available for a column in tibble

- a tibble allows cells containing lists
- a tibble allows cells containing data frames.

```
subset(starwars, select = c('name', 'height', 'mass', 'hair_color', 'films', 'vehicles'))
```

```
# A tibble: 87 x 6
##
                        height mass hair color
                                                  films
                                                           vehicles
     name
     <chr>>
                        <int> <dbl> <chr>
                                                  st>
                                                            st>
##
   1 Luke Skywalker
                           172
                                 77 blond
                                                  <chr [5]> <chr [2]>
##
   2 C-3PO
                          167
                                75 <NA>
                                                  <chr [6]> <chr [0]>
##
   3 R2-D2
                           96
                                32 <NA>
                                                  <chr [7]> <chr [0]>
  4 Darth Vader
                                                  <chr [4]> <chr [0]>
##
                                136 none
   5 Leia Organa
                           150
                                49 brown
                                                  <chr [5]> <chr [1]>
##
   6 Owen Lars
                           178
                                120 brown, grey
                                                 <chr [3]> <chr [0]>
##
## 7 Bern Whitesun lars
                          165
                               75 brown
                                                 <chr [3]> <chr [0]>
## 8 R.5-D4
                           97
                                32 <NA>
                                                 <chr [1]> <chr [0]>
                                                  <chr [1]> <chr [0]>
   9 Biggs Darklighter
                           183 84 black
  10 Obi-Wan Kenobi
                           182
                                 77 auburn, white <chr [6]> <chr [1]>
  # ... with 77 more rows
```

List-column: put a vector in each case

head(starwars\$films, 4)

```
## [[1]]
## [1] "The Empire Strikes Back" "Revenge of the Sith"
  [3] "Return of the Jedi" "A New Hope"
  [5] "The Force Awakens"
##
## [[2]]
## [1] "The Empire Strikes Back" "Attack of the Clones"
  [3] "The Phantom Menace" "Revenge of the Sith"
  [5] "Return of the Jedi" "A New Hope"
##
## [[3]]
  [1] "The Empire Strikes Back" "Attack of the Clones"
  [3] "The Phantom Menace" "Revenge of the Sith"
  [5] "Return of the Jedi"
                                "A New Hope"
  [7] "The Force Awakens"
##
## [[4]]
## [1] "The Empire Strikes Back" "Revenge of the Sith"
  [3] "Return of the Jedi" "A New Hope"
```

{forcats}



Figure 6: a suite of useful tools that solve common problems with factors

forcats versus base factors

- easy use in conjuction with other tidyverse packages
- correct inconsistent behaviours of R base factors facilities
- → Slides borrowed to Antoine Bichat https://abichat.github.io/slides/factors_dates_strings

Convert to factor

Base R

forcats equivalent

```
forcats::as_factor(fruits) # Use appearance order

## [1] banana apple mango apple pear apple banana pitaya mango mango
## [11] apple
## Levels: banana apple mango pear pitaya
## equivalent to factor(countries, levels = unique(countries))
```

Remark

Appearance order increases reproducibility (independent from locale()).

Change level names

recode

```
fct_recode(fruits, dragonfruit = "pitaya")

## [1] banana apple mango apple pear apple
## [7] banana dragonfruit mango mango apple
## Levels: apple banana mango pear dragonfruit
```

relabel

```
fct_relabel(fruits, stringr::str_to_title)

## [1] Banana Apple Mango Apple Pear Apple Banana Pitaya Mango Mango
## [11] Apple
## Levels: Apple Banana Mango Pear Pitaya
```

Remark

When converting from strings to factors, fct_recode() and fct_relabel() use alphabetical order.

Reorder levels

You can reorder levels:

- manually with fct_relevel(),
- by appearance with fct_inorder(),
- by frequency with fct_infreq(),
- according to another variable with fct_reorder(),
- according to the last value of another variable with fct_reorder2(),
- randomly with fct_shuffle(),
- by reversing order with fct_rev()...

Reorder by frequency

[11] apple

Levels: apple mango banana pear pitaya

```
fct_count(fruits, sort = TRUE)

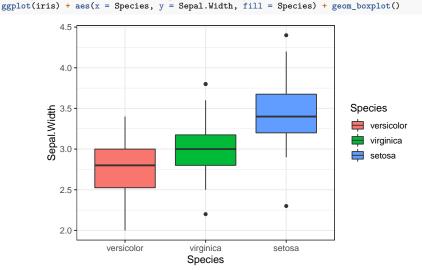
## # A tibble: 5 x 2
## f n
## <fct> <int>
## 1 apple 4
## 2 mango 3
## 3 banana 2
## 4 pear 1
## 5 pitaya 1

fct_infreq(fruits)
```

[1] banana apple mango apple pear apple banana pitaya mango mango

According to another variable

levels(iris\$Species)



Handling many modalities

A data set about nuclear testings around the world (enjoy!):

```
library(tidytuesdayR)
nuclear <- tt_load("2019-08-20") **nuclear_explosion

##
## Downloading file 1 of 1: `nuclear_explosions.csv`
nuclear **type <- stringr::str_to_title(nuclear **type)
fct_count(nuclear **type, sort = TRUE)

## # A tibble: 20 x 2</pre>
```

```
##
                 n
  <fct> <int>
##
   1 Shaft 1015
##
   2 Tunnel 310
##
   3 Atmosph 185
##
## 4 Shaft/Gr 85
##
   5 Airdrop
               78
##
   6 Tower
                75
## 7 Balloon
                62
## 8 Surface
                62
   9 Shaft/Lg
                56
  10 Barge
                40
  11 Ug
                 32
## 12 Gallery
## 13 Rocket
                 13
  14 Crater
## 15 Uw
## 16 Space
                 4
```

Lump least common factors

```
##
## Airdrop Atmosph Shaft Shaft/Gr Tunnel Other
## 78 185 1015 85 310 378
table(fct_lump_min(nuclear$type, min = 20))
##
##
Airdrop Atmosph Balloon Barge Shaft Shaft/Gr Shaft/Lg Surface
## 28 Airdrop Atmosph Balloon Barge Shaft Shaft/Gr Shaft/Lg Surface
## 310 32 51
```

Lump least common factors

##

##

##

78

75

Tower

185

310

Tunnel

62

Ug

32

40

51

Other

```
table(fct_lump(nuclear$type, n = 5))
##
    Airdrop Atmosph Shaft Shaft/Gr
                                        Tunnel
                                                  Other
                                           310
##
        78
                185
                      1015
                                   85
                                                    378
table(fct_lump_min(nuclear$type, min = 20))
##
##
    Airdrop Atmosph Balloon
                                Barge
                                         Shaft Shaft/Gr Shaft/Lg Surface
```

1015

85

56

62

Manually collapse levels

4 fct> 4 int> ## 1 Underground 1511 ## 2 Air 338 ## 3 Other 151

51

4 Water

{stringr}



Figure 7: cohesive set of functions designed to work more easily with

stringr versus base string utilities

String manipulation is cumbersome in R base. However, string plays a big role in many data cleaning and preparation.

- easy use in conjunction with other tidyverse packages
- faster and correct implementations of common string manipulations

See A. Bichat's slides: https://abichat.github.io/slides/factors_dates_strings/#73

{lubridate}



Figure 8: cohesive set of functions designed to make working with date as easy as possible

lubridate versus base R utilities

Data manipulation is always boring², whatever the system used...

See A. Bichat's slides: https://abichat.github.io/slides/factors_dates_strings/#38

²In my humble opinion...

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- ② Structures and types: tibble, forcats, string
- 3 data wrangling: readr, tidyr, dplyr
- 4 Manipulation: magrittr, purra
- 5 Visualization: ggplot2

{readr}



Figure 9: a fast and friendly way to read rectangular data (like csv, tsv and so on)

- offer coherent/unified functions compared to base::read.table and friends
- offer interactive reading
- output tibble rather than data.frame
- read_csv, read_delim, read_rds, read_file, read_table, etc

→ Read the manual when needed!

{tidyr}



Figure 10: a set of functions that help you get to tidy data

library(tidyr)

- → helps transforming messy data sets into tidy data sets.
 - evolution of base function reshape
 - more useful functions are spread/gather, unite/separate, nest/unest

Grades dataset

1 Tommy m.15 10 11 12 ## 2 Mary f.15 15 13 13 ## 3 Gary m.16 16 10 17 ## 4 Cathy f.14 14 12 10

Name	Sexage	Test1	Test2	Test3
Tommy	m.15	10	11	12
Mary	f.15	15	13	13
Gary	m.16	16	10	17
Cathy	f.14	14	12	10

separate()

Separate one column into multiple columns

```
grades <- separate(grades, Sexage, into = c("Sex", "Age"))
grades</pre>
```

Name	Sex	Age	Test1	Test2	Test3
Tommy	m	15	10	11	12
Mary	f	15	15	13	13
Gary	m	16	16	10	17
Cathy	f	14	14	12	10

Remark

The inverse of separate() is unite()

gather()

Gather columns into key-value pairs

```
grades <- gather(grades, Test1, Test2, Test3, key = Test, value = Grade)
grades</pre>
```

```
# A tibble: 12 x 5
##
    Name Sex
              Age
                  Test Grade
    <chr> <chr> <chr> <chr> <chr> <dbl>
   1 Tommy m
             15 Test1
   2 Mary f 15 Test1
                        15
##
   3 Garv m
           16 Test1 16
##
           14 Test1
##
   4 Cathy f
                        14
   5 Tommv m
           15 Test2
##
                        11
##
   6 Mary f
           15 Test2
                        13
## 7 Gary m
           16 Test2
 8 Cathy f
           14 Test2
                        12
##
           15 Test3
##
   9 Tommy m
  10 Marv f
             15 Test3
                        13
           16 Test3
  11 Garv m
                        17
 12 Cathy f
             14 Test3
```

Remark 1

The inverse of gather() is spread()

Remark 2

pivot_longer()/pivot_wider(): updates of gather and spread

nest()

Nesting creates a list-column of data frames

nest(iris, !Species)

Remark

The inverse of nest() is unnest()

dplyr



Figure 11: a consistent set of verbs (a grammar) that solves the most common data manipulation challenges

Typical operations

- create and pick variables
- pick and reorder observations
- create summaries
- •
- → Functions in this package are verbs and work similarly

mtcars dataset

```
data(mtcars)
as_tibble(mtcars)
```

```
A tibble: 32 x 11
                                                                              cyl disp
##
                                             mpg
                                                                                                                                                          hp
                                                                                                                                                                          drat
                                                                                                                                                                                                                             wt qsec
                                                                                                                                                                                                                                                                                                   VS
                                                                                                                                                                                                                                                                                                                                      am
                                                                                                                                                                                                                                                                                                                                                           gear
                                  <dbl> 
##
                                                                                                                                                                                                                                                                                                                                                                                        <dbl>
                                                                                                                                                                                                                  2.62
##
                                       21
                                                                                                           160
                                                                                                                                                    110
                                                                                                                                                                                3.9
                                                                                                                                                                                                                                                  16.5
                                                                                                                                                                                                                                                                                                                                                                              4
                                                                                                                                                                                                                                                                                                                                                                                                                4
                                        21
                                                                                                           160
                                                                                                                                                                                3.9
                                                                                                                                                                                                                  2.88
                                                                                                                                                                                                                                                  17.0
                                                                                                                                                                                                                                                                                                                                                                                                                4
##
                                                                                                                                                    110
                                                                                                                                                                                                                  2.32
##
                                       22.8
                                                                                                           108
                                                                                                                                                          93
                                                                                                                                                                                 3.85
                                                                                                                                                                                                                                                     18.6
##
                                        21.4
                                                                                                           258
                                                                                                                                                    110
                                                                                                                                                                                 3.08
                                                                                                                                                                                                                   3.22
                                                                                                                                                                                                                                                     19.4
                                       18.7
                                                                                                           360
                                                                                                                                                    175
                                                                                                                                                                                                                  3.44
                                                                                                                                                                                                                                                  17.0
##
                                                                                                                                                                                3.15
                                                                                                                                                                                2.76
##
                                       18.1
                                                                                                           225
                                                                                                                                                    105
                                                                                                                                                                                                                  3.46
                                                                                                                                                                                                                                                    20.2
                                        14.3
                                                                                                           360
                                                                                                                                                    245
                                                                                                                                                                                3.21
                                                                                                                                                                                                                  3.57
                                                                                                                                                                                                                                                     15.8
                                                                                                                                                                                                                                                                                                                                                                                                                4
##
                                                                                                           147.
##
                                        24.4
                                                                                                                                                          62
                                                                                                                                                                                 3.69
                                                                                                                                                                                                                  3.19
                                                                                                                                                                                                                                                     20
                                        22.8
                                                                                                           141.
                                                                                                                                                          95
                                                                                                                                                                                 3.92
                                                                                                                                                                                                                  3.15
                                                                                                                                                                                                                                                     22.9
                                       19.2
                                                                                                           168.
                                                                                                                                                    123
                                                                                                                                                                                3.92
                                                                                                                                                                                                                 3.44
                                                                                                                                                                                                                                                18.3
                           ... with 22 more rows
```

Select rows with filter()

Arguments

- data
- g filtering expressions

Output

- a tibble
- do not modify the original data

Example

Reorder rows with arrange()

Principle

works like filter() but reorder rows according to a series of conditions

Example

```
as_tibble(arrange(mtcars, desc(carb), mpg))
    A tibble: 32 x 11
              cyl
                    disp
                             hp
                                 drat
                                          wt
                                              asec
                                                                  gear
                                                                        carb
                                                       VS
      <dbl> <dbl> <dbl> <dbl> <dbl>
                                <dbl> <dbl>
                                             <dbl> <dbl> <dbl>
                                                                 <dbl>
                                                                       <dbl>
       15
                    301
                            335
                                 3.54
                                        3.57
                                                                     5
                                              14.6
##
       19.7
                    145
                            175
                                 3.62
                                        2.77
                                              15.5
##
       10.4
                    472
                            205
                                 2.93
                                        5.25
                                              18.0
       10.4
                    460
                            215
                                        5.42
                                              17.8
##
##
       13.3
                    350
                            245
                                 3.73
                                        3.84
                                              15.4
       14.3
                    360
                            245
                                 3.21
                                        3.57
                                              15.8
       14.7
                    440
                            230
                                 3.23
                                        5.34
                                              17.4
                                 4.22
       15.8
                    351
                            264
                                        3.17
                                              14.5
       17.8
                    168.
                            123
                                 3.92
                                        3.44
                                              18.9
       19.2
                    168.
                            123
                                 3.92
                                        3.44
                                             18.3
     ... with 22 more rows
```

Selecting columns with select() I

```
Similar to base::subsect(, select = c("","") )
```

With names

can be quoted or unquoted

9 22.8 3.15 10 19.2 3.44

... with 22 more rows

Selecting columns with select() |

6 3.92 3.44

... with 22 more rows

With indexes

10 19.2

```
as_tibble(select(mtcars, 1,2,5:7))
    A tibble: 32 x 5
##
       mpg cyl drat
                       wt gsec
##
     <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
##
      21
              6 3.9
                       2.62
                           16.5
      21
              6 3.9
                       2.88
                            17.0
      22.8
              4 3.85
                      2.32
                            18.6
      21.4
           6 3.08
                      3.22
                            19.4
   5 18.7
           8 3.15
                      3.44
                            17.0
           6 2.76
   6 18.1
                      3.46
                            20.2
      14.3
           8 3.21
                      3.57
                            15.8
      24.4
           4 3.69 3.19
                            20
           4 3.92 3.15
      22.8
                            22.9
```

18.3

Selecting columns with select() III

With scoping

... with 22 more rows

See starts_with, end_with, matches, any_of, last_col, everything ...

```
as_tibble(select(mtcars, contains('t')))
  # A tibble: 32 x 2
##
      drat
             wt
##
     <dbl> <dbl>
      3.9 2.62
## 2 3.9 2.88
## 3 3.85 2.32
  4 3.08 3.22
   5 3.15 3.44
  6 2.76 3.46
##
## 7 3.21 3.57
##
  8 3.69 3.19
   9 3.92
          3.15
  10 3.92 3.44
```

Renaming columns with rename()

rename() keeps all variables

```
as_tibble(rename(iris, petal_length = Petal.Length))
  # A tibble: 150 x 5
     Sepal.Length Sepal.Width petal_length Petal.Width Species
##
##
           <dbl>
                     <dbl>
                                 <dbl>
                                           <dbl> <fct>
## 1
             5.1
                       3.5
                                  1.4
                                             0.2 setosa
## 2
            4.9
                                  1.4
                                            0.2 setosa
            4.7
## 3
                     3.2
                                  1.3
                                            0.2 setosa
            4.6
                                  1.5
## 4
                      3.1
                                            0.2 setosa
## 5
                      3.6
                                  1.4
                                            0.2 setosa
          5.4
                                  1.7
## 6
                      3.9
                                            0.4 setosa
            4.6
                                1.4
## 7
                     3.4
                                            0.3 setosa
                                1.5
## 8
             5
                      3.4
                                            0.2 setosa
##
            4.4
                      2.9
                                1.4
                                            0.2 setosa
## 10
            4.9
                       3.1
                                  1.5
                                             0.1 setosa
  # ... with 140 more rows
```

Renaming columns with select()

Renaming can be done with select()

select() only keeps the variables specified

```
as_tibble(select(iris, petal_length = Petal.Length))
    A tibble: 150 x 1
     petal_length
##
             <dbl>
               1.4
##
##
               1.4
               1.3
##
              1.5
               1.4
              1.7
               1.4
               1.5
               1.4
               1.5
     ... with 140 more rows
```

Add new variables with mutate()

mutate keeps the existing variables

2.31

2.75

... with 22 more rows

95

3.15

3.44

22.9

18.3

4

8 16

24

22.8

19.2

```
as tibble(
          mutate(mtcars.
                                                cv12 = 2 * cv1,
                                                cy14 = 2 * cy12,
                                               disp = disp * 0.0163871,
                                               drat = NULL)
                        A tibble: 32 \times 12
                                                                         cyl disp
##
                                                                                                                                                                                                                                             VS
                                                                                                                                                                                                                                                                                                gear carb cyl2
                                         mpg
                                                                                                                                              hp
                                                                                                                                                                             wt
                                                                                                                                                                                                  gsec
                                                                                                                                                                                                                                                                             am
                                <dbl> 
##
                                    21
                                                                                                   2.62
                                                                                                                                        110
                                                                                                                                                                  2.62
                                                                                                                                                                                                  16.5
                                                                                                                                                                                                                                                                                                                                                                            12
                                                                                                                                                                                                                                                                                                                                                                                                             24
                                                                                                                                                                                                 17.0
##
                                    21
                                                                                                   2.62
                                                                                                                                        110
                                                                                                                                                                   2.88
                                                                                                                                                                                                                                                                                                                                                                            12
                                                                                                                                                                                                                                                                                                                                                                                                             24
                                    22.8
                                                                                                  1.77
                                                                                                                                      93
                                                                                                                                                                  2.32
                                                                                                                                                                                               18.6
                                                                                                                                                                                                                                                                                                                                                                                8
                                                                                                                                                                                                                                                                                                                                                                                                           16
##
                                                                                                                                                                                                                                                                                                                   4
##
                                    21.4
                                                                                   6 4.23
                                                                                                                                       110
                                                                                                                                                                  3.22
                                                                                                                                                                                              19.4
                                                                                                                                                                                                                                                                                                                                                                                                           24
##
                                    18.7
                                                                                                   5.90
                                                                                                                                        175
                                                                                                                                                                  3.44
                                                                                                                                                                                              17.0
                                                                                                                                                                                                                                                                                   0
                                                                                                                                                                                                                                                                                                                                                                            16
                                                                                                                                                                                                                                                                                                                                                                                                           32
                                    18.1
                                                                                                   3.69
                                                                                                                                        105
                                                                                                                                                                   3.46
                                                                                                                                                                                                  20.2
                                                                                                                                                                                                                                                                                                                                                                            12
                                                                                                                                                                                                                                                                                                                                                                                                           24
##
##
                                     14.3
                                                                                                   5.90
                                                                                                                                        245
                                                                                                                                                                   3.57
                                                                                                                                                                                                  15.8
                                                                                                                                                                                                                                                                                                                                                                            16
                                                                                                                                                                                                                                                                                                                                                                                                           32
                                    24.4
                                                                                                   2.40
                                                                                                                                      62
                                                                                                                                                                  3.19
                                                                                                                                                                                                  20
                                                                                                                                                                                                                                                                                                                                                                                 8
                                                                                                                                                                                                                                                                                                                                                                                                           16
 ##
```

Add new variables with transmute()

transmute drops the existing variables

8 16 2.40 16 2.31 24 2.75 ... with 22 more rows

```
as_tibble(
 transmute(mtcars.
       cv12 = 2 * cv1,
       cy14 = 2 * cy12,
       disp = disp * 0.0163871,
       drat = NULL)
## # A tibble: 32 x 3
      cvl2 cvl4 disp
     <dbl> <dbl> <dbl>
##
      12
             24 2.62
   2 12 24 2.62
     8 16 1.77
##
          24 4.23
##
     16
          32 5.90
     12
          24 3.69
     16 32 5.90
```

Create summary statistics with summarise()

Reduction is done by means of statistical functions, among which

```
Center: mean(), median()
Spread: sd(), IQR(), mad()
Range: min(), max(), quantile()
Position: first(), last(), nth(),
Count: n(), n_distinct()
Logical: any(), all()
```

Example

```
summarise(mtcars, Mean_mpg = mean(mpg), Var_disp = var(disp))
### Mean_mpg Var_disp
## 1 20.09062 15360.8
```

group rows according to factors with group_by()

 $\mathtt{group_by()}$ does not do much visible expect creating a grouped data frame with type $\mathtt{grouped_df}$

```
A tibble: 32 x 11
    Groups:
                cvl, am [6]
##
               cvl
                   disp
                             hp
                                 drat
                                         wt
                                              qsec
                                                       VS
      <dbl> <dbl> <dbl> <dbl>
                                <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                                <dbl>
                    160
                            110
                                 3.9
                                       2.62
                                              16.5
       21
                           110
                                       2.88
##
                    160
                                 3.9
                                              17.0
                                       2.32
       22.8
                 4 108
                           93
                                 3.85
                                             18.6
       21.4
                    258
                            110
                                       3.22
                                              19.4
                                 3.08
       18.7
                    360
                            175
                                 3.15
                                       3.44
                                              17.0
##
       18.1
                            105
                                 2.76
                                       3.46
                                              20.2
       14.3
                    360
                            245
                                 3.21
                                       3.57
                                              15.8
                                3.69
       24.4
                 4 147.
                           62
                                       3.19
                                              20
```

3.15

3.44 18.3

22.9

Remark

22.8

19.2

group by (mtcars, cyl,am)

ungroup() performs the reverse operation.

95 3.92

123

3.92

141.

168.

... with 22 more rows

Combine summarise() and group_by()

Magic of group_by() comes true when used in conjunction with summarise()

```
grp_mtcars <- group_by(mtcars, cyl, carb)
summarise(grp_mtcars, Count = n(), Mean_mpg = mean(mpg), Var_disp = var(disp))</pre>
```

```
# A tibble: 9 x 5
  # Groups: cyl [3]
     cyl carb Count Mean mpg Var disp
##
##
    <dbl> <dbl> <dbl> <dbl> <dbl>
                           <dh1>
## 1
                  27.6 457.
                6 25.9 732.
## 2
## 3
                  19.8 544.
      6 4 4 19.8 19.3
## 4
## 5
                    19.7
                          NΑ
## 6
        2 4 17.2
                           1886.
                3 16.3
## 7
        4 6 13.2
                           3341.
## 8
## 9
                     15
                            NA
```

Common remarks and extension

Remarks

Most primitive in dyplr do no modify the original table

Scoping

rename, filter, select, summarise, etc. all have scoped variant

- rename_all(): apply operation on all variables
- rename_at(): apply an operation on a subset of specified variables
- rename_if():) apply an operation on the subset of predicated variables

Others verbs/functions

- distinct() subset unique rows
- relocate() change column position
- top_n(), sample_n() ... select rows
- n(), if_else() ... vector function for selection
- any function from stringr (str_to_title, toupper, etc.)

More on https://dplyr.tidyverse.org/reference/index.html

Exercises in dplyr vs base R

Exercises adapted from UseR 2017 on data. table

Question 1

Subset all rows where id column equals 1 & code column is not equal to "c"

base

```
base::subset(DF1, id == 1 & code != "c"

## id code valA valB

## 1 1 a 1 10

## 2 1 a 2 11

## 4 1 a 4 13

with(DF1, DF1[id == 1 & code != "c",])

## id code valA valB

## 1 1 a 1 10

## 2 1 a 2 11

## 4 1 a 4 13
```

dplyi

```
filter(TB1, id == 1 & code != "c")

### # A tibble: 3 x 4

### id code valA valB

### <int> <chr> <int> <int> <chr> <int> <int> <chr> <int> <int> <chr> <int > int > <chr > <chr > <int > int > <chr > <chr > <int > int > <chr > <ch > int > <ch > int > <ch > <ch > <ch > <ch > int > <ch >
```

Question 1

Subset all rows where id column equals 1 & code column is not equal to "c"

base

dplyı

Subset all rows where id column equals 1 & code column is not equal to "c"

base

```
filter(TB1, id == 1 & code != "c")

## # A tibble: 3 x 4

## id code valA valB

## <int> <int> <int> <int>
## 1 1 a 1 10

## 2 1 a 2 11

## 3 1 a 4 13
```

Select valA and valB columns from DF1

```
DF1[, c("valA", "valB")]

## valA valB

## 1 1 10

## 2 2 11

## 3 3 12

## 4 4 13

## 5 5 14

## 6 6 15

## 7 7 16

## 8 8 17

## 9 9 18
```

dplyi

```
## # A tibble: 9 x 2
## valA valB
## 1 1 10
## 2 2 11
## 3 3 12
## 4 4 13
## 5 5 14
```

Select valA and valB columns from DF1

base R

```
DF1[, c("valA", "valB")]

## valA valB

## 1 1 10

## 2 2 11

## 3 3 12

## 4 4 13

## 5 5 14

## 6 6 15
```

dplyr

8 ## 9

```
## # A tibble: 9 x 2
## valA valB
## valA valB
## (int> <int>
## 1 10
## 2 2 11
## 3 3 12
## 4 4 13
## 5 5 15
```

7 16 8 17

18

Select valA and valB columns from DF1

base R

dplyr

9

select(TB1, valA, valB)

8 17

18

```
## # A tibble: 9 x 2
## valA valB
## <int> <int> cint>
1 1 10
## 2 2 11
## 3 3 12
## 4 4 13
## 5 5 14
## 6 6 15
```

Get sum(valA) and sum(valB) for id > 1 as a 1-row, 2-col data.frame

Get sum(valA) and sum(valB) for id > 1 as a 1-row, 2-col data.frame

base R

```
colSums(DF1[ DF1$id > 1, c("valA", "valB")])
## valA valB
    30
```

Get sum(valA) and sum(valB) for id > 1 as a 1-row, 2-col data.frame

base R

```
colSums(DF1[ DF1$id > 1, c("valA", "valB")])
## valA valB
## 30 66
```

```
TB1 %% filter(id > 1) %>% select(valA, valB) %>% summarise_all(sum)

## # A tibble: 1 x 2

## valA valB

## <int> <int> ## 1 30 66
```

Replace valB with valB+1 for all rows where code == "c"

Replace valB with valB+1 for all rows where code == "c"

base R

```
DF1$valB[DF1$code == "c"] = DF1$valB[DF1$code == "c"] + 1
DF1
    id code valA valB
         а
                 10
## 2
    1 a 2 11
## 3 1 c
              3 13
```

6 2 a 6 15 ## 7 2 a 7 16 ## 8 2 c 8 18

1 a 4 13

1 c 5 15

9 2 b 9 18

5

Replace valB with valB+1 for all rows where code == "c"

base R

```
DF1$valB[DF1$code == "c"] = DF1$valB[DF1$code == "c"] + 1
DF1

## id code valA valB
## 1 1 a 1 10
## 2 1 a 2 11
## 3 1 c 3 13
## 4 1 a 4 13
## 5 1 c 5 15
## 6 2 a 6 15
## 7 2 a 7 16
```

dplyr

8 2 c 8 18 ## 9 2 b 9 18

69 / 136

Add a new column valC column with values equal to valB^2 - valA^2

base R

```
DF1 < transform(DF1, valC = valB*2 - valA*2)
### DF1$valC <- DF1$valB*2 - DF1$valA*2 # alternate solution

DF1

## 1d code valA valB valC

## 1 1 a 1 10 99

## 2 1 a 2 11 117

## 3 1 c 3 13 160

## 4 1 a 4 13 153

## 4 1 a 4 13 153

## 6 2 a 6 15 200

## 6 2 a 6 15 189

## 7 2 a 7 16 207

## 8 2 c 8 18 260
```

Add a new column valC column with values equal to valB^2 - valA^2

base R

```
DF1 <- transform(DF1, valC = valB^2 - valA^2)

## DF1$valC <- DF1$valB^2 - DF1$valA^2 # alternate solution

DF1

## id code valA valB valC

## 1 1 a 1 10 99

## 2 1 a 2 11 117

## 3 1 c 3 13 160

## 4 1 a 4 13 153

## 5 1 c 5 15 200
```

dplyr

```
TBi <- mutate(TB1, valC = valB^2 - valA^2
TB1

## # A tibble: 9 x 5

## id code valA valB valC

## <int> <chr> <int> <int> <chr> <int> <int> <chr> <int> = 1 10 99

## 2 1 a 2 11 117
```

6 2 a 6 15 189 ## 7 2 a 7 16 207 ## 8 2 c 8 18 260 ## 9 2 b 9 18 243

Add a new column valC column with values equal to valB^2 - valA^2

base R

```
DF1 <- transform(DF1, valC = valB^2 - valA^2)</pre>
## DF1$valC <- DF1$valB^2 - DF1$valA^2 # alternate solution
DF1
    id code valA valB valC
         а
                 10 99
         a 2 11 117
## 2 1
## 3 1 c 3 13 160
## 4 1 a 4 13 153
## 5 1 c 5 15 200
```

7 2 a 7 16 207 ## 8 2 c 8 18 260 ## 9 2 b 9 18 243

6 2 a 6 15 189

```
dplyr
TB1 <- mutate(TB1, valC = valB^2 - valA^2)
TB1
## # A tibble: 9 x 5
##
       id code valA valB valC
    <int> <chr> <int> <int> <dbl>
## 1
     1 a
                1 10
## 2
     1 a
                            117
```

Get sum(valA) and sum(valB) grouped by id and code (i.e., for each unique combination of id,code)

```
base
```

```
## id code valA valB valC
## 1 1 a 7 34 369
## 2 2 a 13 31 396
## 3 2 5 9 18 243
## 4 1 c 8 28 360
## 5 2 c 8 18 260
aggregate(DF1[, c("valA", "valB")], list(DF1$id, DF1$code), sum)
## Group.1 Group.2 valA valB
## 1 1 a 7 34
## 2 2 a 13 31
## 3 2 b 9 18
## 4 1 c 8 28
## 5 2 c 8 18
```

dplyı

```
## # A tibble: 5 x 5
## # Groups: id [2]
```

Get sum(valA) and sum(valB) grouped by id and code (i.e., for each unique combination of id,code)

base

```
aggregate(.~ id + code, DF1, sum)
    id code valA valB valC
                 34
                    369
     2 a 13
                 31 396
     2 b 9 18 243
                 28 360
                 18 260
aggregate(DF1[, c("valA", "valB")], list(DF1$id, DF1$code), sum)
    Group.1 Group.2 valA valB
## 1
                        34
## 2
                a 13
                        31
    2 b 9 18
                        28
## 5
                        18
```

dplyı

```
## # A tibble: 5 x 5
## # Groups: id [2]
```

Get sum(valA) and sum(valB) grouped by id and code (i.e., for each unique combination of id,code)

base

```
aggregate(.~ id + code, DF1, sum)

## id code valA valB valC
## 1 1 a 7 34 369
## 2 2 a 13 31 396
## 3 2 b 9 18 243
## 4 1 c 8 28 360
## 5 2 c 8 18 260

aggregate(DF1[, c("valA", "valB")], list(DF1$id, DF1$code), sum)

## Group.1 Group.2 valA valB
## 1 1 a 7 34
## 2 2 a 13 31
## 2 2 a 13 31
## 3 2 b 9 18
## 4 1 c 8 28
## 5 2 c 8 18
```

```
TB1 %>% group_by(id, code) %>% summarise_all(sum)

## # A tibble: 5 x 5

## # Groups: id [2]

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```

Get sum(valA) and sum(valB) grouped by id for id >= 2 & code %in% c("a", "c")

base

```
## id valA valB valC
## 1 2 21 49 656
```

Get sum(valA) and sum(valB) grouped by id for id >= 2 & code %in% c("a", "c")

base

```
aggregate(.~ id , subset(DF1, id >=2 & code %in% c("a","c"), -code), sum)
## id valA valB valC
## 1 2 21 49 656
```

```
TB1 %>%

group_by(id) %>%

filter(id >=2, code %in% c("a", "c")) %>%

select(-code, -valC) %>%

summarise_all(sum)

## # A tibble: 1 x 3

## id valA valB

## <int> <int> <int>
```

Get sum(valA) and sum(valB) grouped by id for id >= 2 & code %in% c("a", "c")

base

```
aggregate(.~ id , subset(DF1, id >=2 & code %in% c("a","c"), -code), sum)
## id valA valB valC
## 1 2 21 49 656
```

```
TB1 %>%

group_by(id) %>%

filter(id >=2, code %in% c("a", "c")) %>%

select(-code, -valC) %>%

summarise_all(sum)
```

```
## # A tibble: 1 x 3
## id valA valB
## <int> <int> <int> <int> <int>
```

Replace valA with max(valA)-min(valA) grouped by code

base

```
DF1 <- transform(DF1, valA = rep(tapply(valA, code, function(x) diff(range(x)))[code]))

## id code valA valB valC

## 1 1 a 6 10 99

## 2 1 a 6 11 117

## 3 1 c 5 13 160

## 4 1 a 6 13 153

## 5 1 c 5 15 200

## 6 2 a 6 15 189

## 7 2 a 6 16 207

## 8 2 c 5 18 260

## 8 2 c 5 18 263
```

Replace valA with max(valA)-min(valA) grouped by code

base

```
DF1 <- transform(DF1, valA = rep(tapply(valA, code, function(x) diff(range(x)))[code]))
DF1
    id code valA valB valC
## 1 1
         а
             6
                 10
                     99
## 2
                 11 117
         а
## 3 1 c 5 13 160
## 4
    1 a 6 13 153
## 5
                15 200
## 6
                15 189
## 7 2 a 6 16 207
## 8 2 c 5 18 260
## 9 2 b
                18 243
```

```
TB1 <- TB1 %>% group_by(code) %>% mutate(valA= max(valA)-min(valA)
TB1

## # A tibble: 9 x 5
## # Groups: code [3]
## id code valA valB valC
## <int> <int> <idbl>
## 1 a 6 10 99
## 2 1 a 6 11 117
```

Replace valA with max(valA)-min(valA) grouped by code

base

```
DF1 <- transform(DF1, valA = rep(tapply(valA, code, function(x) diff(range(x)))[code]))
DF1
    id code valA valB valC
## 1 1
         а
           6
                 10
                   99
## 2
         a 6 11 117
## 3 1 c 5 13 160
## 4 1 a 6 13 153
## 5 1 c 5 15 200
## 6 2 a 6 15 189
## 7 2 a 6 16 207
## 8 2 c 5 18 260
## 9 2 b 0 18 243
```

dplyr

2

1 a

3 1 c 5 19

6

117

135

```
TB1 <- TB1 %>% group_by(code) %>% mutate(valA= max(valA)-min(valA))
TB1
    A tibble: 9 x 5
## # Groups: code [3]
       id code valA valB valC
##
     <int> <chr> <int> <int> <dbl>
## 1
         1 a
                    6
                         10
```

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Create a new col named valD with max(valB)-min(valA) grouped by code

base

```
DF1 <- transform(DF1, valD = by(DF1, code, function(x) max(x$valB) - min(x$valA))[code])

## id code valA valB valC valD

## 1 1 a 6 10 99 10

## 2 1 a 6 11 117 10

## 3 1 c 5 13 160 13

## 4 1 a 6 13 153 10

## 5 1 c 5 15 200 13

## 6 2 a 6 15 189 10

## 7 2 a 6 16 207 10

## 8 2 c 5 18 260 13

## 9 2 b 0 18 243 18
```

dply

```
TB1 <- TB1 %>% group_by(code) %>% mutate(valD= max(valB)-min(valATB1

## # A tibble: 9 x 6
## # Groups: code [3]
## id code valA valB valC valD
## <int> <int > <
```

Create a new col named valD with max(valB)-min(valA) grouped by code

base

```
DF1 <- transform(DF1, valD = by(DF1, code, function(x) max(x$valB) - min(x$valA))[code])
DF1
    id code valA valB valC valD
## 1 1
         а
              6
                      99
                           10
## 2
                  11 117
                           10
          а
## 3
                13 160
                           13
## 4
                  13 153
                           10
## 5
                  15
                     200
                           13
## 6
                  15 189
                          10
## 7 2 a 6 16 207
                          10
## 8
    2 c 5 18 260
                           13
## 9 2
                  18 243
                           18
```

Create a new col named valD with max(valB)-min(valA) grouped by code

base

2

1 a

3 1 6 5 19

6 11

117

135

10

```
DF1 <- transform(DF1, valD = by(DF1, code, function(x) max(x$valB) - min(x$valA))[code])
DF1
    id code valA valB valC valD
## 1 1
         а
                 10
                     99
                          10
## 2
                 11 117
                         10
## 3 1 c 5 13 160
                         13
## 4 1 a 6 13 153
                         10
## 5 1 c 5 15 200
                         13
## 6 2 a 6 15 189
## 7 2 a 6 16 207
                         10
                        10
## 8 2 c 5 18 260
                        13
## 9 2 b 0 18 243
                          18
```

```
dplyr

TB1 <- TB1 %>% group_by(code) %>% mutate(valD= max(valB)-min(valA))
TB1

## # A tibble: 9 x 6

## # Groups: code [3]

## id code valA valB valC valD

## <int> <chr <int> <chr <int> <dbl> <int> 
## 1 a 6 10 99 10
```

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Outline

- 1 Introduction
- ② Structures and types: tibble, forcats, strings
- 3 data wrangling: readr, tidyr, dplyr
- 4 Manipulation: magrittr, purrr
- 5 Visualization: ggplot2

{magrittr}



Figure 12: a set of operators which make your code more readable

library(magrittr)

Provides the following operators

- Pipe %>%
- Reassignment pipe %<>%
- T-Pipe %T>%

Motivation: make Tom eat an apple

Everyday language

Tom eats an apple

Subject - Verb - Complement

Programming language

eat(Tom, apple)

Verb - Subject - Complement

Pipes

- → get closer to everyday language in your code
- → clearly expressing a sequence of multiple operations

Pipe %>%

- when you read code, %>% is pronounced "then"
- the keybord shortcut for %>% is Ctrl + shift + M

Objective

- Helps writing R code which is easy to read (and thus, easy to understand)
- x %>% f() is equivalent to f(x)
- x %>% f(y) is equivalent to f(x, y)
- x %>% f(y,.) is équivalent to f(y,x)

Example

Pipe %>%

- when you read code, %>% is pronounced "then"
- the keybord shortcut for %>% is Ctrl + shift + M

Objective

- Helps writing R code which is easy to read (and thus, easy to understand)
- x %>% f() is equivalent to f(x)
- x %>% f(y) is equivalent to f(x, y)
- x %>% f(y,.) is équivalent to f(y,x)

Example

```
2^mean(log(seq_len(10), base = 2), na.rm = TRUE)

## [1] 4.528729

10 W/W seq_len() W/
```

[1] 4.528729

Pipe %>%

- when you read code, %>% is pronounced "then"
- the keybord shortcut for %>% is Ctrl + shift + M

Objective

- Helps writing R code which is easy to read (and thus, easy to understand)
- x %>% f() is equivalent to f(x)
- x %>% f(y) is equivalent to f(x, y)
- x %>% f(y,.) is équivalent to f(y,x)

Example

```
2^mean(log(seq_len(10), base = 2), na.rm = TRUE)
## [1] 4.528729

10 %>%
    seq_len() %>%
    log(base = 2) %>%
    mean(na.rm = TRUE) %>%
    {2^.}

## [1] 4.528729
```

Exercise

Consider

```
x \leftarrow c(0.109, 0.359, 0.63, 0.996, 0.515, 0.142, 0.017, 0.829, 0.907)
```

Compute the logarithm of x, return suitably lagged and iterated differences, compute the exponential function and round the result

- 1 In base R
- Using %>%

(Re)assignment pipe %<>%

For affectation, magrittr provides the operator %<>% which allows to replace code like

```
mtcars <- mtcars%>% transform(cyl = cyl * 2)
```

by

```
mtcars %<>% transform(cyl = cyl * 2)
```

T-pipe %T>%

Problem with functions requiring early side effects along succession of %>%

- you might want to plot or print and object
- such function do not send back anything and break the pipe

Solution

- to overcome such an issue, use the "tee" pipe %T>%
- works like %>% except that it sends left side in place of right side of the expression
- "tee"because it looks like a pipe with a T shape

T-pipe %T>%: example without T

```
rnorm (100) %>%
  matrix(ncol = 2) %>%
  plot() %>%
  str()
```

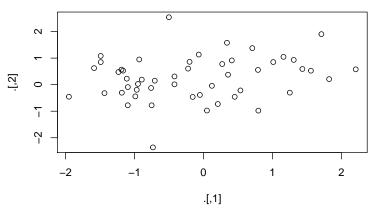


Figure 13: plot of bivariate Gaussian sample

T-pipe T>: example with T

```
rnorm (100) %>%
  matrix(ncol = 2) %T>%
  plot() %>%
  str()
```

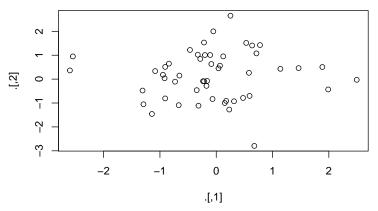


Figure 14: plot of bivariate Gaussian sample

Exposition Operator %\$%

When working with functions that do not take data argumentbut still useful in a pipeline, e.g., when your data is first processed and then passed into the function.

Example

```
iris %>%
  subset(Sepal.Length > mean(Sepal.Length)) %$%
  cor(Sepal.Length, Sepal.Width)
```

When not to use the pipe

Consider other solutions when

Pipes contain too many steps

Create intermediate objects with meaningful names

Multiple inputs or outputs are required

E.g., when several objects need to combine together

Complex dependance structures exists between your entries

Pipes are fundamentally *linear*: expressing complex relationships with them yield confusing code.

Functional programming: general idea

Definition

R is a Functional programming language with first class functions: it places functions at the same level as variables. One can

- pass functions as arguments to other functions
- 2 return functions from other functions
- 3 store functions in data structures

Ingredients

In R the tools/ingredients allowing functional programming are

- closure, i.e. functions that output functions
- list. in which you can store functions
- anonymous functions, i.e. function that does not deserve a name
- functionals, i.e. functions that take function(s) as input

→ we briefly review some of R's functional tools, which you probably already use

Functional programming: general idea

Definition

R is a Functional programming language with first class functions: it places functions at the same level as variables. One can

- pass functions as arguments to other functions
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Ingredients

In R the tools/ingredients allowing functional programming are

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- list, in which you can store functions
- anonymous functions, i.e. function that does not deserve a name
- functionals, i.e. functions that take function(s) as input

we briefly review some of R's functional tools, which you probably already use

{purrr}



Figure 15: enhances R's functional programming (FP) toolkit

Some slides borrowed to - Happy dev with $\{purrr\}$ https://colinfay.me/happy-dev-purrr/ (C. Fay) - Modeling in the tidyverse https://abichat.github.io/slides/modelingtidyverse/ (A. Bichat)

Functional programming "phylosophy"

Never use for loops

Base R

- *apply() functions and friends for lists and data frames
 - apply, lapply(), sapply(), tapply(), mapply(), ...
 - Map(), Reduce()
 - Vectorize()

Tidyverse variants

map() function and variants

- map(), map_dbl(), map_chr(), map_lgl(), ...
- map2(), map2_dbl(), map2_chr(), map2_lgl(), ...
- pmap(), pmap_dbl(), pmap_chr(), pmap_lgl(), ...
- reduce()

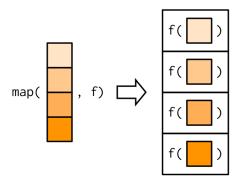


Figure 16: map

- map() applies the function to each element and returns a list
- map_lgl(), map_int(), map_dbl() and map_chr() applies the function to each element and returns a atomic vector of the corresponding type

map*(): examples I

```
map(1:5, rnorm)
## [[1]]
  [1] 0.6786101
##
## [[2]]
## [1] -0.8344392 -1.0176957
##
   [[3]]
   [1] -0.4142210 1.6200032 -0.5265256
##
## [[4]]
   [1] -0.1924844 1.0187318 0.1121379 1.4153514
##
## [[5]]
  [1] -0.4068349 1.0349484 1.4408870 -1.1577407 0.6536112
map(1:5, rnorm) %>%
  map_dbl(mean)
```

map*() (additional arguments)

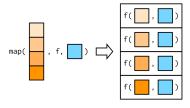


Figure 17: map

```
map(1:4, rnorm, n = 6)

## [[1]]
## [1] 2.3709584 0.4353018 1.3631284 1.6328626 1.4042683 0.8938755
##
## [[2]]
## [1] 3.511522 1.905341 4.018424 1.937286 3.304870 4.286645
##
## [[3]]
## [1] 1.6111393 2.7212112 2.8666787 3.6359504 2.7157471 0.3435446
##
## [[4]]
## [[4]]
## [1] 1.559533 5.320113 3.693361 2.218692 3.828083 5.214675
```

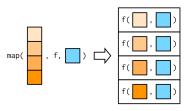


Figure 18: map

```
map(1:4, rnorm, n = 6) %>%
map_dbl(function(x) x[2])
```

[1] 0.4353018 1.9053410 2.7212112 5.3201133

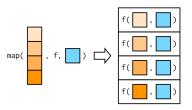


Figure 19: map

```
map(1:4, rnorm, n = 6) %>%
map_dbl(~ .[2])
```

[1] 0.4353018 1.9053410 2.7212112 5.3201133

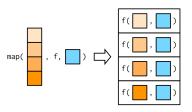


Figure 20: map

```
map(1:4, rnorm, n = 6) %>%
map_dbl(2)
```

[1] 0.4353018 1.9053410 2.7212112 5.3201133

Examples

Split a data frame into pieces, fit a model to each piece, compute the summary, then extract the R2.

```
mtcars %>%
  split(.$cyl) %>% # from base R
  map(~ lm(mpg ~ wt, data = .)) %>%
  map(summary) %>%
  map_dbl("r.squared")
```

```
## 4 6 8
## 0.5086326 0.4645102 0.4229655
```

A more complicated example

```
iris %>%
group_by(Species) %>%
nest() %>%
mutate(model = map(data, ~ lm(data = ., Sepal.Length ~ Petal.Length))) %>%
mutate(Summary = map(model, summary)) %>%
mutate(`R squared` = map_dbl(Summary, ~ .$r.squared))
```

Advantages of map() vs the apply() family

Stable and consistent grammar

```
apply(X, MARGIN, FUN, ...)
lapply(X, FUN, ...)
sapply(X, FUN, ..., simplify = TRUE, USE.NAMES = TRUE)
tapply(X, INDEX, FUN = NULL, ..., default = NA, simplify = TRUE)
mapply(FUN, ..., MoreArgs = NULL, SIMPLIFY = TRUE, USE.NAMES = TRUE)
ending
mapply(env, FUN, ..., all.names = FALSE, USE.NAMES = TRUE)
...
```

VS

```
map(.x, .f, ...)
map_if(.x, .p, .f, ...)
map_chr(.x, .f, ...)
map_int(.x, .f, ...)
map_dbl(.x, .f, ...)
...
```

Advantages of map() vs the apply() family

Type stability

```
sapply(iris$Sepal.Length, as.numeric) %>% class()
   [1] "numeric"
sapply(iris$Sepal.Length, as.data.frame) %>% class()
## [1] "list"
VS
map_dbl(iris$Sepal.Length, as.numeric) %>% class()
## [1] "numeric"
map_df(iris$Sepal.Length, as.data.frame) %>% class()
## [1] "data.frame"
```

Advantages of map() vs the apply() family

Anonymous functions & verbosity

```
lapply(list, function(x) x + 2)
mapply(function(x, y) x + y, list1, list2)
lapply(list, function(x) x[[2]])
lapply(list, function(x) x$foo)
```

VS

```
map(list, ~ . + 2)
map2(list1, list2, ".x + .y)
map(list, 2)
map(list, "foo")
```

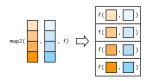


Figure 21: map2

map2() and $map2_*()$ are variants of map() and $map_*()$ which work with two arguments

```
map2(1:4, c(2, 5, 5, 10), runif, n = 5)

## [[1]]
## [1] 1.970967 1.618838 1.333427 1.346748 1.398485
##
## [[2]]
## [1] 4.354078 2.116809 4.246386 4.031830 2.513793
##
## [[3]]
## [1] 3.522176 4.028826 4.351215 4.965634 4.519089
##
## [[4]]
## [[4]]
## [1] 7.398931 9.098138 5.136844 5.627720 8.968951
```

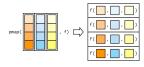


Figure 22: pmap

pmap() and pmap_*() are generalized versions of map() and map_*() which work with any number of arguments

```
## [[1]]
## [1] 1.693205 1.240545
##
## [[2]]
## [1] 2.128966 2.421437 2.649156
##
## [[3]]
## [1] 3.958797 3.394821
##
## [[4]]
## [1] 8.316135 4.047308 6.252940 7.086446 4.009423
```

pmap(list(n = c(2, 3, 2, 5), min = 1:4, max = c(2, 5, 5, 10)), runif)

reduce()

```
rerun(4, sample(1:10, 6))

## [[1]]
## [1] 9 4 7 1 2 5

##
## [[2]]
## [1] 7 2 3 8 1 5

##
## [[3]]
## [1] 5 6 9 2 1 10

##
## [[4]]
## [1] 5 9 1 6 10 7
```

reduce()

[1] 1 5

```
rerun(4, sample(1:10, 6))

## [[1]]
## [1] 9 4 7 1 2 5
##
## [[2]]
## [1] 7 2 3 8 1 5
##
## [[3]]
## [1] 5 6 9 2 1 10
##
## [[4]]
## [1] 5 9 1 6 10 7

rerun(4, sample(1:10, 6)) %>%
reduce(intersect)
```

Outline

- Introduction
- 2 Structures and types: tibble, forcats, string
- 3 data wrangling: readr, tidyr, dplyr
- Manipulation: magrittr, purr
- **5** Visualization: ggplot2

ggplot2



Figure 23: a system for declaratively creating graphics, based on The Grammar of Graphics

Fully documented (Wickham, 2016) http://ggplot2.tidyverse.org/



Learning ggplot2

R for data science (Wickham & Grolemund, 2017), http://r4ds.had.co.nz

See chapters data visualisation and graphics for communication



R for data science (Chang, 2012), http://www.cookbook-r.com/Graphs/



This course

A short introduction, mostly based on examples

ggplot2: grammar of graphics

Implements the grammar of graphics (Wilkinson, 2006)



Elements that composes a the grammar of ggplot

- a data set (data),
- a graphical projection/mapping (aes),
- a geometrical representation (geom),
- a statistical transformation (stats),
- a coordinate system (coord),
- some scales (scale),
- some groupings (facet).

Grammar of Graphics in ggplot: summary

→ any plot can be described by a combination of these 7 parameters.

ggplot2: standard steps

Supply data and specify mapping

with functions ggplot() and aes()

Create a layer

Combine data, mapping, a geometric object, a stat (statistical transformation) and a position adjustment

- by using geom() (overide the statistical transformation and position)
- by using stat() (specifying a statistical transformation with stat)
- add layers to the current ggplot object with the + operator

Adjustements

- the position (position_)
- the coordinate system (coord_)
- some annotations (annotation_)
- faceting (facet_)

Example: good old iris data set

as_tibble(iris)

```
## # A tibble: 150 x 5
##
     Sepal.Length Sepal.Width Petal.Length Petal.Width Species
##
            <dbl>
                       <dbl>
                                   <dbl>
                                              <dbl> <fct>
## 1
              5.1
                         3.5
                                     1.4
                                                0.2 setosa
              4.9
                         3
                                     1.4
## 2
                                                0.2 setosa
## 3
             4.7
                       3.2
                                    1.3
                                                0.2 setosa
             4.6
                                    1.5
## 4
                        3.1
                                                0.2 setosa
##
             5
                         3.6
                                     1.4
                                                0.2 setosa
##
             5.4
                        3.9
                                     1.7
                                               0.4 setosa
             4.6
                        3.4
                                    1.4
##
                                               0.3 setosa
                                    1.5
##
              5
                        3.4
                                               0.2 setosa
##
              4.4
                        2.9
                                    1.4
                                                0.2 setosa
              4.9
##
                         3.1
                                    1.5
                                                0.1 setosa
    ... with 140 more rows
```

Initializing the plot object

Supply data and mapping

All layers use a common data set and common set of aesthetics

```
ggplot(data = iris, aes(x = Species, y = Sepal.Length))
```

Supply data

All layers use a common data set, but with specific aesthetics

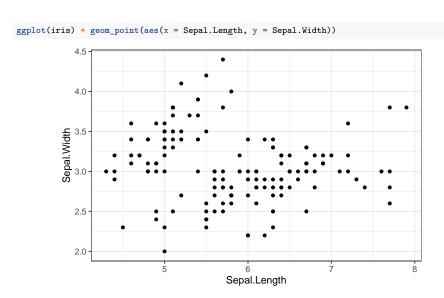
```
ggplot(data = iris)
```

Simple initialization

Each layer use a specific data set

```
ggplot()
```

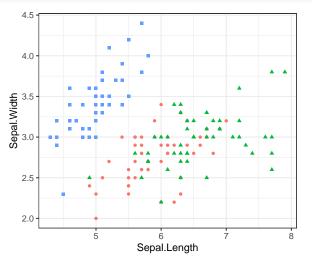
Add a layer: scatterplot



Add a layer: scatterplot + annotation

some aesthetic are optional

ggplot(iris) + geom_point(aes(x = Sepal.Length, y = Sepal.Width, color = Species, shape = Speci



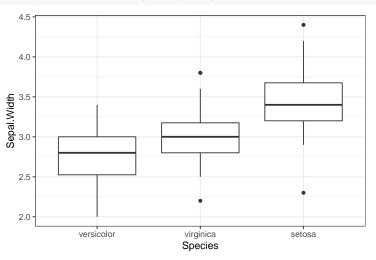
Species

- versicolor
- virginica
- setosa

Add a layer: boxplot

the aes depends on the geometry (here, a factor is expected for \boldsymbol{x})

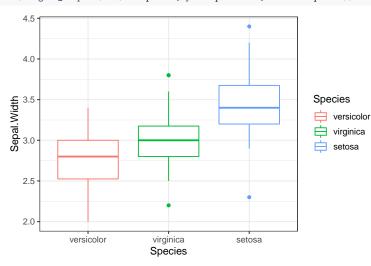
ggplot(iris) + geom_boxplot(aes(x = Species, y = Sepal.Width))



Add a layer: boxplot + annotation

the aes depends on the geometry (here, a factor is expected for x)

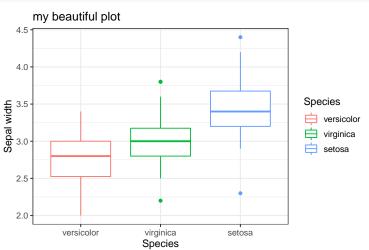
ggplot(iris) + geom_boxplot(aes(x = Species, y = Sepal.Width, color = Species))



Add a layer: boxplot + annotation (Cont'd)

the aes depends on the geometry (here, a factor is expected for x)

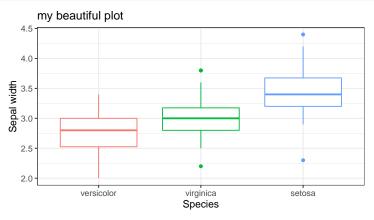
```
ggplot(iris) +
  geom_boxplot(aes(x = Species, y = Sepal.Width, color = Species)) +
labs("species", y = "Sepal width", title = "my beautiful plot")
```



Add a layer: boxplot + annotation (Cont'd)

the aes depends on the geometry (here, a factor is expected for x)

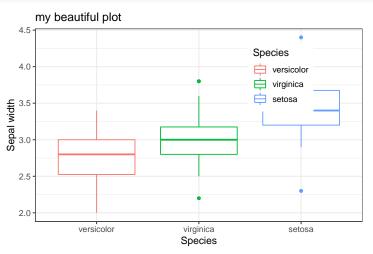
```
ggplot(iris) +
  geom_boxplot(aes(x = Species, y = Sepal.Width, color = Species)) +
  labs("species", y = "Sepal width", title = "my beautiful plot") +
  theme(legend.position = "bottom")
```



Add a layer: boxplot + annotation (Cont'd)

the aes depends on the geometry (here, a factor is expected for x)

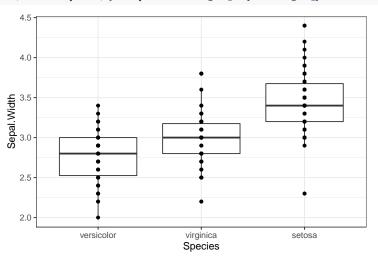
```
ggplot(iris) +
  geom_boxplot(aes(x = Species, y = Sepal.Width, color = Species)) +
  labs("species", y = "Sepal width", title = "my beautiful plot") +
  theme(legend.position = c(.75, .75))
```



Add several layers: boxplot + points

Note how I changed the use of ggplot since aesthetic where common to both

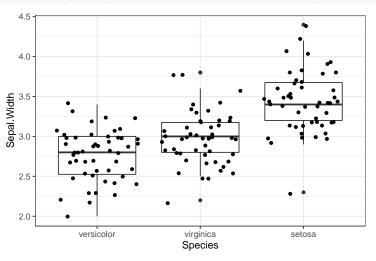
ggplot(iris, aes(x = Species, y = Sepal.Width)) + geom_boxplot() + geom_point()



Add several layers: boxplot + jitter

Note how I changed the use of ggplot since aesthetic where common to both

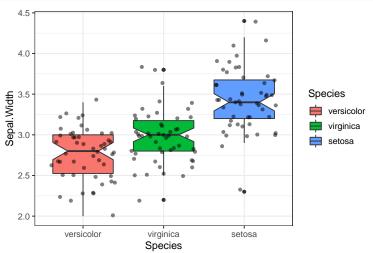
```
ggplot(iris, aes(x = Species, y = Sepal.Width)) + geom_boxplot() + geom_jitter()
```



Add several layers: boxplot + jitter

Note how I changed the use of ggplot since aesthetic where common to both

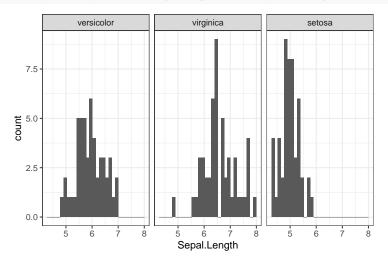
```
ggplot(iris, aes(x = Species, y = Sepal.Width)) +
  geom_boxplot(aes(fill = Species), notch = TRUE) +
  geom_jitter(alpha = .5)
```



Faceting

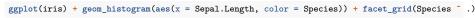
Note how I changed the use of ggplot since aesthetic where common to both

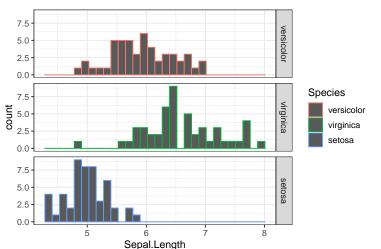
ggplot(iris) + geom_histogram(aes(x = Sepal.Length)) + facet_grid(. ~ Species)



Faceting (Cont'd)

Note how I changed the use of ggplot since aesthetic where common to both





Use ggplot2 in conjonction with other packages

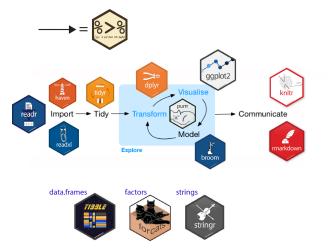


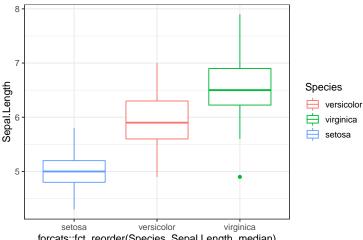
Figure 24: Remember the data process scheme?

The model/visualization part need constant wrangling/new arragement of your data set

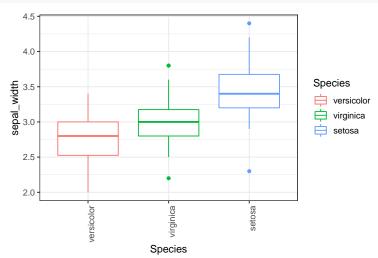
Example: forcats

Automatically more readable graphs

```
ggplot(iris) +
  geom_boxplot(aes(
    x = forcats::fct_reorder(Species, Sepal.Length, median),
   y = Sepal.Length, color = Species))
```

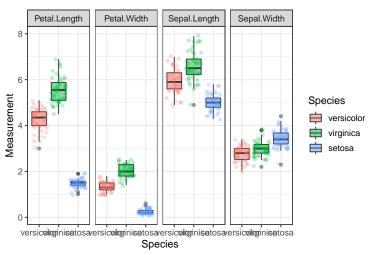


Example: dplyr + % > % for renaming before ploting



Example: dplyr + % for gathering new data

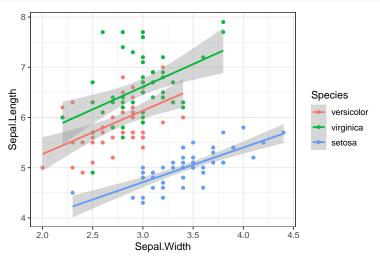
```
iris %>%
  gather(key = "Attribute", value = "Measurement", -Species) %>%
  ggplot(aes(x = Species, y = Measurement)) + geom_boxplot(aes(fill = Species), alpha = .5) +
  geom_jitter(aes(color = Species), alpha = 0.25) + facet_grid(. ~ Attribute)
```



Add a model layer

Adjust one linear model per species

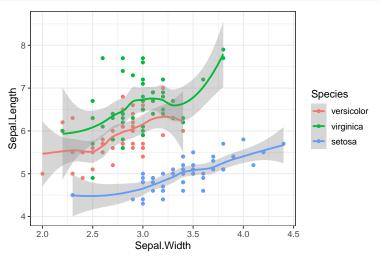
```
ggplot(iris, aes(x = Sepal.Width, y = Sepal.Length, colour = Species)) +
   geom_point() + geom_smooth(method = lm)
```



Add a model layer (Cont'd)

Adjust one nonlinear model per species

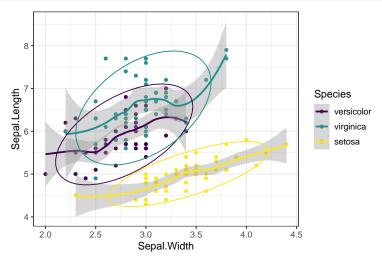
```
ggplot(iris, aes(x = Sepal.Width, y = Sepal.Length, color = Species)) +
  geom_point() + geom_smooth(method = loess)
```



Add model + stat layers and colorblind pallete

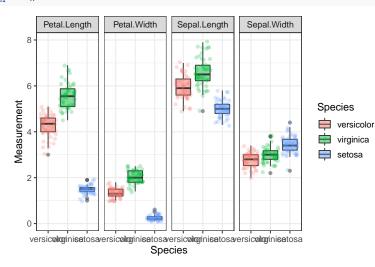
Adjust one nonlinear model per species

```
ggplot(iris, aes(x = Sepal.Width, y = Sepal.Length, color = Species)) +
geom_point() + geom_smooth(method = loess) +
stat_ellipse() + viridis::scale_color_viridis(discrete = TRUE)
```



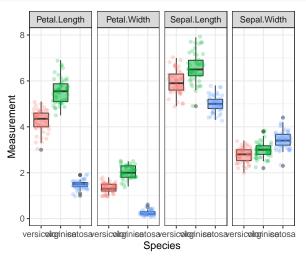
Transform coordinate: log-scales

```
ggplot(diamonds, aes(carat, price)) +
  geom_point()
```



Transform coordinate: log-scales

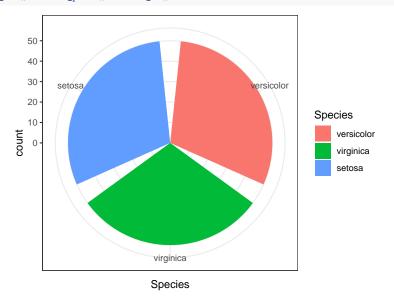
```
ggplot(diamonds, aes(carat, price)) +
  geom_point() + coord_trans(x = "log10") + coord_trans(y = "log10")
```



Species
versicolor
virginica
setosa

Changing coordinate system: polar

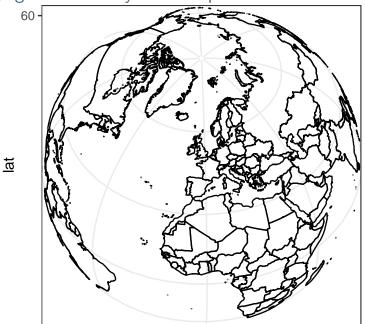
```
ggplot(iris, mapping = aes(x = Species, fill = Species)) +
  geom_bar() + coord_polar() + theme_bw()
```



Changing coordinate system: maps I

```
# World map, using geom_path instead of geom_polygon
world <- map_data("world")
worldmap <- ggplot(world, aes(x = long, y = lat, group = group)) +
    geom_path() +
    scale_y_continuous(breaks = (-2:2) * 30) +
    scale_x_continuous(breaks = (-4:4) * 45)
# Orthographic projection centered on Paris
worldmap + coord_map("ortho", orientation = c(48, -2, 0))</pre>
```

Changing coordinate system: maps II



References

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Wickham, H., & Grolemund, G. (2017). *R for data science: Visualize, model, transform, tidy, and import data.* "O'Reilly Media, Inc.". Retrieved from http://r4ds.had.co.nz

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