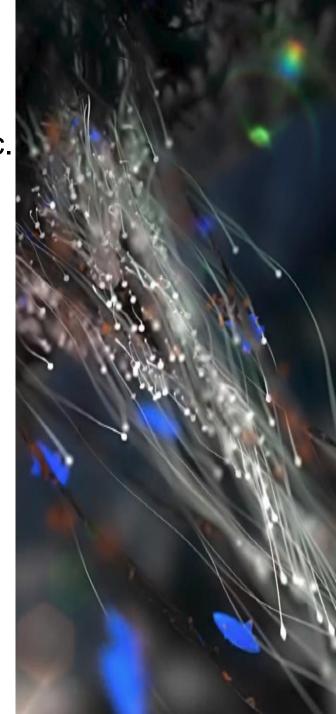
Computer Graphics -Particle Systems

Junjie Cao @ DLUT Spring 2016

http://jjcao.github.io/ComputerGraphics/

Particle Systems Overview

- Emitters generate tons of "particles"
 - Sprinkler, waterfall, chimney, gun muzzle, exhaust pipe, etc.
- Describe the external forces with a force field
 - E.g., gravity, wind
- Integrate the laws of mechanics (ODEs)
 - Makes the particles move
- In the simplest case, each particle is independent
- If there is enough **randomness** (in particular at the emitter) you get nice effects
 - sand, dust, smoke, sparks, flame, water, ...



Demo

- Sprinkler: http://www.youtube.com/watch?v=rhvH12nC6_Q
- Fire: http://www.youtube.com/watch?v=6hG00etwRBU

Generalizations

- More advanced versions of behavior
 - flocks, crowds
- Forces between particles
 - Not independent any more

- See
 - http://www.red3d.com/cwr/boids/ for discussion on how to do flocking.
 - http://www.blendernation.com/2008/01/05/simulating-flocks-herds-and-swarmsusing-experimental-blender-boids-particles/

Generalizations – Next Class

- Mass-spring and deformable surface dynamics
 - surface represented as a set of points
 - forces between neighbors keep the surface coherent

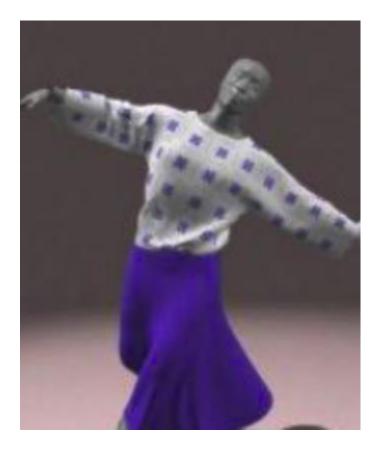


Image Witkin & Baraff

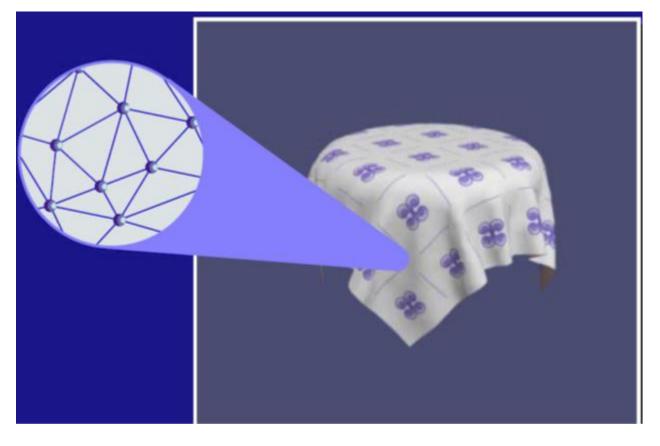


Image Michael Kass

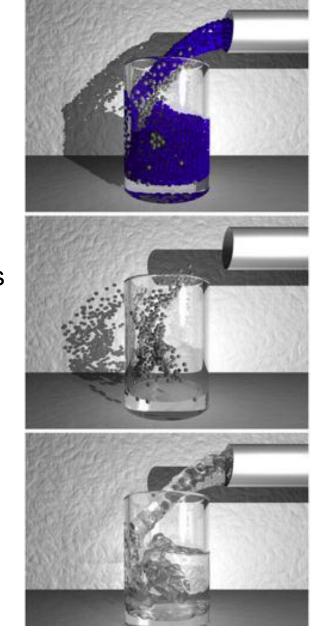
Cloth Video

Siggraph07 Efficient Simulation of Inextensible Cloth, <u>Eitan</u>
 <u>Grinspun</u> @ Columba University



Generalizations

- It's not all hacks: Smoothed Particle Hydrodynamics (SPH)
 - A family of "real" particle-based fluid simulation techniques.
 - Fluid flow is described by the Navier-Stokes Equations, a nonlinear partial differential equation (PDE)
 - SPH discretizes the fluid as small packets (particles!), and evaluates pressures and forces based on them.



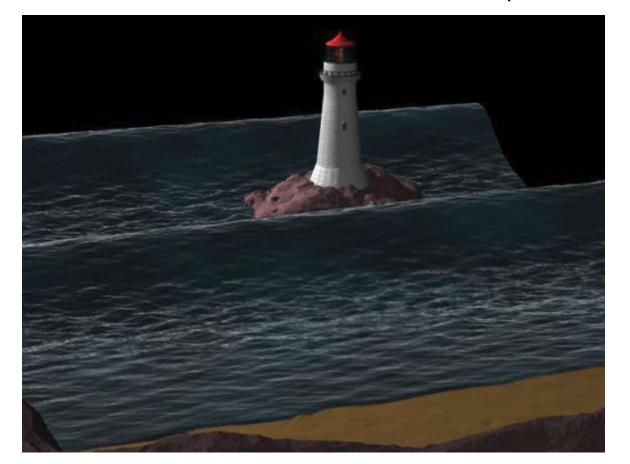
Müller et al. 2005

Demo

 These Stanford folks use SPH for resolving the small-scale spray and mist that would otherwise be too much for the grid solver to handle.

 Losasso, F., Talton, J., Kwatra, N. and Fedkiw, R., "Two-way Coupled SPH and Particle Level Set Fluid Simulation", IEEE TVCG 08, 797-804

(2008).



Real-time particles in games

• EA Fight Night 4 Physics Trailer

Take-Home Message

- Particle-based methods can range from pure heuristics (hacks that happen to look good) to "real" simulation
- Basics are the same: Things always boil down to integrating ODEs!
 - Also in the case of grids/computational meshes



Andrew Selle et al.

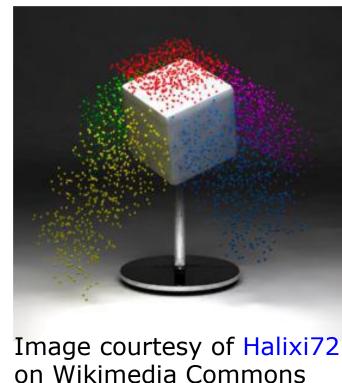
Questions?



http://www.cs.columbia.edu/cg/ESIC/esic.html

What is a Particle System?

- Collection of many small simple pointlike things
 - Described by their current state: position, velocity, age, color, etc.
- Particle motion influenced by external force fields and internal forces between particles
- Particles created by generators or emitters
 - With some randomness
- Particles often have lifetimes
- Particles are often independent
- Treat as points for dynamics, but rendered as anything you want



Simple Particle System: Sprinkler

```
PL: linked list of particle = empty;
spread=0.1;//how random the initial velocity is
colorSpread=0.1; //how random the colors are
For each time step
   Generate k particles
   p=new particle();
   p->position=(0,0,0);
   p->velocity=(0,0,1)+spread*(rnd(), rnd(), rnd());
   p.color=(0,0,1)+colorSpread*(rnd(), rnd(),rnd());
   PL->add(p);
For each particle p in PL
   p->position+=p->velocity*dt; //dt: time step
   p->velocity-=g*dt; //g: gravitation constant
   glColor(p.color);
   glVertex(p.position);
```

Demo with Processing

Test it online

https://processing.org/examples/simpleparticlesystem.html

Ordinary Differential Equations

 Many dynamical systems can be described via an ordinary differential equation (ODE) in generalized coordinates:

change in configuration over time $\frac{d}{dt}q=f(q,\dot{q},t)$

ODE doesn't have to describe mechanical phenomenon, e.g.,

$$\frac{d}{dt}u(t) = au$$

"rate of growth is proportional to value"

- Solution? $u(t) = be^{at}$
- Describes exponential decay (a < 1), or really great stock (a > 1)
- "Ordinary" means "involves derivatives in time but not space"
- We'll talk about spatial derivatives (PDEs) in another lecture...

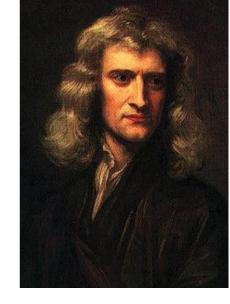
Newtonian Mechanics

Point mass: 2nd order ODE

$$ec{F}=mec{a}$$
 or $ec{F}=mrac{d^2ec{x}}{dt^2}$

- Position x and force F are vector quantities
 - We know **F** and **m**, want to solve for **x**

You have all seen this a million times before



Reduction to 1st Order

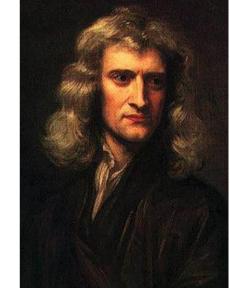
Point mass: 2nd order ODE

$$\vec{F}=m\vec{a}$$
 or $\vec{F}=mrac{d^2\vec{x}}{dt^2}$

 Can also write as a system of two first order ODEs, by introducing new "dummy" variable for velocity:

$$\left\{egin{array}{ll} rac{d}{dt}ec{m{x}}=ec{m{v}} & ext{2 unknowns } (\mathbf{x},\mathbf{v}) \ rac{d}{dt}ec{m{v}}=ec{m{F}}/m & ext{instead of just } \mathbf{x} \end{array}
ight.$$

- Corresponds to system of first order ODEs
 - Splitting things up this way will make it easy to talk about solving these equations numerically (among other things)



Notation

Let's stack the pair (x, v) into a bigger state vector X

$$oldsymbol{X} = egin{pmatrix} ec{oldsymbol{x}} \ ec{oldsymbol{v}} \end{pmatrix}$$

 $m{X} = egin{pmatrix} m{ec{x}} \ m{v} \end{pmatrix}$ For a particle in 3D, state vector $m{X}$ has 6 numbers

$$\frac{d}{dt}\mathbf{X} = f(\mathbf{X}, t) = \begin{pmatrix} \vec{\mathbf{v}} \\ \vec{\mathbf{F}}(x, v)/m \end{pmatrix}$$

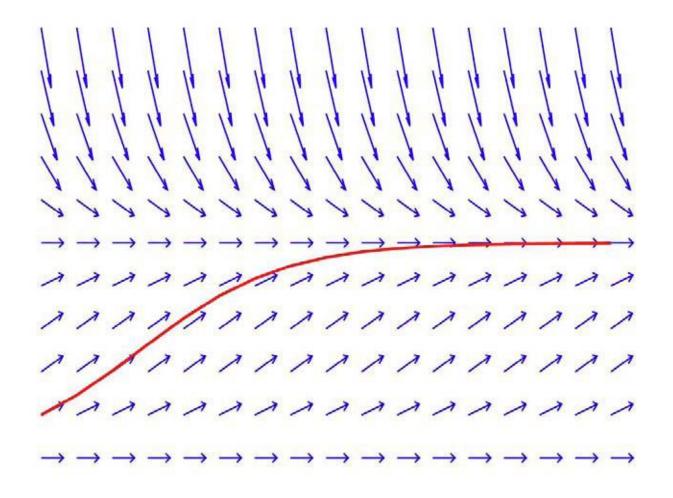
Now, Many Particles

- We have N point masses
 - Let's just stack all xs and vs in a big vector of length 6N
 - **F**i denotes the force on particle *i* When particles don't interact, **F**i only depends on **x**i and **v**i.

$$egin{aligned} egin{aligned} rac{d}{dt} ec{m{x}} &= ec{m{v}} \ rac{d}{dt} ec{m{v}} &= ec{m{F}}/m \ ec{m{c}} \ m{v}_1 \ dots \ m{v}_N \ m{v}_N \end{pmatrix} & \qquad rac{d}{dt} m{X} = f(m{X},t) = egin{pmatrix} m{v}_1 \ m{F}^1(m{X},t) \ dots \ m{v}_N \ m{F}^N(m{X},t) \end{pmatrix} \end{aligned}$$

Path through a Vector Field

• X(t): path in multidimensional phase space



$$\frac{\mathrm{d}}{\mathrm{d}t}\boldsymbol{X} = f(\boldsymbol{X}, t)$$

"When we are at state **X** at time *t*, where will **X** be after an infinitely small time interval d*t*?"

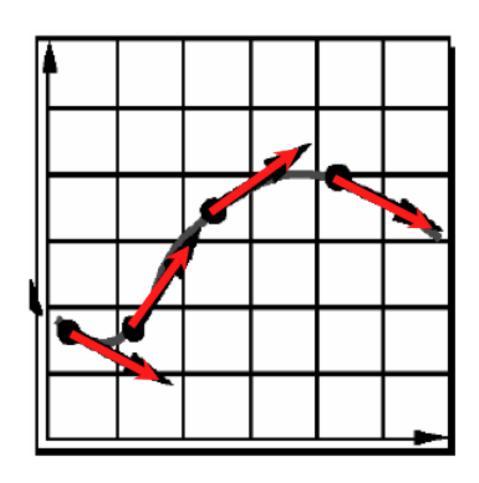
f=d/dt X is a vector that sits at each point in phase space, pointing the direction.

Numerics of ODEs

- Numerical solution is called "integration of the ODE"
- Many techniques
 - Today, the simplest one
 - next we'll look at some more advanced techniques

Intuitive Solution: Take Steps

- Current state X
 - Examine f(X,t) at (or near) current state
 - Take a step to new value of X



$$\frac{\mathrm{d}}{\mathrm{d}t}\boldsymbol{X} = f(\boldsymbol{X}, t)$$

$$\Rightarrow$$
 "d $X = dt f(X, t)$ "

f = d/dt X is a vector
 that sits at each
 point in phase
 space, pointing the
 direction.

Euler's Method

- Simplest and most intuitive
- Pick a step size h
- Given **X**0=**X**(*t*0), take step:

$$t_1 = t_0 + h$$
$$\mathbf{X}_1 = \mathbf{X}_0 + h f(\mathbf{X}_0, t_0)$$

- Piecewise-linear approximation to the path
- · Basically, just replace dt by a small but finite number

Euler, Visually

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{X} = f(\mathbf{X}, t)$$

$$\mathbf{X}_1 = \mathbf{X}_0 + h f(\mathbf{X}_0, t_0)$$

$$h f(\mathbf{X}, t)$$

$$\mathbf{X}_1 = \mathbf{X}_0 + h f(\mathbf{X}_0, t_0)$$

Effect of Step Size

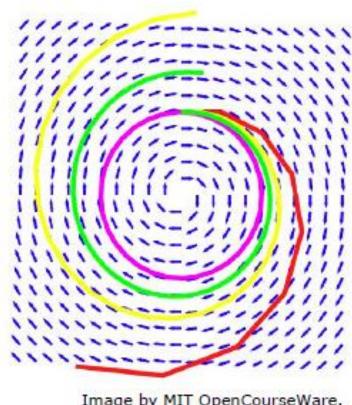
- Step size controls accuracy
- Smaller steps more closely follow curve
 - May need to take many small steps per frame
 - Properties of f(X, t) determine this (more later)
- Moves along tangent; can leave solution curve, e.g.:

$$f(\mathbf{X},t) = \begin{pmatrix} -y \\ x \end{pmatrix}$$

Exact solution is circle:

$$\mathbf{X}(t) = \begin{pmatrix} r\cos(t+k) \\ r\sin(t+k) \end{pmatrix}$$

- Euler spirals outward no matter how small h is
 - will just diverge more slowly



More Accurate Alternatives

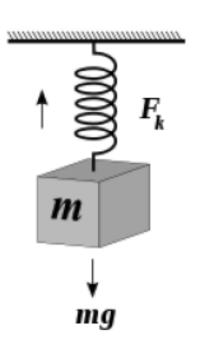
- Midpoint, Trapezoid, Runge-Kutta
 - Also, "implicit methods" (next week)

More on this during next class

 Extremely valuable resource: SIGGRAPH 2001 course notes on physically based modeling

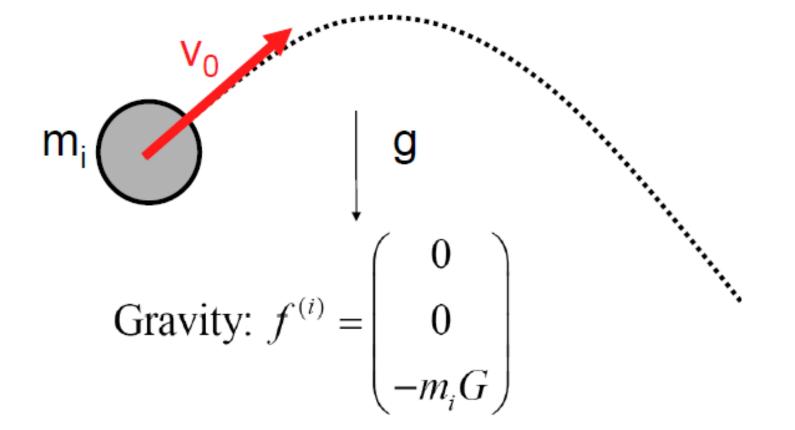
What is a Force?

- A force changes the motion of the system
 - Newton says: When there are no forces, motion continues uniformly in a straight line (good enough for us)
- Forces can depend on location, time, velocity
 - Gravity, spring, viscosity, wind, etc.
- For point masses, forces are vectors
 - le., to get total force, take vector sum of everything



Forces: Gravity on Earth

- Depends only on particle mass
 - $f(\mathbf{X},t) = \text{constant}$
- Hack for smoke, etc: make gravity point up!
 - Well, you can call this buoyancy, too.



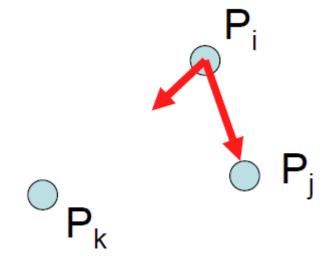


Forces: Gravity (N-body problem)

- Gravity depends on all other particles
- Opposite for pairs of particles
- Force in the direction of pi-pj with magnitude inversely proportional to square distance

$$\|oldsymbol{F}_{ij}\| = rac{G\,m_i\,m_j}{r^2}$$
 where G=6.67×10-11 Nm²/kg²

• Testing all pairs is O(n2)!



Real-Time Gravity Demo

http://www.youtube.com/watch?v=uhTuJZiAG64

An Aside on Gravity

- That was Brute Force
 - Meaning all O(n2) pairs of particles were considered when computing forces
 - Yes, computers are fast these days, but this gets prohibitively expensive soon. (The square in *n*2 wins.)
- Hierarchical techniques approximate forces caused by many distant attractors by one force, yields O(n)!
 - Fast Multipole Method", Greengard and Rokhlin, J Comput Phys 73, p. 325 (1987)
 - This inspired very cool hierarchical illumination rendering algorithms in graphics (hierarchical radiosity, etc.)

Forces: Viscous Damping

$$f^{(i)} = -dv^{(i)}$$

- Damping force on particle i determined its velocity
 - Opposes motion
 - E.g. wind resistance
- Removes energy, so system can settle
- Small amount of damping can stabilize solver
- Too much damping makes motion like in glue

Forces: Spatial Fields

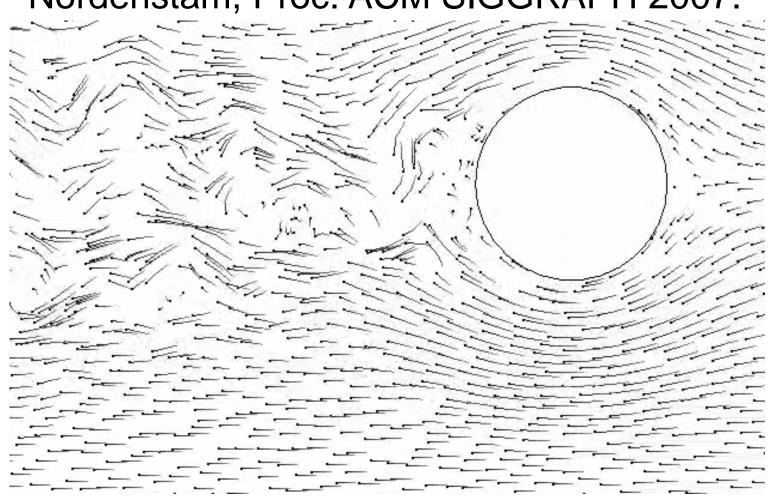
- Externally specified force (or velocity) fields in space
- Force on particle i depends only on its position
- Arbitrary functions
 - wind
 - attractors, repulsors
 - vortices
- Can depend on time
- Note: these add energy, may need damping

Processing demo

http://processing.org/learning/topics/smokeparticlesystem.html

Example: Procedural Spatial Field

Curl noise for procedural fluid flow, R. Bridson, J. Hourihan, and M. Nordenstam, Proc. ACM SIGGRAPH 2007.



Plausible,
conrollable force
fields – just
advecting particles
along the flow gives
cool results!

And it's simple, too!

Curl-Noise for Procedural Fluid Flow



Robert Bridson

Jim Hourihan

Markus Nordenstam

Many cool paper with example code used in famous film: The Hobbit, Avatar, Harry Potter, X-Man First Class

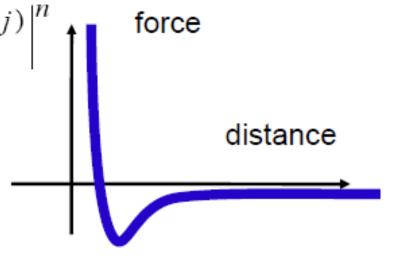
Forces: Other Spatial Interaction

Spatial interaction:
$$f^{(i)} = \sum_{j} f(x^{(i)}, x^{(j)})$$

• E.g., approximate fluid using Lennard-Jones force:

$$f(x^{(i)}, x^{(j)}) = \frac{k_1}{|x^{(i)} - x^{(j)}|^m} - \frac{k_2}{|x^{(i)} - x^{(j)}|^n}$$
 force

- Repulsive + attractive force
- Again, O(N²) to test all pairs
 - usually only local
 - Use buckets to optimize. Cf. 6.839



Lennard-Jones forces

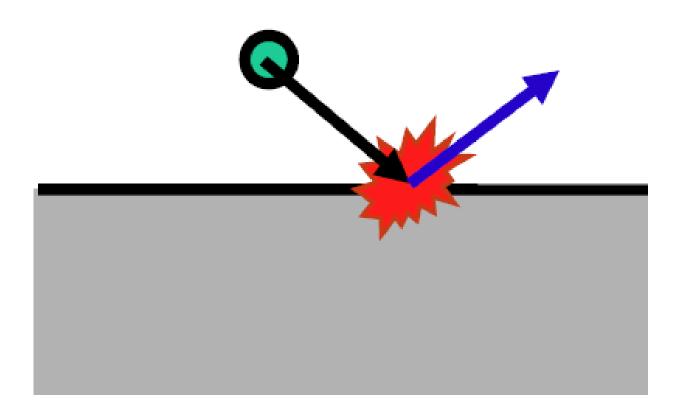
http://www.youtube.com/watch?v=nl7maklgYnl&feature=related

 http://www.youtube.com/watch?v=XfjYlKxKIWQ&feature=autoplay&list= PL0605C44C6E8D5EDB&lf=autoplay&playnext=2

http://www.youtube.com/watch?v=dHWCT7RPjPo

Collisions

- Detection
- Response
- Covered later



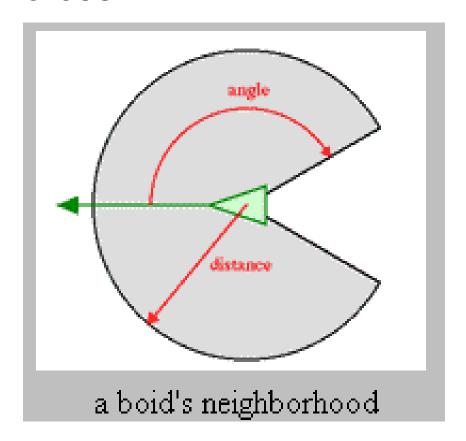
More Advanced "Forces"

- Flocking birds, fish shoals
 - http://www.red3d.com/cwr/boids/
- Crowds (www.massivesoftware.com)

Flocks ("Boids")

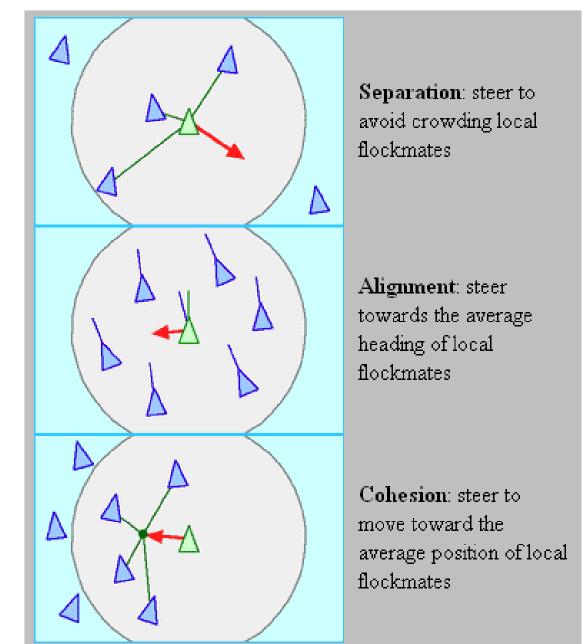
- From Craig Reynolds
- Each bird modeled as a complex particle ("boid")
- A set of forces control its behavior
- Based on location of other birds and control forces





Flocks ("Boids")

 ("Boid" was an abbreviation of "birdoid". His rules applied equally to simulated flocking birds, and shoaling fish.)



Demos

- Predator-Prey
 - http://www.youtube.com/watch?v=rN8DzlgMt3M
- Massive software
 - http://www.massivesoftware.com/
 - Used for battle scenes in the Lord of The Rings
- Processing
 - http://processing.org/learning/topics/flocking.html, simple implementation
- Lord of The Rings = Battle of the Helm's deep

Where do particles come from?

- Often created by generators or emitters
 - Can be attached to objects in the model
- Given rate of creation: particles/second
 - record tlast of last particle created

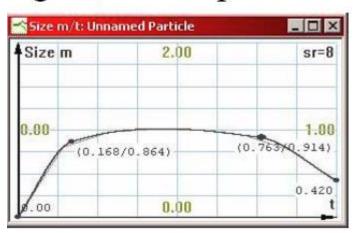
$$n = \lfloor (t - t_{last}) rate \rfloor$$

- create n particles. update *tlast* if n > 0
- Create with (random) distribution of initial x and v
 - if creating n > 1 particles at once, spread out on path

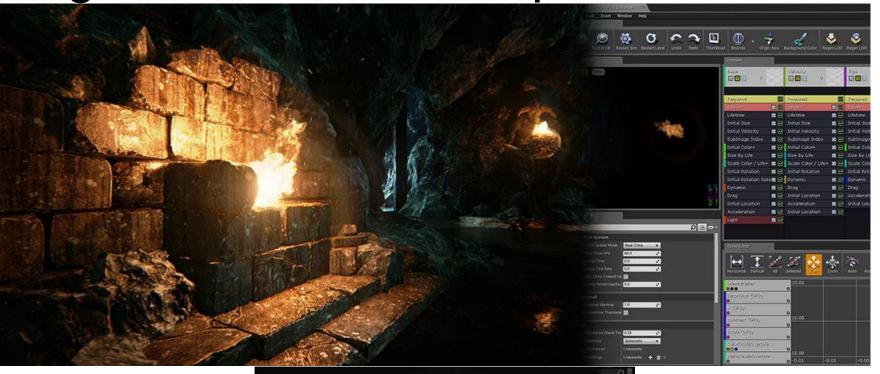
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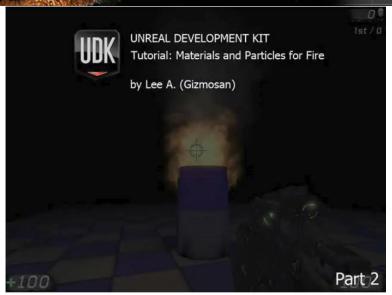
Particle Controls

- In production tools, all these variables are time-varying and controllable by the user (artist)
 - Emission rate, color, velocity distribution, direction spread, textures, etc. etc.
 - All as a function of time!
- Example: ParticleFX (Max Payne Particle Editor)
 - Custom editor software
 - You can download it (for Windows) and easily create your own particle systems.
 Comes with examples!
 - This is what we used for all the particles in the game! Again, reuse splines!



Unreal Engine: materials and particles for fire





Rendering and Motion Blur

- Often not shaded (just emission, think sparks)
 - But realistic non-emissive particles needs shadows, etc.
- Most often, particles don't contribute to the z-buffer, i.e., they do not fully occlude stuff that's behind
 - Rendered with z testing on (particles get occluded by solid stuff)
- Draw a line for motion blur
 - (x, x+v dt)
 - Or an elongated quad with texture
- Often use texture maps (fire, clouds, smoke puffs)
 - Called "billboards" or "sprites"
 - Always parallel to image plane



Metal Gear Solid by Konami

More Eyecandy from NVIDIA

- Fluid flow solved using a regular grid solver
 - This gives a velocity field
- 0.5M smoke particles advected using the field
 - That means particle velocity is given by field
- Particles are for rendering, motion solved using other methods

https://www.youtube.com/watch?v=RuZQpWo9Qhs

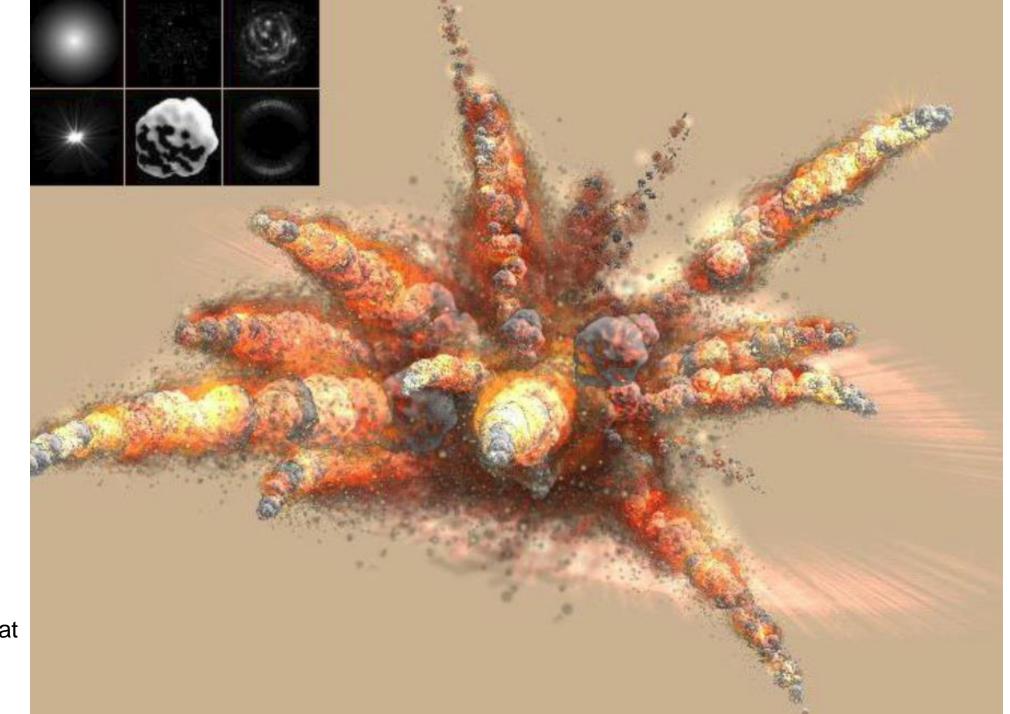
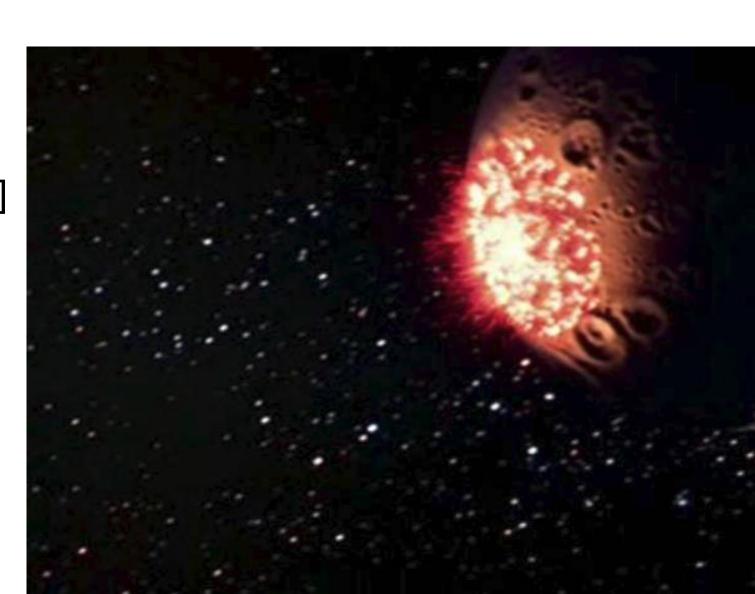


Image from Sameboat

Star Trek 2 – The Wrath of Khan

- One of the earliest particle systems (from 1982)
- Also, fractal landscapes

• Described in [Reeves, 1983]



Particle Modeling [Reeves 1983]

- The grass is made of particles
 - The entire lifetime of the particle is drawn at once.
 - This can be done procedurally on the GPU these days!



That's All for Today!

- Further reading
 - Witkin, Baraff, Kass: Physically-based Modeling Course Notes, SIGGRAPH 2001
 - Extremely good, easy-to-read resource. Highly recommended!
 - William Reeves: Particle systems—a technique for modeling a class of fuzzy objects, Proc. SIGGRAPH 1983
 - The original paper on particle systems

particlesystems.org