

INTELLIGENT SYSTEMS – LAB GROUP A3

# OSM-GPS



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## GITHUB REPOSITORY

<https://github.com/jupcan/osm-gps>

## COMPONENTES DEL GRUPO

Juan Perea Campos

Samuel González Linde

Javier Abengózar Palop

## 1. TASK 1 DOCUMENTATION

### 1.1 APPLICATION REQUIREMENTS

The main goal of the laboratory assignment is to implement a search algorithm in order to obtain an optimal route for a vehicle that circulates through a set of places of a town. The route must pass through several concrete places.

We are going to talk about NODES and ARCS. The application will be fed of the essential information by XML files generated from OpenStreetMap (OSM) and converted to graphml format. So, the first requirement Task 1 is the programming of classes that allows us to represent a map with the information of an XML file. The class named '*graph*' will contain three methods called '*belongNode*', '*positionNode*' and '*adjacentNodes*'.

### 1.2 PROGRAMMING LANGUAGE

Since we could choose whatever language to work on, several decisions had to take place before starting to work. At first, we decided to use java language as it has been our most used programming language, but the decision changed when we found that other languages could improve the way of working with data structures, so the final choice was **python**. Also, the simply way the aforementioned language provides to do basic programming methodology will allow us to focus on the main issues of the code related with the artificial intelligent field.

### 1.3 STRUCTURES OF CREATED ARTIFACTS

We will use three important libraries for this task that will allow us to build the proper structure, manage files information and print data structures with a desired format, essential to solve the problem. The first one is '*lxml*' which contains the element etree, enabling the XML file reading and its analysis to build a tree that we will be using as base to create and store all the data in our chosen data structure. To solve the main goal of the laboratory part, this data structure is essential, so we decided to import a library able to build this kind of abstraction. The second imported library is just one we decided to use in order to print the file name we are using each time in a simple way, it is called '*os.path*'. And the third library is '*pprint*' that will help us to print in a pretty way data structures.

```
from lxml import etree
from os.path import basename
from pprint import pprint
```

## GRAPH CLASS

To achieve the objective, we have created a class named *graph*. It contains the needed variables and methods to read XML files, check if a node belongs to a graph and its position and the adjacent edges of a specific node.

```
class graph():
    _path = ""
    def __init__(self, path):
        self._path = path
        self._keys, self._nodes, self._edges = self._readFile()
```

This class has as attributes:

- ‘\_path’: path of the XML file containing the map information.
- ‘\_keys’: a dictionary containing all keys information which appear in the XML files and help us as a guide for all the type of keys that exists.
- ‘\_nodes’: a dictionary containing all nodes that conform the graph.
- ‘\_edges’: a dictionary containing all edges that conform the graph.

The path will be the parameter use in the constructor to create each graph.

It also has four methods:

1. **readFile():** this method takes care for the reading of the XML file containing the essential information needed to create the tree. The previous mentioned element from the lxml library etree can build a tree with *.parse(path)* receiving as a parameter the path of the file. With the method *.getroot()* we get the tree’s root (and later its nodes). The method is defined to represent the keys, nodes and edges in a dictionary to access to a specific element in an easy way. It collects the keys from the XML files and store them in the dictionaries. This method returns three dictionaries containing keys, nodes and edges respectively.

```
def _readFile(self):
    data = etree.parse(self._path)
    root = data.getroot()
    ns = {'n': 'http://graphml.graphdrawing.org/xmlns'}

    keys, nodes, edges = {}, {}, {}
    print(basename(self._path)) #print file name
    for key in root: #get desired key values for each file
        keys[(key.get('attr.name'), key.get('for'))] = (key.get('id'))
    key_y = keys[('y', 'node')]
    key_x = keys[('x', 'node')]
    key_name = keys[('name', 'edge')]
    key_length = keys[('length', 'edge')]

    for node in root.findall('n:graph/n:node', ns):
        data = dict((d.get('key'), d.text) for d in node)
```

```

        values = (data.get(key_y), data[key_x])
        nodes[node.get('id')] = values

    for edge in root.findall('n:graph/n:edge', ns):
        data = dict((d.get('key'), d.text) for d in edge)
        values = (data.get(key_name, 'sinNombre'), data[key_length])
        edges[(edge.get('source'), edge.get('target'))] = values
    return keys, nodes, edges

```

2. **belongNode():** this method checks if a node belongs to the graph, with the argument 'id' as a parameter representing it the node to be checked.

```

def belongNode(self, id):
    #input: osm node id, output: true/false
    if id in self._nodes:
        return True
    else:
        return False

```

3. **positionNode():** the method checks if a node belongs to the graph by using the previous created method and if so it returns its coordinates, latitude and longitude (x,y). It also receives the 'id' of a node as a parameter.

```

def positionNode(self, id):
    #input: osm node id, output: latitude&longitude[(y,x)]
    try:
        node_exists = self.belongNode(id)
        if node_exists:
            print([self._nodes[id]])
        else:
            raise ValueError
    except ValueError:
        print("Error. The node does not exist.")

```

4. **adjacentNode():** receives the 'id' of a node as a parameter, checks if it belongs to the graph we are using and, if so it prints a list of the adjacent arcs for the given node. The output is also a dictionary in which the key for each street of the map is made up of the tuple (origin, target) since this must be always *UNIQUE*. A given node id could be repeated for several arcs.

```

def adjacentNode(self, id):
    #input: osm node id, output: list of adjacent arcs
    try:
        node_exists = self.belongNode(id)
        streets = {}
        if node_exists:
            adjacents = [key for key in self._edges.keys() if id in key[0]]
            for data in adjacents:
                streets[data] = tuple(self._edges[data])
            pprint(streets)
        else:
            raise ValueError
    except ValueError:
        print("Error. The node does not exist.")

```

## MAIN CLASS

In the main class we only create an object of the class *'graph'* and call its methods to give us the results, we also check the access time to any of the dictionaries created. We have also added a way to read from the input and write one more node at a time by separating it by comas, to check the correctness of the results in a faster way.

```

#!/usr/bin/python3
# -*- coding: utf-8 -*-
from graph import graph
import time

def main():
    try:
        filename = input('file: ')
        if filename.isdigit():
            raise ValueError
        town1 = graph('data/%s.graphml.xml' % filename)
        nodes = [i for i in input('nodes: ').split(',')]
        for node in nodes:
            start_time = time.time()
            print(town1.belongNode(node))
            town1.positionNode(node)
            town1.adjacentNode(node)
            print("%s seconds" % (time.time() - start_time))

    except ValueError:
        print("Error. Not a valid input.")

if __name__ == '__main__':
    main()

```

When executing in the command line, an input example could be the following one:

```
file: ciudad_real.graphml.xml  
nodes: 796725819,765309509,827212358
```

## 1.4 JUSTIFICATION OF USED ARTIFACTS - ACCESSING TIMES

- Number of elements (n): 1.000, 10.000, 100.000, 1.000.000 and 10.000.000:
- Checking of the access time for n element sized list
- 5 access tests for each n, mean of access
- Average list access time

Working with the first element of the list, mid element of the list and final element of the list in order to take the values of the accessing time in different positions. The same properties described before will be used to test the accessing times of the dictionaries.

## LIST TIMES

<i>n = 1.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000143051	0,00000095367	0,00000071526	0,00000047684	0,00000095367	0,00000090599
<i>middle element:</i>	0,00000882149	0,00000715256	0,00000619888	0,0000064373	0,00000691414	0,00000710487
<i>last element:</i>	0,00000047684	0,00000047684	0,00000023842	0,00000047684	0,00000071526	0,00000047684
<i>average/access:</i>	0,00000268221	0,00000214577	0,00000178814	0,00000184775	0,00000214577	<b>0,00000212193</b>
<i>n = 10.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000095367	0,00000095367	0,00000143051	0,00000119209	0,00000095367	0,00000109672
<i>middle element:</i>	0,00000786781	0,00000977516	0,00001072884	0,00000929832	0,00000858307	0,00000925064
<i>last element:</i>	0,00000047684	0,00000047684	0,00000047684	0,00000047684	0,00000047684	0,00000047684
<i>average/access:</i>	0,00000232458	0,00000280142	0,00000315905	0,00000274181	0,00000250340	<b>0,00000270605</b>
<i>n = 100.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000166893	0,00000119209	0,00000095367	0,00000119209	0,00000095367	0,00000119209
<i>middle element:</i>	0,00001072884	0,00000953674	0,00000977516	0,00000977516	0,000010252	0,00001001358
<i>last element:</i>	0,00000047684	0,00000047684	0,00000047684	0,00000023842	0,00000047684	0,00000042916
<i>average/access:</i>	0,00000321865	0,00000280142	0,00000280142	0,00000280142	0,00000292063	<b>0,00000290871</b>
<i>n = 1.000.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000095367	0,00000119209	0,00000095367	0,00000143051	0,00000143051	0,00000119209
<i>middle element:</i>	0,00001001358	0,00000953674	0,00001144409	0,00000929832	0,00000929832	0,00000991821
<i>last element:</i>	0,00000047683	0,00000047684	0,00000047684	0,00000023842	0,00000047684	0,00000042915
<i>average/access:</i>	0,00000286102	0,00000280142	0,00000321865	0,00000274181	0,00000280142	<b>0,00000288486</b>
<i>n = 10.000.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000190735	0,00000166893	0,00000143051	0,00000143051	0,00000143051	0,00000157356
<i>middle element:</i>	0,00001692772	0,00001621246	0,00000977516	0,00001096725	0,00001168251	0,00001311302
<i>last element:</i>	0,00000047684	0,00000071526	0,00000047684	0,00000047684	0,00000047684	0,00000052452
<i>average/access:</i>	0,00000482798	0,00000464916	0,00000292063	0,00000321865	0,00000339747	<b>0,00000380278</b>
<i>n</i>	<b>1.000</b>	<b>10.000</b>	<b>100.000</b>	<b>1.000.000</b>	<b>10.000.000</b>	
<i>time (s)</i>	<b>0,00212192600</b>	<b>0,00270605050</b>	<b>0,00290870650</b>	<b>0,00288486350</b>	<b>0,00380277650</b>	



## DICTIONARIES TIMES

<i>n = 1.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000071526	0,00000095367	0,00000071526	0,00000119209	0,00000071526	0,00000085831
<i>middle element:</i>	0,00000238419	0,00000309944	0,00000149042	0,00000357628	0,00000286102	0,00000268227
<i>last element:</i>	0,00000071526	0,00000047684	0,00000095367	0,00000071526	0,00000071526	0,00000071526
<i>average/access:</i>	0,00000095368	0,00000113249	0,00000078984	0,00000137091	0,00000107289	0,00000106396
<i>n = 10.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000095367	0,00000095367	0,00000119209	0,00000095367	0,00000095367	0,00000100135
<i>middle element:</i>	0,00000333786	0,00000286102	0,00000357628	0,00000452995	0,0000038147	0,00000362396
<i>last element:</i>	0,00000071526	0,00000047684	0,00000071526	0,00000095367	0,00000071526	0,00000071526
<i>average/access:</i>	0,00000125170	0,00000107288	0,00000137091	0,00000160932	0,00000137091	0,00000133514
<i>n = 100.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000119209	0,00000119209	0,00000166893	0,00000119209	0,00000166893	0,00000138283
<i>middle element:</i>	0,0000038147	0,00000452995	0,00000452995	0,0000038147	0,00000429153	0,00000419617
<i>last element:</i>	0,00000119209	0,00000071526	0,00000095367	0,00000143051	0,00000095367	0,00000104904
<i>average/access:</i>	0,00000154972	0,00000160933	0,00000178814	0,00000160933	0,00000172853	0,00000165701
<i>n = 1.000.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00000143051	0,00000119209	0,00000166893	0,00000143051	0,00000166893	0,00000147819
<i>middle element:</i>	0,00000500679	0,00000452995	0,00000476837	0,00000548363	0,00000452995	0,00000486374
<i>last element:</i>	0,00000095367	0,00000095367	0,00000119209	0,00000095367	0,00000119209	0,00000104904
<i>average/access:</i>	0,00000184774	0,00000166893	0,00000190735	0,00000196695	0,00000184774	0,00000184774
<i>n = 10.000.000</i>						
	<i>1st access</i>	<i>2nd access</i>	<i>3rd access</i>	<i>4th access</i>	<i>5th access</i>	<i>average/element</i>
<i>first element:</i>	0,00006480217	0,00000166893	0,00000143051	0,00001049042	0,00000190735	0,00001605988
<i>middle element:</i>	0,00001335144	0,00000524521	0,00000476837	0,00001597404	0,00000429153	0,00000872612
<i>last element:</i>	0,00009584427	0,00000071526	0,00000119209	0,00002503395	0,00000071526	0,00002470017
<i>average/access:</i>	0,00004349947	0,00000190735	0,00000184774	0,00001287460	0,00000172854	0,00001237154
<i>n</i>	1.000	10.000	100.000	1.000.000	10.000.000	
<i>time (s)</i>	0,00106395900	0,00133514350	0,00165700800	0,00184774250	0,01237154000	

## GRAPHICAL RESULTS

Figure 1

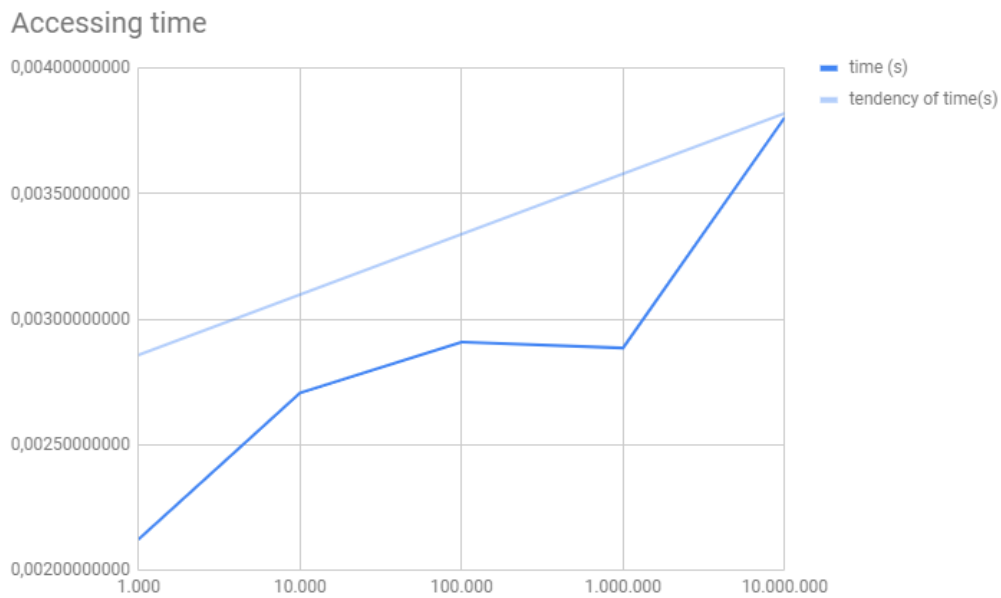
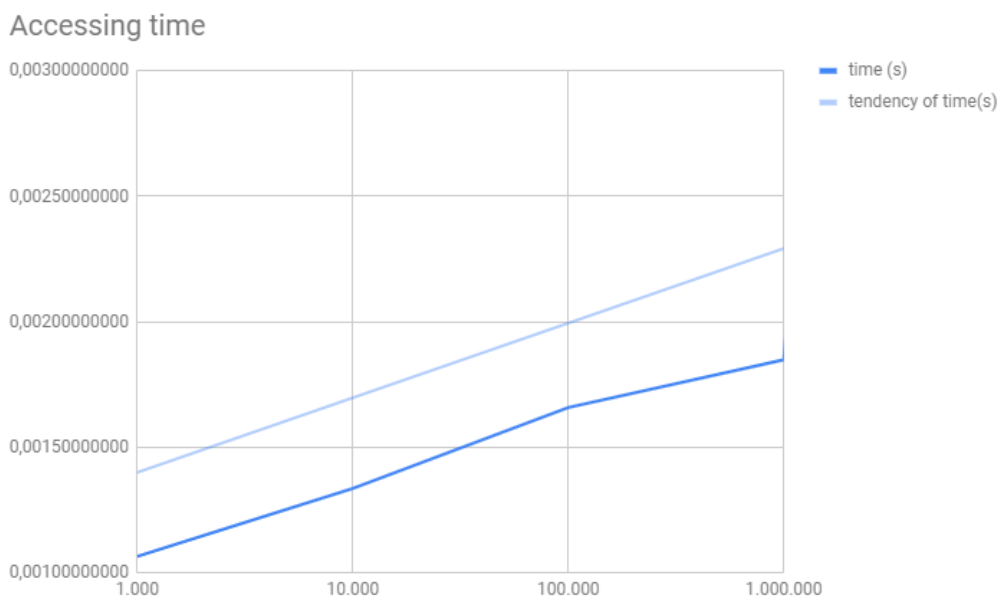


Figure 2

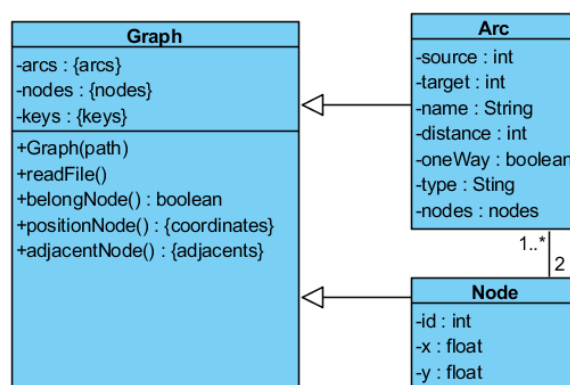
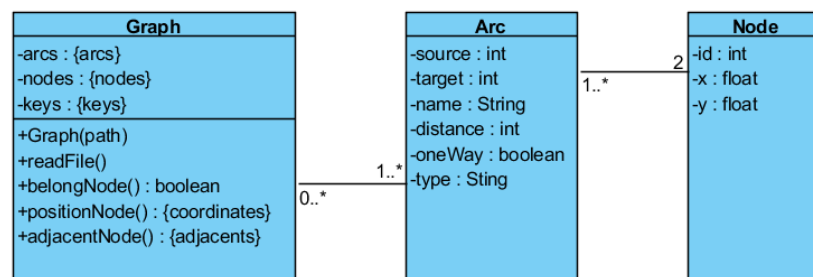


As we can see, comparing both figures being the first one for list data structures and the second one for dictionaries, last mentioned ones have a lower accessing time to data that will be key for us since when our program starts to be more complex and doing searches, the time could grow exponentially causing lots of memory problems.

That's the **main reason** has led us to **use dictionaries instead of list**. At first, we used list and look for the desired data by means of a sequential access which was not efficient enough, in python we can also access a list member by checking its index but the language behind the scenes, iterates through the list until it finds the number or reaches the end of the list so it's the same as going across all elements in a 'for', however in a dictionary python can attempt to directly access the target number in the set, rather than iterate through every item in the list and compare every item to the target number.

## 1.5 UML SKETCHES

This does not clearly represent the implementation of our code but was used as first draft to start thinking about our goals, so we found it interesting to also show it over here.



## 1.6 BIBLIOGRAPHY

- [https://docs.quantifiedcode.com/python-anti-patterns/performance/using\\_key\\_in\\_list\\_to\\_check\\_if\\_key\\_is\\_contained\\_in\\_a\\_list.html](https://docs.quantifiedcode.com/python-anti-patterns/performance/using_key_in_list_to_check_if_key_is_contained_in_a_list.html)
- <https://stackoverflow.com/>

## 2. TASK 2 DOCUMENTATION

### 2.1 APPLICATION REQUIREMENTS

The second task is about the definition and implementation of several elements needed to solve main problem. These elements are *Frontier*, *State*, *Space State*, *Problem* and *TreeNode*. Now, the 'graph' class is named "stateSpace" and 'adjacentNodes' method has been replaced by 'successors' method.

### 2.2 STRUCTURES OF CREATED ARTIFACTS

To the ones imported in the task1 we are adding mostly calls to other classes so that we can use their content. Also mention an array bisection algorithm '**bisect**' that provides support for maintaining a list in sorted order without having to sort the list after each insertion in the class 'frontier'. The library '**json**' is imported in class 'problem' to read json files which represent the statement of the problem. In class 'state', '**haslib**' is imported to generate the MD5 representation of each of the states.

#### STATE SPACE

To achieve the objective, we have created a class 'stateSpace' that receives as a parameter the file's path containing the map information. It contains the needed variables and methods to read XML files and create the State Space, check if a node belongs to a graph and its position and generation of a specific state's successors list.

This class has as attributes:

- '**\_path**': path of the XML file containing the map information.
- '**\_keys**': a dictionary containing all keys information which appear in the XML files and help us as a guide for all the type of keys that exists.
- '**\_nodes**': a dictionary containing all nodes that conform the graph.
- '**\_edges**': a dictionary containing all edges that conform the graph.

The path will be the parameter use in the constructor to create each graph.

Methods:

1. **readFile()**: This method takes care for the reading of the XML file containing the essential information needed to create the tree. The previous mentioned element from the lxml library etree can build a tree with *.parse(path)* receiving as a parameter the path of the file. With the method *.getroot()* we get the tree's root (and later its nodes). The method is defined to represent the keys, nodes and edges in a structure as it can be a dictionary in order to access to a specific element in an easy way. It collects the keys from the XML files and store them in the dictionaries.

2. **belongNode():** This method checks if a node belongs to the graph, with the argument 'id' as a parameter representing it the node to be checked.
3. **positionNode():** The method checks if a node belongs to the graph by using the previous created method and if so it returns its coordinates, latitude and longitude (x,y). It also receives the 'id' of a node as a parameter.
4. **successors() :** Receives the 'id' of a node as a parameter, checks if it belongs to the created graph. The output is a list of state successors of the given node.

## PROBLEM

In order to represent the statement of the task, we've created the class 'problem'. This class is composed of the next elements:

- **file:** .json file.
- **init\_state:** the initial state of the problem
- **state\_space:** the generation of the graph from a xml file in the class 'stateSpace'.

Methods:

1. **readJson():** this method load the json\_data received as a parameter in the constructor.
2. **isGoal():** receives as input an specific state and checks if it meets the requirements to be a goal state otherwise it returns false.

## STATE

The description of the current state in the state space is represented by the class 'state'. This class is composed of the next elements:

- **current:** the current position represented as a node.
- **nodes:** ordered list of nodes to visit.
- **md5:** MD5 representation of the state.

Methods:

1. **createCode():** its input parameters are the current node and a list of nodes (that is a state) and generates a representation of them in form of md5.
2. **visited():** receives a list of nodes and a specific node's id. The method checks if the node belongs to the list. If it does, it is removed.

## FRONTIER

The representation of the element frontier necessary to solve the search problem is collected in the class '**frontier**'. Its attributes are:

- **frontier** : ordered list containing tree nodes in ascending order depending on the 'f' attribute of each node that it's a randomly generated attribute.

Methods:

1. **createFrontier()**: creates an empty one.
2. **insert()**: adds a node to the frontier.
3. **remove()**: removes a node from the frontier
4. **isEmpty()** : true if the frontier has items, false otherwise.

## TREENODE

This class represent the node inside a tree, element needed to solve the tree search problem. Its attributes are:

- **parent**: current state parent node.
- **state**: current state node.
- **cost**: from the initial node to the current one
- **action**: from the parent to reach the current state.
- **d**: depth of the node.
- **f**: random value that determines the insertion order in the frontier.

## MAIN

We have created main class to work with this previous mentioned classes and generate tests which helps us to complete the task. Contains a method called '**stressTest**' that receives a frontier and a problem and test the maximum memory addressing capability.

When executing in the command line, an input example could be the following one:

```
json file: example
example.json
data/anchuras.graphml.xml
[(127.1360111900787, <treeNode.treeNode object at 0x7f33cc1c8fd0>),
(591.7378136374725, <treeNode.treeNode object at 0x7f33cc1d9e80>),
(612.2393770939552, <treeNode.treeNode object at 0x7f33cc1d9e10>)]
[(591.7378136374725, <treeNode.treeNode object at 0x7f33cc1d9e80>),
(612.2393770939552, <treeNode.treeNode object at 0x7f33cc1d9e10>)]
True
4331489738 state md5: 331b41c249f9d392954ce4a36df65ca7
4331489740 state md5: 229da16d1c640e1e81747a47bdd716fa
4331489763 state md5: 6d7014c2db65e030d3ae0af84286edfe
[("I'm in 4331489739 and I go to 4331489738", "(4331489738, ['4331489528',
'4331489668', '4331489711', '4762868815', '4928063625'])", '48.137'), ("I'm in
4331489739 and I go to 4331489740", "(4331489740, ['4331489528', '4331489668',
'4331489711', '4762868815', '4928063625'])", '108.841'), ("I'm in 4331489739 and
I go to 4331489763", "(4331489763, ['4331489528', '4331489668', '4331489711',
'4762868815', '4928063625'])", '63.11')]
```

## 2.3 JUSTIFICATION OF USED ARTIFACTS – FRONTIER DATA STRUCTURE

### DICTIONARY

Our **first idea** was to use dictionaries, as we did before, to be the data structure to represent the frontier. Once we had implemented the stress test, we had to deal with the data order, the frontier wasn't ordered and we wanted to sort it in an ascendant order in some way, so we used the function `dict(sorted("dictionary"))` which takes the dictionary and order it by a key; that decision causes us to have a very bad timing on inserting *TreeNode* elements in the frontier as the bigger the number of nodes in the frontier, the bigger the time it takes to reorder them in an ascendant way.

That's because every time an element was inserted in the frontier the sorted function was called. So first thousand elements weren't a problem but when it reached ten thousand elements the insertion time was affected because of the way of sorting.

So, one night of stress test results only into 256 thousands elements inserted. That way of sorting was the worst choice as it had an exponential growth.



## LIST

Once we tried using dictionaries and realized we went in the wrong way, we tried using lists plus the **bisect module** to be able to make an ordered insert and not calling a sort method after an element is inserted or at the end when the list is completed. As mentioned in the documentation for the module: *"provides support for maintaining a list in sorted order without having to sort the list after each insertion"* so exactly what we were looking for.

We get the index where the element should be placed in real time with bisect and then call `insort(frontier, node)` to insert the required values in the previously give index that corresponds to the position so that the order remains correct.

```
bisect.insort(self._frontier, (node._f, node))
```

The complexity of this algorithm is  $O(n \log n)$ , little bit worse than linear but enough for what we need it for or at least that's what we think up to date, if not we will improve it.

## PRIORITY QUEUE

We tried the priority queues by using 2 different modules:

- **heapq**: the speed of the insertion of nodes in the frontier drastically increased. In a minute a few millions of nodes could have been introduced in the frontier.

```
heapq.heappush(self._frontier, (node._f, node))
```

The reason for that was that this structure does not order the whole bunch of elements instead of that it just get the element with the lower "*f*" and then puts it on the front of the queue. Even when the first element (the lower one) was removed, the speed of retaking the next lower element was quite good.

- **queue**: as we wanted the frontier to be all ordered we considered this one.

```
frontier = queue.PriorityQueue()
```

By using that module, the frontier is defined as a Priority Queue object.

This time, the whole frontier would be ordered by "*f*" **but not the objects inside**.

```
frontier.put((node._f, node))
```

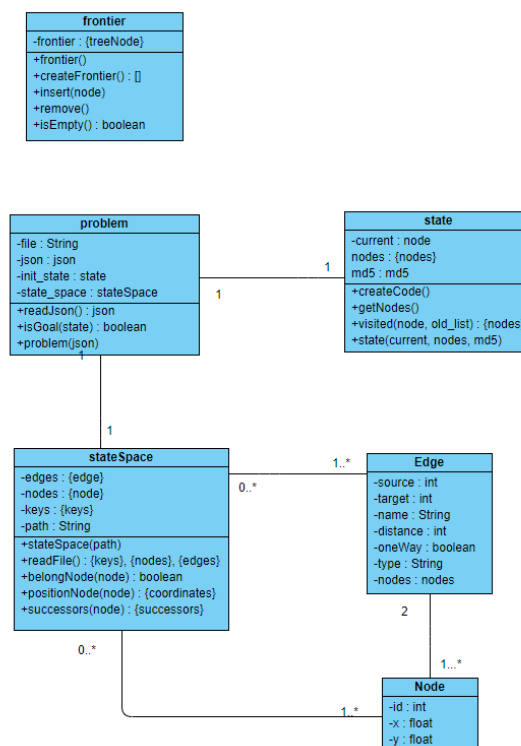
In the following table, we represent some of the values we got depending of the previous modules mentioned before that we have tried. These values were obtained by executing the stress test a total time of 1 minute each.

module used	avg time (s)	min time (s)	max time (s)	# elements
bisect	0,00006409883	0,00000143051	0,00312209129	784.241
heapq	0,00000186862	0,00000119209	0,01135897636	4.570.800
queue	0,00000377094	0,00000286102	0,02315831184	5.454.733

As we can see the most optimal ones may be **heapq** or **queue** but they only sort the first value of the frontier which is the key of priority queues data structure, if we only need to have it ordered cause of the elimination of nodes (the one with the lower f should be removed) and do not take into account how the rest of nodes are ordered, then the way to go must be one of those modules instead of the bisection one we are using at the moment.

## 2.4 UML SKETCHES

This does not clearly represent the implementation of our code but was used to represent the general idea and thinking about our goal, so we found it interesting to also show it over here.



## 2.5 BIBLIOGRAPHY

- <https://stackoverflow.com/>
- <https://docs.python.org/2/library/bisect.html>
- <https://docs.python.org/3/library/queue.html>
- <https://docs.python.org/2/library/heapq.html>
- <https://stackoverflow.com/questions/11215851/python-equivalent-of-javas-compareto>