

## Instructions for R Homework 3\*

### Question 1

You sample 100 people's showering habits and find the average shower time is 12.2 minutes. Given that the population variance in shower time is 15, use the `qnorm()` command to construct an 86% confidence interval for a sampled mean. Make sure you are using `qnorm()` correctly.

*Note:* `qnorm(x)` returns the  $Z_x$  such that  $P(Z > Z_x) = x$ , where  $Z \sim N(0, 1)$ . For a  $100 - \gamma\%$  confidence interval, we have that  $\alpha = \frac{1-\gamma}{2}$ . See `help(qnorm)` for more details.

### Question 2

Load the housing data we've been using:

```
df <- read.csv("https://mattbutner.github.io/data/housing_df.csv")
```

- Use a combination of the `mean()`, `sd()`, `length()`, `qnorm()`, and `sqrt()` functions to construct a 90% confidence interval for the CRIM variables.
- Interpret the confidence interval from CRIM.

\* For all HW assignments, I need to see all the code used

### Question 3

In the assignment HW3.Rmd there is a block of code that simulates a bunch of random samples of the same size, constructs the mean and a confidence interval for each sample, and reports the percent of the confidence intervals that capture the true population mean.

To begin, make sure you have `sample_size <- 100` `num_samples <- 50` `ci_level <- 0.95` set up in the beginning of this chunk. You will need to install the user written package `ggplot2`. To do this, type `install.packages("ggplot2")` into the console before you run the R script. No need to provide the R code for these questions (you can set `include = FALSE`).

Run the chunk with the initial settings. This will be the comparison.

- a. Increase the sample size from 100 to 200, by changing `sample_size` and rerunning the code.
  - What happens to the width of the confidence intervals?
  - Does the true population mean fall inside more of the confidence intervals?
- b. Return the sample size back to 100. Now change the number of samples from 50 to 100.
  - How does this change the percentage of the confidence intervals that capture the population mean?
  - As you increase the number of samples, towards infinity, what percentage of the confidence intervals will capture the true population mean?
- c. Return the number of samples back to 50. Now change the confidence level to 0.8.
  - How does the width of the confidence intervals change?
  - Does the percentage of confidence intervals that capture the population mean increase or decrease?

## Question 4

You started taking the bus to work. The local transit authority says that a bus should arrive at your bus stop every five minutes. After a while, you notice you spend a lot more than five minutes waiting for the bus, so you start to keep a record.

You spend the next two months recording how long it takes for the bus to arrive to the bus stop. This gives a total of sixty observations that denote the number of minutes it took for the bus to arrive (rounded to the nearest minute). These observations are hosted at [https://mattbutner.github.io/data/bus\\_stop\\_time.csv](https://mattbutner.github.io/data/bus_stop_time.csv)

- Load these data into R as a data frame using the `read.csv()` command.
- Create a histogram of the `time_until_bus` variable using `hist()`. Would you say that five minutes is a reasonable guess for the average arrival time based on this picture alone?
- Create 95% confidence interval for the bus arrival times using the  $z$ -distribution. Does 5 minutes fall within the 95% confidence interval?
- How would you communicate your finding to the local transit authority?