DELIMITED CONTINUATIONS DELIMITED CONTINUATIONS

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HISTORY

- → Delimited continuations introduced by Matthias Felleisen 35 years ago.
- → Flurry of initial publications, mostly in Scheme.
- → Not much mainstream adoption.
- → Recently: some renewed interest.



- → Initial proposal in early 2020; revised version accepted in late 2020.
- → Implementation in limbo for several years.
- → Started at Tweag last year; patch landed last fall.
- → Finally released this past March in GHC 9.6!

Problem: nobody knows what they are.

DEMYSTIFICATION

TERMINOLOGY

"continuations"

"native, first-class, delimited continuations"

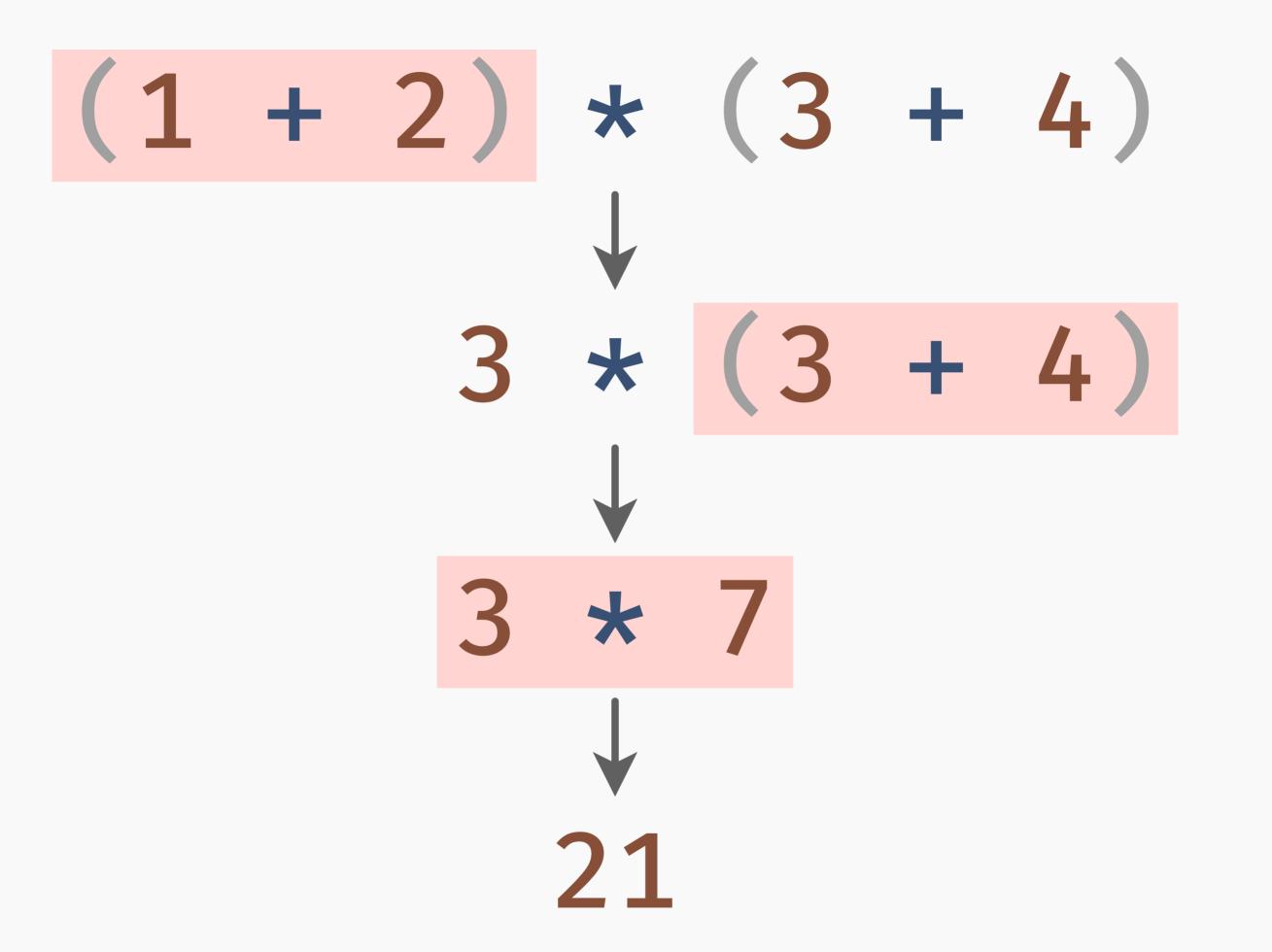
- (1) continuations
- (2) delimited
- (3) first-class
- (4) native

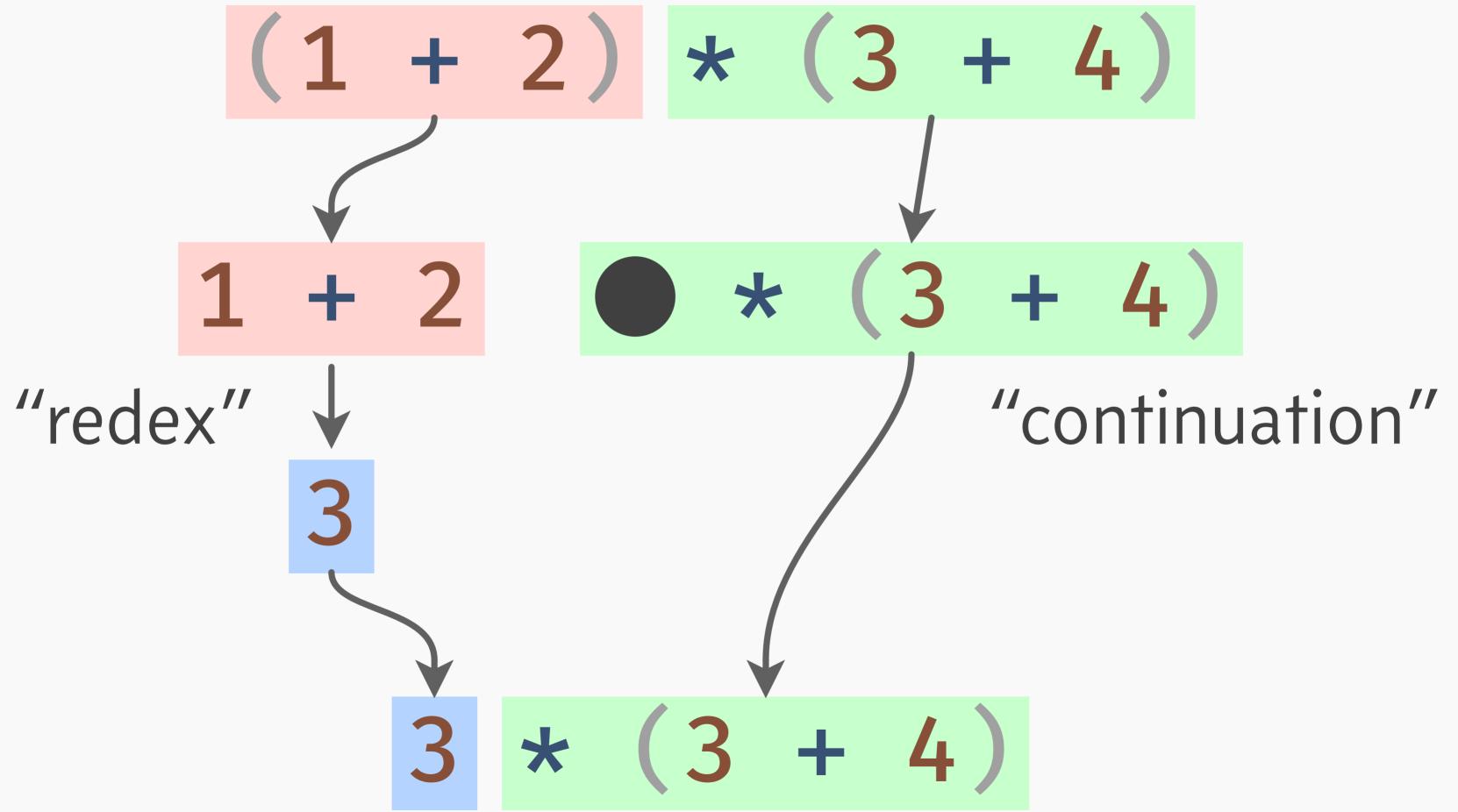
A "continuation" is a concept, not a language feature.

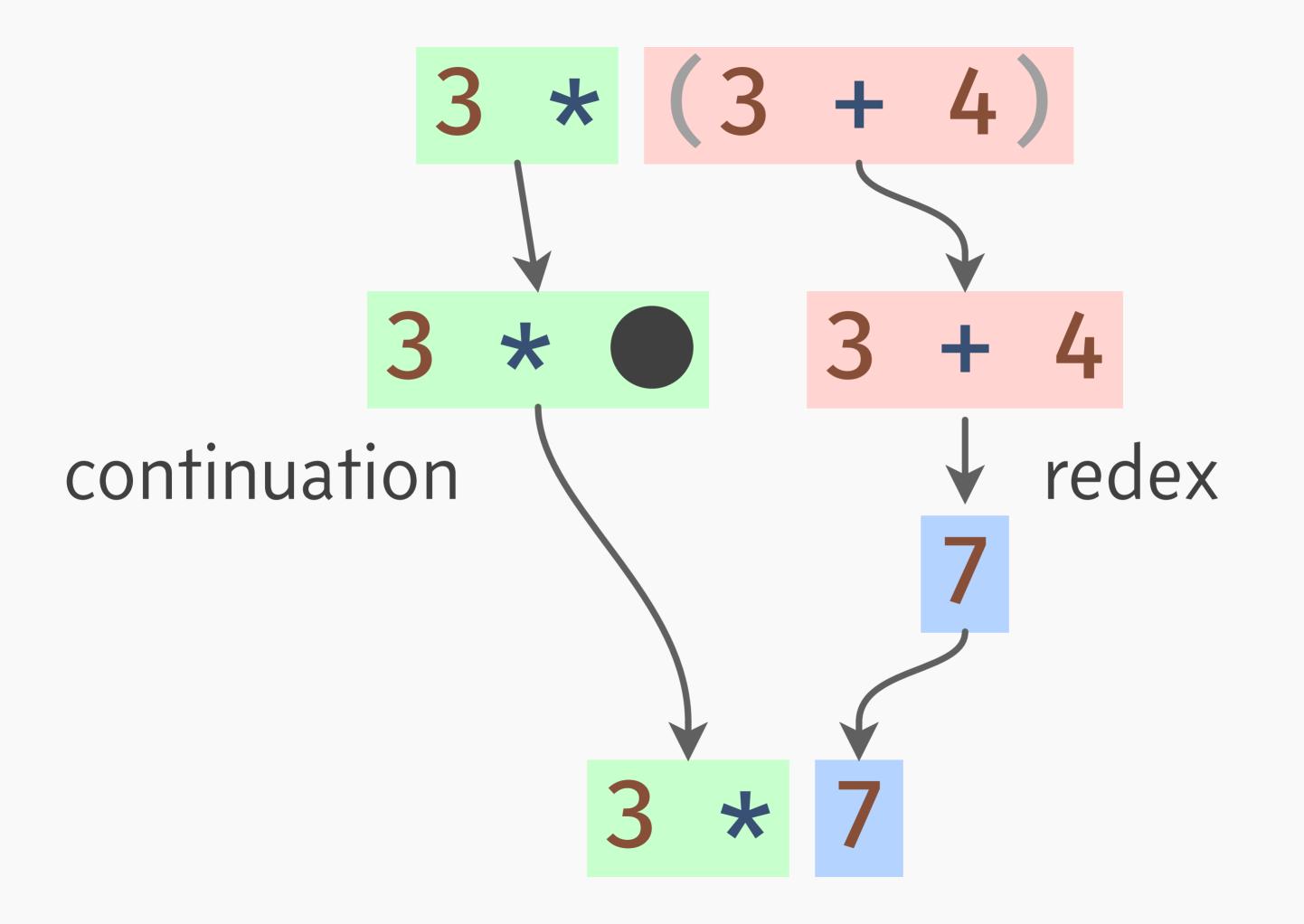
(Like "scope" or "value".)

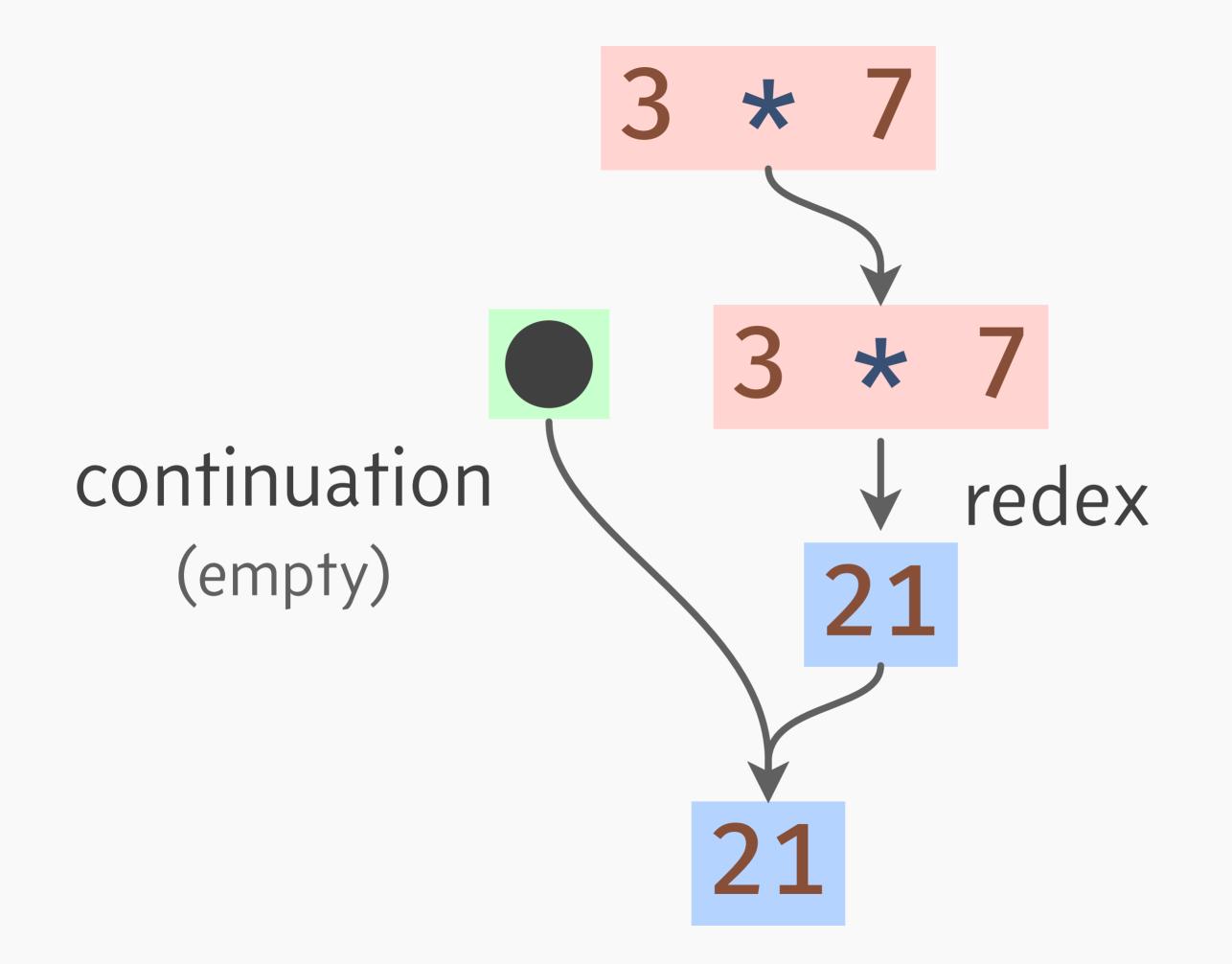
Applies to most programming languages!

Useful for talking about evaluation.



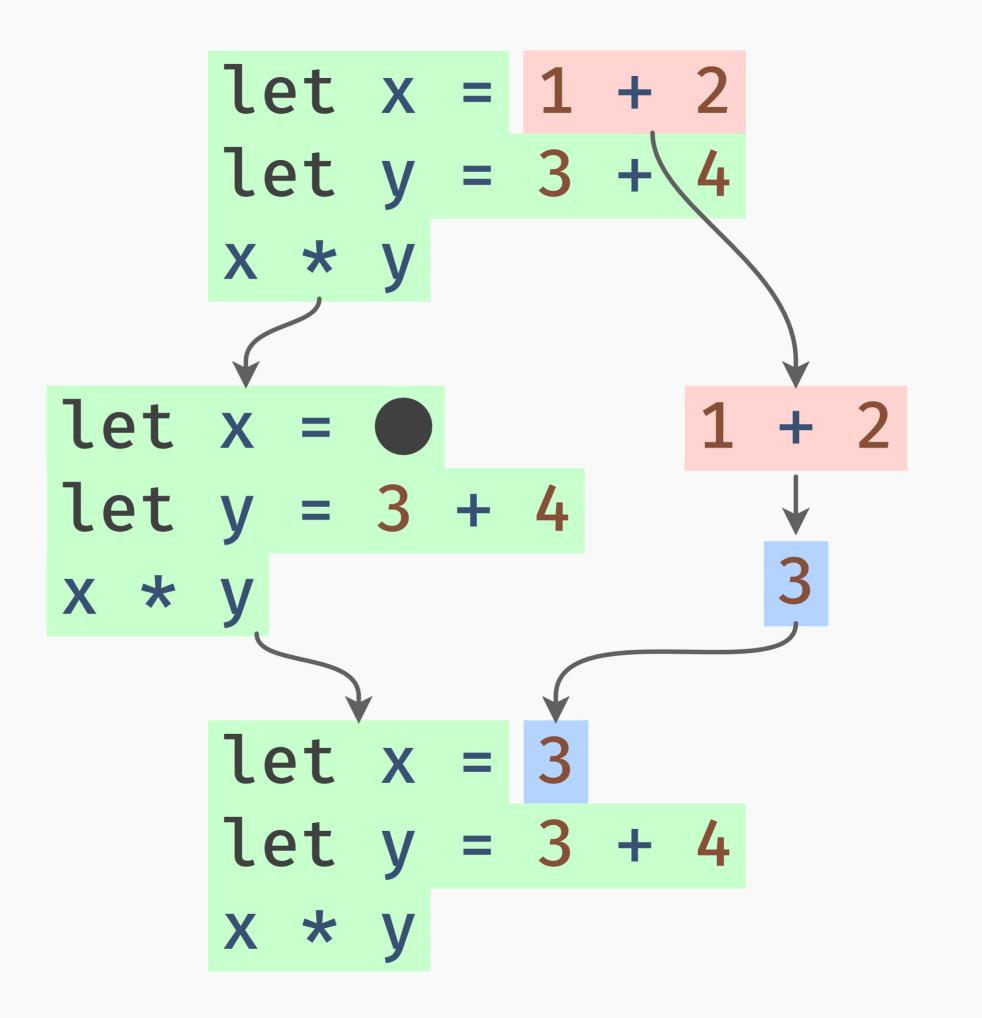




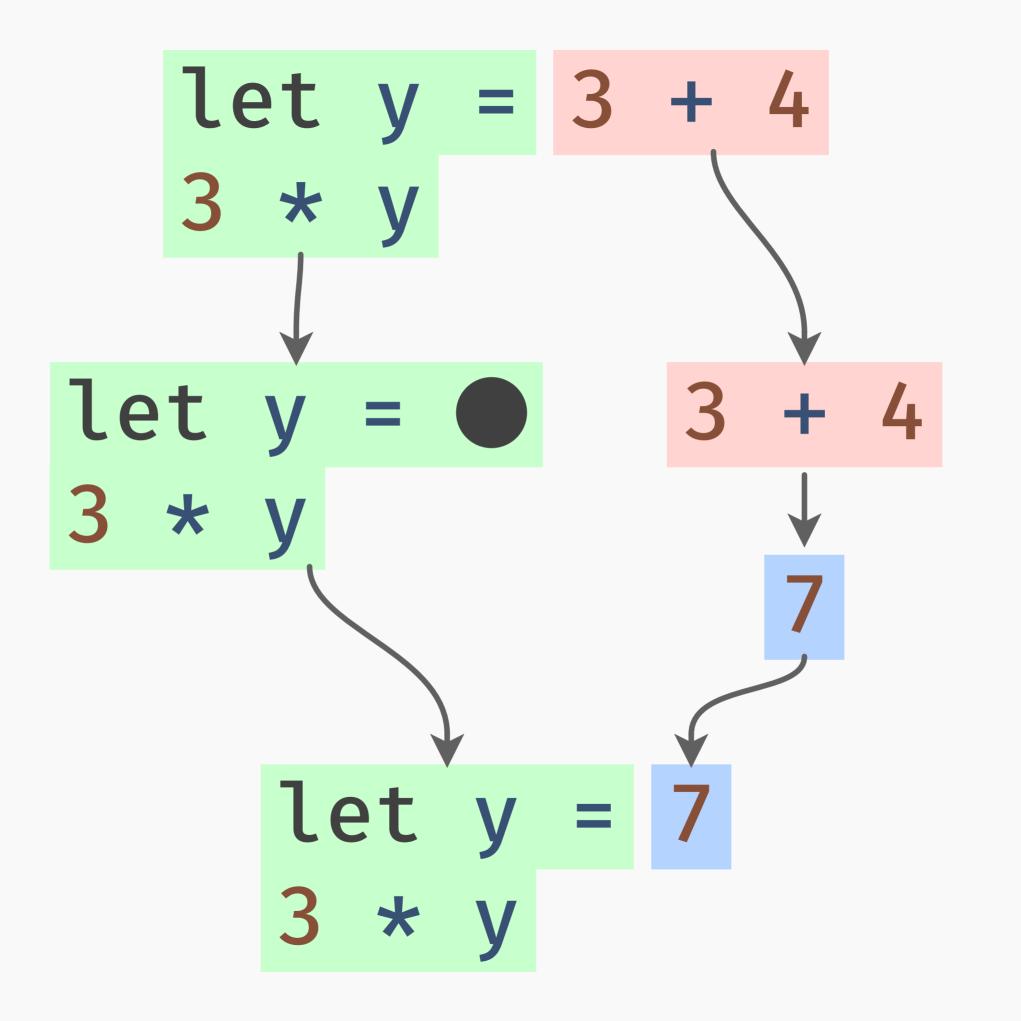


What is the continuation?

- → The "context" in which the redex is evaluated.
- → An expression with a hole.
- → The place the redex's value is "returned to".
- → "The rest of the program."



```
let x = 3
let y = 3 + 4
X * Y
let y = 3 + 4
3 * Y
```



Why care about continuations?

Evaluation is extremely regular:

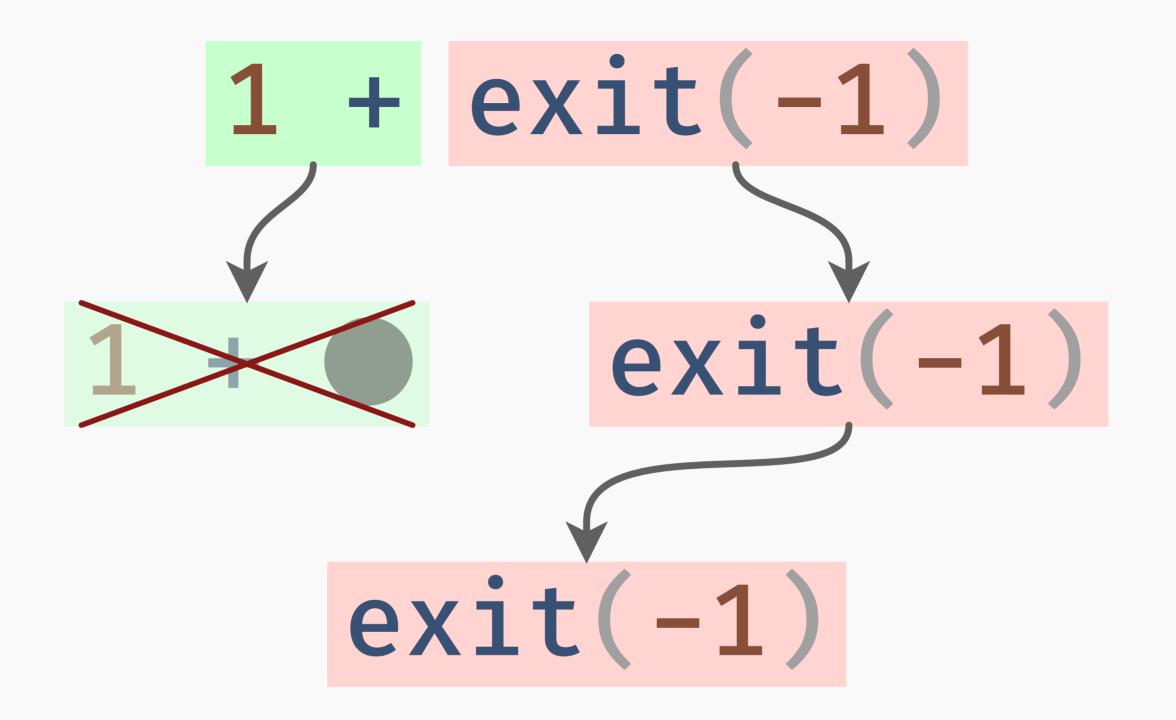
- 1 Split the redex and continuation.
- (2) Reduce the redex.
- (3) Substitute the result into the continuation.
- 4 Repeat.

Why is the continuation itself interesting?

Compiler writers care about the continuation!

Most programmers don't have much reason to, most of the time.

...but what about operators that use different rules?



Continuation is thrown away!

exit is still not terribly interesting.

What about throw / catch?

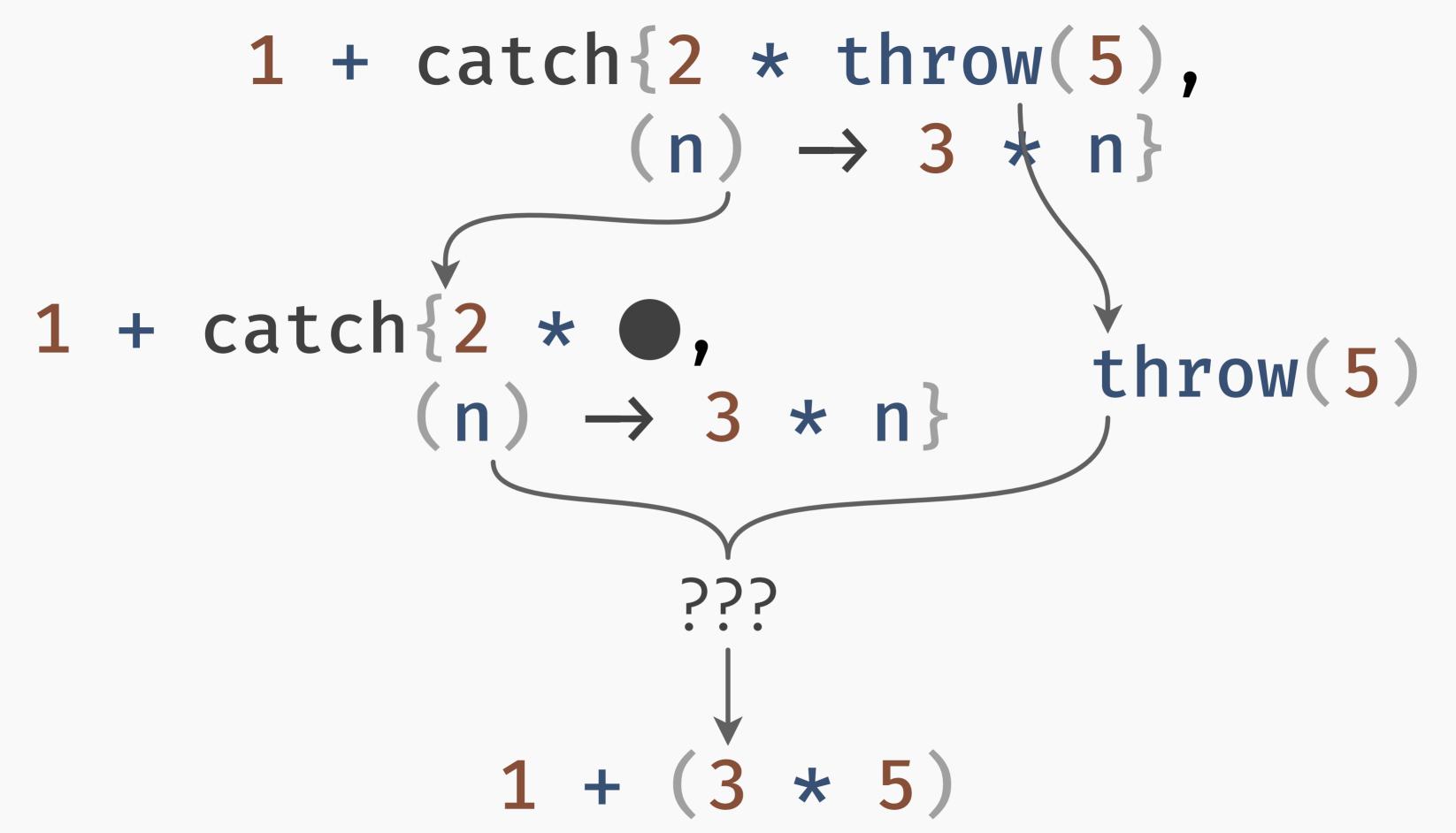
throw(exn)

Raises exn as an exception.

catch{body, handler}

Evaluates **body**, and if an exception is raised, evaluates **handler(exn)**.

```
1 + catch{2 * throw(5)}
           (n) \rightarrow 3 * n
       1 + (3 * 5)
          1 + 15
```



1 + catch{2 * •, (n)
$$\rightarrow$$
 3 * n}

catch{•, (n) \rightarrow 3 * n}

1 + •

catch delimits the discarded continuation.

INTERLUDE: NOTATION

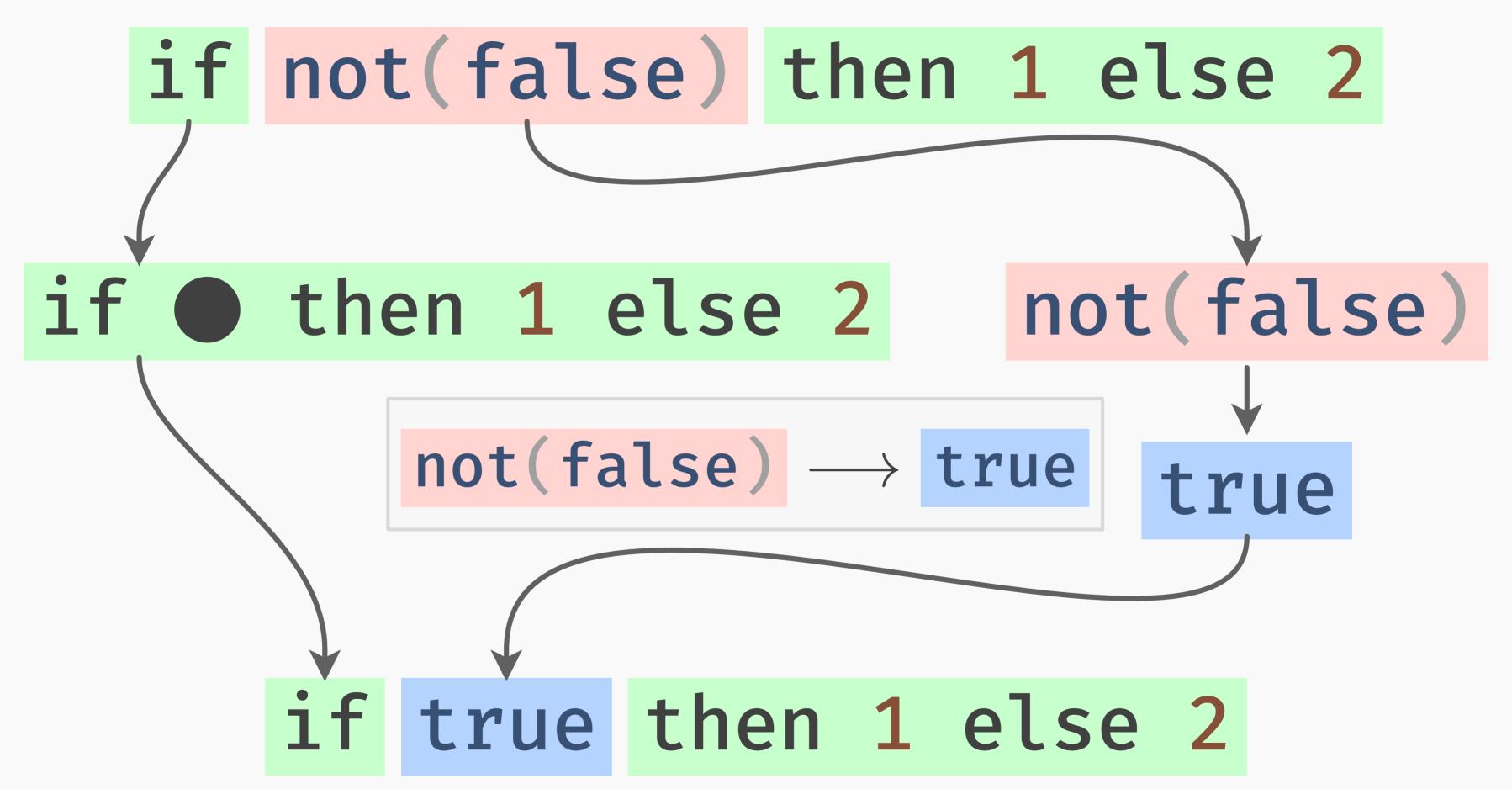
 $A\longrightarrow B$ "A reduces to B."

$$not(false) \longrightarrow true$$

 $not(true) \longrightarrow false$

if true then e_1 else $e_2 \longrightarrow e_1$ if false then e_1 else $e_2 \longrightarrow e_2$

if not(false) then 1 else 2?



$\frac{\mathsf{not}(\mathsf{false}) \longrightarrow \mathsf{true}}{E[\mathsf{not}(\mathsf{false})] \longrightarrow E[\mathsf{true}]}$

- \rightarrow E stands for "some arbitrary continuation".
- $\rightarrow E[x]$ denotes "plugging the hole" in E with x.

```
E= if lacktriangle then 1 else 2 x= not(false) E[x]= if not(false) then 1 else 2
```

Why bother with all of this?

$$E[\mathsf{exit}(v)] \longrightarrow \mathsf{exit}(v)$$

$$E_1[\mathsf{catch}\{E_2[\mathsf{throw}(v)],\ f\}] \longrightarrow E_1[f(v)]$$

Lots of operations can be described this way!

- (1) continuations <
- (2) delimited <
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What makes something "first class"?

How could a continuation be a value?

```
(x) \rightarrow 1 + (x * 2)
(x) \rightarrow \text{if } x > 0 \text{ then 1 else -1}
(x) \rightarrow \text{f(catch\{throw(x), handle}\})
```

What is a "first-class continuation"?

Answer: a continuation reified as a function.

call_cc

"call with current continuation"

$$E[\operatorname{call_cc}(f)] \longrightarrow E[f((x) \rightarrow E[x])]$$

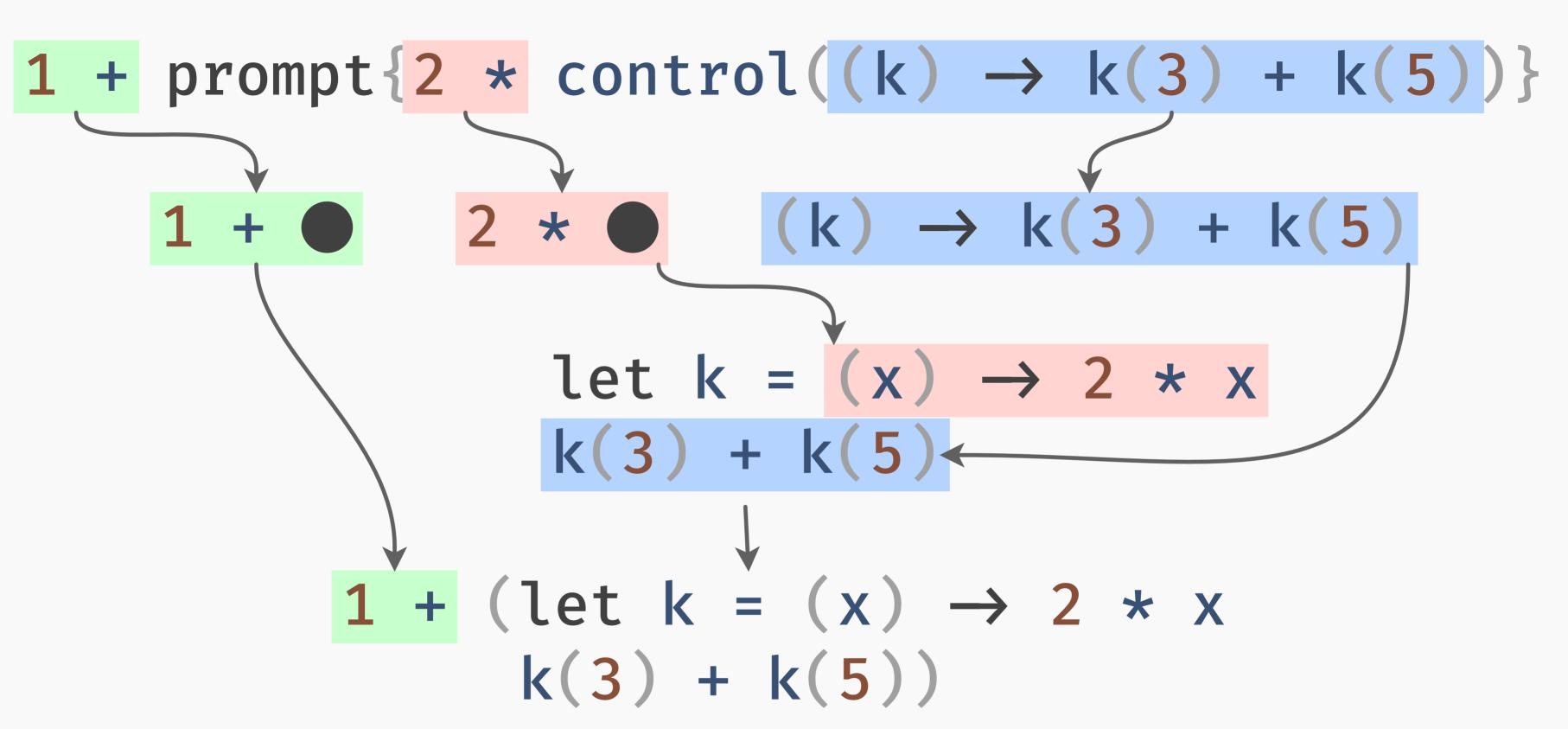
This has some problems!

1+(0 * 2)

```
print(1 + ( * 2))
shutdown_runtime()
run_libc_atexit()
exit_process()
```

We need more control! prompt / control

$$E_1[\mathsf{prompt}\{E_2[\mathsf{control}(f)]\}] \ \longrightarrow E_1[f((\mathsf{x}) o E_2[\mathsf{x}])]$$

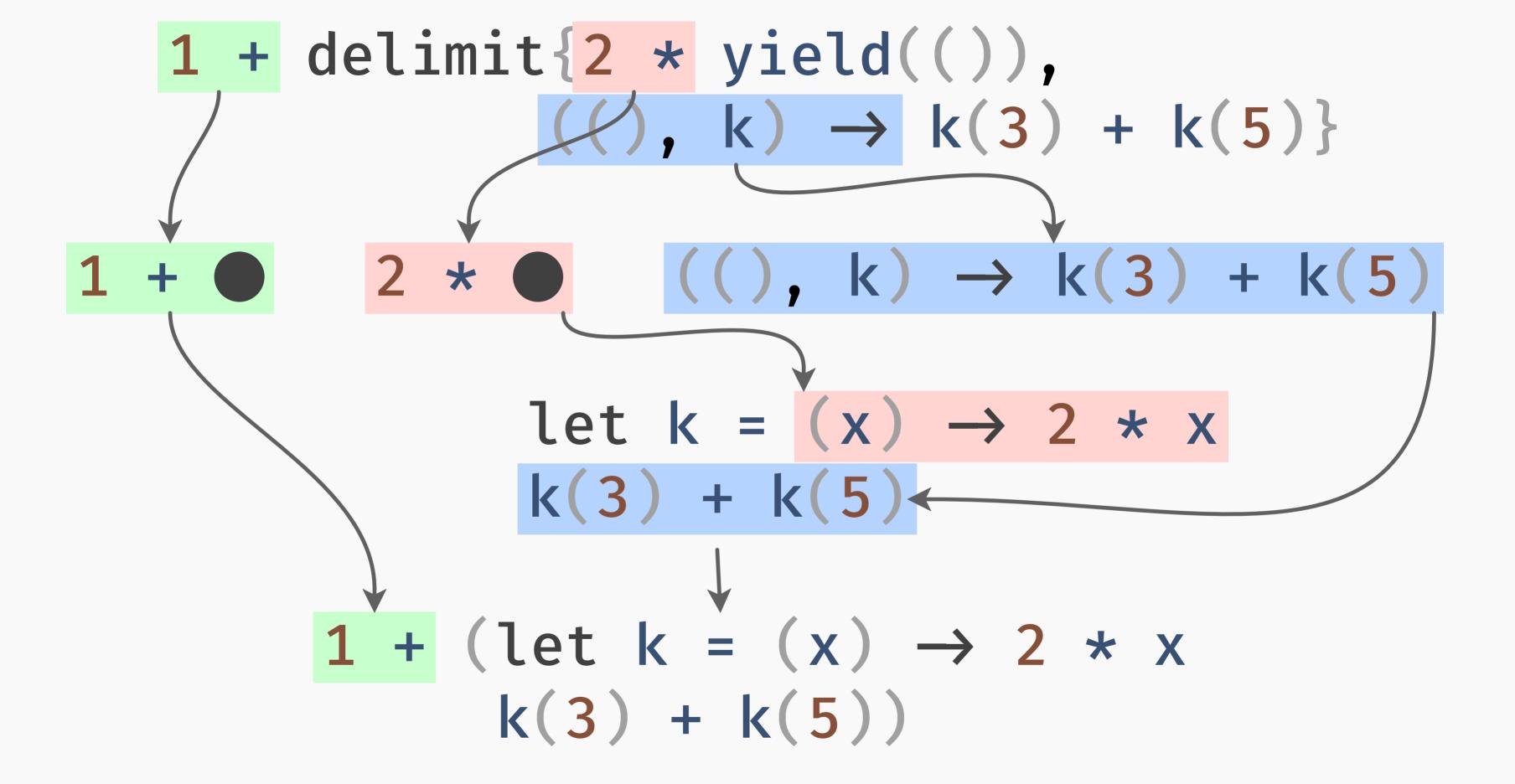


```
1 + prompt{2 * control((k) \rightarrow k(3) + k(5))}
          1 + (let k = (x) \rightarrow 2 * x
                 k(3) + k(5)
                  1 + (6 + 10)
                       1 + 16
```

Why is this so confusing?

$$E_1[\mathsf{catch}\{E_2[\mathsf{throw}(v)], f\}] \longrightarrow E_1[f(v)]$$
 $E_1[\mathsf{prompt}\{E_2[\mathsf{control}(f)]\}] \longrightarrow E_1[f(x) \to E_2[x])]$
 $E_1[\mathsf{delimit}\{E_2[\mathsf{yield}(v)], f\}] \longrightarrow E_1[f(v, (x) \to E_2[x])]$

delimit / yield provide resumable exceptions.



Why prompt / control?

- → In some sense "simpler".
- → Historical relationship to call_cc.
- → Easier to statically type.

TYPES

Even typing exceptions is hard!

```
throw: Exception → a

catch{body, handler}: b
    body: b

handler: Exception → b
```

yield : DelimiterTag → a

```
delimit{body, handler}: b
    body : b
```

handler: DelimiterTag \rightarrow (a \rightarrow b) \rightarrow b

$$E_1[\text{delimit}\{E_2[\text{yield}(v)], f\}]$$

 $\longrightarrow E_1[f(v, (x) \rightarrow E_2[x])]$

prompt{body} : b body : b

control:
$$((a \rightarrow b) \rightarrow b) \rightarrow a$$

$$E_1[\mathsf{prompt}\{E_2[\mathsf{control}(f)]\}]$$

 $\longrightarrow E_1[f((\mathbf{x}) \to E_2[\mathbf{x}])]$

Solution: tagged prompts.

```
new_prompt_tag : () → PromptTag<b
```

prompt{tag, body} : b

tag: PromptTag

body: b

control: (PromptTag\rightarrow b)
$$\rightarrow$$
 b)) \rightarrow a

$$E_1[\mathsf{prompt}\{tag, E_2[\mathsf{control}(tag, f)]\}]$$

$$\longrightarrow E_1[f((\mathbf{x}) \to E_2[\mathbf{x}])]$$

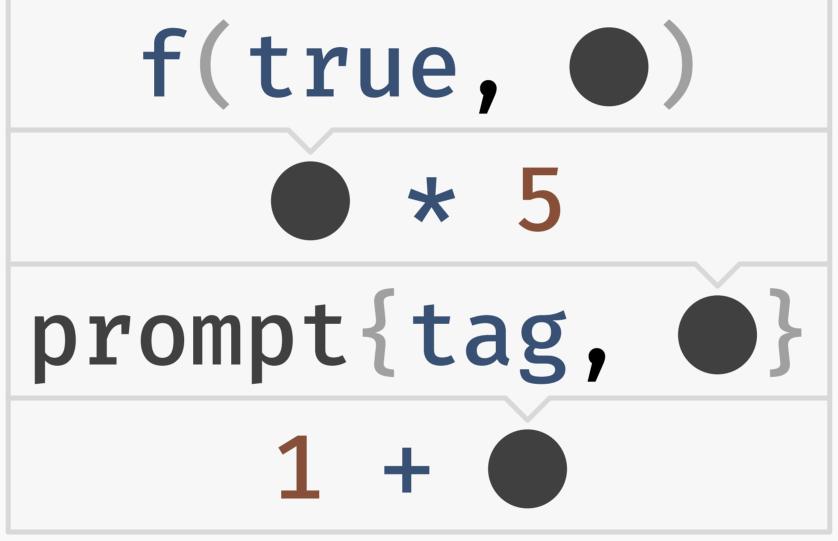
- (1) continuations <
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How do we implement this?

Option one: continuation-passing style. Problem: slow! (See my talk from ZuriHac 2020.)

Option two: bake them into the runtime.

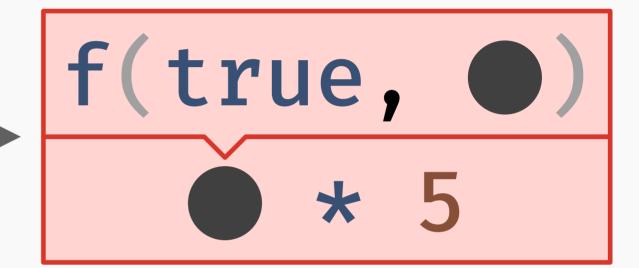
1 + prompt{tag, f(true, •) * 5}



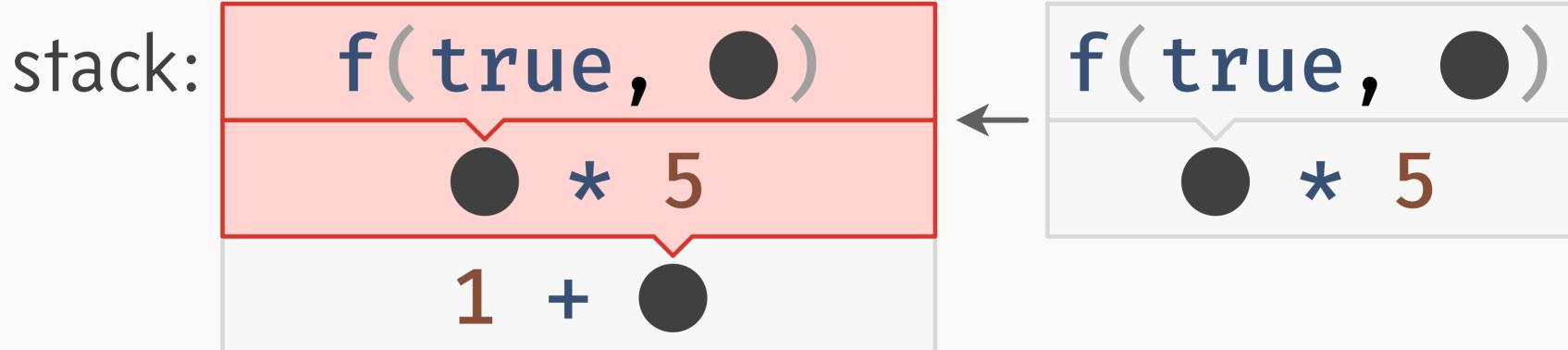
This is a call stack!

redex: control(tag, g)

```
stack: f(true, •)
     prompt{tag, •}
```



redex: "hello"



redex: "hello"

```
stack: f(true, •)
```



Capture/restore are just memcpy!

- (1) continuations <
- (2) delimited <
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MISCELLANY

- → Can further optimize implementation for specific use cases.
- → Strict monads permit embedding into a lazy language.
- → Reality is always at least a little more complicated (e.g. stack overflow, async exceptions).
- → We sorely lack non-synthetic continuation benchmarks!

The unsung hero of this talk: reduction semantics.

- (1) continuations <
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Still extremely useful!

- → Continuations are a concept that arises naturally in evaluation.
- → Special operators like catch delimit portions of the continuation.
- → First-class continuations allow reifying the continuation as a function.
- → Remarkably, this corresponds to manipulation of the call stack.

Thanks!

```
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```

Tweag: https://www.tweag.io/