

Towards Multi-Level Arithmetic Optimizations



The Real Number Illusion

- Most numerical code is written with **real numbers** in mind.
- Yet, compilers only obey low-level **machine numbers**: floats and ints.
- This discourages (“unsafe-math”) or misses many **optimization opportunities**, especially in **machine learning**, **linear algebra**, or **signal processing**.

Arithmetic Optimizations

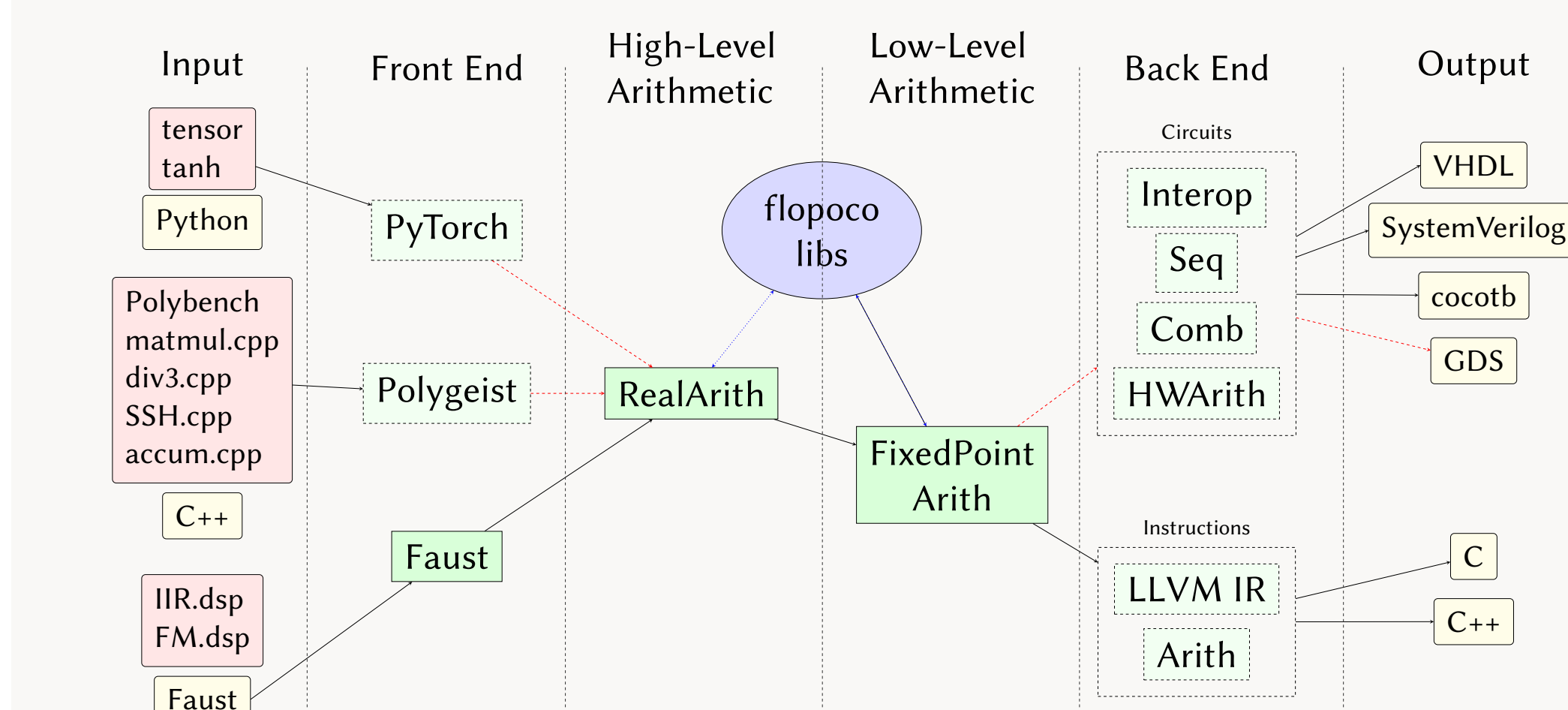
- ... beyond existing low-level rewrites in current compilers:
- Operator specialization: squarers, constant multipliers
- Expression fusion: $\frac{1}{\sqrt{x^2+y^2}}$ or $\sin(\omega t + \phi)$
- Optimizations tailored to target semantics Useful when compiling to hardware [Lah+18; Ugu+20; For+22; DK24], but not only.

Semantics First, Bits Later

- Separation of concerns** thanks to MLIR:
- Higher levels capture “mathematical intent”,
- Lower levels deal with “machine numbers”.

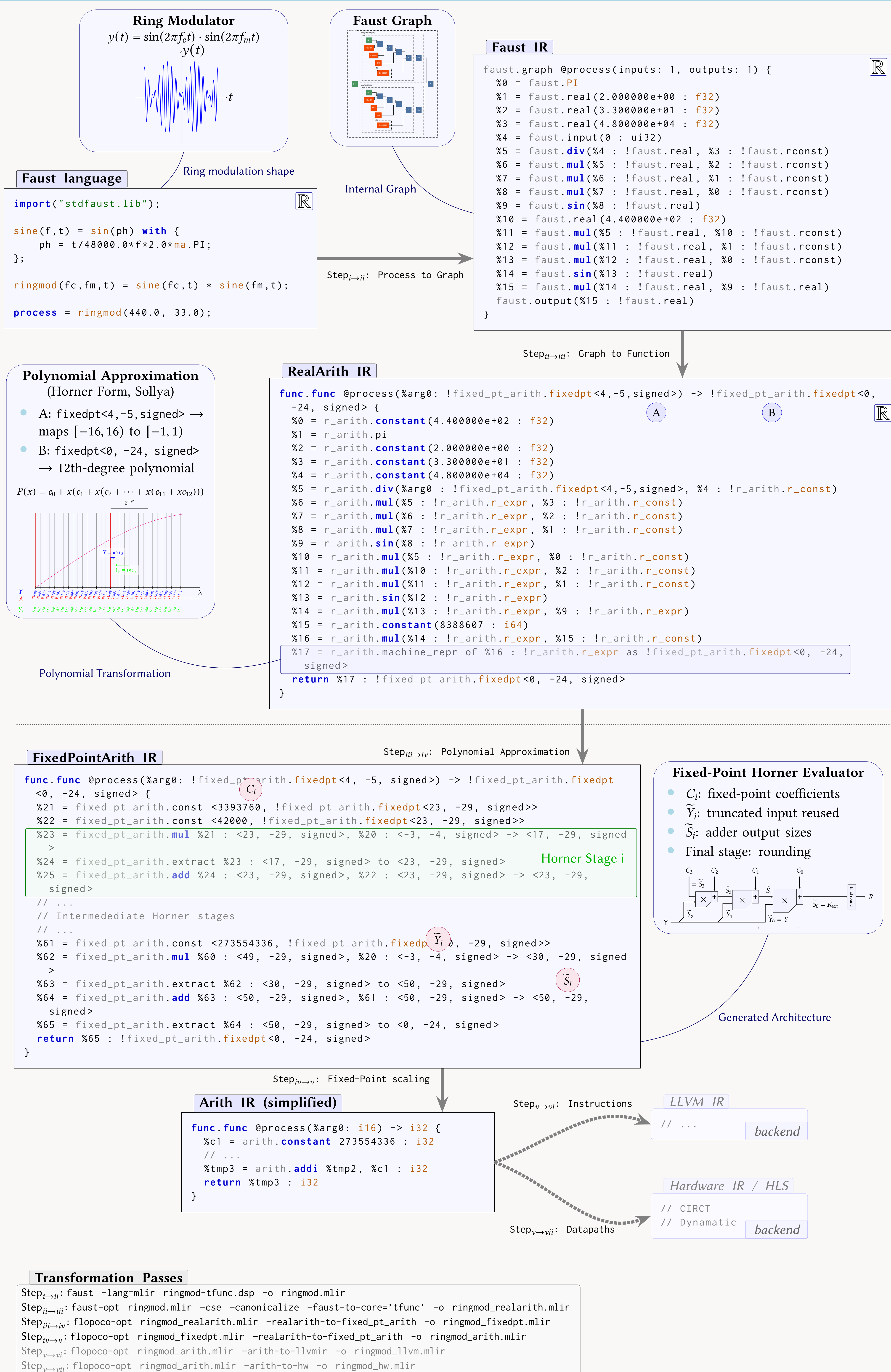
Our contributions:

- real_arith and fixed_pt_arith dialects
- Polynomial approximation lowering from real expressions
- Precision-tuned Horner architecture derived from dialect-level ops
- End-to-end MLIR flow evaluated on signal processing workloads



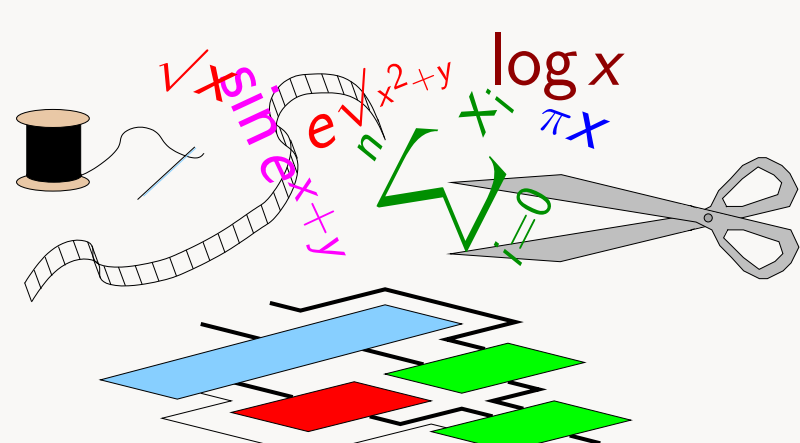
Overall contribution: proposed dialects (in dark green), integrated in a High-Level Synthesis ecosystem.

Example: End-to-End Audio compilation flow



Open-Source Tools

- Sollya** [SMC10]
- ScaleHLS** [Ye+22]
- Dynatomic** [Che+22], <https://dynatomic.epfl.ch/>
- SODA-OPT** [Ago+22], <https://github.com/pnnl/soda-opt>
- CIRCT** <https://circt.llvm.org/>
- Faust** <https://faust.grame.fr>
- FloPoCo** <https://www.flopoco.org>



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