An Account with my Personal, Ecclectic Comments on the Isabelle Architecture

Version: Isabelle 2017

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Abstract

While Isabelle is mostly known as part of Isabelle/HOL (an interactive theorem prover), it actually provides a system framework for developing a wide spectrum of applications. A particular strength of the Isabelle framework is the combination of text editing, formal verification, and code generation.

This is a programming-tutorial of Isabelle and Isabelle/HOL, a complementary text to the unfortunately somewhat outdated "The Isabelle Cookbook" in https://nms.kcl.ac.uk/christian.urban/Cookbook/. The reader is encouraged not only to consider the generated .pdf, but also consult the loadable version in Isabelle/jedit in order to make experiments on the running code.

Keywords: ["LCF-Architecture", "Isabelle", "SML", "PIDE", "Tactic Programming"]

1 SML and Fundamental SML libraries

1.1 Text, Antiquotations, and the Isabelle/Pure bootstrap

Isabelle is written in SML, the "Standard Meta-Language", which is is an impure functional programming language allowing, in principle, variables and side-effects:

```
 \begin{aligned} \mathbf{ML} \langle \ val \ X &= \ Unsynchronized.ref \ \theta; \\ X &:= \ !X \ + \ 1; \\ X \rangle \end{aligned}
```

However, since Isabelle is a platform involving parallel execution, concurrent computing, and, as an interactive environment, involves backtracking / re-evaluation as a consequence of user- interaction, imperative programming is discouraged and nearly never used in the entire Isabelle code-base. Isabelle then implements an own top-level for an extensible language, Isar, in which domain-specific components can be developed and integrated into the system on the fly. Thus, the Isabelle code-base consists mainly of SML and .thy-files containing mixtures of Isar commands and SML. Furthermore, a rich text annotation language is provided for a specific style of literate programming.

Text enriched by "formal content", i.e. machine-checked, typed references to all sorts of entities in form *antiquotations* allows for coping with sources that rapidly evolve and were developed by distributed teams as is typical in open-source developments. A paradigmatic example for antiquotation in Texts and Program snippets is here:

1, \$ISABELLE_HOME/src/Pure/ROOT.ML

```
\mathbf{ML} \langle \ val \ x = @\{thm \ refl\} \rangle
```

In a way, literate specification with a maximum of formal content is a way to ensure "Agile Development", at least for its objectives, albeit not for its popular methods and processes like SCRUM.

A maximum of formal content inside text documentation also ensures the consistency of this present text with the underlying Isabelle version.

It is instructive to study the fundamental bootstrapping sequence of the Isabelle system; it is written in the Isar format and gives an idea of the global module dependencies: \$ISABELLE_HOME/src/Pure/ROOT.ML. Loading this file (for example by hovering over this hyperlink in the antiquotation holding control or command key in Isabelle/jedit and activating it) allows the Isabelle IDE to support hyperlinking *inside* the Isabelle source.

The bootstrapping sequence is also reflected in the following diagram:

1.2 Elements of the SML library

Elements of the \$ISABELLE_HOME/src/Pure/General/basics.ML SML library are basic exceptions. Note that exceptions should be catched individually, uncatched exceptions except those generated by the specific "error" function are discouraged in Isabelle source programming since they might produce races. Finally, a number of commonly used "squigglish" combinators is listed:

$\mathbf{ML} \langle \! \langle $			
¹ sdf			

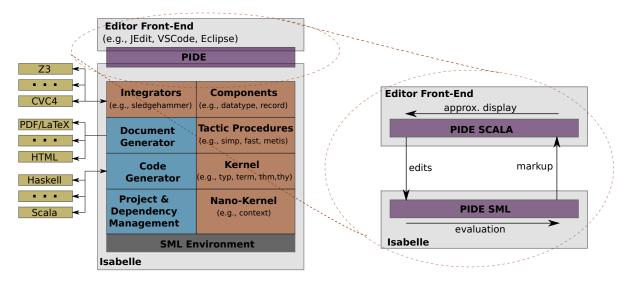


Figure 1.1: The system architecture of Isabelle (left-hand side) and the asynchronous communication between the Isabelle system and the IDE (right-hand side).

```
exception Bind
   exception Chr
   exception Div
   exception Domain
   exception Fail of string
   exception Match
   exception Overflow
   exception Size
   exception Span
   exception Subscript
*)
exnName: exn \rightarrow string; (* -- very interisting to query an unknown exception *)
exnMessage: exn \rightarrow string;
op \ ! : \ 'a \ Unsynchronized.ref \ -> \ 'a;
op := : ('a \ Unsynchronized.ref * 'a) \rightarrow unit;
op \#>: ('a -> 'b)*('b -> 'c) -> 'a -> 'c; (* reversed function composition *)
op o: (('b -> 'c) * ('a -> 'b)) -> 'a -> 'c;
op ?: bool * ('a -> 'a) -> 'a -> 'a;
ignore: 'a \rightarrow unit;
op before : ('a * unit) \rightarrow 'a;
I: 'a \rightarrow 'a;
K: 'a \rightarrow 'b \rightarrow 'a
\rangle\rangle
```

Some basic examples for the programming style using these combinators can be found in the "The Isabelle Cookbook" section 2.3.

An omnipresent data-structure in the Isabelle SML sources are tables implemented in \$ISABELLE_HOME/src/Pure/General/table.ML. These generic tables are presented in an efficient purely functional implementation using balanced 2-3 trees. Key operations are:

 $\mathbf{ML}\langle$

```
signature\ TABLE\text{-}reduced\ =
sig
 type\ key
 type \ 'a \ table
 exception\ DUP\ of\ key
 exception\ SAME
 exception\ UNDEF\ of\ key
 val empty: 'a table
 val \ dest: 'a table \rightarrow (key * 'a) \ list
 val keys: 'a table -> key list
 val\ lookup\text{-}key: 'a table\ ->\ key\ ->\ (key\ *\ 'a)\ option
 val lookup: 'a table -> key -> 'a option
 val\ defined\colon 'a\ table\ ->\ key\ ->\ bool
 val\ update:\ key*\ 'a\ ->\ 'a\ table\ ->\ 'a\ table
 (* \dots *)
end
```

... where key is usually just a synonym for string.

2 Prover Architecture

2.1 The Nano-Kernel: Contexts, (Theory)-Contexts, (Proof)-Contexts

What I call the 'Nano-Kernel' in Isabelle can also be seen as an acyclic theory graph. The meat of it can be found in the file \$ISABELLE_HOME/src/Pure/context.ML. My notion is a bit criticisable since this component, which provides the type of theory and Proof.context, is not that Nano after all. However, these type are pretty empty place-holders at that level and the content of \$ISABELLE_HOME/src/Pure/theory.ML is registered much later. The sources themselves mention it as "Fundamental Structure". In principle, theories and proof contexts could be REGISTERED as user data inside contexts. The chosen specialization is therefore an acceptable meddling of the abstraction "Nano-Kernel" and its application context: Isabelle.

Makarius himself says about this structure:

"Generic theory contexts with unique identity, arbitrarily typed data, monotonic development graph and history support. Generic proof contexts with arbitrarily typed data."

In my words: a context is essentially a container with

- \bullet an id
- a list of parents (so: the graph structure)
- a time stamp and
- a sub-context relation (which uses a combination of the id and the time-stamp to establish this relation very fast whenever needed; it plays a crucial role for the context transfer in the kernel.

A context comes in form of three 'flavours':

- theories: theory's, containing a syntax and axioms, but also user-defined data and configuration information.
- Proof-Contexts: Proof.context containing theories but also additional information if Isar goes into prove-mode. In general a richer structure than theories coping also with fixes, facts, goals, in order to support the structured Isar proof-style.
- Generic: Context.generic, i.e. the sum of both.

All context have to be seen as mutable; so there are usually transformations defined on them which are possible as long as a particular protocol (begin_thy - end_thy etc) are respected.

Contexts come with type user-defined data which is mutable through the entire lifetime of a context.

2.1.1 Mechanism 1 : Core Interface.

To be found in \$ISABELLE_HOME/src/Pure/context.ML:

 $\mathbf{ML} \langle \! \langle$

Context.parents-of: theory -> theory list; Context.ancestors-of: theory -> theory list;

```
Context.proper-subthy: theory* theory -> bool; \\ Context.Proof: Proof.context -> Context.generic; (*constructor*) \\ Context.proof-of: Context.generic -> Proof.context; \\ Context.certificate-theory-id: Context.certificate -> Context.theory-id; \\ Context.theory-name: theory -> string; \\ Context.map-theory: (theory -> theory) -> Context.generic -> Context.generic; \\ \rangle\rangle
```

2.1.2 Mechanism 2 : global arbitrary data structure that is attached to the global and local Isabelle context θ

2.2 The LCF-Kernel: terms, types, theories, proof_contexts, thms

The classical LCF-style kernel is about

- 1. Types and terms of a typed λ -Calculus including constant symbols, free variables, λ -binder and application,
- 2. An infrastructure to define types and terms, a *signature*, that also assigns to constant symbols types
- 3. An abstract type of theorem and logical operations on them
- 4. (Isabelle specific): a notion of *theory*, i.e. a container providing a signature and set (list) of theorems.

2.2.1 Terms and Types

A basic data-structure of the kernel is \$ISABELLE_HOME/src/Pure/term.ML

```
\mathbf{ML}\langle\langle\ open\ Term;\ signature\ TERM'=sig
```

```
type\ indexname = string * int
 type \ class = string
 type \ sort = \ class \ list
 type \ arity = string * sort \ list * sort
 datatype \ typ =
   Type of string * typ list
    TFree of string * sort |
    TVar \ of \ indexname * sort
 datatype\ term =
   Const of string * typ |
   Free of string * typ |
    Var\ of\ indexname * typ \mid
   Bound of int |
   Abs \ of \ string * typ * term \mid
   \$ of term * term
 exception\ TYPE\ of\ string\ *\ typ\ list\ *\ term\ list
 exception TERM of string * term list
end
\rangle\rangle
```

 $\mathbf{ML} \langle \! \langle \ \mathit{Type.typ-instance} : \ \mathit{Type.tsig} \ -> \ \mathit{typ} \ * \ \mathit{typ} \ -> \ \mathit{bool} \ (* \ \mathit{raises} \ \ \mathit{TYPE-MATCH} \ *) \ \rangle \! \rangle$

there is a joker type that can be added as place-holder during term construction. Jokers can be eliminated by the type inference.

```
\mathbf{ML}\langle\!\langle Term.dummyT: typ \rangle\!\rangle
```

2.2.2 Type-Certification (=checking that a type annotation is consistent)

```
 \begin{aligned} \mathbf{ML} &\langle \\ Sign.typ\text{-}instance: theory -> typ * typ -> bool; \\ Sign.typ\text{-}match: theory -> typ * typ -> Type.tyenv -> Type.tyenv; \\ Sign.typ\text{-}unify: theory -> typ * typ -> Type.tyenv * int -> Type.tyenv * int; \\ Sign.const\text{-}type: theory -> string -> typ option; \\ Sign.certify\text{-}term: theory -> term -> term * typ * int; (* core routine for CERTIFICATION of types*) \\ Sign.cert\text{-}term: theory -> term -> term; (* short-cut for the latter *) \\ Sign.tsig\text{-}of: theory -> Type.tsig (* projects the type signature *) \\ &\rangle \end{aligned}
```

Sign.typ_match etc. is actually an abstract wrapper on the structure Type which contains the heart of the type inference. It also contains the type substitution type Type.tyenv which is is actually a type synonym for (sort * typ) Vartab.table which in itself is a synonym for 'a Symtab.table, so possesses the usual Symtab.empty and Symtab.dest operations.

Note that *polymorphic variables* are treated like constant symbols in the type inference; thus, the following test, that one type is an instance of the other, yields false:

```
 \begin{aligned} \mathbf{ML} & \langle val \ ty = @\{typ \ 'a \ option\}; \\ val \ ty' = @\{typ \ int \ option\}; \\ val \ Type(List.list,[S]) = @\{typ \ ('a) \ list\}; \ (* \ decomposition \ example \ *) \\ val \ false = Sign.typ-instance \ @\{theory\}(ty', \ ty); \\ \rangle \end{aligned}
```

In order to make the type inference work, one has to consider *schematic* type variables, which are more and more hidden from the Isar interface. Consequently, the typ antiquotation above will not work for schematic type variables and we have to construct them by hand on the SML level:

Type generalization — the conversion between free type variables and schematic type variables — is apparently no longer part of the standard API (there is a slightly more general replacement in Term_Subst.generalizeT_same, however). Here is a way to overcome this by a self-baked generalization function:

\mathbf{ML}

```
val\ generalize-typ = Term.map-type-tfree\ (fn\ (str,sort) => Term.TVar((str,0),sort)); \\val\ generalize-term = Term.map-types\ generalize-typ; \\val\ true = Sign.typ-instance\ @\{theory\}\ (ty',\ generalize-typ\ ty)
```

... or more general variants thereof that are parameterized by the indexes for schematic type variables instead of assuming just 0.

Example:

```
\mathbf{ML}\langle val\ t = generalize\text{-}term\ @\{term\ []\}\rangle
```

Now we turn to the crucial issue of type-instantiation and with a given type environment tyenv. For this purpose, one has to switch to the low-level interface Term_Subst.

$\mathbf{ML}\langle$

```
Term-Subst.map-types-same: (typ -> typ) -> term -> term; \\ Term-Subst.map-aterms-same: (term -> term) -> term -> term; \\ Term-Subst.instantiate: ((indexname * sort) * typ) list * ((indexname * typ) * term) list -> term -> term; \\ Term-Subst.instantiateT: ((indexname * sort) * typ) list -> typ -> typ; \\ Term-Subst.generalizeT: string list -> int -> typ -> typ; \\ (* this is the standard type generalisation function !!! \\ only type-frees in the string-list were taken into account. *) \\ Term-Subst.generalize: string list * string list -> int -> term -> term \\ (* this is the standard term generalisation function !!! \\ only type-frees and frees in the string-lists were taken into account. *) \\ \end{cases}
```

Apparently, a bizarre conversion between the old-style interface and the new-style tyenv is necessary. See the following example.

```
\mathbf{ML}
```

```
val \ S = Vartab.dest \ tyenv;
val \ S' = (map \ (fn \ (s,(t,u)) => ((s,t),u)) \ S) : ((indexname * sort) * typ) \ list;
(* \ it \ took \ me \ quite \ some \ time \ to \ find \ out \ that \ these \ two \ type \ representations,
obscured \ by \ a \ number \ of \ type-synonyms, \ where \ actually \ identical. *)
val \ ty = t-schematic;
val \ ty' = Term-Subst.instantiate T \ S' \ t-schematic;
val \ t = (generalize-term (sterm \ subst.);
```

```
val\ t' = Term-Subst.map-types-same\ (Term-Subst.instantiateT\ S')\ (t) (* or alternatively:*) val\ t'' = Term.map-types\ (Term-Subst.instantiateT\ S')\ (t)
```

2.2.3 Type-Inference (= inferring consistent type information if possible)

Type inference eliminates also joker-types such as dummyT and produces instances for schematic type variables where necessary. In the case of success, it produces a certifiable term.

```
 \begin{array}{l} \mathbf{ML} \langle \langle \\ \mathit{Type-Infer-Context.infer-types: Proof.context } -> \mathit{term list } -> \mathit{term list } \\ \rangle \rangle \end{array}
```

2.2.4 thy and the signature interface

$ML\langle$

```
Sign.tsig-of: theory -> Type.tsig;
Sign.syn-of: theory -> Syntax.syntax;
Sign.of-sort: theory -> typ * sort -> bool;
```

2.2.5 Thm's and the LCF-Style, "Mikro"-Kernel

The basic constructors and operations on theorems\$ISABELLE_HOME/src/Pure/thm.ML, a set of derived (Pure) inferences can be found in \$ISABELLE_HOME/src/Pure/drule.ML.

The main types provided by structure thm are certified types ctyp, certified terms cterm, thm as well as conversions conv.

$ML\langle$

```
\begin{array}{l} signature \ BASIC\text{-}THM = \\ sig \\ type \ ctyp \\ type \ cterm \\ exception \ CTERM \ of \ string * \ cterm \ list \\ type \ thm \\ type \ conv = \ cterm \ -> \ thm \\ exception \ THM \ of \ string * \ int * \ thm \ list \\ end; \end{array}
```

Certification of types and terms on the kernel-level is done by the generators:

$\mathbf{ML}\langle$

```
\begin{array}{lll} Thm.global\text{-}ctyp\text{-}of\colon theory & -> typ & -> ctyp;\\ Thm.ctyp\text{-}of\colon Proof.context & -> typ & -> ctyp;\\ Thm.global\text{-}cterm\text{-}of\colon theory & -> term & -> cterm;\\ Thm.cterm\text{-}of\colon Proof.context & -> term & -> cterm;\\ \end{array}
```

... which perform type-checking in the given theory context in order to make a type or term "admissible" for the kernel.

We come now to the very heart of the LCF-Kernel of Isabelle, which provides the fundamental inference rules of Isabelle/Pure.

Besides a number of destructors on thm's, the abstract data-type thm is used for logical objects of the form $\Gamma \vdash_{\theta} \phi$, where Γ represents a set of local assumptions, θ the "theory" or more precisely the global context in which a formula ϕ has been constructed just by applying the following operations representing logical inference rules:

$$\frac{\Theta,\Pi,\Gamma\vdash q:B}{\Theta,\Pi,\Gamma\vdash p:(A\Longrightarrow B)\vdash (\lambda p:A.\ q):(A\Longrightarrow B)} \ (imp\text{-}intro)$$

$$\frac{\Theta_1,\Pi_1,\Gamma_1\vdash p:(A\Longrightarrow B)\vdash \Theta_2,\Pi_2,\Gamma_2\vdash q:A}{\Theta_1\cup\Theta_2,\Pi_1\cup\Pi_2,\Gamma_1\cup\Gamma_2\vdash p\ q:B} \ (imp\text{-}elim)$$

$$\frac{\Theta,\Pi,\Gamma\vdash p[x]:B[x]\vdash x\notin FV\Gamma}{\Theta,\Pi,\Gamma\vdash (\lambda x.\ p[x]):(\bigwedge x.\ B[x])} \ (all\text{-}intro)$$

$$\frac{\Theta,\Pi,\Gamma\vdash p:(\bigwedge x.\ B[x])}{\Theta,\Pi,\Gamma\vdash p\ a:B[a]} \ (all\text{-}elim)$$

$$\frac{\Theta,\Pi,\{p:A\}\vdash p:A}{\Theta,\Pi,\{p:A\}\vdash p:A} \ (assm)$$

$$\frac{(c:A[?\overline{\alpha}])\in\Theta}{\Theta,\emptyset,\emptyset\vdash c:A[\overline{\tau}]} \ (axiom)$$

$$\frac{\Theta,\Pi,\Gamma\vdash p[\alpha]:B[\alpha]\quad \alpha\notin TV\Gamma}{\Theta,\Pi,\Gamma\vdash p[?\alpha]:B[?\alpha]} \ (type\text{-}gen)$$

$$\frac{(c:A[?\overline{\alpha}])\in\Theta}{\Theta,\emptyset,\emptyset\vdash c:A[\overline{\tau}]} \ (type\text{-}inst)$$

$$(a) \ \text{Pure Kernel Inference Rules II}$$

Figure 2.1:

```
 \begin{aligned} \mathbf{ML} & (*inference\ rules*) \\ Thm.assume:\ cterm\ ->\ thm; \\ Thm.implies-intr:\ cterm\ ->\ thm\ ->\ thm; \\ Thm.implies-elim:\ thm\ ->\ thm\ ->\ thm; \\ Thm.forall-intr:\ cterm\ ->\ thm\ ->\ thm; \\ Thm.forall-elim:\ cterm\ ->\ thm\ ->\ thm; \\ Thm.transfer:\ theory\ ->\ thm\ ->\ thm; \\ Thm.generalize:\ string\ list\ *\ string\ list\ ->\ int\ ->\ thm\ ->\ thm; \\ Thm.instantiate:\ ((indexname*sort)*ctyp)list\ *\ ((indexname*typ)*cterm)\ list\ ->\ thm\ ->\ thm; \\ \end{aligned}
```

They reflect the Pure logic depicted in a number of presentations such as M. Wenzel, *Parallel Proof Checking in Isabelle/Isar*, PLMMS 2009, or similar papers. Notated as logical inference rules, these operations were presented as follows:

Note that the transfer rule:

$$\frac{\Gamma \vdash_{\theta} \phi \qquad \qquad \theta \sqsubseteq \theta'}{\Gamma \vdash_{\theta'} \phi}$$

which is a consequence of explicit theories characteristic for Isabelle's LCF-kernel design and a remarkable difference to its sisters HOL-Light and HOL4; instead of transfer, these systems reconstruct proofs in an enlarged global context instead of taking the result and converting it.

Besides the meta-logical (Pure) implication $_\Longrightarrow_$, the Kernel axiomatizes also a Pure-Equality $_\equiv_$ used for definitions of constant symbols:

```
\mathbf{ML}
```

```
Thm.reflexive: cterm -> thm;
Thm.symmetric: thm -> thm;
Thm.transitive: thm -> thm -> thm;

The operation:

ML( Thm.trivial: cterm -> thm; )
```

... produces the elementary tautologies of the form $A \Longrightarrow A$, an operation used to start a backward-style proof.

The elementary conversions are:

```
\mathbf{ML}\langle
```

```
Thm.beta-conversion: bool -> conv;
Thm.eta-conversion: conv;
Thm.eta-long-conversion: conv;
```

On the level of Drule, a number of higher-level operations is established, which is in part accessible by a number of forward-reasoning notations on Isar-level.

```
\mathbf{ML} \langle
```

```
op RSN: thm * (int * thm) -> thm;

op RS: thm * thm -> thm;

op RLN: thm \ list * (int * thm \ list) -> thm \ list;

op RL: thm \ list * thm \ list -> thm \ list;

op MRS: thm \ list * thm -> thm;

op OF: thm * thm \ list -> thm;

op COMP: thm * thm -> thm;
```

2.2.6 Theories

This structure yields the datatype hy*_which_becomes_he content of ontext.theory*._In_a_way,_the_LF-Kernel registers itself into the Nano-Kernel, which inspired me (bu) to this naming.

```
\mathbf{ML} \langle \! \langle
```

```
(* intern Theory. Thy;
datatype thy = Thy of
\{pos: Position.T,
 id: serial.
 axioms: term Name-Space.table,
 defs: Defs.T,
 wrappers: wrapper\ list* * wrapper\ list*;
*)
Theory.check: Proof.context \rightarrow string * Position.T \rightarrow theory;
Theory.local\text{-}setup: (Proof.context \rightarrow Proof.context) \rightarrow unit;
Theory.setup: (theory -> theory) -> unit; (* The thing to extend the table of commands with parser -
callbacks. *)
Theory.get-markup: theory -> Markup.T;
Theory.axiom\text{-}table:\ theory\ ->\ term\ Name\text{-}Space.table;
Theory.axiom\text{-}space:\ theory\ ->\ Name\text{-}Space.\ T;
Theory.axioms-of: theory \rightarrow (string * term) list;
Theory.all-axioms-of: theory \rightarrow (string * term) list;
Theory.defs-of: theory \rightarrow Defs. T;
Theory.at-begin: (theory -> theory option) -> theory -> theory;
Theory.at-end: (theory -> theory option) -> theory -> theory;
Theory.begin-theory: string * Position.T \rightarrow theory list \rightarrow theory;
Theory.end-theory: theory \rightarrow theory;
\rangle\rangle
```

2.3 Backward Proofs, Tactics and Tacticals

tactic's are in principle relations on theorems; this gives a natural way to represent the fact that HO-Unification (and therefore the mechanism of rule-instantiation) are non-deterministic in principle. Heuristics may choose particular preferences between the theorems in the range of this relation, but the Isabelle Design accepts this fundamental fact reflected at this point in the prover architecture. This potentially infinite relation is implemented by a function of theorems to lazy lists over theorems, which gives both sufficient structure for heuristic considerations as well as a nice algebra, called TACTICAL's, providing a bottom element no_tac (the function that always fails), the top-element all_tac (the function that never fails), sequential composition op THEN, (serialized) non-deterministic composition op ORELSE, conditionals, repetitions over lists, etc. The following is an excerpt of ~~/src/Pure/tactical.ML:

```
ML(
signature\ TACTICAL = sig
type\ tactic = thm\ -> thm\ Seq.seq

val\ all\text{-}tac:\ tactic
val\ no\text{-}tac:\ tactic
val\ COND:\ (thm\ -> bool)\ -> tactic\ -> tactic\ -> tactic

val\ THEN:\ tactic\ *\ tactic\ -> tactic
val\ THEN':\ ('a\ -> tactic)\ *\ ('a\ -> tactic)\ -> 'a\ -> tactic
val\ TRESE':\ ('a\ -> tactic)\ *\ ('a\ -> tactic)\ -> 'a\ -> tactic
val\ TRY:\ tactic\ -> tactic
val\ EVERY:\ tactic\ list\ -> tactic
val\ FIRST:\ tactic\ list\ -> tactic
(*\ ...\ *)
val\ PIRST:\ tactic\ list\ -> tactic
val\ PIRST:\ tactic\ list\ -> tactic
val\ PIRST:\ tactic\ list\ -> tactic
```

The next layer in the architecture describes \mathtt{tactic} 's, i.e. basic operations on theorems in a backward reasoning style (bottom up development of proof-trees). An initial state for some property A — the goal — is constructed via the kernel $\mathtt{Thm.trivial}$ -operation into $A \Longrightarrow A$, and tactics either refine the premises — the subgoals the of this meta-implication — producing more and more of them or eliminate them. Subgoals of the form $[B_1; B_2; A; B_3; B_4] \Longrightarrow A$ can be eliminated via the $\mathtt{Tactic.assume_tac-tactic}$, and a subgoal C_m can be refined via the theorem $[E_1; E_2; E_3] \Longrightarrow C_m$ the $\mathtt{Tactic.resolve_tac-tactic}$ to new subgoals E_1, E_2, E_3 . In case that a theorem used for resolution has no premise E_i , the subgoal C_m is also eliminated ("closed").

The following abstract of the most commonly used tactic's drawn from ~~/src/Pure/tactic.ML looks as follows:

```
\mathbf{ML}
```

```
signature\ BASIC-TACTIC = sig \\ (* \dots *) \\ val\ assume-tac:\ Proof.context -> int -> tactic \\ val\ compose-tac:\ Proof.context -> (bool*\ thm*\ int) -> int -> tactic \\ val\ resolve-tac:\ Proof.context -> thm\ list -> int -> tactic \\ val\ eresolve-tac:\ Proof.context -> thm\ list -> int -> tactic \\ val\ forward-tac:\ Proof.context -> thm\ list -> int -> tactic \\ val\ dresolve-tac:\ Proof.context -> thm\ list -> int -> tactic \\ val\ rotate-tac:\ int -> in
```

```
val\ defer-tac:\ int\ ->\ tactic val\ prefer-tac:\ int\ ->\ tactic (*\ ...\ *) end;
```

2.4 The Isar Engine

```
Toplevel.theory;
Toplevel.presentation-context-of; (* Toplevel is a kind of table with call-bacl functions *)
Consts.the-const; (* T is a kind of signature ... *)
Variable.import-terms;
Vartab.update;
fun control-antiquotation name s1 s2 =
  Thy-Output.antiquotation name (Scan.lift Args.cartouche-input)
   (fn \{state, ...\} = senctores s1 s2 o Thy-Output.output-text state \{markdown = false\});
Output.output;
Syntax.read-input;
Input.source-content;
 basic-entity @{binding const} (Args.const {proper = true, strict = false}) pretty-const #>
*)
\rangle\rangle
\mathbf{ML} \langle \! \langle
Config.get @{context} Thy-Output.display;
Config.get @\{context\} \ Thy-Output.source;
Config.get @{context} Thy-Output.modes;
Thy-Output.document-command;
(* is:
fun\ document-command\ markdown\ (loc,\ txt) =
  Toplevel.keep (fn \ state =>
   (case loc of
     NONE = > ignore (output-text state markdown txt)
   \mid SOME (-, pos) =>
       error (Illegal target specification -- not a theory context ^ Position.here pos))) o
  Toplevel.present-local-theory\ loc\ (fn\ state => ignore\ (output-text\ state\ markdown\ txt));
end;
*)
\rangle\rangle
\mathbf{ML}\langle\langle Thy\text{-}Output.document\text{-}command \{markdown = true} \rangle\rangle
\mathbf{ML}\langle\langle Latex.output-ascii;
     Latex.output-token
(* Hm, generierter output for
subsection*[Shaft-Encoder-characteristics]{*Shaft Encoder Characteristics*}:
```

```
\begin{isamarkuptext}
\end{isamarkuptext}\isamarkuptrue\%
Shaft \setminus Encoder \setminus Characteristics \setminus \{ \setminus isacharverbatimclose \} \%
Generierter\ output\ for:\ text\^\cartouche>\langle label\{sec:Shaft-Encoder-characteristics\}\rangle
\begin{supersystem} begin{supersystem} is a mark up text \}\%
\label{sec:Shaft-Encoder-characteristics}\%
\ensuremath{\ }\ensuremath{\ }\ens
*)
\rangle\!\rangle
ML\langle\langle
Thy-Output.maybe-pretty-source:
       (Proof.context -> 'a -> Pretty.T) -> Proof.context -> Token.src -> 'a list -> Pretty.T list;
Thy-Output.output: Proof.context -> Pretty.T list -> string;
 (* nuescht besonderes *)
fun\ document-antiq\ check-file\ ctxt\ (name,\ pos) =
    (* val dir = master-directory (Proof-Context.theory-of ctxt); *)
    (* val - = check-path check-file ctxt dir (name, pos); *)
      space-explode / name
      |> map Latex.output-ascii
      |> space\text{-}implode \ (Latex.output\text{-}ascii \ / \ ^ \setminus discretionary\{\}\{\}\{\})
      |> enclose \setminus isatt\{ \}
  end;
\mathbf{ML} \langle \! \langle \mathit{Type-Infer-Context.infer-types} \ \rangle \! \rangle
ML\langle\langle Type\text{-}Infer\text{-}Context.prepare\text{-}positions \rangle\rangle
2.4.1 Transaction Management in the Isar-Engine: The Toplevel
Thy-Output.output-text: Toplevel.state -> {markdown: bool} -> Input.source -> string;
Thy-Output.document-command;
Toplevel.exit: Toplevel.transition -> Toplevel.transition;
Toplevel.keep: (Toplevel.state -> unit) -> Toplevel.transition -> Toplevel.transition;
Toplevel.keep': (bool -> Toplevel.state -> unit) -> Toplevel.transition -> Toplevel.transition;
Toplevel.ignored: Position.T \rightarrow Toplevel.transition;
Toplevel.generic-theory: (generic-theory -> generic-theory) -> Toplevel.transition:
Toplevel.theory': (bool -> theory -> theory) -> Toplevel.transition -> Toplevel.transition;
Toplevel.theory: (theory -> theory) -> Toplevel.transition -> Toplevel.transition;
```

```
Toplevel.present-local-theory:
(xstring * Position.T) option ->
           (Toplevel.state -> unit) -> Toplevel.transition -> Toplevel.transition;
(* where text treatment and antiquotation parsing happens *)
(*fun\ document-command\ markdown\ (loc,\ txt) =
     Toplevel.keep (fn state =>
         (case loc of
             NONE =  ignore (output-text state markdown txt)
         \mid SOME (-, pos) =>
                  error (Illegal target specification -- not a theory context ^ Position.here pos))) o
    Toplevel.present-local-theory\ loc\ (fn\ state => ignore\ (output-text\ state\ markdown\ txt));\ *)
Thy-Output.document-command: \ \{markdown: bool\} \ -> (xstring*Position.T) \ option*Input.source \ -> (xstring*Position.T) \ 
                                                                        Toplevel.transition −> Toplevel.transition;
(* Isar Toplevel Steuerung *)
Toplevel.keep: (Toplevel.state -> unit) -> Toplevel.transition -> Toplevel.transition; (* val keep' = add-trans o Keep;
               fun\ keep\ f = add\text{-}trans\ (Keep\ (fn\ - => f));
           *)
Top level. present-local-theory: (xstring*Position.T) \ option \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> \ (Top level. state \ -> \ unit) \ -> 
          Toplevel.transition → Toplevel.transition;
         (* fun present-local-theory target = present-transaction (fn int =>
                         (fn\ Theory\ (gthy,\ -) =>
                                            let \ val \ (finish, \ lthy) = Named-Target.switch \ target \ qthy;
                                            in Theory (finish lthy, SOME lthy) end
                         \mid - = > raise \ UNDEF);
               fun present-transaction f g = add-trans (Transaction (f, g));
               fun\ transaction\ f = present-transaction\ f\ (K\ ());
Toplevel.theory: (theory -> theory) -> Toplevel.transition -> Toplevel.transition;
      (* fun theory' f = transaction (fn int =>
                                    (fn\ Theory\ (Context.Theory\ thy,\ -) =>
                                                   let val thy' = thy
                                                                                     |> Sign.new-group
                                                                                      |> f int
                                                                                      |> Sign.reset-group;
                                                  in Theory (Context. Theory thy', NONE) end
                                    \mid - = > raise \ UNDEF);
            fun\ theory\ f = theory'\ (K\ f);\ *)
Thy-Output.document-command: \{markdown: bool\} \rightarrow (xstring * Position.T) option * Input.source \rightarrow
          Toplevel.transition \rightarrow Toplevel.transition;
          (* fun document-command markdown (loc, txt) =
                            Toplevel.keep (fn state =>
                                   (case loc of
                                            NONE => ignore (output-text state markdown txt)
                                                          \mid SOME (-, pos) = >
                                            error (Illegal target specification -- not a theory context ^ Position.here pos))) o
                              Toplevel.present-local-theory\ loc\ (fn\ state => ignore\ (output-text\ state\ markdown\ txt));
         *)
```

```
Thy-Output.output-text: Toplevel.state \rightarrow \{markdown: bool\} \rightarrow Input.source \rightarrow string;
                     (* this is where antiquotation expansion happens: uses eval-antiquote *)
\rangle\!\rangle
\mathbf{ML}\langle\!\langle
(* Isar Toplevel Steuerung *)
Toplevel.keep: (Toplevel.state \rightarrow unit) \rightarrow Toplevel.transition \rightarrow Toplevel.transition;
   (* val keep' = add-trans o Keep;
     fun \ keep \ f = add-trans \ (Keep \ (fn - => f));
Toplevel.present-local-theory: (xstring * Position.T) option -> (Toplevel.state -> unit) ->
   Toplevel.transition -> Toplevel.transition;
   (* \textit{fun present-local-theory target} = \textit{present-transaction (fn int} =>
         (fn\ Theory\ (gthy,\ -) =>
                let \ val \ (finish, \ lthy) = Named-Target.switch \ target \ gthy;
                in Theory (finish lthy, SOME lthy) end
         \mid - = > raise \ UNDEF);
      fun present-transaction f g = add-trans (Transaction (f, g));
     fun\ transaction\ f = present-transaction\ f\ (K\ ());
Toplevel.theory: (theory -> theory) -> Toplevel.transition -> Toplevel.transition;
  (* fun theory' f = transaction (fn int =>
             (fn\ Theory\ (Context.Theory\ thy,\ -) =>
                   let val thy' = thy
                                |> Sign.new-group
                                |>fint
                                |> Sign.reset-group;
                   in Theory (Context. Theory thy', NONE) end
             \mid - = > raise \ UNDEF);
     fun\ theory\ f = theory'\ (K\ f);\ *)
Thy-Output.document-command: {markdown: bool} -> (xstring * Position.T) option * Input.source ->
   Toplevel.transition -> Toplevel.transition;
   (* fun document-command markdown (loc, txt) =
          Toplevel.keep (fn \ state =>
             (case loc of
                NONE =  ignore (output-text state markdown txt)
                     \mid SOME (-, pos) =>
                error (Illegal target specification -- not a theory context ^ Position.here pos))) o
           Toplevel.present-local-theory\ loc\ (fn\ state => ignore\ (output-text\ state\ markdown\ txt));
   *)
Thy-Output.output-text: Toplevel.state -> {markdown: bool} -> Input.source -> string;
                     (* this is where antiquotation expansion happens : uses eval-antiquote *)
```

 $\rangle\!\rangle$

2.4.2 Configuration flags of fixed type in the Isar-engine.

```
\mathbf{ML} \langle \! \langle
Config.get @{context} Thy-Output.quotes;
Config.get @{context} Thy-Output.display;
val\ C = Synchronized.var\ Pretty.modes\ latEEex;
(* Synchronized: a mechanism to bookkeep global
   variables \ with \ synchronization \ mechanism \ included \ *)
Synchronized.value\ C;
(*
fun\ output\ ctxt\ prts =
   603 prts
         |> Config.get ctxt quotes ? map Pretty.quote
          |> (if Config.get ctxt display then
                map (Pretty.indent (Config.get ctxt indent) #> string-of-margin ctxt #> Output.output)
   606
   607
                \# > space\text{-}implode \ \backslash is a sep \backslash \backslash is a new line \% \backslash n
   608
               \#> Latex.environment\ is abelle
   609
              else
   610
                map
                 ((if Config.get ctxt break then string-of-margin ctxt else Pretty.unformatted-string-of)
   611
                    #> Output.output)
   612
   613
                \# > space\text{-}implode \ \backslash \ is a sep \backslash \ is a new line \% \backslash n
   614
                \# > enclose \\isa{ });
\rangle\!\rangle
```

3 Front End

Introduction ... TODO

3.1 Basics: string, bstring and xstring

string is the basic library type from the SML library in structure String. Many Isabelle operations produce or require formats thereof introduced as type synonyms bstring (defined in structure Binding and xstring (defined in structure Name_Space. Unfortunately, the abstraction is not tight and combinations with elementary routines might produce quire crappy results.

```
\mathbf{ML} \langle val \ b = Binding.name-of@\{binding \ here\} \rangle
```

... produces the system output val it = "here": bstring, but note that it is trappy to believe it is just a string.

However, there is an own XML parser for this format. See Section Markup.

 $\mathbf{ML} \langle fun \ dark-matter \ x = XML.content-of \ (YXML.parse-body \ x) \rangle$

3.2 Parsing issues

Parsing combinators represent the ground building blocks of both generic input engines as well as the specific Isar framework. They are implemented in the structure Token providing core type Token.T.

```
ML\(\langle open Token\)\\
ML\(\langle (* Provided types: *) (* type 'a parser = T list -> 'a * T list type 'a context-parser = Context.generic * T list -> 'a * (Context.generic * T list) *\)

(* conversion between these two: *)

fun parser2contextparser pars (ctxt, toks) = let val (a, toks') = pars toks in (a,(ctxt, toks')) end;

val -= parser2contextparser: 'a parser -> 'a context-parser;

(* bah, is the same as Scan.lift *)

val -= Scan.lift Args.cartouche-input: Input.source context-parser;

Token.is-command;

Token.content-of; (* textueller kern eines Tokens. *)
```

```
Tokens and Bindings

ML\(\lambda\)
val H = @{binding here}; (* There are bindings consisting of a text-span and a position, where "positions" are absolute references to a file *)

Binding.make: bstring * Position.T -> binding;

Binding.pos-of @{binding erzerzer};

Position.here: Position.T -> string;

(* Bindings *)

ML\(\circ^{\text{cartouche}}(val X = @{here});)

\)

3.2.1 Input streams.

ML\(\lambda\)
Input.source-explode: Input.source -> Symbol-Pos.T list;

(* conclusion: Input.source-explode converts f @{thm reft}}

into:

[(, {offset=14, id=-2769}), (f, {offset=15, id=-2769}), (, {offset=16, id=-2769}),

(@, {offset=17, id=-2769}), (, {offset=18, id=-2769}), (t, {offset=19, id=-2769}),
```

3.2.2 Scanning and combinator parsing.

 $(l, \{offset=26, id=-2769\}), (\}, \{offset=27, id=-2769\})]$

Is used on two levels:

 $*)\rangle\!\rangle$

- 1. outer syntax, that is the syntax in which Isar-commands are written, and
- 2. inner-syntax, that is the syntax in which lambda-terms, and in particular HOL-terms were written.

 $\begin{array}{l} (h, \{o\mathit{ffset}=20, \ id=-2769\}), \ (m, \{o\mathit{ffset}=21, \ id=-2769\}), \ (\ , \{o\mathit{ffset}=22, \ id=-2769\}), \ (r, \{o\mathit{ffset}=23, \ id=-2769\}), \ (e, \{o\mathit{ffset}=24, \ id=-2769\}), \ (f, \{o\mathit{ffset}=25, \ id=-2769\}), \ (f, \{o\mathit{$

A constant problem for newbies is this distinction, which makes it necessary that the " ... " quotes have to be used when switching to inner-syntax, except when only one literal is expected when an inner-syntax term is expected.

\mathbf{ML}

```
Scan.peek : ('a -> 'b -> 'c * 'd) -> 'a * 'b -> 'c * ('a * 'd); \\ Scan.optional: ('a -> 'b * 'a) -> 'b -> 'a -> 'b * 'a; \\ Scan.option: ('a -> 'b * 'a) -> 'a -> 'b option * 'a; \\ Scan.repeat: ('a -> 'b * 'a) -> 'a -> 'b list * 'a; \\ Scan.lift : ('a -> 'b * 'c) -> 'd * 'a -> 'b * ('d * 'c); \\ Scan.lift (Parse.position Args.cartouche-input); \\ >
```

"parsers" are actually interpreters; an 'a parser is a function that parses an input stream and computes (=evaluates, computes) it into 'a. Since the semantics of an Isabelle command is a transition => transition or theory \Rightarrow theory function, i.e. a global system transition. parsers of that type can be constructed and be bound as call-back functions to a table in the Toplevel-structure of Isar.

The type 'a parser is already defined in the structure Token.

Syntax operations: Interface for parsing, type-checking, "reading" (both) and pretty-printing. Note that this is a late-binding interface, i.e. a collection of "hooks". The real work is done ... see below.

Encapsulates the data structure "syntax" — the table with const symbols, print and ast translations, ... The latter is accessible, e.g. from a Proof context via Proof_Context.syn_of.

```
ML
```

```
Parse.nat: int parser;
Parse.int: int parser;
Parse.enum-positions: string -> 'a parser -> ('a list * Position.T list) parser;
Parse.enum: string -> 'a parser -> 'a list parser;
Parse.input: 'a parser -> Input.source parser;

Parse.enum: string -> 'a parser -> 'a list parser;
Parse.enum: string -> 'a parser -> 'a list parser;
Parse.!!!: (T list -> 'a) -> T list -> 'a;
Parse.position: 'a parser -> ('a * Position.T) parser;

(* Examples *)
Parse.position Args.cartouche-input;
```

Inner Syntax Parsing combinators for elementary Isabelle Lexems

\mathbf{ML}

```
Syntax.parse-sort: Proof.context -> string -> sort; \\ Syntax.parse-typ: Proof.context -> string -> typ; \\ Syntax.parse-term: Proof.context -> string -> term; \\ Syntax.parse-prop: Proof.context -> string -> term; \\ Syntax.check-term: Proof.context -> term -> term; \\ Syntax.check-props: Proof.context -> term list -> term list; \\ Syntax.uncheck-sort: Proof.context -> sort -> sort; \\ Syntax.uncheck-typs: Proof.context -> typ list -> typ list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list -> term list; \\ Syntax.uncheck-terms: Proof.context -> term list ->
```

In contrast to mere parsing, the following operators provide also type-checking and internal reporting to PIDE — see below. I did not find a mechanism to address the internal serial-numbers used for the PIDE protocol, however, rumours have it that such a thing exists. The variants <code>_global</code> work on theories instead on <code>Proof.contexts</code>.

\mathbf{ML}

```
Syntax.read-sort: Proof.context -> string -> sort; \\ Syntax.read-typ: Proof.context -> string -> typ; \\ Syntax.read-term: Proof.context -> string -> term; \\ Syntax.read-typs: Proof.context -> string list -> typ list; \\ Syntax.read-sort-global: theory -> string -> sort; \\ Syntax.read-typ-global: theory -> string -> typ; \\ Syntax.read-term-global: theory -> string -> term; \\ Syntax.read-prop-global: theory -> term; \\ Syntax.read-prop-global: theory
```

The following operations are concerned with the conversion of pretty-prints and, from there, the generation of (non-layouted) strings.

$ML\langle$

```
Syntax.pretty-term: Proof.context \ -> term \ -> Pretty.T; \\ Syntax.pretty-typ: Proof.context \ -> typ \ -> Pretty.T; \\ Syntax.pretty-sort: Proof.context \ -> sort \ -> Pretty.T; \\ Syntax.pretty-classrel: Proof.context \ -> class list \ -> Pretty.T; \\ Syntax.pretty-arity: Proof.context \ -> arity \ -> Pretty.T; \\ Syntax.string-of-term: Proof.context \ -> term \ -> string; \\ Syntax.string-of-typ: Proof.context \ -> typ \ -> string; \\ Syntax.lookup-const: Syntax.syntax \ -> string \ -> string option; \\ >
```

```
 \begin{aligned} \mathbf{ML} &\langle \\ \textit{fun read-terms ctxt} = \\ &\textit{grouped 10 Par-List.map-independent (Syntax.parse-term ctxt)} \ \# > \textit{Syntax.check-terms ctxt}; \\ &\rangle \\ &\mathbf{ML} &\langle \\ &\textit{(* More High-level, more Isar-specific Parsers *)} \\ &\textit{Args.name;} \\ &\textit{Args.const;} \\ &\textit{Args.const;} \\ &\textit{Args.cartouche-input: Input.source parser;} \\ &\textit{Args.text-token: Token.T parser;} \\ &\textit{val Z = let val attribute = Parse.position Parse.name --} \\ &\textit{Scan.optional (Parse.\$\$\$ = |-- Parse.!!! Parse.name) ;} \\ &\textit{in (Scan.optional(Parse.\$\$\$, |-- (Parse.enum, attribute))) end ;} \\ &\textit{(* this leads to constructions like the following, where a parser for a *)} \\ &\textit{fn name => (Thy-Output.antiquotation name (Scan.lift (Parse.position Args.cartouche-input)));} \\ \end{aligned}
```

3.3

 $\mathbf{ML} \langle Sign.add\text{-}trrules \rangle$

3.4 The PIDE Framework

3.4.1 Markup

Markup Operations, and reporting. Diag in Isa_DOF Foundations TR. Markup operation send via side-effect annotations to the GUI (precisely: to the PIDE Framework) that were used for hyperlinking applicating to binding occurrences, info for hovering, ...

```
\mathbf{ML}\langle\!\langle
(* Position.report is also a type consisting of a pair of a position and markup. *)
(* It would solve all my problems if I find a way to infer the defining Position.report
  from a type definition occurence ... *)
Position.report: Position.T \rightarrow Markup.T \rightarrow unit;
Position.reports: Position.report \ list -> unit;
    (*???I think this is the magic thing that sends reports to the GUI.*)
Markup.entity: string \rightarrow string \rightarrow Markup.T;
Markup.properties: Properties.T \rightarrow Markup.T \rightarrow Markup.T;
Properties.get: Properties.T \rightarrow string \rightarrow string option;
Markup.enclose: Markup.T \rightarrow string \rightarrow string;
(* example for setting a link, the def flag controls if it is a defining or a binding
occurence of an item *)
fun\ theory-markup\ (def:bool)\ (name:string)\ (id:serial)\ (pos:Position.T) =
 if\ id = 0\ then\ Markup.empty
   Markup.properties (Position.entity-properties-of def id pos)
     (Markup.entity Markup.theoryN name);
Markup.theoryN: string;
```

serial(); (* A qlobal, lock-quarded seriel counter used to produce unique identifiers,

```
be it on the level of thy-internal states or as reference in markup in
             PIDE *)
(* From Theory:
fun\ check\ ctxt\ (name,\ pos) =
 let
   val thy = Proof\text{-}Context.theory\text{-}of ctxt;
   val thy' =
     Context.get-theory thy name
      handle\ ERROR\ msg =>
        let
          val\ completion =
            Completion.make (name, pos)
             (fn\ completed =>
               map Context.theory-name (ancestors-of thy)
               |> filter completed
               |> sort-strings
               |> map (fn \ a => (a, (Markup.theoryN, a))));
          val\ report = Markup.markup-report\ (Completion.reported-text\ completion);
        in error (msg ^ Position.here pos ^ report) end;
   val - = Context-Position.report \ ctxt \ pos \ (get-markup \ thy');
 in thy' end;
fun\ init-markup\ (name,\ pos)\ thy =
 let
   val\ id = serial\ ();
   val - = Position.report pos (theory-markup true name id pos);
 in map-thy (fn (-, -, axioms, defs, wrappers) => (pos, id, axioms, defs, wrappers)) thy end;
fun \ get\text{-}markup \ thy =
 let val \{pos, id, ...\} = rep-theory thy
 in theory-markup false (Context.theory-name thy) id pos end;
*)
fun theory-markup def thy-name id pos =
 if\ id = 0\ then\ Markup.empty
   Markup.properties (Position.entity-properties-of def id pos)
     (Markup.entity\ Markup.theoryN\ thy-name);
fun\ get{-}markup\ thy =
 let\ val\ \{pos,\ id,\ ...\} = rep-theory\ thy
 in theory-markup false (Context.theory-name thy) id pos end;
fun\ init-markup\ (name,\ pos)\ thy =
 let
   val\ id = serial\ ();
   val - = Position.report pos (theory-markup true name id pos);
 in map-thy (fn (-, -, axioms, defs, wrappers)) => (pos, id, axioms, defs, wrappers)) thy end;
\mathit{fun}\ \mathit{check}\ \mathit{ctxt}\ (\mathit{name},\ \mathit{pos}) =
 let
```

```
val\ thy = \textit{Proof-Context.theory-of\ ctxt};
   val thy' =
     Context.get-theory thy name
      handle\ ERROR\ msg =>
        let
          val\ completion =
           Completion.make (name, pos)
             (fn\ completed =>
               map Context.theory-name (ancestors-of thy)
               |> filter completed
               |> sort-strings
               |> map (fn \ a => (a, (Markup.theoryN, a))));
          val\ report = Markup.markup-report\ (Completion.reported-text\ completion);
        in error (msg ^ Position.here pos ^ report) end;
   val -= Context-Position.report ctxt pos (get-markup thy');
 in thy' end;
*)
\rangle\rangle
```

3.5 Output: Very Low Level

```
\mathbf{ML} \langle Output.output; (* output is the structure for the hooks with the target devices. *) Output.output bla-1:; \rangle
```

3.6 Output: LaTeX

```
 \begin{split} \mathbf{ML} \langle & Thy\text{-}Output.verbatim\text{-}text; \\ & Thy\text{-}Output.output\text{-}text: Toplevel.state} \ -> \{markdown: bool\} \ -> Input.source} \ -> string; \\ & Thy\text{-}Output.antiquotation:} \\ & binding \ -> \\ & 'a \ context\text{-}parser} \ -> \\ & (\{context: Proof.context, source: Token.src, state: Toplevel.state\} \ -> 'a \ -> string) \ -> \\ & theory \ -> theory; \\ & Thy\text{-}Output.output: Proof.context} \ -> Pretty.T \ list \ -> string; \\ & Thy\text{-}Output.output-text: Toplevel.state} \ -> \{markdown: bool\} \ -> Input.source} \ -> string; \\ & Thy\text{-}Output.output: Proof.context} \ -> Pretty.T \ list \ -> string; \\ & \mathbf{ML} \langle \! \langle Syntax\text{-}Phases.reports\text{-}of\text{-}scope;} \rangle \! \rangle \end{split}
```

 $\mathbf{ML} \langle \! \langle$

```
(* interesting piece for LaTeX Generation:
fun\ verbatim\text{-}text\ ctxt\ =
 if Config.get ctxt display then
   split-lines #> map (prefix (Symbol.spaces (Config.get ctxt indent))) #> cat-lines #>
   Latex.output-ascii \#> Latex.environment is abellett
 else
   split-lines #>
   map\ (Latex.output-ascii\ \#>\ enclose\ \setminus isatt\{\ \})\ \#>
   space-implode \setminus isasep \setminus isanewline \% \setminus n;
(* From structure Thy-Output *)
fun\ pretty\text{-}const\ ctxt\ c =
 let
   val\ t = Const\ (c,\ Consts.type\text{-}scheme\ (Proof\text{-}Context.consts\text{-}of\ ctxt)\ c)
     handle\ TYPE\ (msg,\ \text{-},\ \text{-}) => error\ msg;
   val([t'], -) = Variable.import-terms true[t] ctxt;
 in pretty-term ctxt t' end;
 basic-entity @\{binding\ const\}\ (Args.const\ \{proper=true,\ strict=false\})\ pretty-const\ \#>
*)
Pretty.enclose: string -> string -> Pretty.T list -> Pretty.T; (* not to confuse with: String.enclose *)
(* At times, checks where attached to Pretty – functions and exceptions used to
  stop the execution/validation of a command *)
fun pretty-theory ctxt (name, pos) = (Theory.check ctxt (name, pos); Pretty.str name);
Pretty.enclose;
Pretty.str;
Pretty.mark-str;
Pretty.text\ bla-d;
Pretty.quote; (* Pretty.T transformation adding *)
Pretty.unformatted-string-of: Pretty.T \rightarrow string;
Latex.output-ascii;
Latex.environment is a bq;
Latex.output-ascii a-b:c'é;
(* Note: *)
space-implode sd \& e \ sf \ dfg \ [qs,er,alpa];
fun pretty-command (cmd \ as \ (name, \ Command \ \{comment, ...\})) =
 Pretty.block \\
   (Pretty.marks-str
     ([Active.make-markup\ Markup.sendbackN\ \{implicit=true,\ properties=[Markup.padding-line]\},
       command-markup false cmd], name) :: Pretty.str : :: Pretty.brk 2 :: Pretty.text comment);
*)
\rangle\rangle
\mathbf{ML} \langle \! \langle
Thy	ext{-}Output.output-text;
fun\ output-text state\ \{markdown\}\ source =
```

```
let
   val is-reported =
     (case try Toplevel.context-of state of
       SOME\ ctxt =>\ Context	ext{-}Position.is	ext{-}visible\ ctxt
     | NONE = > true |;
   val pos = Input.pos-of source;
   val\ syms = Input.source-explode\ source;
   val - =
     if is-reported then
       Position.report pos (Markup.language-document (Input.is-delimited source))
     else();
   val\ output-antiquotes = map\ (eval-antiquote state)\ \#>\ implode;
   fun output-line line =
     (if Markdown.line-is-item line then \\item \else\) ^
       output-antiquotes (Markdown.line-content line);
   fun\ output-blocks blocks = space-implode \n\n\ (map\ output-block blocks)
   and output-block (Markdown.Par lines) = cat-lines (map output-line lines)
     | output\text{-}block (Markdown.List \{kind, body, ...\}) =
        Latex.environment\ (Markdown.print-kind\ kind)\ (output-blocks\ body);
 in
   if Toplevel.is-skipped-proof state then
   else if markdown andalso exists (Markdown.is-control o Symbol-Pos.symbol) syms
     let
       val \ ants = Antiquote.parse \ pos \ syms;
       val\ reports = Antiquote.antiq-reports\ ants;
       val\ blocks = Markdown.read-antiquotes\ ants;
       val - = if is-reported then Position.reports (reports @ Markdown.reports blocks) else ();
     in output-blocks blocks end
   else
     let
       val\ ants = Antiquote.parse\ pos\ (Symbol-Pos.trim-blanks\ syms);
       val\ reports = Antiquote.antiq-reports\ ants;
       val - = if is-reported then Position.reports (reports @ Markdown.text-reports ants) else ();
     in output-antiquotes ants end
 end;
*)
\rangle\!\rangle
\mathbf{ML} \langle \! \langle
Outer-Syntax.print-commands @{theory};
Outer	ext{-}Syntax.command : Outer	ext{-}Syntax.command	ext{-}keyword -> string ->
                       (Toplevel.transition \rightarrow Toplevel.transition) parser \rightarrow unit;
(* creates an implicit thy-setup with an entry for a call-back function, which happens
  to be a parser that must have as side-effect a Toplevel-transition-transition.
  Registers Toplevel.transition -> Toplevel.transition parsers to the Isar interpreter.
  *)
(*Example: text is:
```

Even the parsers and type checkers stemming from the theory-structure are registered via hooks (this can be confusing at times). Main phases of inner syntax processing, with standard implementations of parse/unparse operations were treated this way. At the very very end in ~~/src/Pure/Syntax/syntax_phases.ML, it sets up the entire syntax engine (the hooks) via:

Thus, Syntax_Phases does the actual work, including markup generation and generation of reports. Look at:

 \mathbf{end}