
ACM TEMPLATE



ATM_osphere

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Contents

1 Datastructure

1.1 KD tree

```

1 bool Div[MaxN];
2 void BuildKD(int deep,int l, int r, Point p[]) {
3     if (l > r) return;
4     int mid = l + r >> 1;
5     int minX, minY, maxX, maxY;
6     minX = min_element(p + l, p + r + 1, cmpX)->x;
7     minY = min_element(p + l, p + r + 1, cmpY)->y;
8     maxX = max_element(p + l, p + r + 1, cmpX)->x;
9     maxY = max_element(p + l, p + r + 1, cmpY)->y;
10    Div[mid] = (maxX - minX >= maxY - minY);
11    nth_element(p + l, p + mid, p + r + 1, Div[mid] ? cmpX : cmpY);
12    BuildKD(l, mid - 1, p);
13    BuildKD(mid + 1, r, p);
14 }
15 long long res;
16 void Find(int l, int r, Point a, Point p[]) {
17     if (l > r) return;
18     int mid = l + r >> 1;
19     long long dist = dist2(a, p[mid]);
20     if (dist > 0)//NOTICE
21         res = min(res, dist);
22     long long d = Div[mid] ? (a.x - p[mid].x) : (a.y - p[mid].y);
23     int l1, l2, r1, r2;
24     l1 = l, l2 = mid + 1;
25     r1 = mid - 1, r2 = r;
26     if (d > 0)
27         swap(l1, l2), swap(r1, r2);
28     Find(l1, r1, a, p);
29     if (d * d < res)
30         Find(l2, r2, a, p);
31 }

```

1.2 Binary indexed tree

```

1 int read(int k) {
2     int sum = 0;
3     for (; k; k^=k&-k) sum+=tree[k];
4     return sum;
5 }
6 void update(int k, int v) {
7     for (; k<=MaxN; k+=k&-k) tree[k]+=v;
8 }
9 int find_Kth(int k) {
10    int idx = 0;
11    for(int i=20; i>=0; i--) {
12        idx |= 1 << i;
13        if(idx <= MaxN && tree[idx] < k)
14            k -= tree[idx];
15        else idx ^= 1 << i;
16    }
17    return idx + 1;
18 }

```

1.3 Splay

```

1 //Node
2 struct Node {

```

```

3   int size,key;
4   Node *c[2], *p;
5 } mem[MaxN], *cur, *nil;
6 //Initialize functions without memory pool
7 Node *newNode(int v, Node *p) {
8     cur->c[0] = cur->c[1] = nil, cur->p = p;
9     cur->size = 1;
10    cur->key = v;
11    return cur++;
12 }
13 void Init() {
14     cur = mem;
15     nil = newNode(0, cur);
16     nil->size = 0;
17 }
18 //Splay tree
19 struct SplayTree {
20     Node *root;
21     void Init() {
22         root = nil;
23     }
24     void Pushup(Node *x) {
25         if (x == nil) return;
26         Pushdown(x);
27         Pushdown(x->c[0]);
28         Pushdown(x->c[1]);
29         x->size = x->c[0]->size + x->c[1]->size + 1;
30     }
31     void Pushdown(Node *x) {
32         if (x == nil) return;
33         //do something
34     }
35     void Rotate(Node *x, int f) {
36         if (x == nil) return;
37         Node *y = x->p;
38         y->c[f ^ 1] = x->c[f], x->p = y->p;
39         if (x->c[f] != nil)
40             x->c[f]->p = y;
41         if (y->p != nil)
42             y->p->c[y->p->c[1] == y] = x;
43         x->c[f] = y, y->p = x;
44         Pushup(y);
45     }
46     void Splay(Node *x, Node *f) {
47         static Node *stack[maxn];
48         int top = 0;
49         stack[top++] = x;
50         for (Node *y = x; y != f; y = y->p)
51             stack[top++] = y->p;
52         while (top)
53             Pushdown(stack[--top]);
54         while (x->p != f) {
55             Node *y = x->p;
56             if (y->p == f)
57                 Rotate(x, x == y->c[0]);
58             else {
59                 int fd = y->p->c[0] == y;
60                 if (y->c[fd] == x)
61                     Rotate(x, fd ^ 1), Rotate(x, fd);
62                 else
63                     Rotate(y, fd), Rotate(x, fd);
64             }
65         }
66         Pushup(x);

```

```

67     if (f == nil)
68         root = x;
69 }
70 void Select(int k, Node *f) {
71     Node *x = root;
72     Pushdown(x);
73     int tmp;
74     while ((tmp = x->c[0]->size) != k) {
75         if (k < tmp) x = x->c[0];
76         else
77             x = x->c[1], k -= tmp + 1;
78         Pushdown(x);
79     }
80     Splay(x, f);
81 }
82 void Select(int l, int r) {
83     Select(l, nil), Select(r + 2, root);
84 }
85 Node *Make_tree(int a[], int l, int r, Node *p) {
86     if (l > r) return nil;
87     int mid = l + r >> 1;
88     Node *x = newNode(a[mid], p);
89     x->c[0] = Make_tree(a, l, mid - 1, x);
90     x->c[1] = Make_tree(a, mid + 1, r, x);
91     Pushup(x);
92     return x;
93 }
94 void Insert(int pos, int a[], int n) {
95     Select(pos, nil), Select(pos + 1, root);
96     root->c[1]->c[0] = Make_tree(a, 0, n - 1, root->c[1]);
97     Splay(root->c[1]->c[0], nil);
98 }
99 void Insert(int v) {
100     Node *x = root, *y = nil;
101     //Need pushdown
102     while (x != nil) {
103         y = x;
104         y->size++;
105         x = x->c[v >= x->key];
106     }
107     y->c[v >= y->key] = x = newNode(v, y);
108     Splay(x, nil);
109 }
110 void Remove(int l, int r) {
111     Select(l, r);
112     //Recycle(root->c[1]->c[0]);
113     root->c[1]->c[0] = nil;
114     Splay(root->c[1], nil);
115 }
116 };

```

1.4 Dynamic tree

```

1 struct SplayTree {
2     void Pushup(Node *x) {
3         if (x == nil) return;
4         Pushdown(x);
5         Pushdown(x->c[0]);
6         Pushdown(x->c[1]);
7         x->size = x->c[0]->size + x->c[1]->size + 1;
8     }
9     void Pushdown(Node *x) {
10        if (x == nil) return;

```

```

11     if (x->rev) {
12         x->rev = 0;
13         x->c[0]->rev ^= 1;
14         x->c[1]->rev ^= 1;
15         swap(x->c[0], x->c[1]);
16     }
17 }
18 bool isRoot(Node *x) {
19     return (x == nil) || (x->p->c[0] != x && x->p->c[1] != x);
20 }
21 void Rotate(Node *x, int f) {
22     if (isRoot(x)) return;
23     Node *y = x->p;
24     y->c[f ^ 1] = x->c[f], x->p = y->p;
25     if (x->c[f] != nil)
26         x->c[f]->p = y;
27     if (y != nil) {
28         if (y == y->p->c[1])
29             y->p->c[1] = x;
30         else if (y == y->p->c[0])
31             y->p->c[0] = x;
32     }
33     x->c[f] = y, y->p = x;
34     Pushup(y);
35 }
36 void Splay(Node *x) {
37     static Node *stack[MaxN];
38     int top = 0;
39     stack[top++] = x;
40     for (Node *y = x; !isRoot(y); y = y->p)
41         stack[top++] = y->p;
42     while (top)
43         Pushdown(stack[--top]);
44     while (!isRoot(x)) {
45         Node *y = x->p;
46         if (isRoot(y))
47             Rotate(x, x == y->c[0]);
48         else {
49             int fd = y->p->c[0] == y;
50             if (y->c[fd] == x)
51                 Rotate(x, fd ^ 1), Rotate(x, fd);
52             else
53                 Rotate(y, fd), Rotate(x, fd);
54         }
55     }
56     Pushup(x);
57 }
58 Node *Access(Node *u) {
59     Node *v = nil;
60     while (u != nil) {
61         Splay(u);
62         v->p = u;
63         u->c[1] = v;
64         Pushup(u);
65         u = (v = u)->p;
66         if (u == nil)
67             return v;
68     }
69 }
70 Node *LCA(Node *u, Node *v) {
71     Access(u);
72     return Access(v);
73 }
74 Node *Link(Node *u, Node *v) {

```

```

75     Access(u);
76     Splay(u);
77     u->rev = true;
78     u->p = v;
79 }
80 void ChangeRoot(Node *u) {
81     Access(u)->rev ^= 1;
82 }
83 Node *GetRoute(Node *u, Node *v) {
84     ChangeRoot(u);
85     return Access(v);
86 }
87 };

```

1.5 Partition tree

```

1  int n,m;
2  struct elem {
3      int v,index;
4  } a[120000];
5  int d[30][120000];
6  int s[30][120000];
7  bool cmp(elem a,elem b) {
8      if (a.v == b.v)
9          return a.index <= b.index;
10     return a.v < b.v;
11 }
12 void build(int depth,int l,int r) {
13     if (l == r)
14         return;
15     int mid = (l+r)/2;
16     int tl,tr;
17     tl = tr = 0;
18     for (int i = l; i <= r; i++) {
19         if (cmp(a[d[depth][i]],a[mid])) {
20             d[depth+1][l+tl] = d[depth][i];
21             tl++;
22         } else {
23             d[depth+1][mid+1+tr] = d[depth][i];
24             tr++;
25         }
26         s[depth][i] = tl;
27     }
28     build(depth+1,l,mid);
29     build(depth+1,mid+1,r);
30 }
31 int find(int depth,int dl,int dr,int fl,int fr,int k) {
32     if (fl == fr)
33         return a[d[depth][fl]].v;
34     int ls,rs;
35     int mid = (dl+dr)/2;
36     ls = (fl == dl)? 0 : s[depth][fl-1];
37     rs = s[depth][fr];
38     return (rs-ls < k)?
39         find(depth+1,mid+1,dr,mid+fl-dl-ls+1,mid+fr-dl-rs+1,k-(rs-ls))
40         : find(depth+1,dl,mid,dl+ls,dl+rs-1,k);
41 }
42 int main() {
43     while (scanf("%d%d",&n,&m) != EOF) {
44         for (int i = 1; i <= n; i++) {
45             scanf("%d",&a[i].v);
46             a[i].index = i;
47         }

```

```

48     sort(a+1,a+n+1,cmp);
49     for (int i = 1; i <= n; i++)
50         d[0][a[i].index] = i;
51     build(0,1,n);
52     int l,r,k;
53     for (int i = 1; i <= m; i++) {
54         scanf("%d%d%d",&l,&r,&k);
55         printf("%d\n",find(0,1,n,l,r,k));
56     }
57 }
58 return 0;
59 }

```

2 Dynamic programming

2.1 RMQ

```

1 void init() {
2     int i,j;
3     int n=N,k=1,l=0;
4     for (i=0; i<n; i++) {
5         f[i][0]=ele[i].num;
6         if (i+1>k*2) {
7             k*=2;
8             l++;
9         }
10        lent[i+1]=l;
11    }
12    for (j=1; (1<<j)-1<n; j++)
13        for (i=0; i+(1<<j)-1<n; i++)
14            f[i][j]=max(f[i][j-1],f[i+(1<<(j-1))][j-1]);
15 }
16 int fint(int x,int y) {
17     int k=lent[y-x+1];
18     return max(f[x][k],f[y-(1<<k)+1][k]);
19 }

```

2.2 2D-LIS

```

1 #include<cstdio>
2 #include<map>
3 using namespace std;
4 map<int,int> mp[100001];
5 bool check(int idx,int x,int y) {
6     if (!idx) return 1;
7     if (mp[idx].begin()->first>=x) return 0;
8     map<int,int> ::iterator it=mp[idx].lower_bound(x);
9     it--;
10    if (it->second<y) return 1;
11    else return 0;
12 }
13 int main() {
14     int n;
15     scanf("%d",&n);
16     int l=0,r=0;
17     for (int i=0; i<n; i++) {
18         int x,y;
19         scanf("%d%d",&x,&y);
20         int tl=l,tr=r;
21         while (tl<tr) {
22             int mid=(tl+tr+1)/2;

```



```

23     if (check(mid,x,y))
24         tl=mid;
25     else
26         tr=mid-1;
27 }
28 if (tl==r) r++;
29 int idx=tl+1;
30 map<int,int> ::iterator itl=mp[idx].lower_bound(x),itr=itl;
31 while (itr!=mp[idx].end() && itr->second>y) itr++;
32 if (mp[idx].find(x)!=mp[idx].end())
33     y=min(y,mp[idx][x]);
34 if (itl!=itr) mp[idx].erase(itl,itr);
35 if (mp[idx].find(x)==mp[idx].end() || mp[idx][x]>y)
36     mp[idx][x]=y;
37 }
38 printf("%d\n",r);
39 return 0;
40 }

```

3 Geometry

3.1 2D

3.1.1 Point

```

1 //Use cross product instead of atan2
2 bool cmp(const Point& a,const Point& b) {
3     if (a.y*b.y <= 0) {
4         if (a.y > 0 || b.y > 0) return a.y < b.y;
5         if (a.y == 0 && b.y == 0) return a.x < b.x;
6     }
7     return a*b > 0;
8 }

```

3.1.2 Line

```

1 Point operator &(const Line& b) const {
2     Point res = s;
3     double t = ((s - b.s) * (b.s - b.e)) / ((s - e) * (b.s - b.e));
4     res.x += (e.x - s.x) * t;
5     res.y += (e.y - s.y) * t;
6     return res;
7 }

```

3.1.3 Functions

```

1 Point nearestPointToLine(Point P, Line L) {
2     Point result;
3     double a, b, t;
4     a = L.e.x-L.s.x;
5     b = L.e.y-L.s.y;
6     t = ( (P.x-L.s.x)*a+(P.y-L.s.y)*b )/(a*a+b*b);
7     if (t >= 0 && t <= 1) {
8         result.x = L.s.x+a*t;
9         result.y = L.s.y+b*t;
10    }
11    return result;
12 }
13 //Segment
14 bool inter(Line l1,Line l2) {

```

```

15  return
16      max(l1.s.x,l1.e.x) >= min(l2.s.x,l2.e.x) &&
17      max(l2.s.x,l2.e.x) >= min(l1.s.x,l1.e.x) &&
18      max(l1.s.y,l1.e.y) >= min(l2.s.y,l2.e.y) &&
19      max(l2.s.y,l2.e.y) >= min(l1.s.y,l1.e.y) &&
20      sgn((l2.s-l1.s)*(l1.e-l1.s))*sgn((l2.e-l1.s)*(l1.e-l1.s)) <= 0 &&
21      sgn((l1.s-l2.s)*(l2.e-l2.s))*sgn((l1.e-l2.s)*(l2.e-l2.s)) <= 0;
22  }
23  bool onSeg(Line a,Point b) {
24      return ((a.s-b)*(a.e-b) == 0 &&
25          (b.x-a.s.x)*(b.x-a.e.x) <= 0 &&
26          (b.y-a.s.y)*(b.y-a.e.y) <= 0);
27  }
28  int inPoly(Point p,Point poly[], int n) {
29      int i, count;
30      Line ray, side;
31      count = 0;
32      ray.s = p;
33      ray.e.y = p.y;
34      ray.e.x = -1;//-∞
35      for (i = 0; i < n; i++) {
36          side.s = poly[i];
37          side.e = poly[(i+1)%n];
38          if(OnSeg(p, side))
39              return 1;
40          if (side.s.y == side.e.y)
41              continue;
42          if (OnSeg(side.s, ray)) {
43              if (side.s.y > side.e.y) count++;
44          } else if (OnSeg(side.e, ray)) {
45              if (side.e.y > side.s.y) count++;
46          } else if (inter(ray, side)) {
47              count++;
48          }
49      }
50      return ((count % 2 == 1) ? 0 : 2);
51  }
52  Point centerOfPolygon(Point poly[],int n) {
53      Point p, p0, p1, p2, p3;
54      double m, m0;
55      p1 = poly[0];
56      p2 = poly[1];
57      p.x = p.y = m = 0;
58      for (int i = 2; i < n; i++) {
59          p3 = poly[i];
60          p0.x = (p1.x + p2.x + p3.x) / 3.0;
61          p0.y = (p1.y + p2.y + p3.y) / 3.0;
62          m0 = p1.x*p2.y+p2.x*p3.y+p3.x*p1.y-p1.y*p2.x-p2.y*p3.x-p3.y*p1.x;
63          if (cmp(m + m0,0.0) == 0)
64              m0 += eps;
65          p.x = (m * p.x + m0 * p0.x) / (m + m0);
66          p.y = (m * p.y + m0 * p0.y) / (m + m0);
67          m = m + m0;
68          p2 = p3;
69      }
70      return p;
71  }

```

3.1.4 Half plane intersection

```

1  bool HPICmp(Line a, Line b) {
2      if (fabs(a.k - b.k) > EPS) return a.k < b.k;
3      return ((a.s - b.s) * (b.e - b.s)) < 0;

```

```

4 }
5 Line Q[MAXN];
6 void HPI(Line line[], int n, Point res[], int &resn) {
7     int tot = n;
8     sort(line, line + n, HPIcmp);
9     tot = 1;
10    for (int i = 1; i < n; i++)
11        if (fabs(line[i].k - line[i - 1].k) > EPS)
12            line[tot++] = line[i];
13    int head = 0, tail = 1;
14    Q[0] = line[0];
15    Q[1] = line[1];
16    resn = 0;
17    for (int i = 2; i < tot; i++) {
18        if (fabs((Q[tail].e - Q[tail].s) * (Q[tail - 1].e - Q[tail - 1].s)) < EPS ||
19            fabs((Q[head].e - Q[head].s) * (Q[head + 1].e - Q[head + 1].s)) < EPS)
20            return;
21        while (head < tail && (((Q[tail] & Q[tail - 1]) - line[i].s) * (line[i].e - line[
22            i].s)) > EPS)
23            tail--;
24        while (head < tail && (((Q[head] & Q[head + 1]) - line[i].s) * (line[i].e - line[
25            i].s)) > EPS)
26            head++;
27        Q[++tail] = line[i];
28    }
29    while (head < tail && (((Q[tail] & Q[tail - 1]) - Q[head].s) * (Q[head].e - Q[head
30        ].s)) > EPS)
31        tail--;
32    while (head < tail && (((Q[head] & Q[head + 1]) - Q[tail].s) * (Q[tail].e - Q[tail
33        ].s)) > EPS)
34        head++;
35    if (tail <= head + 1) return;
36    for (int i = head; i < tail; i++)
37        res[resn++] = Q[i] & Q[i + 1];
38    if (head < tail + 1)
39        res[resn++] = Q[head] & Q[tail];
40 }

```

3.1.5 Convex hull

```

1 bool GScmp(Point a, Point b) {
2     if (fabs(a.x - b.x) < eps)
3         return a.y < b.y - eps;
4     return a.x < b.x - eps;
5 }
6 void GS(Point p[], int n, Point res[], int &resn) {
7     resn = 0;
8     int top = 0;
9     sort(p, p+n, GScmp);
10    if (conPoint(p, n)) {
11        res[resn++] = p[0];
12        return;
13    }
14    if (conLine(p, n)) {
15        res[resn++] = p[0];
16        res[resn++] = p[n-1];
17        return;
18    }
19    for (int i = 0; i < n; i++)
20        if (resn < 2 ||
21            (res[resn-1]-res[resn-2])*(p[i]-res[resn-1]) > 0)
22            res[resn++] = p[i++];
23    else

```

```

24     --resn;
25     top = resn-1;
26     for (int i = n-2; i >= 0;)
27         if (resn < top+2 ||
28             (res[resn-1]-res[resn-2])*(p[i]-res[resn-1]) > 0)
29             res[resn++] = p[i--];
30         else
31             --resn;
32     resn--;
33 }

```

3.1.6 Intersections of line and polygon

```

1 //Intersecting segment between [la,lb]
2 int Gao(int la,int lb,Line line) {
3     if (la > lb)
4         lb += n;
5     int l = la,r = lb,mid;
6     while (l < r) {
7         mid = l+r+1>>1;
8         if (cmp((line.e-line.s)*(p[la]-line.s),0)*cmp((line.e-line.s)*(p[mid]-line.s),0)
9             >= 0)
10             l = mid;
11         else
12             r = mid-1;
13     }
14     return l%n;
15 }
16 double theta[maxn];
17 void Gettheta() {
18     for (int i = 0; i < n; i++) {
19         Point v = p[(i+1)%n]-p[i];
20         theta[i] = atan2(v.y,v.x);
21     }
22     for (int i = 1; i < n; i++)
23         if (theta[i-1] > theta[i]+eps)
24             theta[i] += 2*pi;
25 }
26 void Calc(Line l) {
27     double tnow;
28     Point v = l.e-l.s;
29     tnow = atan2(v.y,v.x);
30     if (cmp(tnow,theta[0]) < 0) tnow += 2*pi;
31     int pl = lower_bound(theta,theta+n,tnow)-theta;
32     tnow = atan2(-v.y,-v.x);
33     if (cmp(tnow,theta[0]) < 0) tnow += 2*pi;
34     int pr = lower_bound(theta,theta+n,tnow)-theta;
35     //Farest points with l on polygon
36     pl = pl%n;
37     pr = pr%n;
38     if (cmp(v*(p[pl]-l.s),0)*cmp(v*(p[pr]-l.s),0) >= 0)
39         return 0.0;
40     int xa = Gao(pl,pr,l);
41     int xb = Gao(pr,pl,l);
42     if (xa > xb) swap(xa,xb);
43     //Intersecting with line  $P_{xa} \rightarrow P_{xa+1}$  and  $P_{xb} \rightarrow P_{xb+1}$ 
44     if (cmp(v*(p[xa+1]-p[xa]),0) == 0) return 0.0;
45     if (cmp(v*(p[xb+1]-p[xb]),0) == 0) return 0.0;
46     Point pa,pb;
47     //Intersections
48     pa = Line(p[xa],p[xa+1])&l;
49     pb = Line(p[xb],p[xb+1])&l;
50 }

```

3.2 3D

3.2.1 Point

```

1 Point3D operator *(const Point3D& b) const {
2     return Point3D(y*b.z-z*b.y,z*b.x-x*b.z,x*b.y-y*b.x);
3 }
4 //Rotate around V, notice that |V|=1
5 Point3D Trans(Point3D pa,Point3D V,double theta) {
6     double s = sin(theta);
7     double c = cos(theta);
8     double x,y,z;
9     x = V.x;
10    y = V.y;
11    z = V.z;
12    Point3D pp =
13        Point3D(
14            (x*x*(1-c)+c)*pa.x+(x*y*(1-c)-z*s)*pa.y+(x*z*(1-c)+y*s)*pa.z,
15            (y*x*(1-c)+z*s)*pa.x+(y*y*(1-c)+c)*pa.y+(y*z*(1-c)-x*s)*pa.z,
16            (x*z*(1-c)-y*s)*pa.x+(y*z*(1-c)+x*s)*pa.y+(z*z*(1-c)+c)*pa.z);
17    return pp;
18 }

```

3.2.2 Functions

```

1 bool lineIntersect(Line3D L1, Line3D L2) {
2     Point3D s = L1.s-L1.e;
3     Point3D e = L2.s-L2.e;
4     Point3D p = s*e;
5     if (ZERO(p)) return false; //Parallel
6     p = (L2.s-L1.e)*(L1.s-L1.e);
7     return ZERO(p&L2.e); //Common face
8 }
9 //Please check whether a, b, c, d on a plane first
10 bool segmentIntersect(Point a,Point b,Point c,Point d) {
11     Point ret = (a-b)*(c-d);
12     Point t1 = (b-a)*(c-a);
13     Point t2 = (b-a)*(d-a);
14     Point t3 = (d-c)*(a-c);
15     Point t4 = (d-c)*(b-c);
16     return sgn(t1&ret)*sgn(t2&ret) < 0 &&
17         sgn(t3&ret)*sgn(t4&ret) < 0;
18 }
19 //Distance from point p to line L
20 double distance(Point3D p, Line3D L) {
21     return (Norm((p-L.s)*(L.e-L.s))/Norm(L.e-L.s));
22 }
23 //Angle between line L1 and L2,  $\theta \in [0, \pi]$ 
24 double calcTheta(Line3D L1, Line3D L2) {
25     Point3D u = L1.e - L1.s;
26     Point3D v = L2.e - L2.s;
27     return acos( (u & v) / (Norm(u)*Norm(v)) );
28 }

```

3.2.3 Convex hull

Don't forget Randomshuffle!

```

1 struct pt {
2     double x, y, z;
3     pt() {}
4     pt(double _x, double _y, double _z): x(_x), y(_y), z(_z) {}

```

```

5  pt operator - (const pt p1) {}
6  pt operator * (pt p) {}
7  double operator ^ (pt p) {}
8  };
9  struct _3DCH {
10     struct fac {
11         int a, b, c;
12         bool ok;
13     };
14     int n;
15     pt P[MAXV];
16     int cnt;
17     fac F[MAXV*8];
18     int to[MAXV][MAXV];
19     double vlen(pt a) {
20         return sqrt(a.x*a.x+a.y*a.y+a.z*a.z);
21     }
22     double area(pt a, pt b, pt c) {
23         return vlen((b-a)*(c-a));
24     }
25     double volume(pt a, pt b, pt c, pt d) {
26         return (b-a)*(c-a)^(d-a);
27     }
28     double ptof(pt &p, fac &f) {
29         pt m = P[f.b]-P[f.a], n = P[f.c]-P[f.a], t = p-P[f.a];
30         return (m * n) ^ t;
31     }
32     void deal(int p, int a, int b) {
33         int f = to[a][b];
34         fac add;
35         if (F[f].ok) {
36             if (ptof(P[p], F[f]) > eps)
37                 dfs(p, f);
38             else {
39                 add.a = b, add.b = a, add.c = p, add.ok = 1;
40                 to[p][b] = to[a][p] = to[b][a] = cnt;
41                 F[cnt++] = add;
42             }
43         }
44     }
45     void dfs(int p, int cur) {
46         F[cur].ok = 0;
47         deal(p, F[cur].b, F[cur].a);
48         deal(p, F[cur].c, F[cur].b);
49         deal(p, F[cur].a, F[cur].c);
50     }
51     bool same(int s, int t) {
52         pt &a = P[F[s].a], &b = P[F[s].b], &c = P[F[s].c];
53         return fabs(volume(a, b, c, P[F[t].a])) < eps && fabs(volume(a, b, c,
54             P[F[t].b])) < eps && fabs(volume(a, b, c, P[F[t].c])) < eps;
55     }
56     void construct() {
57         cnt = 0;
58         if (n < 4)
59             return;
60         bool sb = 1;
61         for (int i = 1; i < n; i++) {
62             if (vlen(P[0] - P[i]) > eps) {
63                 swap(P[1], P[i]);
64                 sb = 0;
65                 break;
66             }
67         }
68         if (sb) return;

```

```

69     sb = 1;
70     for (int i = 2; i < n; i++) {
71         if (vlen((P[0] - P[1]) * (P[1] - P[i])) > eps) {
72             swap(P[2], P[i]);
73             sb = 0;
74             break;
75         }
76     }
77     if (sb) return;
78     sb = 1;
79     for (int i = 3; i < n; i++) {
80         if (fabs((P[0] - P[1]) * (P[1] - P[2]) ^ (P[0] - P[i])) > eps) {
81             swap(P[3], P[i]);
82             sb = 0;
83             break;
84         }
85     }
86     if (sb) return;
87     fac add;
88     for (int i = 0; i < 4; i++) {
89         add.a = (i+1)%4, add.b = (i+2)%4, add.c = (i+3)%4, add.ok = 1;
90         if (ptof(P[i], add) > 0)
91             swap(add.b, add.c);
92         to[add.a][add.b] = to[add.b][add.c] = to[add.c][add.a] = cnt;
93         F[cnt++] = add;
94     }
95     for (int i = 4; i < n; i++) {
96         for (int j = 0; j < cnt; j++) {
97             if (F[j].ok && ptof(P[i], F[j]) > eps) {
98                 dfs(i, j);
99                 break;
100             }
101         }
102     }
103     int tmp = cnt;
104     cnt = 0;
105     for (int i = 0; i < tmp; i++) {
106         if (F[i].ok) {
107             F[cnt++] = F[i];
108         }
109     }
110 }
111 double area() {
112     double ret = 0.0;
113     for (int i = 0; i < cnt; i++) {
114         ret += area(P[F[i].a], P[F[i].b], P[F[i].c]);
115     }
116     return ret / 2.0;
117 }
118 double volume() {
119     pt O(0, 0, 0);
120     double ret = 0.0;
121     for (int i = 0; i < cnt; i++) {
122         ret += volume(O, P[F[i].a], P[F[i].b], P[F[i].c]);
123     }
124     return fabs(ret / 6.0);
125 }
126 int facetCnt_tri() {
127     return cnt;
128 }
129 int facetCnt() {
130     int ans = 0;
131     for (int i = 0; i < cnt; i++) {
132         bool nb = 1;

```

```

133     for (int j = 0; j < i; j++) {
134         if (same(i, j)) {
135             nb = 0;
136             break;
137         }
138     }
139     ans += nb;
140 }
141 return ans;
142 }
143 pt Fc[MAXV*8];
144 double V[MAXV*8];
145 pt Center() {
146     pt O(0,0,0);
147     for (int i = 0; i < cnt; i++) {
148         Fc[i].x = (O.x+P[F[i].a].x+P[F[i].b].x+P[F[i].c].x)/4.0;
149         Fc[i].y = (O.y+P[F[i].a].y+P[F[i].b].y+P[F[i].c].y)/4.0;
150         Fc[i].z = (O.z+P[F[i].a].z+P[F[i].b].z+P[F[i].c].z)/4.0;
151         V[i] = volume(O,P[F[i].a],P[F[i].b],P[F[i].c]);
152     }
153     pt res = Fc[0],tmp;
154     double m = V[0];
155     for (int i = 1; i < cnt; i++) {
156         if (fabs(m+V[i]) < eps)
157             V[i] += eps;
158         tmp.x = (m*res.x+V[i]*Fc[i].x)/(m+V[i]);
159         tmp.y = (m*res.y+V[i]*Fc[i].y)/(m+V[i]);
160         tmp.z = (m*res.z+V[i]*Fc[i].z)/(m+V[i]);
161         m += V[i];
162         res = tmp;
163     }
164     return res;
165 }
166 };

```

3.3 Circle

3.3.1 Functions

```

1 //Common area of two circle
2 double area(int x1,int y1,int x2,int y2,double r1,double r2) {
3     double s=dis(x2-x1,y2-y1);
4     if(r1+r2<s) return 0;
5     else if(r2-r1>s) return PI*r1*r1;
6     else if(r1-r2>s) return PI*r2*r2;
7     double q1=acos((r1*r1+s*s-r2*r2)/(2*r1*s));
8     double q2=acos((r2*r2+s*s-r1*r1)/(2*r2*s));
9     return (r1*r1*q1+r2*r2*q2-r1*s*sin(q1));
10 }

```

3.3.2 Union

```

1 for (int i = 1; i <= n; i++)
2     ans[i] = 0.0;
3 for (int i = 0; i < n; i++) {
4     tote = 0;
5     e[tote++] = Event(-pi,1);
6     e[tote++] = Event(pi,-1);
7     for (int j = 0; j < n; j++)
8         if (j != i) {
9             lab = Point(c[j].c.x-c[i].c.x,c[j].c.y-c[i].c.y);
10            AB = lab.Length();

```



```

11     AC = c[i].r;
12     BC = c[j].r;
13     if (cmp(AB+AC,BC) <= 0) {
14         e[tote++] = Event(-pi,1);
15         e[tote++] = Event(pi,-1);
16         continue;
17     }
18     if (cmp(AB+BC,AC) <= 0) continue;
19     if (cmp(AB,AC+BC) > 0) continue;
20     theta = atan2(lab.y,lab.x);
21     fai = acos((AC*AC+AB*AB-BC*BC)/(2.0*AC*AB));
22     a0 = theta-fai;
23     if (cmp(a0,-pi) < 0) a0 += 2*pi;
24     a1 = theta+fai;
25     if (cmp(a1,pi) > 0) a1 -= 2*pi;
26     if (cmp(a0,a1) > 0) {
27         e[tote++] = Event(a0,1);
28         e[tote++] = Event(pi,-1);
29         e[tote++] = Event(-pi,1);
30         e[tote++] = Event(a1,-1);
31     } else {
32         e[tote++] = Event(a0,1);
33         e[tote++] = Event(a1,-1);
34     }
35 }
36 sort(e,e+tote,Eventcmp);
37 cur = 0;
38 for (int j = 0; j < tote; j++) {
39     if (cur != 0 && cmp(e[j].tim,pre[cur]) != 0) {
40         ans[cur] += Area(e[j].tim-pre[cur],c[i].r);
41         ans[cur] += xmult(Point(c[i].c.x+c[i].r*cos(pre[cur]),c[i].c.y+c[i].r*sin(pre[
42             cur])),
43             Point(c[i].c.x+c[i].r*cos(e[j].tim),c[i].c.y+c[i].r*sin(e[j].
44                 tim)))/2.0;
45     }
46     cur += e[j].typ;
47     pre[cur] = e[j].tim;
48 }
49 for (int i = 1; i < n; i++)
50     ans[i] -= ans[i+1];

```

3.3.3 Area of intersection part with polygon

```

1 bool InCircle(Point a,double r) {
2     return cmp(a.x*a.x+a.y*a.y,r*r) <= 0;
3     //ε should big enough
4 }
5 double CalcArea(Point a,Point b,double r) {
6     Point p[4];
7     int tot = 0;
8     p[tot++] = a;
9     Point tv = Point(a,b);
10    Line tmp = Line(Point(0,0),Point(tv.y,-tv.x));
11    Point near = LineToLine(Line(a,b),tmp);
12    if (cmp(near.x*near.x+near.y*near.y,r*r) <= 0) {
13        double A,B,C;
14        A = near.x*near.x+near.y*near.y;
15        C = r;
16        B = C*C-A;
17        double tvl = tv.x*tv.x+tv.y*tv.y;
18        double tmp = sqrt(B/tvl);
19        p[tot] = Point(near.x+tmp*tv.x,near.y+tmp*tv.y);

```

```

20     if (OnSeg(Line(a,b),p[tot]) == true) tot++;
21     p[tot] = Point(near.x-tmp*tv.x,near.y-tmp*tv.y);
22     if (OnSeg(Line(a,b),p[tot]) == true) tot++;
23 }
24 if (tot == 3) {
25     if (cmp(Point(p[0],p[1]).Length(),Point(p[0],p[2]).Length()) > 0)
26         swap(p[1],p[2]);
27 }
28 p[tot++] = b;
29 double res = 0.0,theta,a0,a1,sgn;
30 for (int i = 0; i < tot-1; i++) {
31     if (InCircle(p[i],r) == true && InCircle(p[i+1],r) == true) {
32         res += 0.5*xmult(p[i],p[i+1]);
33     } else {
34         a0 = atan2(p[i+1].y,p[i+1].x);
35         a1 = atan2(p[i].y,p[i].x);
36         if (a0 < a1) a0 += 2*pi;
37         theta = a0-a1;
38         if (cmp(theta,pi) >= 0) theta = 2*pi-theta;
39         sgn = xmult(p[i],p[i+1])/2.0;
40         if (cmp(sgn,0) < 0) theta = -theta;
41         res += 0.5*r*r*theta;
42     }
43 }
44 return res;
45 }
46 area2 = 0.0;
47 for (int i = 0; i < resn; i++) //counterclockwise
48     area2 += CalcArea(p[i],p[(i+1)%resn],r);

```

3.4 Matrix

3.4.1 基本矩阵

按向量 $\overrightarrow{(x,y,z)}$ 平移:

$$\begin{pmatrix} 1 & 0 & 0 & x \\ 0 & 1 & 0 & y \\ 0 & 0 & 1 & z \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

按比例 (x,y,z) 缩放:

$$\begin{pmatrix} x & 0 & 0 & 0 \\ 0 & y & 0 & 0 \\ 0 & 0 & z & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

绕单位向量 $\overrightarrow{(x,y,z)}$ 旋转 $angle$ 角度:

$$\begin{pmatrix} x^2 \times (1-c) + c & x \times y \times (1-c) - z \times s & x \times z \times (1-c) + y \times s & 0 \\ y \times x \times (1-c) + z \times s & y^2 \times (1-c) + c & y \times z \times (1-c) - x \times s & 0 \\ x \times z \times (1-c) - y \times s & y \times z \times (1-c) + x \times s & z^2 \times (1-c) + c & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{cases} s = \sin(angle) \\ c = \cos(angle) \end{cases}$$

以上矩阵变换都把点当作列向量, 旋转角度的正负由右手定则决定

4 Graph

4.1 Sap

```

1  const int MAXEDGE=50000;
2  const int MAXN=3000;
3  const int inf=0x3fffffff;
4  struct edges {
5      int cap,to,next,flow;
6  } edge[MAXEDGE+100];
7  struct nodes {
8      int head,label,pre,cur;
9  } node[MAXN+100];
10 int L,N;
11 int gap[MAXN+100];
12 void init(int n) {
13     L=0;
14     N=n;
15     for (int i=0; i<N; i++)
16         node[i].head=-1;
17 }
18 void add_edge(int x,int y,int z,int w) {
19     edge[L].cap=z;
20     edge[L].flow=0;
21     edge[L].to=y;
22     edge[L].next=node[x].head;
23     node[x].head=L++;
24     edge[L].cap=w;
25     edge[L].flow=0;
26     edge[L].to=x;
27     edge[L].next=node[y].head;
28     node[y].head=L++;
29 }
30 int maxflow(int s,int t) {
31     memset(gap,0,sizeof(gap));
32     gap[0]=N;
33     int u,ans=0;
34     for (int i=0; i<N; i++) {
35         node[i].cur=node[i].head;
36         node[i].label=0;
37     }
38     u=s;
39     node[u].pre=-1;
40     while (node[s].label<N) {
41         if (u==t) {
42             int min=inf;
43             for (int i=node[u].pre; i!=-1; i=node[edge[i^1].to].pre)
44                 if (min>edge[i].cap-edge[i].flow)
45                     min=edge[i].cap-edge[i].flow;
46             for (int i=node[u].pre; i!=-1; i=node[edge[i^1].to].pre) {
47                 edge[i].flow+=min;
48                 edge[i^1].flow-=min;
49             }
50             u=s;
51             ans+=min;
52             continue;
53         }
54         bool flag=false;
55         int v;
56         for (int i=node[u].cur; i!=-1; i=edge[i].next) {
57             v=edge[i].to;
58             if (edge[i].cap-edge[i].flow &&
59                 node[v].label+1==node[u].label) {

```

```

60     flag=true;
61     node[u].cur=node[v].pre=i;
62     break;
63 }
64 }
65 if (flag) {
66     u=v;
67     continue;
68 }
69 node[u].cur=node[u].head;
70 int min=N;
71 for (int i=node[u].head; i!=-1; i=edge[i].next)
72     if (edge[i].cap-edge[i].flow && node[edge[i].to].label<min)
73         min=node[edge[i].to].label;
74 gap[node[u].label]--;
75 if (!gap[node[u].label]) return ans;
76 node[u].label=min+1;
77 gap[node[u].label]++;
78 if (u!=s) u=edge[node[u].pre^1].to;
79 }
80 return ans;
81 }

```

4.2 Minimal cost maximal flow

```

1 //Use stack instead of queue when get TLE
2 int L,N;
3 int K;
4 struct edges {
5     int to,next,cap,flow,cost;
6 } edge[MAXM];
7 struct nodes {
8     int dis,pre,head;
9     bool visit;
10 } node[MAXN];
11 void init(int n) {
12     N=n;
13     L=0;
14     for (int i=0; i<N; i++)
15         node[i].head=-1;
16 }
17 void add_edge(int x,int y,int cap,int cost) {
18     edge[L].to=y;
19     edge[L].cap=cap;
20     edge[L].cost=cost;
21     edge[L].flow=0;
22     edge[L].next=node[x].head;
23     node[x].head=L++;
24     edge[L].to=x;
25     edge[L].cap=0;
26     edge[L].cost=-cost;
27     edge[L].flow=0;
28     edge[L].next=node[y].head;
29     node[y].head=L++;
30 }
31 bool spfa(int s,int t) {
32     queue<int> q;
33     for (int i=0; i<N; i++) {
34         node[i].dis=0x3fffffff;
35         node[i].pre=-1;
36         node[i].visit=0;
37     }
38     node[s].dis=0;

```

```

39 node[s].visit=1;
40 q.push(s);
41 while (!q.empty()) {
42     int u=q.front();
43     node[u].visit=0;
44     for (int i=node[u].head; i!=-1; i=edge[i].next) {
45         int v=edge[i].to;
46         if (edge[i].cap>edge[i].flow &&
47             node[v].dis>node[u].dis+edge[i].cost) {
48             node[v].dis=node[u].dis+edge[i].cost;
49             node[v].pre=i;
50             if (!node[v].visit) {
51                 node[v].visit=1;
52                 q.push(v);
53             }
54         }
55     }
56     q.pop();
57 }
58 if (node[t].pre==-1)
59     return 0;
60 else
61     return 1;
62 }
63 int mcmf(int s,int t,int &cost) {
64     int flow=0;
65     while (spfa(s,t)) {
66         int max=inf;
67         for (int i=node[t].pre; i!=-1; i=node[edge[i^1].to].pre) {
68             if (max>edge[i].cap-edge[i].flow)
69                 max=edge[i].cap-edge[i].flow;
70         }
71         for (int i=node[t].pre; i!=-1; i=node[edge[i^1].to].pre) {
72             edge[i].flow+=max;
73             edge[i^1].flow-=max;
74             cost+=edge[i].cost*max;
75         }
76         flow+=max;
77     }
78     return flow;
79 }

```

4.3 Johnson Minimal cost flow

```

1 #include <cstdio>
2 #include <cstring>
3 #include <algorithm>
4 #include <queue>
5 #include <stack>
6 using namespace std;
7 const int MAXN = 2003;
8 const int MAXM = 2000 * 1999 / 2 + 2000 * 3;
9 int N, L;
10 int head[MAXN];
11 struct Edge {
12     int to, next, flow, cost;
13 } edge[MAXM * 2];
14 int h[MAXN], dis[MAXN], pre[MAXN];
15 struct Heap {
16     int value[MAXN + 1], id[MAXN + 1];
17     int pos[MAXN];
18     int size;
19     void init() {

```

```

20     size = 1;
21 }
22 void swap2(int p, int q) {
23     swap(value[p], value[q]);
24     swap(id[p], id[q]);
25     pos[id[p]] = p;
26     pos[id[q]] = q;
27 }
28 void push_up(int p) {
29     while (p > 1 && value[p / 2] > value[p]) {
30         swap2(p, p / 2);
31         p /= 2;
32     }
33 }
34 void push_down(int p) {
35     while (p * 2 < size) {
36         int best = p;
37         if (p * 2 < size && value[p] > value[p * 2])
38             best = p * 2;
39         if (p * 2 + 1 < size && value[best] > value[p * 2 + 1])
40             best = p * 2 + 1;
41         if (p == best)
42             break;
43         swap2(p, best);
44         p = best;
45     }
46 }
47 void push(int _value, int _id) {
48     value[size] = _value;
49     id[size] = _id;
50     pos[_id] = size;
51     push_up(size++);
52 }
53 int top() {
54     return id[1];
55 }
56 void pop() {
57     value[1] = value[size - 1];
58     id[1] = id[--size];
59     pos[id[1]] = 1;
60     push_down(1);
61 }
62 void update(int _value, int _id) {
63     int p = pos[_id];
64     value[p] = _value;
65     push_up(p);
66 }
67 } heap;
68 bool inque[MAXN];
69 void init(int n) {
70     N = n;
71     L = 0;
72     memset(head, -1, 4 * n);
73 }
74 void add_edge(int u, int v, int flow, int cost) {
75     edge[L].to = v;
76     edge[L].flow = flow;
77     edge[L].cost = cost;
78     edge[L].next = head[u];
79     head[u] = L++;
80     edge[L].to = u;
81     edge[L].flow = 0;
82     edge[L].cost = -cost;
83     edge[L].next = head[v];

```

```

84     head[v] = L++;
85 }
86 void spfa(int s) {
87     memset(dis, 63, 4 * N);
88     memset(inque, 0, N);
89     memset(pre, -1, 4 * N);
90     dis[s] = 0;
91     queue<int> que;
92     que.push(s);
93     while (!que.empty()) {
94         int u = que.front();
95         inque[u] = 0;
96         que.pop();
97         for (int i = head[u]; i != -1; i = edge[i].next)
98             if (edge[i].flow) {
99                 int v = edge[i].to;
100                 if (dis[v] > dis[u] + edge[i].cost) {
101                     dis[v] = dis[u] + edge[i].cost;
102                     pre[v] = i;
103                     if (!inque[v]) {
104                         inque[v] = 1;
105                         que.push(v);
106                     }
107                 }
108             }
109     }
110 }
111 void dijkstra(int s) {
112     for (int i = 0; i < N; ++i)
113         h[i] += dis[i];
114     memset(dis, 63, 4 * N);
115     memset(pre, -1, 4 * N);
116     memset(inque, 0, N);
117     dis[s] = 0;
118     inque[s] = 1;
119     heap.init();
120     heap.push(0, s);
121     while (heap.size > 1) {
122         int u = heap.top();
123         heap.pop();
124         for (int i = head[u]; i != -1; i = edge[i].next)
125             if (edge[i].flow) {
126                 int v = edge[i].to;
127                 if (dis[v] > dis[u] + edge[i].cost + h[u] - h[v]) {
128                     dis[v] = dis[u] + edge[i].cost + h[u] - h[v];
129                     pre[v] = i;
130                     if (!inque[v]) {
131                         heap.push(dis[v], v);
132                         inque[v] = 1;
133                     } else
134                         heap.update(dis[v], v);
135                 }
136             }
137     }
138 }
139 int minimumCostFlow(int s, int t, int &cost) {
140     int flow = 0;
141     memset(h, 0, 4 * N);
142     for (spfa(s); pre[t] != -1; dijkstra(s)) {
143         int maxs = edge[pre[t]].flow;
144         for (int i = pre[t]; i != -1; i = pre[edge[i ^ 1].to])
145             maxs = min(maxs, edge[i].flow);
146         for (int i = pre[t]; i != -1; i = pre[edge[i ^ 1].to]) {
147             edge[i].flow -= maxs;

```

```

148     edge[i ^ 1].flow += maxs;
149     cost += edge[i].cost * maxs;
150 }
151     flow += maxs;
152 }
153     return flow;
154 }
155 int main() {
156     return 0;
157 }

```

4.4 Bi-connect

```

1 struct edges {
2     int to,next;
3     bool cut,visit;
4 } edge[MAXM<<1];
5 int head[MAXN],low[MAXN],dpt[MAXN],L;
6 bool visit[MAXN],cut[MAXN];
7 void init(int n) {
8     L=0;
9     memset(head,-1,4*n);
10    memset(visit,0,n);
11 }
12 void add_edge(int u,int v) {
13     edge[L].cut=edge[L].visit=0;
14     edge[L].to=v;
15     edge[L].next=head[u];
16     head[u]=L++;
17 }
18 int idx;
19 stack<int> st;
20 int bcc[MAXM];
21 void dfs(int u,int fu,int deg) {
22     cut[u]=0;
23     visit[u]=1;
24     low[u]=dpt[u]=deg;
25     int tot=0;
26     for (int i=head[u]; i!=-1; i=edge[i].next) {
27         int v=edge[i].to;
28         if (edge[i].visit)
29             continue;
30         st.push(i/2);
31         edge[i].visit=edge[i^1].visit=1;
32         if (visit[v]) {
33             low[u]=dpt[v]>low[u]?low[u]:dpt[v];
34             continue;
35         }
36         dfs(v,u,deg+1);
37         edge[i].cut=edge[i^1].cut=(low[v]>dpt[u] || edge[i].cut);
38         if (u!=fu) cut[u]=low[v]>=dpt[u]?1:cut[u];
39         if (low[v]>=dpt[u] || u==fu) {
40             while (st.top()!=i/2) {
41                 int x=st.top()*2,y=st.top()*2+1;
42                 bcc[st.top()]=idx;
43                 st.pop();
44             }
45             bcc[i/2]=idx++;
46             st.pop();
47         }
48         low[u]=low[v]>low[u]?low[u]:low[v];
49         tot++;
50     }

```



```

51     if (u==fu && tot>1) cut[u]=1;
52 }
53 int main() {
54     int n,m;
55     while (scanf("%d%d",&n,&m)!=EOF) {
56         init(n);
57         for (int i=0; i<m; i++) {
58             int u,v;
59             scanf("%d%d",&u,&v);
60             add_edge(u,v);
61             add_edge(v,u);
62         }
63         idx=0;
64         for (int i=0; i<n; i++)
65             if (!visit[i])
66                 dfs(i,i,0);
67     }
68     return 0;
69 }

```

4.5 Cut and bridge

```

1 struct edges {
2     int to,next;
3     bool cut,visit;
4     int from;
5 } edge[MAXN-1<<1];
6 int head[MAXN],low[MAXN],dfn[MAXN],L;
7 bool visit[MAXN],cut[MAXN];
8 void init(int n) {
9     L=0;
10    memset(head,-1,4*n);
11    memset(cut,0,4*n);
12    memset(visit,0,4*n);
13 }
14 void add_edge(int u,int v) {
15     edge[L].from=u;
16     edge[L].cut=edge[L].visit=0;
17     edge[L].to=v;
18     edge[L].next=head[u];
19     head[u]=L++;
20 }
21 int idx;
22 void dfs(int u,int fu) {
23     visit[u]=1;
24     low[u]=dfn[u]=idx++;
25     int tot=0;
26     for (int i=head[u]; i!=-1; i=edge[i].next) {
27         int v=edge[i].to;
28         if (edge[i].visit)
29             continue;
30         edge[i].visit=edge[i^1].visit=1;
31         if (visit[v]) {
32             low[u]=dfn[v]>low[u]?low[u]:dfn[v];
33             continue;
34         }
35         dfs(v,u);
36         edge[i].cut=edge[i^1].cut=low[v]>dfn[u] || edge[i].cut;
37         if (u!=fu) cut[u]=low[v]>=dfn[u]?1:cut[u];
38         low[u]=low[v]>low[u]?low[u]:low[v];
39         tot++;
40     }
41     if (u==fu && tot>1) cut[u]=1;

```

```

42 }
43 int main() {
44     int t;
45     scanf("%d",&t);
46     while (t--) {
47         int n,m;
48         scanf("%d%d",&n,&m);
49         init(n);
50         for (int i=0; i<m; i++) {
51             int u,v;
52             scanf("%d%d",&u,&v);
53             add_edge(--u,--v);
54             add_edge(v,u);
55         }
56         for (int i=0; i<n; i++)
57             if (!visit[i]) {
58                 idx=0;
59                 dfs(i,i);
60             }
61     }
62     return 0;
63 }

```

4.6 Stoer-Wagner

```

1  int map[maxn][maxn];
2  int n;
3  void contract(int x,int y) {
4      int i,j;
5      for (i=0; i<n; i++)
6          if (i!=x) map[x][i]+=map[y][i],map[i][x]+=map[i][y];
7      for (i=y+1; i<n; i++) for (j=0; j<n; j++) {
8          map[i-1][j]=map[i][j];
9          map[j][i-1]=map[j][i];
10     }
11     n--;
12 }
13 int w[maxn],c[maxn];
14 int sx,tx;
15 int mincut() {
16     int i,j,k,t;
17     memset(c,0,sizeof(c));
18     c[0]=1;
19     for (i=0; i<n; i++) w[i]=map[0][i];
20     for (i=1; i+1<n; i++) {
21         t=k=-1;
22         for (j=0; j<n; j++) if (c[j]==0&&w[j]>k)
23             k=w[t=j];
24         c[sx=t]=1;
25         for (j=0; j<n; j++) w[j]+=map[t][j];
26     }
27     for (i=0; i<n; i++) if (c[i]==0) return w[tx=i];
28 }
29 int main() {
30     int i,j,k,m;
31     while (scanf("%d%d",&n,&m)!=EOF) {
32         memset(map,0,sizeof(map));
33         while (m--) {
34             scanf("%d%d%d",&i,&j,&k);
35             map[i][j]+=k;
36             map[j][i]+=k;
37         }
38         int mint=999999999;

```

```

39     while (n>1) {
40         k=mincut();
41         if (k<mint) mint=k;
42         contract(sx,tx);
43     }
44     printf("%d\n",mint);
45 }
46 return 0;
47 }

```

4.7 Euler path

```

1 //Directed graph
2 void solve(int x) {
3     int i;
4     if (!match[x]) {
5         path[++l]=x;
6         return ;
7     }
8     for (i=1; i<=n; i++)
9         if (b[x][i]) {
10             b[x][i]--;
11             match[x]--;
12             solve(i);
13         }
14     path[++l]=x;
15 }
16 //Undirected graph
17 void solve(int x) {
18     int i;
19     if (!match[x]) {
20         path[++l]=x;
21         return ;
22     }
23     for (i=1; i<=n; i++)
24         if (b[x][i]) {
25             b[x][i]--;
26             b[i][x]--;
27             match[x]--;
28             match[i]--;
29             solve(i);
30         }
31     path[++l]=x;
32 }

```

4.8 Strongly connected component

```

1 int dfsnum[2000];
2 int low[2000];
3 int stack[2000];
4 int top;
5 int ans;
6 int an;
7 int be[2000];
8 int flag[2000];
9 void dfs(int x) {
10     dfsnum[x] = low[x] = ans++;
11     stack[++top] = x;
12     flag[x] = 1;
13     for (int i = head[x]; i != -1; i = edge[i].next) {
14         int y = edge[i].to;

```

```

15     if (dfsnum[y] == -1) {
16         dfs(y);
17         low[x] = min(low[x], low[y]);
18     } else if (flag[y] == 1)
19         low[x] = min(low[x], dfsnum[y]);
20 }
21 if (dfsnum[x] == low[x]) {
22     while (stack[top] != x) {
23         flag[stack[top]] = 0;
24         be[stack[top]] = an;
25         top--;
26     }
27     flag[x] = 0;
28     be[x] = an++;
29     top--;
30 }
31 }
32 void SC() {
33     memset(dfsnum, -1, sizeof(dfsnum));
34     memset(flag, 0, sizeof(flag));
35     top = 0;
36     an = 0;
37     ans = 0;
38     for (int i = 0; i < n; i++)
39         if (dfsnum[i] == -1)
40             dfs(i);
41 }

```

4.9 Match

4.9.1 Bipartite graph

```

1 bool check(int u) {
2     for (int i=head[u]; i!=-1; i=edge[i].next) {
3         int v=edge[i].to;
4         if (!use[v]) {
5             use[v]=1;
6             if (pre[v]==-1 || check(pre[v])) {
7                 pre[v]=u;
8                 return 1;
9             }
10        }
11    }
12    return 0;
13 }
14 int match() {
15     int ret=0;
16     memset(pre, -1, sizeof(pre));
17     for (int u=1; u<=N; u++) {
18         memset(use, 0, sizeof(use));
19         if (check(u))
20             ret++;
21     }
22     return ret;
23 }

```

4.9.2 Edmonds

```

1 int N;
2 bool Graph[MaxN+1][MaxN+1];
3 int Match[MaxN+1];
4 bool InQueue[MaxN+1], InPath[MaxN+1], InBlossom[MaxN+1];

```

```

5  int Head,Tail;
6  int Queue[MaxN+1];
7  int Start,Finish;
8  int NewBase;
9  int Father[MaxN+1],Base[MaxN+1];
10 int Count;
11 void CreateGraph() {}
12 void Push(int u) {
13     Queue[Tail] = u;
14     Tail++;
15     InQueue[u] = true;
16 }
17 int Pop() {
18     int res = Queue[Head];
19     Head++;
20     return res;
21 }
22 int FindCommonAncestor(int u,int v) {
23     memset(InPath,false,sizeof(InPath));
24     while (true) {
25         u = Base[u];
26         InPath[u] = true;
27         if (u == Start) break;
28         u = Father[Match[u]];
29     }
30     while (true) {
31         v = Base[v];
32         if (InPath[v]) break;
33         v = Father[Match[v]];
34     }
35     return v;
36 }
37 void ResetTrace(int u) {
38     int v;
39     while (Base[u] != NewBase) {
40         v = Match[u];
41         InBlossom[Base[u]] = InBlossom[Base[v]] = true;
42         u = Father[v];
43         if (Base[u] != NewBase) Father[u] = v;
44     }
45 }
46 void BlossomContract(int u,int v) {
47     NewBase = FindCommonAncestor(u,v);
48     memset(InBlossom,false,sizeof(InBlossom));
49     ResetTrace(u);
50     ResetTrace(v);
51     if (Base[u] != NewBase) Father[u] = v;
52     if (Base[v] != NewBase) Father[v] = u;
53     for (int tu = 1; tu <= N; tu++)
54         if (InBlossom[Base[tu]]) {
55             Base[tu] = NewBase;
56             if (!InQueue[tu]) Push(tu);
57         }
58 }
59 void FindAugmentingPath() {
60     memset(InQueue,false,sizeof(InQueue));
61     memset(Father,0,sizeof(Father));
62     for (int i = 1; i <= N; i++)
63         Base[i] = i;
64     Head = Tail = 1;
65     Push(Start);
66     Finish = 0;
67     while (Head < Tail) {
68         int u = Pop();

```

```

69     for (int v = 1; v <= N; v++)
70         if (Graph[u][v] && (Base[u] != Base[v]) && (Match[u] != v)) {
71             if ((v == Start) ||
72                 ((Match[v] > 0) && (Father[Match[v]] > 0)))
73                 BlossomContract(u,v);
74             else if (Father[v] == 0) {
75                 Father[v] = u;
76                 if (Match[v] > 0)
77                     Push(Match[v]);
78                 else {
79                     Finish = v;
80                     return;
81                 }
82             }
83         }
84     }
85 }
86 void AugmentPath() {
87     int u,v,w;
88     u = Finish;
89     while (u > 0) {
90         v = Father[u];
91         w = Match[v];
92         Match[v] = u;
93         Match[u] = v;
94         u = w;
95     }
96 }
97 void Edmonds() {
98     memset(Match,0,sizeof(Match));
99     for (int u = 1; u <= N; u++)
100         if (Match[u] == 0) {
101             Start = u;
102             FindAugmentingPath();
103             if (Finish > 0) AugmentPath();
104         }
105 }
106 void PrintMatch() {}
107 int main() {
108     CreateGraph();
109     Edmonds();
110     PrintMatch();
111 }

```

4.9.3 KM

```

1  bool visx[N],visy[N];
2  int lx[N],ly[N];
3  int matchy[N];
4  int map[N][N];
5  bool find(int x) {
6      visx[x]=true;
7      int t;
8      for (int y=0; y<ycnt; y++) {
9          if (!visy[y]) {
10             t=lx[x]+ly[y]-map[x][y];
11             if (t==0) {
12                 visy[y]=true;
13                 if (matchy[y]==-1 || find(matchy[y])) {
14                     matchy[y]=x;
15                     return true;
16                 }
17             } else if (lack>t) lack=t;

```

```

18     }
19 }
20 return false;
21 }
22 void KM() {
23     memset(lx,0,sizeof(lx));
24     memset(ly,0,sizeof(ly));
25     memset(matchy,-1,sizeof(matchy));
26     for (int i=0; i<xcnt; i++)
27         for (int j=0; j<ycnt; j++)
28             if (map[i][j]>lx[i])
29                 lx[i]=map[i][j];
30     for (int x=0; x<xcnt; x++) {
31         while (true) {
32             memset(visx,false,sizeof(visx));
33             memset(visy,false,sizeof(visy));
34             lack=INFI;
35             if (find(x)) break;
36             for (int i=0; i<xcnt; i++) {
37                 if (visx[i]) lx[i]-=lack;
38                 if (visy[i]) ly[i]+=lack;
39             }
40         }
41     }
42     int cost=0;
43     for (int i=0; i<ycnt; i++)
44         cost+=map[matchy[i]][i];
45 }

```

4.10 Clique

```

1 bool am[100][100];
2 int ans;
3 int c[100];
4 int U[100][100];
5 int n;
6 bool dfs(int rest,int num) {
7     if (!rest) {
8         if (num>=ans)
9             return 1;
10        else
11            return 0;
12    }
13    int pre=-1;
14    for (int i=0; i<rest && rest-i+num>=ans; i++) {
15        int idx=U[num][i];
16        if (num+c[idx]<ans)
17            return 0;
18        int nrest=0;
19        for (int j=i+1; j<rest; j++)
20            if (am[idx][U[num][j]])
21                U[num+1][nrest++]=U[num][j];
22        if (dfs(nrest,num+1))
23            return 1;
24    }
25    return 0;
26 }
27 int main() {
28     while (scanf("%d",&n),n) {
29         for (int i=0; i<n; i++)
30             for (int j=0; j<n; j++)
31                 scanf("%d",&am[i][j]);
32         ans=0;

```

```

33     for (int i=n-1; i>=0; i--) {
34         int rest=0;
35         for (int j=i+1; j<n; j++)
36             if (am[i][j])
37                 U[0][rest++]=j;
38         ans+=dfs(rest,0);
39         c[i]=ans;
40     }
41     printf("%d\n",ans);
42 }
43 return 0;
44 }

```

4.11 Spanning tree

4.11.1 Count the number of spanning tree

```

1 Matrix laplacian;
2 laplacian.clear();
3 for (int i = 0; i < n; i++)
4     for (int j = 0; j < n; j++)
5         if (i != j && G[i][j]) {
6             laplacian.a[i][j] = -1;
7             laplacian.a[i][i]++;
8         }
9 printf("%d\n",laplacian.det(n-1));

```

4.11.2 Spanning tree on directed graph

```

1 struct Edge {
2     int u,v,cost;
3 };
4 Edge e[1001*1001];
5 int pre[1001],id[1001],visit[1001],in[1001];
6 int zhuliu(int root,int n,int m,Edge e[]) {
7     int res = 0,u,v;
8     while (true) {
9         for (int i = 0; i < n; i++)
10             in[i] = inf;
11         for (int i = 0; i < m; i++)
12             if (e[i].u != e[i].v && e[i].cost < in[e[i].v]) {
13                 pre[e[i].v] = e[i].u;
14                 in[e[i].v] = e[i].cost;
15             }
16         for (int i = 0; i < n; i++)
17             if (i != root)
18                 if (in[i] == inf) return -1;
19         int tn = 0;
20         memset(id,-1,sizeof(id));
21         memset(visit,-1,sizeof(visit));
22         in[root] = 0;
23         for (int i = 0; i < n; i++) {
24             res += in[i];
25             v = i;
26             while (visit[v] != i && id[v] == -1 && v != root) {
27                 visit[v] = i;
28                 v = pre[v];
29             }
30             if (v != root && id[v] == -1) {
31                 for (int u = pre[v] ; u != v ; u = pre[u])
32                     id[u] = tn;
33                 id[v] = tn++;

```



```

34     }
35 }
36 if(tn == 0) break;
37 for (int i = 0; i < n; i++)
38     if (id[i] == -1)
39         id[i] = tn++;
40 for (int i = 0; i < m;) {
41     int v = e[i].v;
42     e[i].u = id[e[i].u];
43     e[i].v = id[e[i].v];
44     if (e[i].u != e[i].v)
45         e[i++].cost -= in[v];
46     else
47         swap(e[i], e[--m]);
48 }
49 n = tn;
50 root = id[root];
51 }
52 return res;
53 }

```

4.12 Kth shortest path

```

1 #include<cstdio>
2 #include<cstring>
3 #include<queue>
4 using namespace std;
5 int K;
6 class states {
7 public:
8     int cost,id;
9 };
10 int dist[1000];
11 class cmp {
12 public:
13     bool operator ()(const states &i,const states &j) {
14         return i.cost>j.cost;
15     }
16 };
17 class cmp2 {
18 public:
19     bool operator ()(const states &i,const states &j) {
20         return i.cost+dist[i.id]>j.cost+dist[j.id];
21     }
22 };
23 struct edges {
24     int to,next,cost;
25 } edger[100000],edge[100000];
26 int headr[1000],head[1000],Lr,L;
27 void dijkstra(int s) {
28     states u;
29     u.id=s;
30     u.cost=0;
31     dist[s]=0;
32     priority_queue<states,vector<states>,cmp> q;
33     q.push(u);
34     while (!q.empty()) {
35         u=q.top();
36         q.pop();
37         if (u.cost!=dist[u.id]) continue;
38         for (int i=headr[u.id]; i!=-1; i=edger[i].next) {
39             states v=u;
40             v.id=edger[i].to;

```

```

41     if (dist[v.id]>dist[u.id]+edger[i].cost) {
42         v.cost=dist[v.id]=dist[u.id]+edger[i].cost;
43         q.push(v);
44     }
45 }
46 }
47 }
48 int num[1000];
49 void init(int n) {
50     Lr=L=0;
51     memset(head,-1,4*n);
52     memset(headr,-1,4*n);
53     memset(dist,63,4*n);
54     memset(num,0,4*n);
55 }
56 void add_edge(int u,int v,int x) {
57     edge[L].to=v;
58     edge[L].cost=x;
59     edge[L].next=head[u];
60     head[u]=L++;
61     edger[Lr].to=u;
62     edger[Lr].cost=x;
63     edger[Lr].next=headr[v];
64     headr[v]=Lr++;
65 }
66 int a_star(int s,int t) {
67     if (dist[s]==0x3f3f3f3f)
68         return -1;
69     priority_queue<states,vector<states>,cmp2> q;
70     states tmp;
71     tmp.id=s;
72     tmp.cost=0;
73     q.push(tmp);
74     while (!q.empty()) {
75         states u=q.top();
76         q.pop();
77         num[u.id]++;
78         if (num[t]==K)
79             return u.cost;
80         for (int i=head[u.id]; i!=-1; i=edge[i].next) {
81             int v=edge[i].to;
82             tmp.id=v;
83             tmp.cost=u.cost+edge[i].cost;
84             q.push(tmp);
85         }
86     }
87     return -1;
88 }
89 int main() {
90     int n,m;
91     scanf("%d%d",&n,&m);
92     init(n);
93     for (int i=0; i<m; i++) {
94         int u,v,x;
95         scanf("%d%d%d",&u,&v,&x);
96         add_edge(u-1,v-1,x);
97     }
98     int s,t;
99     scanf("%d%d%d",&s,&t,&K);
100    if (s==t)
101        K++;
102    dijkstra(t-1);
103    printf("%d\n",a_star(s-1,t-1));
104 }

```

4.13 LCA

```

1  typedef long long ll;
2  const int maxn = 100000 + 100;
3  const int maxk = 20;
4  struct edge
5  {
6      int v, w;
7  } es[maxn * 2];
8  int tot;
9  vector<int> G[maxn];
10 ll dis[maxn];
11 int fa[maxn][maxk];
12 int depth[maxn];
13 int n, m;
14 void init()
15 {
16     for (int i = 1; i <= n; i++)
17     {
18         G[i].clear();
19     }
20     tot = 0;
21 }
22 void addedge(int u, int v, int w)
23 {
24     G[u].push_back(tot);
25     es[tot++] = {v, w};
26     G[v].push_back(tot);
27     es[tot++] = {u, w};
28 }
29 int lca(int x, int y)
30 {
31     if (depth[x] > depth[y]) swap(x, y);
32     for (int k = maxk - 1; k >= 0; k--)
33     {
34         if (depth[fa[y][k]] >= depth[x])
35         {
36             y = fa[y][k];
37         }
38     }
39     if (x == y) return x;
40     for (int k = maxk - 1; k >= 0; k--)
41     {
42         if (fa[x][k] != fa[y][k])
43         {
44             x = fa[x][k];
45             y = fa[y][k];
46         }
47     }
48     return fa[x][0];
49 }
50 void dfs(int cur, int parent)
51 {
52     fa[cur][0] = parent;
53     for (int k = 1; k < maxk; k++)
54     {
55         fa[cur][k] = fa[fa[cur][k - 1]][k - 1];
56     }
57     for (int eno: G[cur])
58     {
59         edge & e = es[eno];
60         if (e.v != parent)
61         {
62             dis[e.v] = e.w + dis[cur];

```

```

63     depth[e.v] = 1 + depth[cur];
64     dfs(e.v, cur);
65 }
66 }
67 }
68 ll dist(int u, int v)
69 {
70     int _lca = lca(u, v);
71     return dis[u] + dis[v] - 2 * dis[_lca];
72 }

```

4.14 VirtualTree

dfs 部分参照 lca 部分自己写

```

1  typedef long long ll;
2  const int inf = 0x3f3f3f3f;
3  const int maxn = 100000;
4  const int maxk = 21;
5  int dfn[maxn], dfs_clock;
6  inline bool cmp(const int & i, const int & j)
7  {
8      return dfn[i] < dfn[j];
9  }
10 int fa[maxn][maxk], depth[maxn];
11 struct edge
12 {
13     int v;
14     ll c;
15 } es[maxn * 2];
16 vector<int> G[maxn], H[maxn];
17 void addH(int u, int v)
18 {
19     H[u].push_back(v);
20 }
21 int lca(int x, int y)
22 {
23     if (depth[x] < depth[y]) swap(x, y);
24     for (int k = maxk - 1; k >= 0; k--)
25     {
26         if (depth[fa[x][k]] >= depth[y])
27         {
28             x = fa[x][k];
29         }
30     }
31     if (x == y) return x;
32     for (int k = maxk - 1; k >= 0; k--)
33     {
34         if (fa[x][k] != fa[y][k])
35         {
36             x = fa[x][k];
37             y = fa[y][k];
38         }
39     }
40     return fa[x][0];
41 }
42 //vertices need to be arrange
43 int key_node[maxn], kcmt;
44 void build()
45 {
46     static int stk[maxn];
47     sort(key_node, key_node + kcmt, cmp);
48     //注释部分可用于去除关键点子树中的多余关键点

```

```

49 // int p = 0;
50 // for (int i = 1; i < kcmt; i++)
51 // {
52 //     if (lca(key_node[i], key_node[p]) != key_node[p])
53 //     {
54 //         key_node[++p] = key_node[i];
55 //     }
56 // }
57 // kcmt = p + 1;
58 int sz = 0;
59 stk[sz++] = 0;
60 for (int i = 0; i < kcmt; i++)
61 {
62     int f = lca(stk[sz - 1], key_node[i]);
63     if (f == stk[sz - 1])
64     {
65         stk[sz++] = key_node[i];
66     }
67     else
68     {
69         while (sz - 2 >= 0 && depth[stk[sz - 2]] >= depth[f])
70         {
71             addH(stk[sz - 2], stk[sz - 1]);
72             sz--;
73         }
74         if (stk[sz - 1] != f)
75         {
76             addH(f, stk[sz - 1]);
77             stk[sz++] = f;
78         }
79         stk[sz++] = key_node[i];
80     }
81 }
82 for (int i = 1; i < sz; i++)
83 {
84     addH(stk[i - 1], stk[i]);
85 }
86 }

```

4.15 Stable marriage problem

假定有 n 个男生和 n 个女生，理想的拍拖状态就是对于每对情侣 (a, b) ，找不到另一对情侣 (c, d) 使得 c 更喜欢 b ， b 也更喜欢 c ，同理，对 a 来说也没有 (e, f) 使得 a 更喜欢 e 而 e 更喜欢 a ，当然最后会有一些人落单。这样子一个状态可以称为理想拍拖状态，它也有一个专业的名词叫稳定婚姻。求解这个问题可以用一个专有的算法，延迟认可算法，其核心就是让每个男生按自己喜欢的顺序逐个向女生表白，例如 leokan 向一个女生求爱，这个过程中，若这个女生没有男朋友，那么这个女生就暂时成为 leokan 的女朋友，或这个女生喜欢她现有男朋友的程度没有喜欢 leokan 高，这个女生也暂时成为 leokan 的女朋友，而她原有的男朋友则再将就找下一个次喜欢的女生来当女朋友。

```

1 #include<string.h>
2 #include<stdio.h>
3 #define N 1050
4 int boy[N][N];
5 int girl[N][N];
6 int ans[N];
7 int cur[N];
8 int n;
9 void getMarry(int g) {
10     for (int i=ans[g]+1; i<n; i++) {
11         int b=girl[g][i]-1;
12         if (cur[b]<0) {
13             ans[g]=i;

```

```

14     cur[b]=g;
15     return;
16 }
17 int og=cur[b];
18 if (boy[b][og] > boy[b][g]) {
19     cur[b]=g;
20     ans[g]=i;
21     getMarry(og);
22     return;
23 }
24 }
25 };
26 int main() {
27     int t,a;
28     scanf("%d",&t);
29     while(t--) {
30         memset(girl,0,sizeof(girl));
31         memset(boy,0,sizeof(boy));
32         scanf("%d",&n);
33         for (int i=0; i<n; i++)
34             for (int j=0; j<n; j++)
35                 scanf("%d",&girl[i][j]);
36         for (int i=0; i<n; i++)
37             for (int j=0; j<n; j++) {
38                 scanf("%d",&a);
39                 boy[i][a-1]=j;
40             }
41         memset(cur,0xff,sizeof(cur));
42         memset(ans,0xff,sizeof(ans));
43         for (int i=0; i<n; i++)
44             getMarry(i);
45         for (int i=0; i<n; i++)
46             printf("%d\n",girl[i][ans[i]]);
47     }
48     return 0;
49 }

```

5 Math

5.1 FFT

5.1.1 Bit operation

$tf(X1, X2) = (tf(X1) - tf(X2), tf(X1) + tf(X2))$

异或: $tf(X1, X2) = (tf(X1) - tf(X2), tf(X1) + tf(X2))$

与: $tf(x1, x2) = (tf(x1) + tf(x2), tf(x1))$

```

1 // Transforms the interval [x, y) in a.
2 void transform(int x, int y) {
3     if ( x == y - 1) {
4         return;
5     }
6     int l2 = ( y - x ) / 2;
7     int z = x + l2;
8     transform(x, z);
9     transform(z, y);
10    for (int i=x; i<z; i++) {
11        int x1 = a[i];
12        int x2 = a[i+l2];
13        a[i] = (x1 - x2 + MOD) % MOD;
14        a[i+l2] = (x1 + x2) % MOD;
15    }

```

```

16 }
17 // Reverses the transform in
18 // the interval [x, y) in a.
19 void untransform(int x, int y) {
20     if ( x == y - 1) {
21         return;
22     }
23     int l2 = ( y - x ) / 2;
24     int z = x + l2;
25     for (int i=x; i<z; i++) {
26         long long y1 = a[i];
27         long long y2 = a[i+l2];
28         // x1 - x2 = y1
29         // x1 + x2 = y2
30         // 2 * x1 = y1 + y2
31         // 2 * x2 = y2 - y1
32
33         // In order to solve those equations, we need to divide by 2
34         // But we are performing operations modulo 1000000007
35         // that needs us to find the modular multiplicative inverse of 2.
36         // That is saved in the INV2 variable.
37
38         a[i] = (int)( ((y1 + y2)*INV2) % MOD );
39         a[i+l2] = (int)( ((y2 - y1 + MOD)*INV2) % MOD );
40     }
41     untransform(x, z);
42     untransform(z, y);
43 }

```

5.1.2 Standard

```

1 struct vir {
2     long double re, im;
3     vir(long double a = 0, long double b = 0) {
4         re = a;
5         im = b;
6     }
7     vir operator +(const vir& b) const {
8         return vir(re + b.re, im + b.im);
9     }
10    vir operator -(const vir& b) const {
11        return vir(re - b.re, im - b.im);
12    }
13    vir operator *(const vir& b) const {
14        return vir(re * b.re - im * b.im, re * b.im + im * b.re);
15    };
16 };
17 void change(vir *x, int len, int loglen) {
18     int i, j, k, t;
19     for (i = 0; i < len; i++) {
20         t = i;
21         for (j = k = 0; j < loglen; j++, t >>= 1)
22             k = (k << 1) | (t & 1);
23         if (k < i) {
24             vir wt = x[k];
25             x[k] = x[i];
26             x[i] = wt;
27         }
28     }
29 }
30 void fft(vir *x, int len, int loglen) {
31     int i, j, t, s, e;
32     change(x, len, loglen);

```

```

33  t = 1;
34  for (i = 0; i < loglen; i++, t <= 1) {
35      s = 0;
36      e = s + t;
37      while (s < len) {
38          vir a, b, wo(cos(PI / t), sin(PI / t)), wn(1, 0);
39          for (j = s; j < s + t; j++) {
40              a = x[j];
41              b = x[j + t] * wn;
42              x[j] = a + b;
43              x[j + t] = a - b;
44              wn = wn * wo;
45          }
46          s = e + t;
47          e = s + t;
48      }
49  }
50 }
51 void dit_fft(vir *x, int len, int loglen) {
52     int i, j, s, e, t = 1 << loglen;
53     for (i = 0; i < loglen; i++) {
54         t >>= 1;
55         s = 0;
56         e = s + t;
57         while (s < len) {
58             vir a, b, wn(1, 0), wo(cos(PI / t), -sin(PI / t));
59             for (j = s; j < s + t; j++) {
60                 a = x[j] + x[j + t];
61                 b = (x[j] - x[j + t]) * wn;
62                 x[j] = a;
63                 x[j + t] = b;
64                 wn = wn * wo;
65             }
66             s = e + t;
67             e = s + t;
68         }
69     }
70     change(x, len, loglen);
71     for (i = 0; i < len; i++)
72         x[i].re /= len;
73 }

```

5.1.3 Usage

```

1  vir x1[MAXN], x2[MAXN];
2  void solve(long long *a, int lena, long long *b, int lenb, long long *ret, int& len)
3  {
4      int len1 = lena << 1;
5      int len2 = lenb << 1;
6      len = 1;
7      int loglen = 0;
8      while (len < len1 || len < len2) {
9          len <= 1;
10         loglen++;
11     }
12     for (int i = 0; i < lena; i++)
13         x1[i] = vir(a[i], 0);
14     for (int i = lena; i < len; i++)
15         x1[i] = vir(0, 0);
16     for (int i = 0; i < lenb; i++)
17         x2[i] = vir(b[i], 0);
18     for (int i = lenb; i < len; i++)
19         x2[i] = vir(0, 0);

```



```

19 | fft(x1, len, loglen);
20 | fft(x2, len, loglen);
21 | for (int i = 0; i < len; i++)
22 |     x1[i] = x1[i] * x2[i];
23 | dit_fft(x1, len, loglen);
24 | for (int i = 0; i < len; i++)
25 |     ret[i] = (long long)(x1[i].re + 0.5);
26 | }

```

5.2 Euler function

```

1 | int getEuler(int x) {
2 |     getFactor(x);
3 |     int ret=x;
4 |     for (int i=0; i<N; i++)
5 |         ret = ret/fac[i]*(fac[i]-1);
6 |     return ret;
7 | }
8 | void getEuler2() {
9 |     memset(euler,0,sizeof(euler));
10 |    euler[1] = 1;
11 |    for (int i = 2; i <= 3000000; i++) {
12 |        if (!euler[i]) {
13 |            for (int j = i; j <= 3000000; j += i) {
14 |                if (!euler[j])
15 |                    euler[j] = j;
16 |                euler[j] = euler[j]/i*(i-1);
17 |            }
18 |        }
19 |    }
20 | }

```

5.3 Ex-GCD

```

1 | //Find one solution (x,y) of  $ax + by = gcd(a,b)$ 
2 | long long ex_gcd(long long a, long long b, long long &x, long long &y) {
3 |     if (b) {
4 |         long long ret = ex_gcd(b, a%b, x, y), tmp = x;
5 |         x = y;
6 |         y = tmp - (a/b)*y;
7 |         return ret;
8 |     } else {
9 |         x = 1;
10 |        y = 0;
11 |        return a;
12 |    }
13 | }

```

5.4 Prime

5.4.1 Get primes

```

1 | int N;
2 | bool isPrime[10001];
3 | int prime[10000];
4 | void getPrime(int n) {
5 |     memset(isPrime,1,++n);
6 |     N=0;
7 |     isPrime[0]=isPrime[1]=0;
8 |     for (int i=2; i<n; i++) {

```

```

9      if (isPrime[i])
10         prime[N++]=i;
11      for (int j=0; j<N && prime[j]*i<n; j++) {
12         isPrime[i*prime[j]]=0;
13         if (i%prime[j]==0)
14             break;
15     }
16 }
17 }

```

5.4.2 Get factors

```

1  const int TIME = 8;
2  int factor[100], fac_top = -1;
3  //GCD of bint
4  bint gcd(bint small, bint big) {
5      while(small) {
6          swap(small, big);
7          small%=big;
8      }
9      return abs(big);
10 }
11 //ret = (a*b)%n (n<2^62)
12 bint muti_mod(bint a, bint b, bint n) {
13     bint exp = a%n, res = 0;
14     while(b) {
15         if(b&1) {
16             res += exp;
17             if(res>n) res -= n;
18         }
19         exp <<= 1;
20         if (exp>n) exp -= n;
21         b>>=1;
22     }
23     return res;
24 }
25 // ret = (a^b)%n
26 bint mod_exp(bint a, bint p, bint m) {
27     bint exp=a%m, res=1;
28     while(p>1) {
29         if(p&1)
30             res=muti_mod(res, exp, m);
31         exp = muti_mod(exp, exp, m);
32         p>>=1;
33     }
34     return muti_mod(res, exp, m);
35 }
36 //miller-rabin
37 bool miller_rabin(bint n, int times) {
38     if(n==2) return 1;
39     if(n<2 || !(n&1)) return 0;
40     bint a, u=n-1, x, y;
41     int t=0;
42     while(u%2==0) {
43         t++;
44         u/=2;
45     }
46     srand(time(0));
47     for(int i=0; i<times; i++) {
48         a = rand() % (n-1) + 1;
49         x = mod_exp(a, u, n);
50         for(int j=0; j<t; j++) {
51             y = muti_mod(x, x, n);

```

```

52     if ( y == 1 && x != 1 && x != n-1 )
53         return false; //must not
54     x = y;
55 }
56 if( y!=1) return false;
57 }
58 return true;
59 }
60 bint pollard_rho(bint n,int c) {
61     bint x,y,d,i = 1,k = 2;
62     srand(time(0));
63     x = rand()%(n-1)+1;
64     y = x;
65     while(true) {
66         i++;
67         x = (muti_mod(x,x,n) + c) % n;
68         d = gcd(y-x, n);
69         if (1 < d && d < n) return d;
70         if( y == x) return n;
71         if(i == k) {
72             y = x;
73             k <<= 1;
74         }
75     }
76 }
77 void findFactor(bint n,int k) {
78     if(n==1)return;
79     if(miller_rabin(n, TIME)) {
80         factor[++fac_top] = n;
81         return;
82     }
83     bint p = n;
84     while(p >= n)
85         p = pollard_rho(p,k--);
86     findFactor(p,k);
87     findFactor(n/p,k);
88 }

```

5.5 区间筛

```

1  const int maxn = 1000000 + 10;
2  int primes[maxn];
3  int ptot;
4  bool nprime[maxn];
5  void intervalprime(int L, int U)
6  {
7      int i, j;
8      int SU = sqrt((double) U);
9      int d = U - L + 1;
10     for (int i = 0; i < d; i++) nprime[i] = 0;
11     //去偶数, 可删(改下面起始点为2, 步长为1)
12     for (int i = (L % 2 != 0); i < d; i+= 2) nprime[i] = 1;
13
14     for (int i = 3; i <= SU; i += 2)
15     {
16         if (i > L && nprime[i - L]) continue;
17         j = (L / i) * i;
18         if (j < L) j += i;
19         j = j - L;
20         for (; j < d; j += i) nprime[j] = 1;
21     }
22     if (L <= 1) nprime[1 - L] = 1;
23     if (L <= 2) nprime[2 - L] = 0;

```

```

24 | ptot = 0;
25 | for (int i = 0; i < d; i++) if (!nprime[i]) primes[ptot++] = i + L;
26 | }

```

5.6 Simpson

```

1 | double Simp(double l, double r) {
2 |     double h = (r-l)/2.0;
3 |     return h*(calc(l)+4*calc((l+r)/2.0)+calc(r))/3.0;
4 | }
5 | double rSimp(double l, double r) {
6 |     double mid = (l+r)/2.0;
7 |     if (abs((Simp(l,r)-Simp(l,mid)-Simp(mid,r)))/15 < eps)
8 |         return Simp(l,r);
9 |     else
10 |         return rSimp(l,mid)+rSimp(mid,r);
11 | }

```

5.7 Chinese remainder theorem

```

1 | int m[10], a[10]; // x mod m_i = a_i
2 | bool solve(int &m0, int &a0, int m, int a) {
3 |     int y, x;
4 |     int g = ex_gcd(m0, m, x, y);
5 |     if (abs(a-a0)%g) return 0;
6 |     x*=(a-a0)/g;
7 |     x%=m/g;
8 |     a0=(x*m0+a0);
9 |     m0*=m/g;
10 |    a0%=m0;
11 |    if (a0<0) a0+=m0;
12 |    return 1;
13 | }
14 | int MLES() {
15 |     bool flag=1;
16 |     int m0=1, a0=0;
17 |     for (int i=0; i<n; i++)
18 |         if (!solve(m0, a0, m[i], a[i])) {
19 |             flag=0;
20 |             break;
21 |         }
22 |     if (flag)
23 |         return a0;
24 |     else
25 |         return -1;
26 | }

```

5.8 Lucas

```

1 | // num[i] = i!
2 | int comLucus(int n, int m, int p) {
3 |     int ans=1;
4 |     for (; n && m && ans; n/=p, m/=p) {
5 |         if (n%p>=m%p)
6 |             ans = ans*num[n%p]%p*getInv(num[m%p]%p)%p
7 |                 *getInv(num[n%p-m%p])%p;
8 |         else
9 |             ans=0;
10 |    }
11 |    return ans;
12 | }

```

5.9 Primitive root

```

1 int getPriRoot(int p) {
2     if (p==2) return 1;
3     int phi = p - 1;
4     getFactor(phi);
5     for (int g = 2; g < p; ++g) {
6         bool flag=1;
7         for (int i = 0; flag && i < N; ++i)
8             if (power(g, phi/fac[i], p) == 1)
9                 flag=0;
10        if (flag)
11            return g;
12    }
13 }

```

5.10 Inverse element

```

1 void getInv2(int x) {
2     inv[1]=1;
3     for (int i=2; i<=x; i++)
4         inv[i]=(mod-(mod/i)*inv[mod%i]%mod)%mod;
5 }

```

5.11 Calculator

注意灵活运用。

双目运算符在 calc() 中，左结合单目运算符在 P() 中，右结合单目运算符在 calc_exp 中。（但是还没遇到过。。）

```

1 #include <iostream>
2 #include <cstdio>
3 #include <cstring>
4 #include <algorithm>
5 #include <string>
6 using namespace std;
7
8 char s[1000000];
9 int n,cur;
10 const string OP = "+-*/";
11
12 char next_char() {
13     if (cur >= n) return EOF;
14     return s[cur];
15 }
16
17 int get_priority(char ch) {
18     if (ch == '*') return 2;
19     return 1;
20 }
21
22 int P();
23
24 int calc(int a,char op,int b) {
25     if (op == '+')
26         return a+b;
27     if (op == '-')
28         return a-b;
29     if (op == '*')
30         return a*b;

```

```

31 }
32
33 int calc_exp(int p) {
34     int a = P();
35     while ((OP.find(next_char()) != OP.npos) &&
36            (get_priority(next_char()) >= p)) {
37         char op = next_char();
38         cur++;
39         a = calc(a,op,calc_exp(get_priority(op)+1));
40     }
41     return a;
42 }
43
44 int totvar,m,var[26],varid[26];
45
46 int P() {
47     if (next_char() == '-') {
48         cur++;
49         return -P();
50     } else if (next_char() == '+') {
51         cur++;
52         return P();
53     } else if (next_char() == '(') {
54         cur++;
55         int res = calc_exp(0);
56         cur++;
57         return res;
58     } else {
59         cur++;
60         return var[varid[s[cur-1]-'a']];
61     }
62 }
63
64 int id[26],minid;
65
66 int main() {
67     while (true) {
68         scanf("%d%d",&totvar,&var[0]);
69         if (totvar == 0 && var[0] == 0) break;
70         for (int i = 1; i < totvar; i++)
71             scanf("%d",&var[i]);
72         scanf("%d",&m);
73         scanf("%s",s);
74         for (int i = 0; i < 26; i++)
75             id[i] = -1;
76         minid = 0;
77         n = strlen(s);
78         for (int i = 0; i < n; i++)
79             if (s[i] >= 'a' && s[i] <= 'z') {
80                 if (id[s[i]-'a'] == -1) {
81                     id[s[i]-'a'] = minid;
82                     minid++;
83                 }
84                 s[i] = 'a'+id[s[i]-'a'];
85             }
86         for (int i = 0; i < totvar; i++)
87             varid[i] = i;
88         int res = 0;
89         do {
90             cur = 0;
91             int tmp = calc_exp(0);
92             if (tmp == m) {
93                 res++;
94                 break;

```

```

95     }
96   } while (next_permutation(varid,varid+totvar));
97   //puts(s);
98   if (res > 0)
99     puts("YES");
100  else
101    puts("NO");
102  }
103  return 0;
104 }

```

5.12 Linear programming

```

1  #define MAXM 20 //max num of basic variables
2  #define INF 1E200
3
4  double A[MAXM+5][MAXN+MAXM+5];
5  double b[MAXM+5],c[MAXN+MAXM+5];
6  int N[MAXN+5],B[MAXM+5];
7  double X[MAXN+MAXM+5],V;
8  int n,m,R,C,nCnt,bCnt;
9  int v1[MAXN],v2[MAXN];
10
11 int fcmp(double a,double b) {
12   if(fabs(a-b)<1E-7) return 0;
13   if(a>b) return 1;
14   return -1;
15 }
16
17 void Pivot(int l,int e) {
18   double t=A[l][e],p=c[e];
19   b[l]=b[l]/t;
20   for(int i=1; i<=C; i++)
21     A[l][i]/=t;
22   V=V-c[e]*b[l];
23   for(int i=1; i<=R; i++) {
24     if(i==l || fcmp(A[i][e],0.0)==0)
25       continue;
26     t=A[i][e];
27     b[i]=b[i]-t*b[l];
28     for(int j=1; j<=C; j++)
29       A[i][j]=A[i][j]-t*A[l][j];
30   }
31   for(int i=1; i<=C; i++)
32     c[i]=c[i]-p*A[l][i];
33   for(int i=1; i<=nCnt; i++) {
34     if(N[i]==e) {
35       N[i]=B[l];
36       break;
37     }
38   }
39   B[l]=e;
40 }
41
42 bool Process(double P[]) {
43   while(true) {
44     int e=-1;
45     double mV=-INF;
46     for(int i=1; i<=nCnt; i++)
47       if(fcmp(P[N[i]],mV)==1)
48         mV=P[N[i]],e=N[i];
49
50     if(fcmp(mV,0.0)<=0) break;

```

```

51     int l=-1;
52     mV=INF;
53     for(int i=1; i<=bCnt; i++) {
54         if(fcmp(A[i][e],0.0)==1) {
55             double t=b[i]/A[i][e];
56             if(fcmp(mV,t)==1 || (fcmp(mV,t)==0&&(l==-1 || B[l]>B[i])))
57                 mV=t,l=i;
58         }
59     }
60     if(l==-1) return false;
61     Pivot(l,e);
62 }
63 return true;
64 }
65
66 bool initSimplex() {
67     nCnt=bCnt=0;
68     for(int i=1; i<=n; i++)
69         N[++nCnt]=i;
70     for(int i=1; i<=m; i++)
71         B[++bCnt]=i+n,A[i][n+i]=1.0;
72     R=bCnt,C=bCnt+nCnt;
73     double minV=INF;
74     int p=-1;
75     for(int i=1; i<=m; i++)
76         if(fcmp(minV,b[i])==1)
77             minV=b[i],p=i;
78     if(fcmp(minV,0.0)>=0)
79         return true;
80     N[++nCnt]=n+m+1;
81     R++,C++;
82     for(int i=0; i<=C; i++)
83         A[R][i]=0.0;
84     for(int i=1; i<=R; i++)
85         A[i][n+m+1]=-1.0;
86     Pivot(p,n+m+1);
87     if(!Process(A[R])) return false;
88     if(fcmp(b[R],0.0)!=0)
89         return false;
90     p=-1;
91     for(int i=1; i<=bCnt&&p!=-1; i++)
92         if(B[i]==n+m+1) p=i;
93     if(p!=-1) {
94         for(int i=1; i<=nCnt; i++) {
95             if(fcmp(A[p][N[i]],0.0)!=0) {
96                 Pivot(p,N[i]);
97                 break;
98             }
99         }
100     }
101     bool f=false;
102     for(int i=1; i<=nCnt; i++) {
103         if(N[i]==n+m+1) f=true;
104         if(f&& i+1<=nCnt)
105             N[i]=N[i+1];
106     }
107     nCnt--;
108     R--,C--;
109     return true;
110 }
111
112 //-1: no solution 1: no bound 0: has a solution -V
113 int Simplex() {
114     if(!initSimplex())

```



```

115     return -1;
116 if(!Process(c))
117     return 1;
118 for(int i=1; i<=nCnt; i++)
119     X[N[i]]=0.0;
120 for(int i=1; i<=bCnt; i++)
121     X[B[i]]=b[i];
122 return 0;
123 }
124
125 int main() {
126     //n = 1;m=1;
127     //V= 0.0;
128     //c[1] = 1.0;
129     //A[1][1] = 1.0;
130     //b[1] = 5.0;
131     //Simplex();
132     //printf("V = %.3f\n",V);
133
134     while(scanf("%d",&v1[1]) == 1) {
135         for(int i = 2; i<=6; i++)
136             scanf("%d",&v1[i]);
137         n = 4;
138         m = 6;
139         for(int i = 0 ; i<=m+1; i++)
140             for(int j=0; j<=n+m+2; j++)
141                 A[i][j] = c[j] = 0;
142         memset(b,0,sizeof(b));
143         V = 0.0;
144         /*
145         n 为未知数个数
146         m 为约束个数
147         目标: siama(c[i]*xi)
148         约束: sigma(A[i][j]*xj) <=b[i]; j = 1 ... n
149         解存在X里面
150         */
151         b[1] = v1[1] ;
152         A[1][1] = 1;
153         A[1][4] = 1;
154         b[2] = v1[2] ;
155         A[2][1] = 1;
156         A[2][3] = 1;
157         b[3] = v1[3] ;
158         A[3][3] = 1;
159         A[3][4] = 1;
160         b[4] = v1[4] ;
161         A[4][2] = 1;
162         A[4][3] = 1;
163         b[5] = v1[5] ;
164         A[5][2] = 1;
165         A[5][4] = 1;
166         b[6] = v1[6] ;
167         A[6][1] = 1;
168         A[6][2] = 1;
169         c[1] = 1;
170         c[2] = 1;
171         c[3] = 1;
172         c[4] = 1;
173         Simplex();
174         //printf("V = %.3f\n",V);
175         printf("%.3f□%.3f□%.3f□%.3f\n",X[1],X[2],X[3],X[4]);
176
177     }
178     return 0;

```

179 | }

5.13 Factorization prime number p into $x^2 + y^2$

```

1  #include <stdio.h>
2  #include <string.h>
3  #include <stdlib.h>
4  int p,expp,A,B,aa,ans,tt;
5  long long M;
6  long long exp(int a,int b,long long mod) {
7      long long ans=1,num=a;
8      while (b!=0) {
9          if (b&1) {
10             ans=((ans%mod)*(num%mod))%mod;
11         }
12         num=((num%mod)*(num%mod))%mod;
13         b>>=1;
14     }
15     return ans;
16 }
17 int calcu(int p,int &x,int &y) {
18     if (p%4!=1) return -1;
19     else {
20         expp=(p-1)/4;
21         A,B;
22         while (1) {
23             aa=rand()%p;
24             if (aa==0) continue;
25             A=exp(aa,expp,p);
26             ans=((long long)A%p)*((long long)A%p)%p;
27             if (ans==p-1) break;
28         }
29         B=1;
30         M=((long long)A*(long long)A+(long long)B*(long long)B)/p;
31         if (M!=1) B=p;
32         while (M!=1) {
33             if (B>A) {
34                 tt=A;
35                 A=B;
36                 B=tt;
37             }
38             tt=A;
39             A=B;
40             B=tt%B;
41             M=((long long)A*(long long)A
42                +(long long)B*(long long)B)/p;
43         }
44         if (B<=A) {
45             x=B;
46             y=A;
47         } else {
48             x=A;
49             y=B;
50         }
51     }
52 }
53 int main() {
54     while (scanf("%d",&p)!=EOF) {
55         int x,y;
56         if (calcu(p,x,y)!=-1)
57             ;
58         return 0;
59     }

```

5.14 Partition ways of an integer

$O(n\sqrt{n})$

```

1  #include <stdio>
2  #include <cmath>
3  #include <cstring>
4  #include <map>
5  #include <algorithm>
6  using namespace std;
7  bool check(int x) {
8      for (int i=2; i*i<=x; i++)
9          if (x%i==0)
10             return 0;
11     return 1;
12 }
13 int p[1000000];
14 inline int calc(int x) {
15     return x*(x+1)/2;
16 }
17 int main() {
18     p[0]=1;
19     for (int i=1; i<1000000; i++) {
20         for (int j=1, k=1; calc(j)<=i; j++, k*=-1) {
21             p[i]+=k*p[i-calc(j)];
22             if (p[i]<0)
23                 p[i]+=1000000;
24             if (p[i]>=1000000)
25                 p[i]-=1000000;
26             if (calc(-j)<=i)
27                 p[i]+=k*p[i-calc(-j)];
28             if (p[i]<0)
29                 p[i]+=1000000;
30             if (p[i]>=1000000)
31                 p[i]-=1000000;
32         }
33         if (!p[i])
34             printf("%d\n", i);
35     }
36     return 0;
37 }

```

5.15 Pell's equation

```

1  import java.math.BigInteger;
2  import java.util.*;
3  public class Main {
4      public static class Fraction {
5          public BigInteger num, den;
6          public Fraction() {
7              num=BigInteger.ZERO;
8              den=BigInteger.ONE;
9          }
10         public Fraction(int _num, int _den) {
11             num=BigInteger.valueOf(_num);
12             den=BigInteger.valueOf(_den);
13         }
14         public Fraction(BigInteger _num, BigInteger _den) {
15             num=_num;
16             den=_den;
17         }
18         public Fraction gen() {
19             BigInteger g=num.gcd(den);

```

```

20     return new Fraction(num.divide(g),den.divide(g));
21 }
22 public Fraction add(Fraction x) {
23     return new Fraction(x.num.multiply(den).add(num.multiply(x.den)),x.den.multiply
        (den)).gen();
24 }
25 public Fraction reciprocal() {
26     return new Fraction(den,num);
27 }
28 public void out() {
29     System.out.println(num+"/"+den);
30 }
31 }
32 public static BigInteger sqrt(BigInteger a) {
33     BigInteger b=a;
34     while (a.compareTo(b.multiply(b))<0)
35         b=b.multiply(b).add(a).divide(b.multiply(BigInteger.valueOf(2)));
36     return b;
37 }
38 public static boolean check(Fraction x,int n) {
39     return x.num.multiply(x.num).add(x.den.multiply(x.den.multiply(BigInteger.valueOf
        (n))))).negate().compareTo(BigInteger.ONE)==0;
40 }
41 static int p[]=new int[1000];
42 static int l;
43 public static void main(String[] args) {
44     BigInteger ans=BigInteger.ZERO;
45     int idx=0;
46     for (int n=2,r=2; n<=1000; n++) {
47         if (n==r*r) {
48             r++;
49             continue;
50         }
51         int tmp=calc(n,0,1),a=tmp,b=n-tmp*tmp;
52         p[0]=tmp;
53         l=1;
54         while (true) {
55             tmp=calc(n,a,b);
56             p[l++]=tmp;
57             a=a-tmp*b;
58             Fraction x=getFrac();
59             if (check(x,n)) {
60                 if (ans.compareTo(x.num)<0) {
61                     ans=x.num;
62                     idx=n;
63                 }
64                 break;
65             }
66             a=-a;
67             b=(n-a*a)/b;
68         }
69     }
70     System.out.println(idx);
71 }
72 private static Fraction getFrac() {
73     Fraction ret=new Fraction(p[l-1],1);
74     for (int i=l-2; i>=0; i--)
75         ret=new Fraction(p[i],1).add(ret.reciprocal());
76     return ret;
77 }
78 private static int calc(int n, int a, int b) {
79     for (long i=2;; i++)
80         if ((i*b-a)*(i*b-a)>n)
81             return (int)i-1;

```

82 | }
83 | }

5.16 Polya

设 G 是 p 个对象的一个置换群，用 k 种颜色去染这 p 个对象，若一种染色方案在群 G 的作用下变为另一种方案，则这两个方案当作是同一种方案，这样的不同染色方案数为：

$$L = \frac{1}{|G|} \times \sum (k^{C(f)}), f \in G$$

$C(f)$ 为循环节， $|G|$ 表示群的置换方法数

对于有 n 个位置的手镯，有 n 种旋转置换和 n 种翻转置换

对于旋转置换：

$$C(f_i) = \gcd(n, i), i \text{ 表示一次转过 } i \text{ 颗宝石}, i = 0 \text{ 时 } c = n;$$

对于翻转置换：

如果 n 为偶数： 则有 $\frac{n}{2}$ 个置换 $C(f) = \frac{n}{2}$ ，有 $\frac{n}{2}$ 个置换 $C(f) = \frac{n}{2} + 1$

如果 n 为奇数： $C(f) = \frac{n}{2} + 1$

5.17 拉格朗日插值法

已知 $y = a_0 + a_1x + a_2x^2 + \cdots + a_{n-1}x^{n-1}$ 曲线上的 n 个点 $(x_1, y_1), (x_2, y_2), (x_3, y_3) \cdots (x_n, y_n)$ 用拉格朗日插值法可以不求系数可知任意 x 对应的 y 值。

$$\begin{aligned} y &= y_1 \frac{(x - x_2)(x - x_3) \cdots (x - x_n)}{(x_1 - x_2)(x_1 - x_3) \cdots (x_1 - x_n)} \\ &+ y_2 \frac{(x - x_1)(x - x_3) \cdots (x - x_n)}{(x_2 - x_1)(x_2 - x_3) \cdots (x_2 - x_n)} \\ &+ \cdots \\ &+ y_n \frac{(x - x_1)(x - x_2) \cdots (x - x_{n-1})}{(x_n - x_1)(x_n - x_2) \cdots (x_n - x_{n-1})} \end{aligned}$$

特别的，如果 $x_1 \sim x_n$ 为连续自然数，那么对于下一个自然数对应的 y 值为：

$$y_{n+1} = (-1)^{n-1} C_n^0 y_1 + (-1)^{n-2} C_n^1 y_2 + \cdots + (-1)^0 C_n^{n-1} y_n$$

这个组合系数可以通过高斯消元求出来，前提是要猜到它满足递推关系。

5.18 正多面体顶点着色

$$\text{正四面体: } N = \frac{(n^4 + 11 \times n^2)}{12}$$

$$\text{正六面体: } N = \frac{(n^8 + 17 \times n^4 + 6 \times n^2)}{24}$$

$$\text{正八面体: } N = \frac{(n^6 + 3 \times n^4 + 12 \times n^3 + 8 \times n^2)}{24}$$

$$\text{正十二面体: } N = \frac{(n^{20} + 15 \times n^{10} + 20 \times n^8 + 24 \times n^4)}{60}$$

$$\text{正二十面体: } N = \frac{(n^{12} + 15 \times n^6 + 44 \times n^4)}{60}$$

5.19 求和公式

$$\begin{aligned}\sum k &= \frac{n \times (n+1)}{2} \\ \sum 2k - 1 &= n^2 \\ \sum k^2 &= \frac{n \times (n+1) \times (2n+1)}{6} \\ \sum (2k-1)^2 &= \frac{n \times (4n^2-1)}{3} \\ \sum k^3 &= \left(\frac{n \times (n+1)}{2}\right)^2 \\ \sum (2k-1)^3 &= n^2 \times (2n^2-1) \\ \sum k^4 &= \frac{n \times (n+1) \times (2n+1) \times (3n^2+3n-1)}{30} \\ \sum k^5 &= \frac{n^2 \times (n+1)^2 \times (2n^2+2n-1)}{12} \\ \sum k \times (k+1) &= \frac{n \times (n+1) \times (n+2)}{3} \\ \sum k \times (k+1) \times (k+2) &= \frac{n \times (n+1) \times (n+2) \times (n+3)}{4} \\ \sum k \times (k+1) \times (k+2) \times (k+3) &= \frac{n \times (n+1) \times (n+2) \times (n+3) \times (n+4)}{5}\end{aligned}$$

5.20 几何公式

球扇形:

全面积: $T = \pi r(2h + r_0)$, h 为球冠高, r_0 为球冠底面半径

体积: $V = \frac{2\pi r^2 h}{3}$

5.21 小公式

Pick 公式: $A = E \times 0.5 + I - 1$ (A 是多边形面积, E 是边界上的整点, I 是多边形内部的整点)

海伦公式: $S = \sqrt{p(p-a)(p-b)(p-c)}$, 其中 $p = \frac{a+b+c}{2}$, abc 为三角形的三条边长

求 $\binom{n}{k}$ 中素因子 P 的个数:

1. 把 n 转化为 P 进制, 并记它每个位上的和为 $S1$
2. 把 $n - k$, k 做同样的处理, 得到 $S2$, $S3$

则 $\binom{n}{k}$ 中素因子 P 的个数: $\frac{S2+S3-S1}{P-1}$

部分错排公式:

$n + m$ 个数中 m 个数必须错排求排列数

```
1 | dp[i] = n*dp[i-1]+(i-1)*(dp[i-1]+dp[i-2]);
2 | dp[0] = n!;
3 | dp[1] = n*n!;
```

$dp[m]$ 为所求解

6 Search

6.1 Dancing links

```
1 | struct DLX {
2 |     int h,n,m,tot;
3 |     int U[MaxN*MaxM],D[MaxN*MaxM],L[MaxN*MaxM],R[MaxN*MaxM],Row[MaxN*MaxM],Col[MaxN*MaxM];
4 |     int S[MaxM],O[MaxN];
```

```

5  bool hasans;
6  void init() {
7      h = 0;
8      hasans = false;
9      tot = m+n;
10     for (int i = 0; i <= m; i++) {
11         D[i] = U[i] = Col[i] = i;
12         Row[i] = S[i] = 0;
13         L[i] = (i+m)%(m+1);
14         R[i] = (i+1)%(m+1);
15     }
16     for (int i = 1; i <= n; i++) {
17         R[i+m] = L[i+m] = i+m;
18         Row[i+m] = i;
19         Col[i+m] = 0;
20     }
21 }
22 void insert(int x,int y) {
23     tot++;
24     Row[tot] = x;
25     Col[tot] = y;
26     S[y]++;
27     int colPos,rowPos;
28     colPos = y;
29     while (true) {
30         colPos = D[colPos];
31         if (colPos == y || Row[colPos] > x)      break;
32     }
33     colPos = U[colPos];
34     if (Row[colPos] == x)      return;
35     U[tot] = colPos;
36     D[tot] = D[colPos];
37     U[D[tot]] = D[U[tot]] = tot;
38     rowPos = x+m;
39     while (true) {
40         rowPos = R[rowPos];
41         if (rowPos == x+m || Col[rowPos] > y)      break;
42     }
43     rowPos = L[rowPos];
44     if (Col[rowPos] == y)      return;
45     L[tot] = rowPos;
46     R[tot] = R[rowPos];
47     L[R[tot]] = R[L[tot]] = tot;
48 }
49 void print(int deep) {
50     for (int i = 0; i < deep; i++)
51         printf("%d_", O[i]);
52     printf("\n");
53 }
54 void cover(int col) {
55     L[R[col]] = L[col];
56     R[L[col]] = R[col];
57     for (int i = D[col]; i != col; i = D[i])
58         for (int j = R[i]; j != i; j = R[j])
59             if (Col[j] != col) {
60                 U[D[j]] = U[j];
61                 D[U[j]] = D[j];
62                 S[Col[j]]--;
63             }
64 }
65 void resume(int col) {
66     for (int i = U[col]; i != col; i = U[i])
67         for (int j = L[i]; j != i; j = L[j])
68             if (Col[j] != col) {

```

```

69         S[Col[j]]++;
70         U[D[j]] = j;
71         D[U[j]] = j;
72     }
73     L[R[col]] = col;
74     R[L[col]] = col;
75 }
76 void initDFS() {
77     for (int i = 1; i <= n; i++) {
78         L[R[i+m]] = L[i+m];
79         R[L[i+m]] = R[i+m];
80     }
81 }
82 void DFS(int deep) {
83     if (hasans == true) return;
84     if (R[0] == 0) {
85         hasans = true;
86         print(deep);
87         return;
88     };
89     int tc = R[0];
90     for (int i = R[0]; i != 0; i = R[i])
91         if (S[i] < S[tc]) tc = i;
92     cover(tc);
93     for (int i = D[tc]; i != tc; i = D[i]) {
94         int temp = O[deep];
95         O[deep] = Row[i];
96         for (int j = R[i]; j != i; j = R[j])
97             cover(Col[j]);
98         DFS(deep+1);
99         for (int j = L[i]; j != i; j = L[j])
100             resume(Col[j]);
101         O[deep] = temp;
102     }
103     resume(tc);
104 }
105 }

```

6.1.1 Usage

```

1 DLX g;
2 g.n = ROW_SIZE;
3 g.m = COL_SIZE;
4 g.init();
5 g.insert(ROW, COL);
6 g.initDFS();
7 g.DFS(0);

```

6.2 Dancing links (A-star)

```

1 namespace DLX {
2     const int MAXN = 1000;
3     const int MAXM = 400;
4     const int INF = 0x3f3f3f3f;
5     int D[MAXN * MAXM], U[MAXN * MAXM], L[MAXN * MAXM], R[MAXN * MAXM], COL[MAXN * MAXM],
        ROW[MAXN * MAXM];
6     int CNT, BEG[MAXN * MAXM], END[MAXN * MAXM], ANS, USE[MAXM], _USE[MAXM];
7     int SUM[MAXM];
8     bool vis[MAXM];
9     void init(int n) {
10         memset(BEG, 0xff, sizeof(BEG));

```



```

11  for(int i = 1; i <= n; i++)
12      SUM[L[i + 1] = R[i - 1] = D[i] = U[i] = i] = 0;
13  L[L[1] = R[n] = 0] = n, CNT = n + 1;
14  ANS = n + 1;
15  }
16  void link(int r, int c) {
17      D[CNT] = D[c], U[CNT] = c, U[D[c]] = CNT, D[c] = CNT, COL[CNT] = c, ROW[CNT] = r,
          SUM[c]++;
18      if (BEG[r] == -1) BEG[r] = END[r] = CNT;
19      R[END[r]] = CNT, L[CNT] = END[r], R[CNT] = BEG[r], L[BEG[r]] = CNT, END[r] = CNT++;
20  }
21  void DLX_Remove_Repeat(int c) {
22      for (int i = D[c]; i != c; i = D[i])
23          L[R[i]] = L[i], R[L[i]] = R[i], SUM[COL[i]]--;
24  }
25  void DLX_Resume_Repeat(int c) {
26      for (int i = U[c]; i != c; i = U[i])
27          L[R[i]] = i, R[L[i]] = i, SUM[COL[i]]++;
28  }
29  int Heuristics() {
30      memset(vis, true, sizeof(vis));
31      int c, i, j, cnt=0;
32      for(c=R[0]; c; c=R[c])
33          if(vis[c])
34              for(cnt++, vis[c] = false, i = D[c]; i != c; i = D[i])
35                  for(j = R[i]; j != i; j = R[j])
36                      vis[COL[j]] = false;
37      return cnt;
38  }
39  void DLX_Dfs(int n) {
40      if (Heuristics() + n >= ANS) return;
41      if (R[0] == 0) {
42          ANS = n;
43          for (int i = 0; i < n; i++)
44              USE[i] = _USE[i];
45          return ;
46      }
47      int i,now = INF,c;
48      for (i = R[0]; i; i = R[i])
49          if (now > SUM[i])
50              now = SUM[c = i];
51      for(i = D[c]; i != c; i = D[i]) {
52          DLX_Remove_Repeat(i);
53          for(int j = R[i]; j != i; j = R[j])
54              DLX_Remove_Repeat(j);
55          _USE[n] = ROW[i];
56          DLX_Dfs(n + 1);
57          for(int j = L[i]; j != i; j = L[j])
58              DLX_Resume_Repeat(j);
59          DLX_Resume_Repeat(i);
60      }
61  }
62  void solve() {
63      //ANS = m
64      DLX_Dfs(0);
65  }
66  };

```

7 String

7.1 Aho-Corasick automation

Don't forget running **BUILD**!

7.1.1 Static memory version

```

1 struct Trie {
2     int next[50][10], fail[50];
3     bool end[50];
4     int L, root;
5     int newNode() {
6         for (int i = 0; i < 10; i++)
7             next[L][i] = -1;
8         end[L] = false;
9         return L++;
10    }
11    void Init() {
12        L = 0;
13        root = newNode();
14    }
15    void Insert(char s[]) {
16        int now = root;
17        for (int i = 0; s[i] != 0; i++) {
18            if (next[now][s[i] - '0'] == -1)
19                next[now][s[i] - '0'] = newNode();
20            now = next[now][s[i] - '0'];
21        }
22        end[now] = true;
23    }
24    void Build() {
25        queue<int> Q;
26        for (int i = 0; i < 10; i++)
27            if (next[root][i] == -1)
28                next[root][i] = root;
29            else {
30                fail[next[root][i]] = root;
31                Q.push(next[root][i]);
32            }
33        while (!Q.empty()) {
34            int now = Q.front();
35            Q.pop();
36            end[now] |= end[fail[now]];
37            for (int i = 0; i < 10; i++)
38                if (next[now][i] == -1)
39                    next[now][i] = next[fail[now]][i];
40                else {
41                    fail[next[now][i]] = next[fail[now]][i];
42                    Q.push(next[now][i]);
43                }
44        }
45    }
46 };

```

7.1.2 Pointer version

```

1 const int CHAR=26;
2 const int TOTLEN=5000000;
3 const int MAXLEN=10000000;
4 struct Vertex {
5     Vertex *fail,*next[CHAR];

```

```

6   Vertex() {}
7   Vertex(bool flag) { //为什么要这样写?
8       fail=0;
9       memset(next,0,sizeof(next));
10  }
11 };
12 int size;
13 Vertex vertex[TOTLEN+1];
14 void init() {
15     vertex[0]=Vertex(0);
16     size=1;
17 }
18 void add(Vertex *pos,int cha) {
19     vertex[size]=Vertex(0);
20     pos->next[cha]=&vertex[size++];
21 }
22 void add(vector<int> s) {
23     int l=s.size();
24     Vertex *pos=&vertex[0];
25     for (int i=0; i<l; i++) {
26         if (pos->next[s[i]]==NULL)
27             add(pos,s[i]);
28         pos=pos->next[s[i]];
29     }
30 }
31 void bfs() {
32     queue<Vertex *> que;
33     Vertex *u=&vertex[0];
34     for (int i=0; i<CHAR; i++)
35         if (u->next[i]!=NULL) {
36             que.push(u->next[i]);
37             u->next[i]->fail=u;
38         } else
39             u->next[i]=u;
40     u->fail=NULL;
41     while (!que.empty()) {
42         u=que.front();
43         que.pop();
44         for (int i=0; i<CHAR; i++)
45             if (u->next[i]!=NULL) {
46                 que.push(u->next[i]);
47                 u->next[i]->fail=u->fail->next[i];
48             } else
49                 u->next[i]=u->fail->next[i];
50     }
51 }

```

7.2 KMP

Match the suffix of $A[\cdots i]$ and the prefix of B

```

1 //Self match
2 int j;
3 p[0] = j = -1;
4 for (int i = 1; i < lb; i++) {
5     while (j >= 0 && b[j + 1] != b[i]) j = p[j];
6     if (b[j + 1] == b[i]) j++;
7     p[i] = j;
8 }
9 //Match
10 j = -1;
11 for (int i = 0; i < la; i++) {
12     while (j >= 0 && b[j + 1] != a[i]) j = p[j];

```

```

13 |   if (b[j + 1] == a[i]) j ++;
14 |   KMP[i] = j + 1;
15 | }

```

7.3 E-KMP

Common prefix of $A[i \dots]$ and B

```

1 | //Self match
2 | int j = 0;
3 | while (j < lb && b[j] == b[j + 1])
4 |     j++;
5 | p[0] = lb, p[1] = j;
6 | int k = 1;
7 | for (int i = 2; i < lb; i++) {
8 |     int Len = k + p[k] - 1, L = p[i - k];
9 |     if (L < Len - i + 1)
10 |         p[i] = L;
11 |     else {
12 |         j = max(0, Len - i + 1);
13 |         while (i + j < lb && b[i + j] == b[j])
14 |             j++;
15 |         p[i] = j, k = i;
16 |     }
17 | }
18 | //Match
19 | j = 0;
20 | while (j < la && j < lb && a[j] == b[j])
21 |     j++;
22 | eKMP[0] = j;
23 | k = 0;
24 | for (int i = 1; i < la; i++) {
25 |     int Len = k + eKMP[k] - 1, L = p[i - k];
26 |     if (L < Len - i + 1)
27 |         eKMP[i] = L;
28 |     else {
29 |         j = max(0, Len - i + 1);
30 |         while (i + j < la && j < lb && a[i + j] == b[j])
31 |             j++;
32 |         eKMP[i] = j, k = i;
33 |     }
34 | }

```

7.4 Manacher

```

1 | const int maxn = 110000;
2 |
3 | char Ma[maxn*2];
4 | int Mp[maxn*2];
5 | void Manacher(char s[], int len) {
6 |     int l = 0;
7 |     Ma[l++] = '.';
8 |     Ma[l++] = ',';
9 |     for (int i = 0; i < len; i++) {
10 |         Ma[l++] = s[i];
11 |         Ma[l++] = ',';
12 |     }
13 |     Ma[l] = 0;
14 |     int pnow = 0, pid = 0;
15 |     for (int i = 1; i < l; i++) {
16 |         if (pnow > i)
17 |             Mp[i] = min(Mp[2*pid-i], pnow-i);

```

```

18     else
19         Mp[i] = 1;
20         for (; Ma[i-Mp[i]] == Ma[i+Mp[i]]; Mp[i]++);
21         if (i+Mp[i] > pnow) {
22             pnow = i+Mp[i];
23             pid = i;
24         }
25     }
26 }
27 /*
28 abaaba
29 . , a , b , a , a , b , a ,
30 0 1 2 1 4 1 2 7 2 1 4 1 2 1
31 */

```

7.5 Suffix array

```

1  const int maxn = 200010;
2  int wx[maxn],wy[maxn],*x,*y,wss[maxn],wv[maxn];
3
4  bool cmp(int *r,int n,int a,int b,int l) {
5      return a+l<n && b+l<n && r[a]==r[b]&&r[a+l]==r[b+l];
6  }
7  void da(int str[],int sa[],int rank[],int height[],int n,int m) {
8      int *s = str;
9      int *x=wx,*y=wy,*t,p;
10     int i,j;
11     for(i=0; i<m; i++)wss[i]=0;
12     for(i=0; i<n; i++)wss[x[i]=s[i]]++;
13     for(i=1; i<m; i++)wss[i]+=wss[i-1];
14     for(i=n-1; i>=0; i--)sa[--wss[x[i]]]=i;
15     for(j=1,p=1; p<n && j<n; j*=2,m=p) {
16         for(i=n-j,p=0; i<n; i++)y[p++]=i;
17         for(i=0; i<n; i++)if(sa[i]-j>=0)y[p++]=sa[i]-j;
18         for(i=0; i<n; i++)wv[i]=x[y[i]];
19         for(i=0; i<m; i++)wss[i]=0;
20         for(i=0; i<n; i++)wss[wv[i]]++;
21         for(i=1; i<m; i++)wss[i]+=wss[i-1];
22         for(i=n-1; i>=0; i--)sa[--wss[wv[i]]]=y[i];
23         for(t=x,x=y,y=t,p=1,i=1,x[sa[0]]=0; i<n; i++)
24             x[sa[i]]=cmp(y,n,sa[i-1],sa[i],j)?p-1:p++;
25     }
26     for(int i=0; i<n; i++) rank[sa[i]]=i;
27     for(int i=0,j=0,k=0; i<n; height[rank[i++]]=k)
28         if(rank[i]>0)
29             for(k?k--:0,j=sa[rank[i]-1];
30                 i+k < n && j+k < n && str[i+k]==str[j+k];
31                 k++);
32 }

```

7.5.1 Longest common prefix

```

1  int lcp(int x,int y) {
2      if (x > y) swap(x,y);
3      if (x == y)
4          return len-sa[x]; //NOTICE!
5      x++;
6      int k = lent[y-x+1];
7      return min(f[x][k],f[y-(1<<k)+1][k]);
8  }
9  //Interval

```

```

10 void getinterval(int pos,int comlen,int& pl,int& pr) {
11     int l,r,mid,cp;
12     l = 0;
13     r = pos;
14     while (l < r) {
15         mid = l+r>>1;
16         cp = lcp(mid,pos);
17         if (cp < comlen)
18             l = mid+1;
19         else
20             r = mid;
21     }
22     pl = l;
23     l = pos;
24     r = len-1;
25     while (l < r) {
26         mid = l+r+1>>1;
27         cp = lcp(pos,mid);
28         if (cp < comlen)
29             r = mid-1;
30         else
31             l = mid;
32     }
33     pr = l;
34 }

```

7.6 Smallest representation

```

1 int Gao(char a[],int len) {
2     int i = 0,j = 1,k = 0;
3     while (i < len && j < len && k < len) {
4         int cmp = a[(j+k)%len]-a[(i+k)%len];
5         if (cmp == 0)
6             k++;
7         else {
8             if (cmp > 0)
9                 j += k+1;
10            else
11                i += k+1;
12            if (i == j) j++;
13            k = 0;
14        }
15    }
16    return min(i,j);
17 }

```

7.7 Hash

```

1 typedef long long ll;
2 typedef unsigned long long ull;
3 const int MAXN = 1000000 + 100;
4 //ll gao[MAXN];
5 ll BL, BR, ML, MR;
6 ull psl[MAXN],psr[MAXN];
7 //call this before everything
8 void init(){
9     int maxx = 1e9;
10    srand(time(0));
11    BL = (ll)maxx + rand() % maxx;
12    BR = (ll)maxx + rand() % maxx;
13    ML = (ll)maxx + rand() % maxx;

```

```

14     MR = (ll)maxx + rand() % maxx;
15 }
16 //n is the max length you need
17 void Hash2(int n){
18     for(int i = 0; i <= n ; i ++){
19         psl[i] = (i == 0 ? 1 : psl[i - 1] * BL) % ML;
20     }
21     for(int i = 0 ; i <= n; i ++){
22         psr[i] = (i == 0 ? 1 : psr[i - 1] * BR) % MR;
23     }
24 }
25 struct _hash{
26     //read your string in here.
27     char str[MAXN];
28     ull hs[MAXN];
29     void build(){
30         int n = strlen(str);
31         ll l = 0, r = 0;
32         for(int i = 0 ; i < n ; i ++){
33             l = (l * BL + str[i]) % ML;
34             r = (r * BR + str[i]) % MR;
35             if(l < 0) l += ML;
36             if(r < 0) r += MR;
37             hs[i + 1] = (l << 32) | r;
38         }
39     }
40     //hash(str[b: e])
41     ll get(int b,int e){
42         ull el = (hs[e] >>32);
43         ull er = (hs[e] & 0xffffffffFULL);
44         ull bl = (hs[b] >> 32);
45         ull br = (hs[b] & 0xffffffffFULL);
46         ll l = el - bl * psl[e-b] % ML;
47         ll r = er - br *psr[e-b] % MR;
48         if(l < 0) l += ML;
49         if(r < 0) r += MR;
50         return (l << 32) | r;
51     }
52 }Hash;

```

8 Tool

8.1 日期函数

```

1 int days[12]={31,28,31,30,31,30,31,31,30,31,30,31};
2 struct date{
3     int year,month,day;
4 };
5 //是否闰年
6 inline bool isleap(int year)
7 {
8     return (year%4==0&&year%100!=0)||year%400==0;
9 }
10 //判合法性
11 inline bool islegal(date a){
12     if (a.month<0||a.month>12) return 0;
13     if (a.month==2)
14         return a.day>0&&a.day<=28+isleap(a.year);
15     return a.day>0&&a.day<=days[a.month-1];
16 }
17 //比较日期大小，正/负表示大于/小于，0表示相等
18 //如果用于sort等，请把-改成<

```

```

19 inline int datecmp(date a,date b){
20     if (a.year!=b.year)
21         return a.year-b.year;
22     if (a.month!=b.month)
23         return a.month-b.month;
24     return a.day-b.day;
25 }
26 //日期转天数偏移({0,1,1}第1天)
27 int date2int(date a){
28     int ret=a.year*365+(a.year-1)/4-(a.year-1)/100+(a.year-1)/400,i;
29     days[1]+=isleap(a.year);
30     for (i=0;i<a.month-1;ret+=days[i++]);
31     days[1]=28;
32     return ret+a.day;
33 }
34 //天数偏移转日期
35 date int2date(int a){
36     date ret;
37     ret.year=a/146097*400;
38     for (a%=146097;a>=365+isleap(ret.year);a-=365+isleap(ret.year),ret.year++);
39     days[1]+=isleap(ret.year);
40     for (ret.month=1;a>=days[ret.month-1];a-=days[ret.month-1],ret.month++);
41     days[1]=28;
42     ret.day=a+1;
43     return ret;
44 }

```

8.2 Bit compression

```

1 int bit[5];
2 inline int getbit26(int sta, int pos) {
3     return sta / bit[pos] % bit[1];
4 }
5 inline int setbit26(int sta, int pos, int val) {
6     return sta / bit[pos + 1] * bit[pos + 1] + val * bit[pos] + sta % bit[pos];
7 }
8 //bin
9 inline int getbit(int sta, int pos) {
10    return (sta >> pos) & 1;
11 }
12 inline int setbit(int sta, int pos, int val) {
13    return ((sta >> (pos + 1)) << (pos + 1)) | (val << pos) | (sta & ((1 << pos) - 1));
14 }

```

8.3 Hash map

```

1 struct hash_map {
2     int head[MOD];
3     struct hash_tables {
4         int key1, key2;
5         long long val;
6         int next;
7     } ele[ELE];
8     int N;
9     int getHash(int key1, int key2) {
10        return (key1 * 1000000 + key2) % MOD;
11    }
12    void init() {
13        memset(head, -1, sizeof(head));
14        N = 0;
15    }

```



```

16 void clear() {
17     for (int i = 0; i < N; i++)
18         head[getHash(ele[i].key1, ele[i].key2)] = -1;
19     N = 0;
20 }
21 int fint(int key1, int key2) {
22     for (int i = head[getHash(key1, key2)]; i != -1; i = ele[i].next) {
23         if (ele[i].key1 == key1 && ele[i].key2 == key2)
24             return i;
25     }
26     return -1;
27 }
28 void insert(int key1, int key2) {
29     int tmp = getHash(key1, key2);
30     ele[N].key1 = key1;
31     ele[N].key2 = key2;
32     ele[N].val = 0;
33     ele[N].next = head[tmp];
34     head[tmp] = N++;
35 }
36 long long get(int key1, int key2) {
37     int tmp = fint(key1, key2);
38     if (tmp == -1) {
39         insert(key1, key2);
40         return ele[N - 1].val;
41     } else
42         return ele[tmp].val;
43 }
44 void set(int key1, int key2, long long val) {
45     int tmp = fint(key1, key2);
46     if (tmp == -1) {
47         insert(key1, key2);
48         ele[N - 1].val = val;
49     } else
50         ele[tmp].val = val;
51 }
52 void add(int key1, int key2, long long val) {
53     int tmp = fint(key1, key2);
54     if (tmp == -1) {
55         insert(key1, key2);
56         ele[N - 1].val += val;
57     } else
58         ele[tmp].val += val;
59 }
60 };

```

8.4 120 bit integer

```

1 struct integer {
2     long long pa, pb;
3     integer() {}
4     integer(long long _pa, long long _pb) {
5         pa = _pa;
6         pb = _pb;
7     }
8     integer negate() {
9         if (pa == 0 && pb == 0)
10             return integer(pa, pb);
11         else if (pa == 0)
12             return integer(pa, -pb);
13         else
14             return integer(-pa, pb);
15     }

```

```

16 integer operator +(const integer& b) const {
17     integer ret = integer(pa + b.pa, pb + b.pb);
18     if (ret.pb >= MOD) {
19         ret.pa += 1;
20         ret.pb -= MOD;
21     }
22     return ret;
23 }
24 bool operator <(const integer& b) const {
25     if (pa == b.pa)
26         return pb < b.pb;
27     return pa < b.pa;
28 }
29 };

```

8.5 Bash script

```

1 while true; do
2     ./gen > input
3     ./sol < input > output.sol
4     ./bf < input > output.bf
5
6     diff output.sol output.bf
7     if [ $? -ne 0 ] ; then break; fi
8 done

```

8.6 Codeblocks settings

```
1 | gnome-terminal -t $TITLE -x
```

8.7 Bit operation

8.7.1 基本操作

注意括号

8.7.2 枚举长为 n 含 k 个 1 的 01 串

```

1 int n = 5, k = 3;
2 for (int s = (1 << k) - 1, u = 1 << n; s < u;) {
3     for (int i = 0; i < n; i++)
4         printf("%d", (((s >> (n - 1 - i)) & 1) == 1));
5     printf("\n");
6
7     int b = s & -s;
8     s = (s + b) | (((s ^ (s + b)) >> 2) / b);
9 }

```

8.8 vimrc

```

1 | syntax on
2
3 | set backspace=start,indent,eol
4 | set showmode
5 | set showcmd
6 | set hlsearch
7 | set nowrap

```

功能	示例	位运算
统计二进制 1 的个数	(1100110 \rightarrow 4D)	__builtin_popcount(x)
取最后一个 1 的 pos(ffs)	(1000010 \rightarrow 2D)	__builtin_ffs(x)
取最后一个 1 的 mask(lsb)	(1000010 \rightarrow 10)	(x & (-x))
去掉最后一位	(101101 \rightarrow 10110)	x shr 1
在最后加一个 0	(101101 \rightarrow 1011010)	x shl 1
在最后加一个 1	(101101 \rightarrow 1011011)	x shl 1+1
把最后一位变成 1	(101100 \rightarrow 101101)	x or 1
把最后一位变成 0	(101101 \rightarrow 101100)	x or 1-1
最后一位取反	(101101 \rightarrow 101100)	x xor 1
把右数第 k 位变成 1	(101001 \rightarrow 101101, $k=3$)	x or (1 shl (k-1))
把右数第 k 位变成 0	(101101 \rightarrow 101001, $k=3$)	x and not (1 shl (k-1))
右数第 k 位取反	(101001 \rightarrow 101101, $k=3$)	x xor (1 shl (k-1))
取末三位	(1101101 \rightarrow 101)	x and 7
取末 k 位	(1101101 \rightarrow 1101, $k=5$)	x and (1 shl k-1)
取右数第 k 位	(1101101 \rightarrow 1, $k=4$)	x shr (k-1) and 1
把末 k 位变成 1	(101001 \rightarrow 101111, $k=4$)	x or (1 shl k-1)
末 k 位取反	(101001 \rightarrow 100110, $k=4$)	x xor (1 shl k-1)
把右边连续的 1 变成 0	(100101111 \rightarrow 100100000)	x and (x+1)
把右起第一个 0 变成 1	(100101111 \rightarrow 100111111)	x or (x+1)
把右边连续的 0 变成 1	(11011000 \rightarrow 11011111)	x or (x-1)
取右边连续的 1	(100101111 \rightarrow 1111)	(x xor (x+1)) shr 1
去掉右起第一个 1 的左边	(100101000 \rightarrow 1000)	x and (x xor (x-1))

```

8 | set smarttab
9 | set autoindent
10 | set tabstop=4
11 | set softtabstop=4
12 | set shiftwidth=4
13 | set number
14 | filetype indent on
15
16 | set makeprg=g++\ '%:p'\ -o\ '%:p.mzry'\ -Wall\ -g
17 | function! Gao()
18 |     exec "silent!w"
19 |     exec "silent!rm!f '%:p.mzry1992'"
20 |     exec "silent!make"
21 |     exec "cw"
22 | endfunction
23 | function! Run()
24 |     call Gao()
25 |     let execFile = expand("%:p").".mzry"
26 |     if filereadable(execFile)
27 |         exec "silent!gnome-terminal -t '%:p.mzry' --working-directory='%:p:h' -x /
                bin/cb_console_runner '%:p.mzry'"
28 |     endif
29 | endfunction
30
31 | colorscheme slate
32 | set gfn=Monospace\ 14
33
34 | map <C-F9> :call Gao()<Enter>
35 | imap <C-F9> <Esc>:call Gao()<Enter>
36 | map <F9> :call Run()<Enter>
37 | imap <F9> <Esc>:call Run()<Enter>
38
39 | map <C-c> :s!^!//<Enter>:noh<Enter>

```

```

40 |imap <C-c> <Esc>:s!^!//<Enter>:noh<Enter>
41 |map <C-x> :s!//!<Enter>:noh<Enter>
42 |imap <C-x> <Esc>:s!//!<Enter>:noh<Enter>

```

9 Appendix

9.1 Template by elfness

9.1.1 AC machine

```

1 |#include<stdio>
2 |#include<cstring>
3 |#include<stdlib>
4 |#include<cmath>
5 |#include<algorithm>
6 |#include<iostream>
7 |using namespace std;
8 |typedef long long LL;
9 |struct tree {
10 |    tree *ne[26],*fail;
11 |    int ct;
12 |} tr[500100],VD,*root,*Q[500100];
13 |int tn;
14 |void init() {
15 |    tr[tn=0]=VD;
16 |    root=tr+(tn++);
17 |}
18 |char s[1000100];
19 |void build() {
20 |    tree *p=root;
21 |    for(int i=0; s[i]; i++) {
22 |        if(p->ne[s[i]-'a']==NULL) {
23 |            tr[tn]=VD;
24 |            p->ne[s[i]-'a']=tr+(tn++);
25 |        }
26 |        p=p->ne[s[i]-'a'];
27 |    }
28 |    p->ct++;
29 |}
30 |void pre() {
31 |    int i,top,tail;
32 |    tree *p,*q;
33 |    top=0;
34 |    tail=0;
35 |    for(i=0; i<26; i++)
36 |        if(root->ne[i]!=NULL) {
37 |            Q[++tail]=root->ne[i];
38 |            root->ne[i]->fail=root;
39 |        } else root->ne[i]=root;
40 |    while(top<tail) {
41 |        p=Q[++top];
42 |        for(i=0; i<26; i++)
43 |            if(p->ne[i]!=NULL) {
44 |                q=p->ne[i];
45 |                Q[++tail]=q;
46 |                q->fail=p->fail->ne[i];
47 |                if(q->fail==NULL)q->fail=root;
48 |            } else p->ne[i]=p->fail->ne[i];
49 |    }
50 |}
51 |int doit() {
52 |    int ret=0;

```

```

53 tree *p=root,*q;
54 for(int i=0; s[i]; i++) {
55     p=p->ne[s[i]-'a'];
56     q=p;
57     while(root!=q&&q->ct!=-1) {
58         ret+=q->ct;
59         q->ct=-1;
60         q=q->fail;
61     }
62 }
63 return ret;
64 }
65 int i,n,_;
66 int main() {
67     for(i=0; i<26; i++)VD.ne[i]=NULL;
68     VD.ct=0;
69     scanf("%d",&_);
70     while(____) {
71         scanf("%d",&n);
72         init();
73         for(i=0; i<n; i++) {
74             scanf("%s",s);
75             build();
76         }
77         pre();
78         scanf("%s",s);
79         printf("%d\n",doit());
80     }
81 }

```

9.1.2 E-KMP

```

1  #include<cstdio>
2  #include<cstring>
3  #include<cstdlib>
4  #include<cmath>
5  #include<algorithm>
6  #include<iostream>
7  using namespace std;
8  typedef long long LL;
9  void e_kmp(char *s,char *t,int *has,int *e_has) {
10     int sp,p,mx,tn;
11     for(sp=p=mx=0; s[p]>0; p++) {
12         if(mx==p || p+e_has[p-sp]>=mx ) {
13             for(tn=mx-p; s[mx]==t[tn]; tn++)mx++;
14             has[sp=p]=mx-p;
15             if(mx==p)sp=++mx;
16         } else has[p]=e_has[p-sp];
17     }
18 }
19 const int V=1001000;
20 char t[V],s[V];
21 int e_has[V],has[V],tn;
22 int main() {
23     scanf("%s%s",s,t);
24     tn=strlen(t);
25     t[tn]=-1;
26     e_has[0] = tn;
27     e_kmp(t+1,t,e_has+1,e_has);
28     e_kmp(s,t,has,e_has);
29 }

```

9.1.3 KM (list)

```

1  #include<cstdio>
2  #include<cstring>
3  #include<cstdlib>
4  #include<cmath>
5  #include<algorithm>
6  using namespace std;
7  const int V=1200;
8  const int En=21000;
9  const int oo=1000000000;
10 struct Edge {
11     int num,ne,w;
12 } e[En];
13 int p[V],K;
14 void add(int x,int y,int z) {
15     e[K].num=y;
16     e[K].w=z;
17     e[K].ne=p[x];
18     p[x]=K++;
19 }
20 bool sx[V],sy[V];
21 int lx[V],ly[V],mat[V];
22 bool path(int u) {
23     sx[u]=true;
24     for(int i=p[u]; i!=-1; i=e[i].ne) {
25         int v=e[i].num;
26         if(!sy[v]&&lx[u]+ly[v]==e[i].w) {
27             sy[v]=true;
28             if(mat[v]==-1||path(mat[v])) {
29                 mat[v]=u;
30                 return true;
31             }
32         }
33     }
34     return false;
35 }
36 int N;
37 int KM() {
38     int i,j;
39     for(i=0; i<N; i++) {
40         lx[i]=-oo;
41         for(j=p[i]; j!=-1; j=e[j].ne)
42             lx[i]=max(lx[i],e[j].w);
43     }
44     for(i=0; i<N; i++) ly[i]=0,mat[i]=-1;
45     for(int u=0; u<N; u++)
46         while(1) {
47             for(i=0; i<N; i++) sx[i]=0,sy[i]=0;
48             if(path(u)) break;
49             int dx=oo;
50             for(i=0; i<N; i++) if(sx[i])
51                 for(j=p[i]; j!=-1; j=e[j].ne)
52                     if(!sy[e[j].num])
53                         dx=min(dx,lx[i]+ly[e[j].num]-e[j].w);
54             if(dx==oo) return -1;
55             for(i=0; i<N; i++) if(sx[i]) lx[i]-=dx;
56             for(i=0; i<N; i++) if(sy[i]) ly[i]+=dx;
57         }
58     int ret=0;
59     for(i=0; i<N; i++) ret+=lx[i]+ly[i];
60     return -ret;
61 }
62 int _,ca,n,m,i,x,y,z,te;

```

```

63 int main() {
64     scanf("%d",&_);
65     ca=0;
66     while(_--) {
67         ca++;
68         scanf("%d%d",&n,&m);
69         N=n;
70         for(i=0; i<n; i++)p[i]=-1;
71         K=0;
72         for(i=0; i<m; i++) {
73             scanf("%d%d%d",&x,&y,&z);
74             x--;
75             y--;
76             add(x,y,-z);
77             add(y,x,-z);
78         }
79         te=KM();
80         printf("Case_%d:_",ca);
81         if(te==-1)puts("NO");
82         else printf("%d\n",te);
83     }
84 }

```

9.1.4 Nearest point pair

```

1  /*
2   * nearestPointPair.cpp
3   *
4   * Created on: 2011-10-10
5   * Author: Fish
6   */
7
8  #include <cstdio>
9  #include <cstring>
10 #include <cstdlib>
11 #include <cmath>
12 #include <algorithm>
13
14 using namespace std;
15
16 const int MaxN = 120000;
17 const int Log = 20;
18
19 struct Point {
20     double x, y;
21     Point() {
22     }
23     Point(double x, double y) :
24         x(x), y(y) {
25     }
26     Point operator-(const Point& p) const {
27         return Point(x - p.x, y - p.y);
28     }
29     double norm() const {
30         return hypot(x, y);
31     }
32     void init() {
33         scanf("%lf%lf", &x, &y);
34     }
35 } p[MaxN];
36 int x[MaxN], y[Log][MaxN], tmp[MaxN], n;
37 bool vst[MaxN];
38

```

```

39 bool comp_x(const int& i, const int& j) {
40     return p[i].x < p[j].x;
41 }
42
43 bool comp_y(const int& i, const int& j) {
44     return p[i].y < p[j].y;
45 }
46
47 double dfs(int k, int l, int r) {
48     double ret = 1e100;
49     if (r - l <= 2) {
50         for (int i = l; i < r; i++)
51             for (int j = i + 1; j <= r; j++)
52                 ret = min(ret, (p[x[i]] - p[x[j]]).norm());
53     }
54     return ret;
55
56     int mid = (l + r) >> 1;
57     int lp = l, rp = mid + 1;
58     for (int i = l; i <= r; i++)
59         vst[x[i]] = i <= mid;
60     for (int i = l; i <= r; i++)
61         if (vst[y[k][i]])
62             y[k + 1][lp++] = y[k][i];
63         else
64             y[k + 1][rp++] = y[k][i];
65     double lhs = dfs(k + 1, l, mid);
66     double rhs = dfs(k + 1, mid + 1, r);
67     double mx = (p[x[mid + 1]].x + p[x[mid]].x) / 2.0;
68     ret = min(lhs, rhs);
69
70     lp = 0;
71     for (int i = l; i <= r; i++)
72         if (fabs(mx - p[y[k][i]].x) < ret)
73             tmp[lp++] = y[k][i];
74
75     for (int i = 0; i < lp; i++)
76         for (int j = 1; j < 8 && i + j < lp && (p[tmp[i + j]].y - p[tmp[i]].y) < ret; j++)
77             ret = min(ret, (p[tmp[i]] - p[tmp[i + j]]).norm());
78
79     return ret;
80 }
81
82 int main() {
83     #ifdef __FISH__
84         freopen("data.in", "r", stdin);
85         freopen("nlogn.out", "w", stdout);
86     #endif
87     while (scanf("%d", &n) == 1 && n) {
88         for (int i = 0; i < n; i++) {
89             p[i].init();
90             x[i] = y[0][i] = i;
91         }
92         sort(x, x + n, comp_x);
93         sort(y[0], y[0] + n, comp_y);
94         printf("%.2f\n", dfs(0, 0, n - 1) / 2.0);
95         // printf("%.6f\n", dfs(0, 0, n - 1));
96     }
97
98     return 0;
99 }

```


9.1.5 SA

```

1  #include<cstdio>
2  #include<cstring>
3  #include<cstdlib>
4  #include<cmath>
5  #include<algorithm>
6  #include<iostream>
7  #include<vector>
8  #include<string>
9  using namespace std;
10 typedef long long LL;
11 const int N=100100;
12 char s[N];    /// 长度+1, 对于非字符串, 加一个小于最小值的元素,
13 int sa[N];    /// 倍增算法, 结果 下标 1~n, 第 i 大的是 sa[i]
14 int rk[N];    /// 第 i 位开始的后缀, 的排名为 rk[i]
15 int wa[N],wb[N],wv[N],rmq[20][N];
16 int sn,to[N];
17 bool cmp(int *y,int a,int b,int L) {
18     return y[a]==y[b]&&y[a+L]==y[b+L];
19 }
20 void da(char *s,int *sa,int len,int dn) {
21     int i,j,p;
22     int *x,*y,*t;
23     x=wa;
24     y=wb;
25     for(i=0; i<dn; i++)rk[i]= 0;
26     for(i=0; i<len; i++)rk[x[i]=s[i]]++;
27     for(i=0; i<dn; i++)rk[i+1]+=rk[i];
28     for(i=len-1; i>=0; i--)sa[--rk[x[i]]]=i;
29     for(j=1,p=1; p<len; j*=2,dn=p) {
30         for(p=0; p<j; p++)y[p]=len-j+p;
31         for(i=0; i<len; i++)if(sa[i]>=j)y[p++]=sa[i]-j;
32         for(i=0; i<len; i++)wv[i]=x[y[i]];
33         for(i=0; i<dn; i++)rk[i]=0;
34         for(i=0; i<len; i++)rk[wv[i]]++;
35         for(i=0; i<dn; i++)rk[i+1]+=rk[i];
36         for(i=len-1; i>=0; i--)sa[--rk[wv[i]]]=y[i];
37         swap(x,y);
38         x[sa[0]]=0;
39         for(p=i=1; i<len; i++) {
40             p+=!cmp(y,sa[i],sa[i-1],j);
41             x[sa[i]]=p-1;
42         }
43     }
44 }
45 void find_height(char *s,int *sa,int len) {
46     int *h=rmq[0];
47     int i,j,k=0;
48     for(i=1; i<=len; i++)
49         rk[sa[i]] = i;
50     for(i=0; i<len; i++) {
51         if(k>0)k--;
52         j=sa[rk[i]-1];
53         while(s[i+k]==s[j+k])k++;
54         h[rk[i]]=k;
55     }
56 }
57 void RMQ(int n) {
58     int i,j;
59     int rn=(int)floor(log(n*2.0)/log(2.0));
60     for(i=1; i<rn; i++)
61         for(j=0; j<n+2-(1<<(i-1)); j++)
62             rmq[i][j]=min(rmq[i-1][j],rmq[i-1][j+(1<<(i-1))]);

```

```

63 }
64 int askRMQ(int a,int b) { /// [a,b] 闭区间
65     int rq=to[b-a];
66     return min(rmq[rq][a],rmq[rq][b+1-(1<<rq)]);
67 }
68 void PT(char *s,int *sa) {
69     int i,sn;
70     sn=strlen(s);
71     for(i=0; i<sn; i++)
72         puts(s+sa[i+1]);
73     puts("");
74     for(i=0; i<sn; i++)
75         printf("rank_%d=%d\n",i,rk[i]);
76 }
77 int lcp(int a,int b,int len) {
78     if(a==b)
79         return len-a;
80     a=rk[a];
81     b=rk[b];
82     if(a>b)swap(a,b);
83     return askRMQ(a+1,b);
84 }
85 void pre_log() {
86     int i;
87     to[0]=to[1]=0;
88     for(i=1; i*2<N; i++)
89         to[i*2]=to[i*2+1]=to[i]+1;
90 }
91 int main() {
92     int T,_=0;
93     pre_log();
94     while(~scanf("%s",s)) {
95         sn=strlen(s);
96         da(s,sa,sn+1,128);
97         find_height(s,sa,sn);
98         RMQ(sn);
99         PT(s,sa);
100         scanf("%d",&T);
101         while(T--) {
102             int a,b;
103             scanf("%d%d",&a,&b);
104             a--,b--;/// 求原串的 a b 开始的后缀的公共前缀
105             printf("lcp_%d=%d\n",lcp(a,b,sn));
106         }
107     }
108     return 0;
109 }

```

9.1.6 SAP

```

1  #include<cstdio>
2  #include<cstring>
3  #include<cstdlib>
4  #include<cmath>
5  #include<algorithm>
6  using namespace std;
7  const int V=220;
8  const int En=200000;
9  const int oo=0x3f3f3f3f;
10 struct Edge {
11     int num,ne,c;
12 } e[En];
13 int d[V],p[V],pre[V],low[V];

```

```

14 int gap[V],cur[V];
15 int N,K,st,ed;
16 void add(int x,int y,int c) {
17     e[K].num=y;
18     e[K].c=c;
19     e[K].ne=p[x];
20     p[x]=K++;
21     e[K].num=x;
22     e[K].c=0;
23     e[K].ne=p[y];
24     p[y]=K++;
25 }
26 int sap() {
27     int ret=0;
28     bool fail;
29     for(int i=0; i<=N; i++) {
30         low[i]=gap[i]=d[i]=0;
31         cur[i]=p[i];
32     }
33     low[st]=oo;
34     gap[0]=N;
35     int u=st;
36     while(d[st]<N) {
37         fail=true;
38         for(int i=cur[u]; i!=-1; i=e[i].ne) {
39             int v=e[i].num;
40             cur[u]=i;
41             if(e[i].c&& d[u]==d[v]+1) {
42                 pre[v]=i;
43                 low[v]=min(low[u],e[i].c);
44                 u=v;
45                 if(u==ed) {
46                     do {
47                         e[pre[u]].c-=low[ed];
48                         e[pre[u]^1].c+=low[ed];
49                         u=e[pre[u]^1].num;
50                     } while(u!=st);
51                     ret+=low[ed];
52                 }
53                 fail=false;
54                 break;
55             }
56         }
57         if(fail) {
58             gap[d[u]]--;
59             if(!gap[d[u]])return ret;
60             d[u]=N;
61             for(int i=p[u]; i!=-1; i=e[i].ne)
62                 if(e[i].c)d[u]=min(d[u],d[e[i].num]+1);
63             gap[d[u]]++;
64             cur[u]=p[u];
65             if(u!=st)u=e[pre[u]^1].num;
66         }
67     }
68     return ret;
69 }

```

9.1.7 一般图最大匹配

```

1 #include <stdio.h>
2 #include <string.h>
3 #include <algorithm>
4 #include <vector>

```

```

5 #define maxn 300
6 #define maxm 90010
7
8 using namespace std;
9
10 int match[maxn];           //标记是否匹配
11 int st[maxn],aim[maxm],nxt[maxm],ln; //边表
12 int q[maxn];               //bfs队列
13 int level[maxn];           //离根深度的奇偶性
14 vector<int> ar[maxn];       //存每个点到根的路径
15 vector<int> a;              //找到的一条增广路
16 int n;
17 void init() {
18     for(int i=0; i<n; i++)st[i]=-1;
19     ln=0;
20 }
21 void in_edge(int x,int y) {
22     aim[ln]=y;
23     nxt[ln]=st[x];
24     st[x]=ln++;
25 }
26 int lca(int p,int q) {      //求p和q的最近公共祖先
27     int ret=0;
28     while (ret<ar[p].size() && ret<ar[q].size() && ar[p][ret]==ar[q][ret]) ret++;
29     return ret-1;
30 }
31 int FindAlterRoad(int sp) {
32     int qn=1;
33     memset(level,-1,sizeof(level));
34     level[q[0]=sp]=1;
35     ar[sp].clear();
36     ar[sp].push_back(sp);
37     for (int p=0; p<qn; p++) {
38         int x=q[p];
39         for (int i=st[x]; i!=-1; i=nxt[i]) {
40             int u=aim[i];
41             if (match[u]==u) continue;
42             if (level[u]==-1) { //u是未访问的点
43                 if (match[u]==-1) { //u是未匹配的,找到增广路
44                     a=ar[x];
45                     a.push_back(u);
46                     return 1;
47                 } else { //u是已匹配的点
48                     int v=match[u];
49                     if (level[v]!=-1) continue;
50                     ar[v]=ar[x];
51                     ar[v].push_back(u);
52                     ar[v].push_back(v);
53                     level[u]=0;
54                     level[v]=1;
55                     q[qn++]=v;
56                 }
57             } else if (level[u]==1) { //u和x同为偶点.形成花
58                 int root=lca(u,x);
59                 vector<int> tmp=ar[x];
60                 for (int i=ar[u].size()-1; i>root; i--) {
61                     int y=ar[u][i];
62                     tmp.push_back(y);
63                     if (level[y]==0) {
64                         level[y]=1;
65                         ar[y]=tmp;
66                         level[y]=1;
67                         q[qn++]=y;
68                     }

```

```

69     }
70     tmp=ar[u];
71     for (int i=ar[x].size()-1; i>root; i--) {
72         int y=ar[x][i];
73         tmp.push_back(y);
74         if (level[y]==0) {
75             level[y]=1;
76             ar[y]=tmp;
77             level[y]=1;
78             q[qn++]=y;
79         }
80     }
81 }
82 }
83 }
84 return 0;
85 }
86 int MaximumMatch() {
87     int ret=0; //最大匹配数
88     memset(match,-1,sizeof(match));
89     for (int i=0; i<n; i++)
90         if (match[i]==-1)
91             if (FindAlterRoad(i)) {
92                 for (int i=0; i<a.size(); i+=2) {
93                     int u=a[i],v=a[i+1];
94                     match[u]=v;
95                     match[v]=u;
96                 }
97                 ret++;
98             } else match[i]=i;
99     return ret;
100 }

```

9.1.8 上下界最大流

```

1  /*
2  Author: elfness@UESTC
3  */
4  #include<cstdio>
5  #include<cstring>
6  #include<cstdlib>
7  #include<cmath>
8  #include<algorithm>
9  #include<iostream>
10 #include<vector>
11 #include<string>
12 using namespace std;
13 typedef long long LL;
14 const int V=1500;
15 const int En=9000000;
16 const int inf=0x3f3f3f3f;
17 struct Edge {
18     int num,ne;
19     int c;
20 } e[En];
21 int p[V],K;
22 void add(int x,int y,int c) {
23     e[K].num=y;
24     e[K].c=c;
25     e[K].ne=p[x];
26     p[x]=K++;
27     e[K].num=x;
28     e[K].c=0;

```

```

29     e[K].ne=p[y];
30     p[y]=K++;
31 }
32 int d[V],pre[V],pree[V],gap[V],cur[V];
33 int N,st,ed;
34 int low[V];
35 int sap() {
36     int ret=0;
37     bool fail;
38     for(int i=0; i<=N; i++) {
39         d[i]=0;
40         gap[i]=0;
41         cur[i]=p[i];
42         low[i]=0;
43     }
44     low[st]=inf;
45     gap[0]=N;
46     int u=st;
47     while(d[st]<N) {
48         fail=true;
49         for(int i=cur[u]; i!=-1; i=e[i].ne) {
50             int v=e[i].num;
51             cur[u]=i;
52             if(e[i].c&&d[u]==d[v]+1) {
53                 pre[v]=u;
54                 pree[v]=i;
55                 low[v]=min(low[u],e[i].c);
56                 u=v;
57                 if(u==ed) {
58                     do {
59                         e[pree[u]].c-=low[ed];
60                         e[pree[u]^1].c+=low[ed];
61                         u=pree[u];
62                     } while(u!=st);
63                     ret+=low[ed];
64                 }
65                 fail=false;
66                 break;
67             }
68         }
69         if(fail) {
70             gap[d[u]]--;
71             if(!gap[d[u]])return ret;
72             d[u]=N;
73             for(int i=p[u]; i!=-1; i=e[i].ne)
74                 if(e[i].c)d[u]=min(d[u],d[e[i].num]+1);
75             gap[d[u]]++;
76             cur[u]=p[u];
77             if(u!=st)u=pree[u];
78         }
79     }
80     return ret;
81 }
82 int n,m,s,t;
83 struct Elf {
84     int u,v,lo,up;
85 } b[12000];
86 int lb[12000];
87 int doit() {
88     int i;
89     N=n+2;
90     st=n;
91     ed=n+1;
92     for(i=0; i<N; i++)p[i]=-1;

```

```

93  K=0;
94  for(i=0; i<n; i++)lb[i]=0;
95  for(i=0; i<m; i++) {
96      lb[b[i].u]-=b[i].lo;
97      lb[b[i].v]+=b[i].lo;
98      add(b[i].u,b[i].v,b[i].up-b[i].lo);
99  }
100 for(i=0; i<n; i++) {
101     if(lb[i]>0)add(st,i,lb[i]);
102     else add(i,ed,-lb[i]);
103 }
104 add(t,s,inf);
105 int te=sap();
106 for(i=p[st]; i!=-1; i=e[i].ne)
107     if(e[i].c!=0)return -1;
108 st=s;
109 ed=t;
110 te=sap();
111 return te;
112 }

```

9.1.9 上下界最小流

```

1  #include<cstdio>
2  #include<cstdlib>
3  #include<cstring>
4  #include<cmath>
5  #include<algorithm>
6  using namespace std;
7  const int V=600;
8  const int En=50000;
9  const int oo=0x3f3f3f3f;
10 struct Edge {
11     int num,ne,c;
12 } e[En];
13 int p[V],K;
14 void add(int x,int y,int c) {
15     e[K].num=y;
16     e[K].c=c;
17     e[K].ne=p[x];
18     p[x]=K++;
19     e[K].num=x;
20     e[K].c=0;
21     e[K].ne=p[y];
22     p[y]=K++;
23 }
24 int d[V],cur[V],low[V],pre[V],gap[V],pree[V];
25 int st,ed,N;
26 int sap() {
27     int ret=0;
28     bool fail;
29     memset(gap,0,sizeof(gap));
30     memset(low,0,sizeof(low));
31     memset(d,0,sizeof(d));
32     for(int i=0; i<N; i++)cur[i]=p[i];
33     gap[0]=N;
34     low[st]=oo;
35     int u=st;
36     while(d[st]<N) {
37         fail=true;
38         for(int i=cur[u]; i!=-1; i=e[i].ne) {
39             int v=e[i].num;
40             cur[u]=i;

```

```

41     if(e[i].c&& d[u]==d[v]+1) {
42         pre[v]=u;
43         pree[v]=i;
44         low[v]=min(low[u],e[i].c);
45         u=v;
46         if(u==ed) {
47             do {
48                 e[pree[u]].c-=low[ed];
49                 e[pree[u]^1].c+=low[ed];
50                 u=pree[u];
51             } while(u!=st);
52             ret+=low[ed];
53         }
54         fail=false;
55         break;
56     }
57 }
58 if(fail) {
59     gap[d[u]]--;
60     if(!gap[d[u]]) return ret;
61     d[u]=N;
62     for(int i=p[u]; i!=-1; i=e[i].ne)
63         if(e[i].c) d[u]=min(d[u],d[e[i].num]+1);
64     gap[d[u]]++;
65     cur[u]=p[u];
66     if(u!=st) u=pre[u];
67 }
68 }
69 return ret;
70 }
71 struct ELF {
72     int u,v,lo;
73 } b[En];
74 int n,m,lb[V],ts,tt;
75 void solve() {
76     N=n+4;
77     ts=0;
78     tt=n+1;
79     st=n+2;
80     ed=n+3;
81     memset(lb,0,sizeof(lb));
82     int i,u,v;
83     for(i=0; i<N; i++) p[i]=-1;
84     K=0;
85     for(i=0; i<m; i++) {
86         u=b[i].u;
87         v=b[i].v;
88         lb[v]+=b[i].lo;
89         lb[u]-=b[i].lo;
90         add(u,v,oo-b[i].lo);
91     }
92     for(i=1; i<=n; i++) {
93         add(ts,i,oo);
94         add(i,tt,oo);
95     }
96     for(i=0; i<n+2; i++) {
97         if(lb[i]>0) add(st,i,lb[i]);
98         else add(i,ed,-lb[i]);
99     }
100     int ans=sap();
101     add(tt,ts,oo);
102     printf("%d\n",sap());
103 }
104 int _,ca,i;

```



```

105 int main() {
106     scanf("%d",&_);
107     ca=0;
108     while(_--) {
109         ca++;
110         scanf("%d%d",&n,&m);
111         for(i=0; i<m; i++) {
112             scanf("%d%d%d",&b[i].u,&b[i].v,&b[i].lo);
113         }
114         printf("Case_#%d:_",ca);
115         solve();
116     }
117 }

```

9.1.10 全局最小割

```

1  using namespace std;
2  #define inf 1000000000
3  bool visit[502],com[502];
4  int map[502][502],W[502],s,t;
5  int maxadj(int N,int V) {
6      int CUT;
7      memset(visit,0,sizeof(visit));
8      memset(W,0,sizeof(W));
9      for(int i=0; i<N; i++) {
10         int Num=0,Max=-inf;
11         for(int j=0; j<V; j++)
12             if(!com[j]&&!visit[j]&&W[j]>Max) {
13                 Max=W[j];
14                 Num=j;
15             }
16         visit[Num]=true;
17         s=t;
18         t=Num;
19         CUT=W[t];
20         for(int j=0; j<V; j++)
21             if(!com[j]&&!visit[j])W[j]+=map[Num][j];
22     }
23     return CUT;
24 }
25 int stoer(int V) {
26     int Mincut=inf;
27     int N=V;
28     memset(com,0,sizeof(com));
29     for(int i=0; i<V-1; i++) {
30         int Cut;
31         s=0,t=0;
32         Cut=maxadj(N,V);
33         N--;
34         if(Cut<Mincut)Mincut=Cut;
35         com[t]=true;
36         for(int j=0; j<V; j++)
37             if(!com[j]) {
38                 map[j][s]+=map[j][t];
39                 map[s][j]+=map[t][j];
40             }
41     }
42     return Mincut;
43 }

```

9.1.11 最小树型图

```

1  #include<stdio>
2  #include<cstring>
3  #include<stdlib.h>
4  #include<cmath>
5  #include<algorithm>
6  using namespace std;
7  const int V=1200;
8  const int En=2100000;
9  struct Elf {
10     int u,v,len;
11 } b[En];
12 const int oo=1000000000;
13 int ret;
14 int N,M,Root;//点数，边数，根，默认从0开始
15 int id[V],pre[V],cnt,vis[V];
16 int in[V];
17 bool TreeMST() {
18     ret=0;
19     int i,u,v;
20     while(1) {
21         for(i=0; i<N; i++)
22             in[i]=oo;
23         memset(pre,-1,sizeof(pre));
24         for(i=0; i<M; i++) {
25             u=b[i].u;
26             v=b[i].v;
27             if(b[i].len<in[v]&&u!=v) {
28                 pre[v]=u;
29                 in[v]=b[i].len;
30             }
31         }
32         for(i=0; i<N; i++) {
33             if(i==Root)continue;
34             if(pre[i]==-1)return false;
35         }
36         in[Root]=0;
37         cnt=0;
38         memset(id,-1,sizeof(id));
39         memset(vis,-1,sizeof(vis));
40         for(i=0; i<N; i++) {
41             ret+=in[i];
42             v=i;
43             while(vis[v]!=i&&id[v]==-1&&v!=Root) {
44                 vis[v]=i;
45                 v=pre[v];
46             }
47             if(v!=Root&&id[v]==-1) {
48                 for(u=pre[v]; u!=v; u=pre[u])
49                     id[u]=cnt;
50                 id[v]=cnt++;
51             }
52         }
53         if(cnt==0)return true;
54         for(i=0; i<N; i++)
55             if(id[i]==-1)id[i]=cnt++;
56         for(i=0; i<M; i++) {
57             v=b[i].v;
58             b[i].u=id[b[i].u];
59             b[i].v=id[b[i].v];
60             if(b[i].u!=b[i].v)
61                 b[i].len-=in[v];
62         }
63         N=cnt;
64         Root=id[Root];

```

```
65 | }  
66 | return true;  
67 | }
```