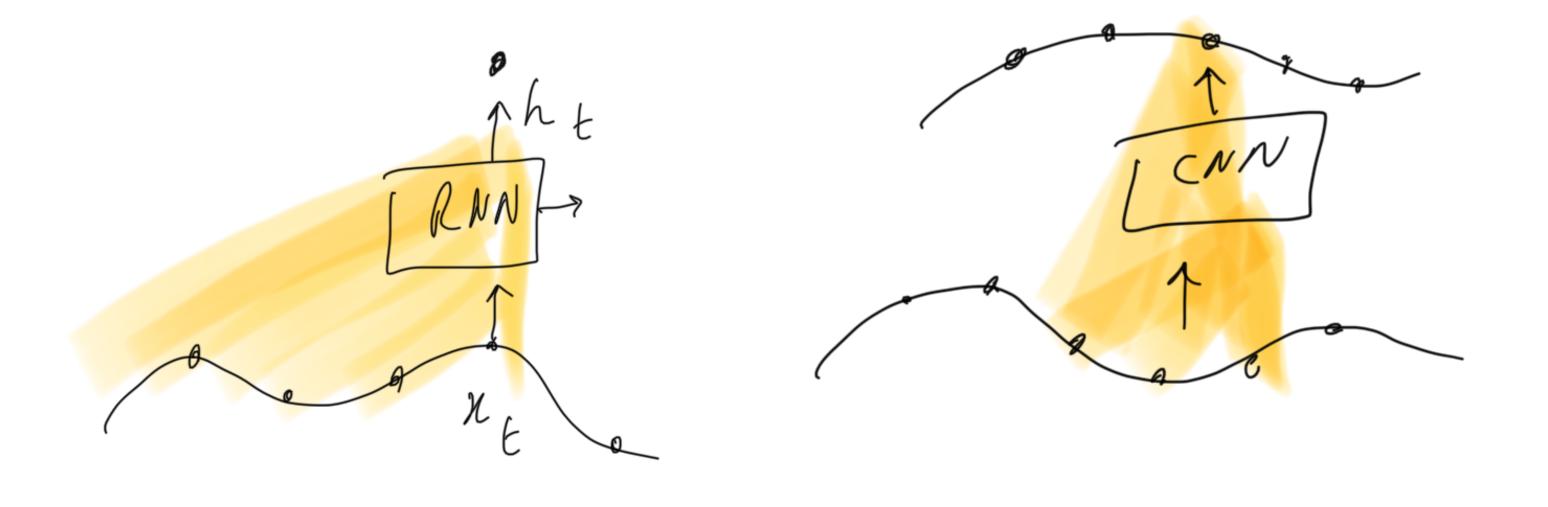
Transformers for Time Series Forecasting

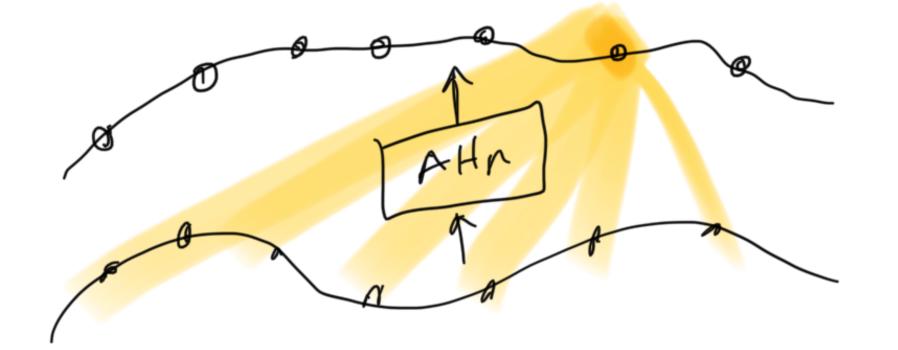
Kashif Rasul (PhD)

ISF: Deep Learning for Forecasting 25.06.2023

Neural Forecasting Models

- 1. Some aspect that learns a representation over history:
 - RNN
 - MLP, CNN
 - Attention/Transformer
 - GNNs etc.
- 2. Some aspect that models the emissions appropriately:
 - Point emissions
 - Probabilistic etc.





Y= {véc, vécz, ··· Vecn} veci EIRD Veci EIRD AHN X= { vec, vec, ··· Vec N?

 $X = \{\vec{n}_1, \vec{n}_2, \dots, \vec{n}_N\} \in \mathbb{R}^{N \times D}$ E = X.XT EIRNXN Similarity Scaling > Score A = Softmax (E, dim=1) Prob. Weights

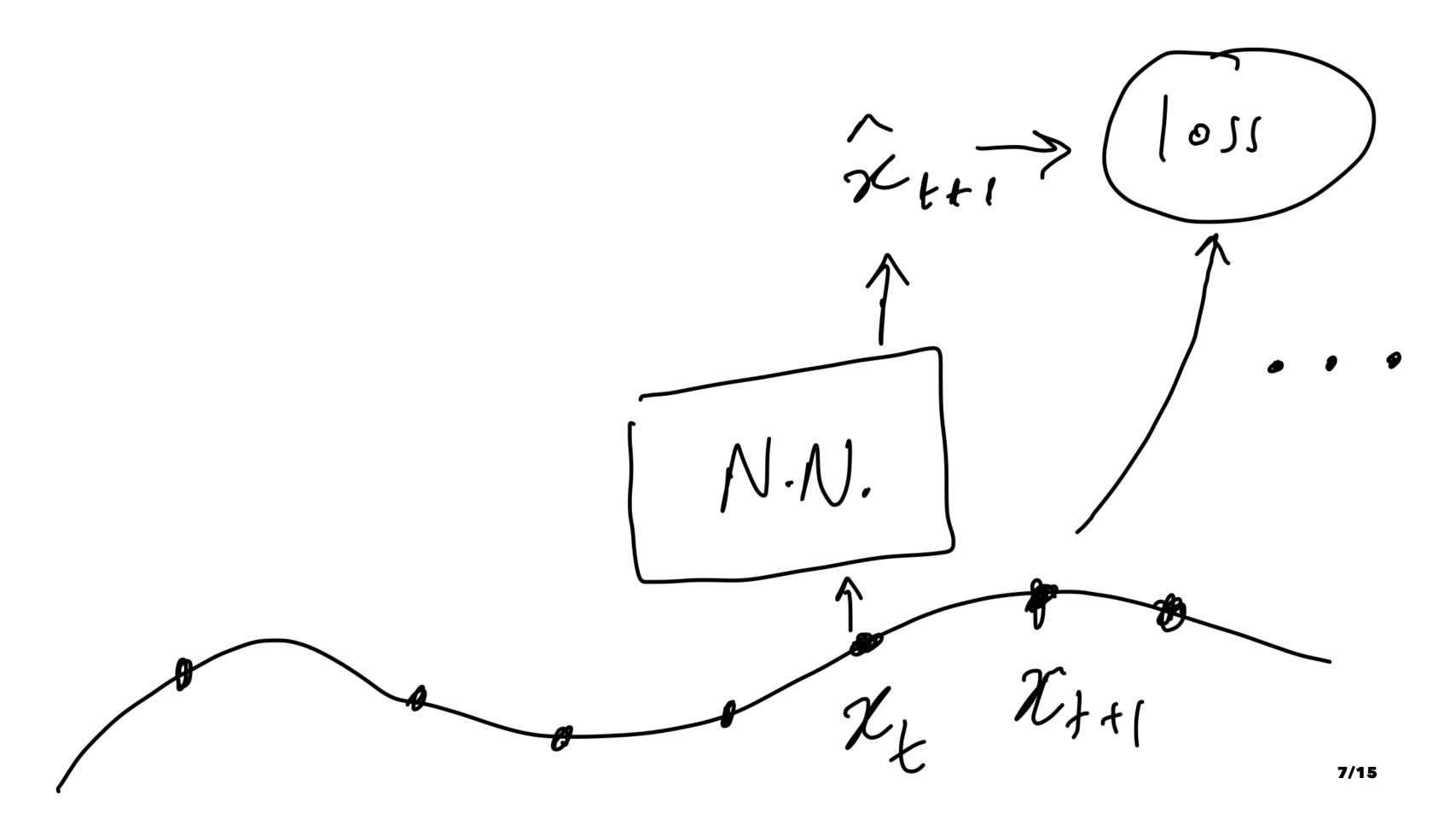
ERNXN Y = A. X e RNXD

5/15

$$X = \{\vec{x}_1, \dots, \vec{x}_N\} \in \mathbb{N}^{N \times 0}$$
Learnable: $Q(X); Y(X); Y(X) : \mathbb{R}^{N \times 0}$

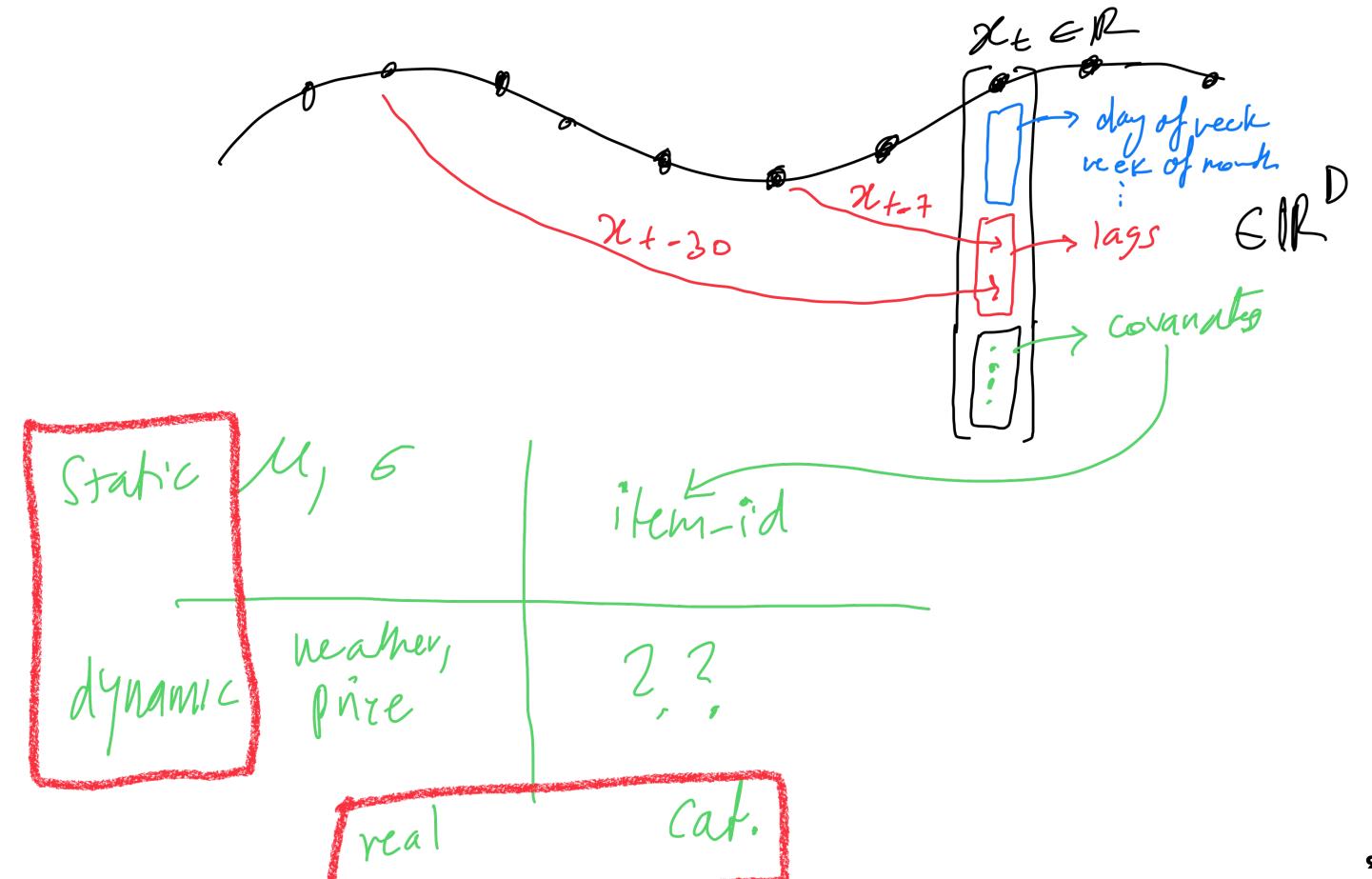
$$E = Q \cdot K^{T}$$

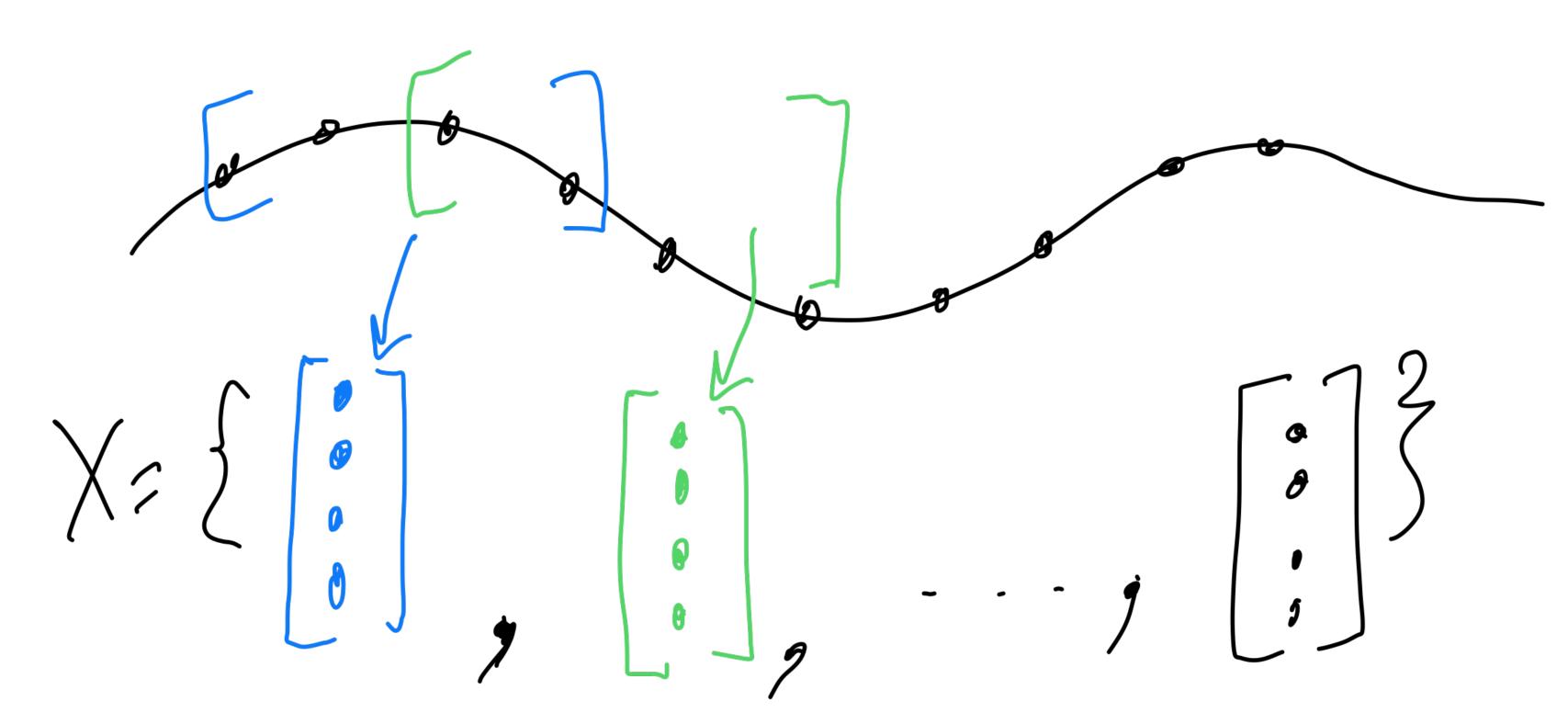
$$Y = A \cdot V \in \mathbb{R}^{N \times 0}$$

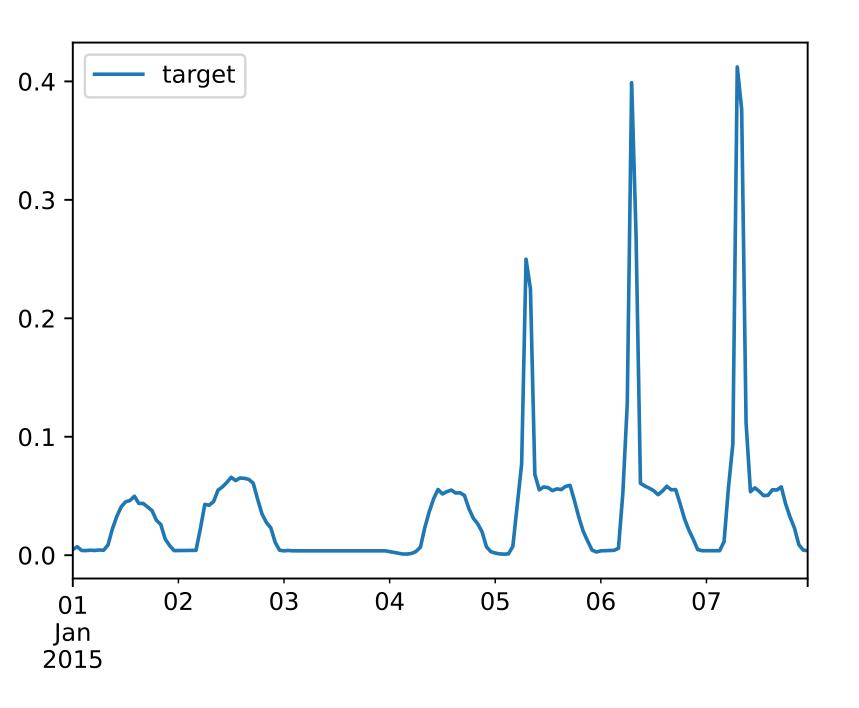


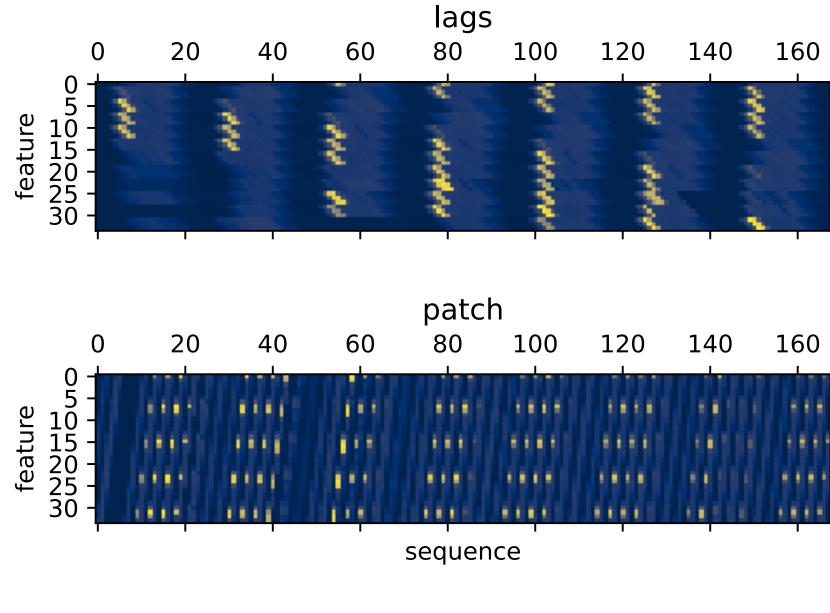
Majvec, vecz, ..., sech

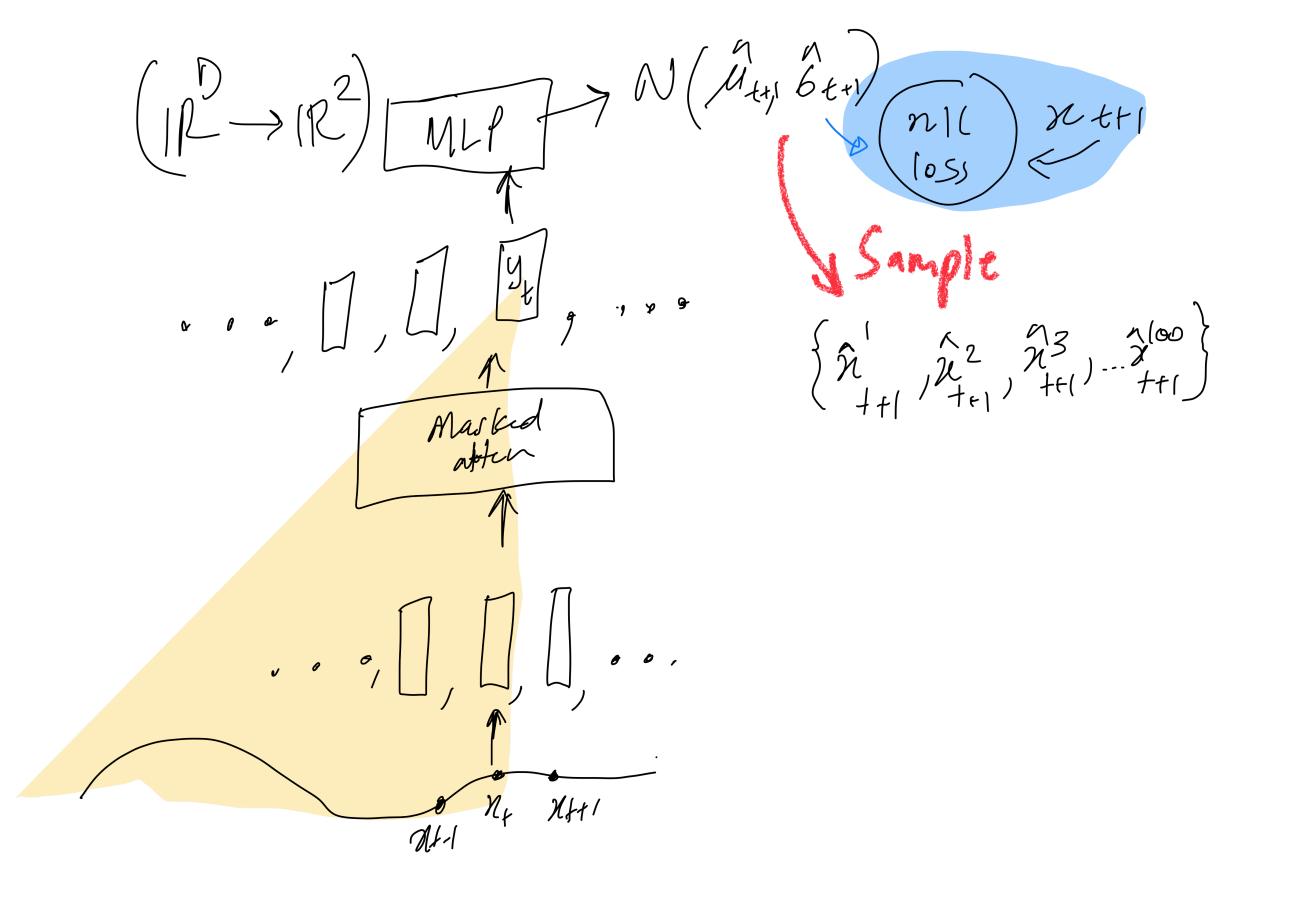
 $M = \begin{pmatrix} -\infty & -\infty \\ -\infty & -\infty \end{pmatrix} \in \mathbb{R}^{N_{RW}}$ A= softmax (E-M, d=1) T= A.X

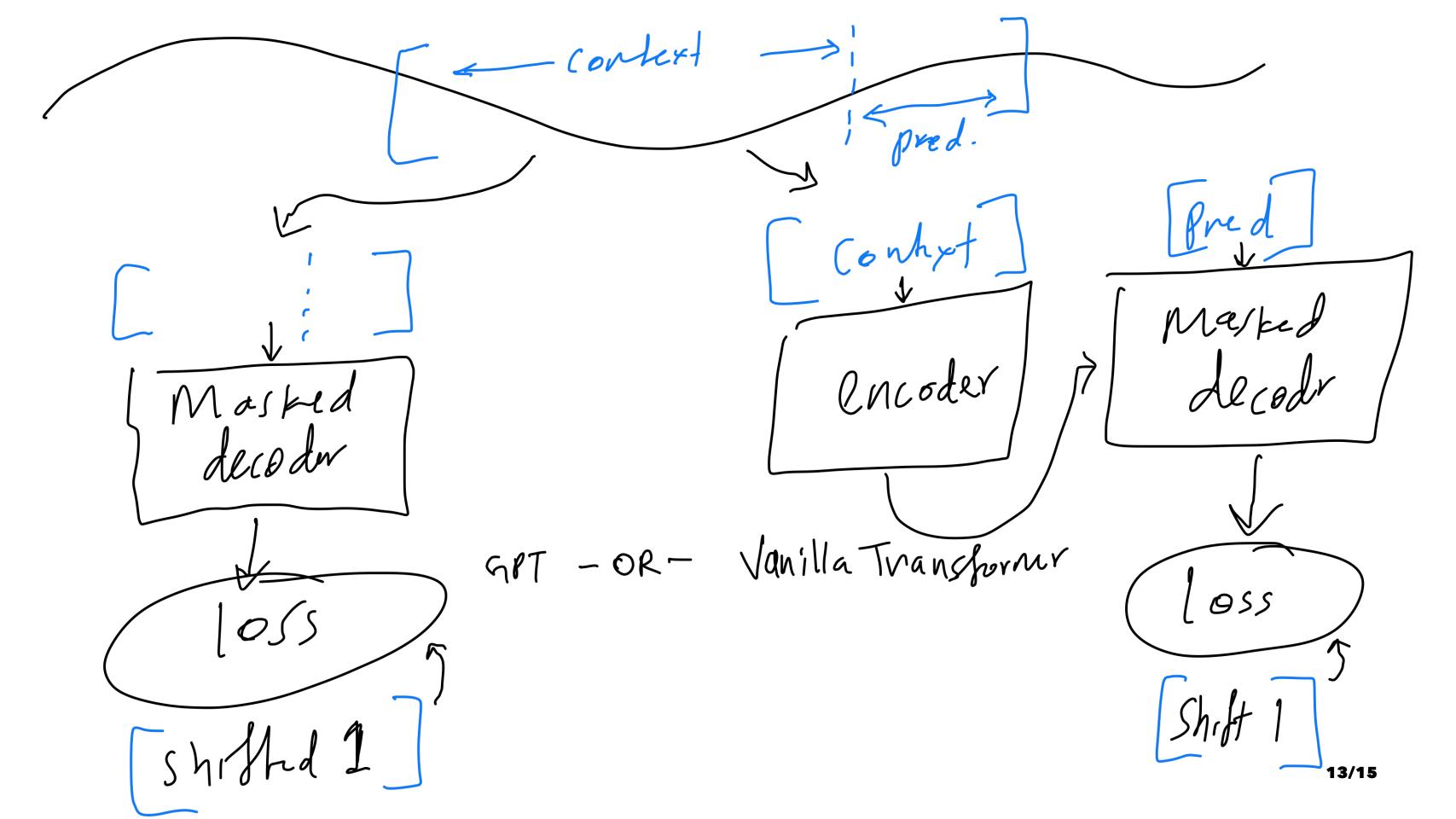












Pros/Cons

- Lean model temporal dependencies efficiently (number of parameters) without forgetting
- de Can handle nans naturally (similar to causal masking)
- Compute and memory is quadratic in number of input sequence size
- Auto-regressive inference can be restrictive for larger models due to need of many samples

Summary

- Transformers provide excellent inductive bias for forecasting
- Temporal covariates naturally serve as positional encoding
- Can potentially condition on any point in the past context window
- Fast to train and allows for auto-regressive sampling
- Naturally incorporate nans/missing data
- Code on Github: <u>kashif/pytorch-transformer-ts</u>