Developer's Guide

 \mathbf{to}

the PARI library

(version 2.11.0)

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Table of Contents

Chapter 1: Work in progress	. 5
1.1 The type t_CLOSURE	. 5
1.1.1 Debugging information in closure	. 6
1.2 The type t_LIST	. 6
1.2.1 Maps as Lists	. 7
1.3 Protection of non-interruptible code	. 8
1.3.1 Multithread interruptions	. 8
1.4 $\mathbf{F} l^2$ field for small primes l	. 9
1.5 Public functions useless outside of GP context	. 9
1.5.1 Conversions	. 9
1.5.2 Output	. 10
1.5.3 Input	. 10
1.5.4 Control flow statements	. 10
1.5.5 Accessors	. 11
1.5.6 Iterators	. 11
1.5.7 Local precision	. 11
1.5.8 Functions related to the GP evaluator	. 11
1.5.9 Miscellaneous	. 12
1.6 Embedded GP interpretor	12
1.7 Readline interface	12
1.8 Constructors called by pari_init functions	13
1.9 Destructors called by pari_close	13
1.10 Constructors and destructors used by the pthreads interface	
Chapter 2: Regression tests, benches	
2.1 Functions for GP2C	
2.1.1 Functions for safe access to components	
Chapter 3: Parallelism	17
3.1 The PARI MT interface	
3.1.1 Miscellaneous	
3.2 Initialization	
Index	

Chapter 1:

Work in progress

This draft documents private internal functions and structures for hard-core PARI developers. Anything in here is liable to change on short notice. Don't use anything in the present document, unless you are implementing new features for the PARI library. Try to fix the interfaces before using them, or document them in a better way. If you find an undocumented hack somewhere, add it here.

Hopefully, this will eventually document everything that we buried in paripriv.h or even more private header files like anal.h. Possibly, even implementation choices! Way to go.

1.1 The type t_CLOSURE.

This type holds closures and functions in compiled form, so is deeply linked to the internals of the GP compiler and evaluator. The length of this type can be 6, 7 or 8 depending whether the object is an "inline closure", a "function" or a "true closure".

A function is a regular GP function. The GP input line is treated as a function of arity 0.

A true closure is a GP function defined in a non-empty lexical context.

An inline closure is a closure that appears in the code without the preceding -> token. They are generally attached to the prototype code 'E' and 'I'. Inline closures can only exist as data of other closures, see below.

In the following example,

```
f(a=Euler)=x->sin(x+a);
g=f(Pi/2);
plot(x=0,2*Pi,g(x))
```

f is a function, g is a true closure and both Euler and g(x) are inline closures.

This type has a second codeword z[1], which is the arity of the function or closure. This is zero for inline closures. To access it, use

```
long closure_arity(GEN C)
```

• z[2] points to a t_STR which holds the opcodes. To access it, use

```
GEN closure_get_code(GEN C).
```

const char * closure_codestr(GEN C) returns as an array of char starting at 1.

- \bullet z[3] points to a t_VECSMALL which holds the operands of the opcodes. To access it, use
- GEN closure_get_oper(GEN C)
- \bullet z[4] points to a t_VEC which hold the data referenced by the pushgen opcodes, which can be t_CLOSURE, and in particular inline closures. To access it, use

```
GEN closure_get_data(GEN C)
```

 \bullet z[5] points to a t_VEC which hold extra data needed for error-reporting and debugging. See Section 1.1.1 for details. To access it, use

GEN closure_get_dbg(GEN C)

Additionally, for functions and true closures,

• z[6] usually points to a t_VEC with two components which are t_STR. The first one displays the list of arguments of the closure without the enclosing parentheses, the second one the GP code of the function at the right of the -> token. They are used to display the closure, either in implicit or explicit form. However for closures that were not generated from GP code, z[6] can point to a t_STR instead. To access it, use

GEN closure_get_text(GEN C)

Additionally, for true closure,

 \bullet z[7] points to a t_VEC which holds the values of all lexical variables defined in the scope the closure was defined. To access it, use

GEN closure_get_frame(GEN C)

1.1.1 Debugging information in closure.

Every t_CLOSURE object z has a component dbg=z[5] which hold extra data needed for error-reporting and debugging. The object dbg is a t_VEC with 3 components:

dbg[1] is a t_VECSMALL of the same length than z[3]. For each opcode, it holds the position of the corresponding GP source code in the strings stored in z[6] for function or true closures, positive indices referring to the second strings, and negative indices referring to the first strings, the last element being indexed as -1. For inline closures, the string of the parent function or true closure is used instead.

dbg[2] is a t_VECSMALL that lists opcodes index where new lexical local variables are created. The value 0 denotes the position before the first offset and variables created by the prototype code 'V'.

dbg[3] is a t_VEC of t_VECSMALLs that give the list of entree* of the lexical local variables created at a given index in dbg[2].

1.2 The type t_LIST.

This type needs to go through various hoops to support GP's inconvenient memory model. Don't use t_LISTs in pure library mode, reimplement ordinary lists! This dynamic type is implemented by a GEN of length 3: two codewords and a vector containing the actual entries. In a normal setup (a finished list, ready to be used),

- the vector is malloc'ed, so that it can be realloc'ated without moving the parent GEN.
- all the entries are clones, possibly with cloned subcomponents; they must be deleted with gunclone_deep, not gunclone.

The following macros are proper lvalues and access the components

long list_nmax(GEN L): current maximal number of elements. This grows as needed.

GEN list_data(GEN L): the elements. If $v = list_data(L)$, then either v is NULL (empty list) or l = lg(v) is defined, and the elements are $v[1], \ldots, v[l-1]$.

In most gerepile scenarios, the list components are not inspected and a shallow copy of the malloc'ed vector is made. The functions gclone, copy_bin_canon are exceptions, and make a full copy of the list.

The main problem with lists is to avoid memory leaks; in the above setup, a statement like a = List(1) would already leak memory, since List(1) allocates memory, which is cloned (second allocation) when assigned to a; and the original list is lost. The solution we implemented is

• to create anonymous lists (from List, gtolist, concat or vecsort) entirely on the stack, not as described above, and to set list_nmax to 0. Such a list is not yet proper and trying to append elements to it fails:

```
? listput(List(),1)
 *** variable name expected: listput(List(),1)
 ***
```

If we had been malloc'ing memory for the List([1,2,3]), it would have leaked already.

• as soon as a list is assigned to a variable (or a component thereof) by the GP evaluator, the assigned list is converted to the proper format (with list_nmax set) previously described.

GEN listcopy(GEN L) return a full copy of the t_LIST L, allocated on the *stack* (hence list_nmax is 0). Shortcut for gcopy.

GEN mklistcopy(GEN x) returns a list with a single element x, allocated on the stack. Used to implement most cases of gtolist (except vectors and lists).

A typical low-level construct:

```
long 1;
/* assume L is a t_LIST */
L = list_data(L); /* discard t_LIST wrapper */
l = L? lg(L): 1;
for (i = 1; i < 1; i++) output( gel(L, i) );
for (i = 1; i < 1; i++) gel(L, i) = gclone( ... );</pre>
```

1.2.1 Maps as Lists.

GP's maps are implemented on top of t_LISTs so as to benefit from their peculiar memory models. Lists thus come in two subtypes: t_LIST_RAW (actual lists) and t_LIST_MAP (a map).

GEN mklist_typ(long t) create a list of subtype t. GEN mklist(void) is an alias for

```
mklist_typ(t_LIST_RAW);
and GEN mkmap(void) is an alias for
mklist_typ(t_LIST_MAP);
```

long list_typ(GEN L) return the list subtype, either t_LIST_RAW or t_LIST_MAP.

void listpop(GEN L, long index) as listpop0, assuming that L is a t_LIST_RAW.

GEN listput(GEN list, GEN object, long index) as listput0, assuming that L is a t_LIST_RAW.

GEN mapdomain (GEN T) vector of keys of the map T.

GEN mapdomain_shallow(GEN T) shallow version of mapdomain.

GEN maptomat(GEN T) convert a map to a factorization matrix.

GEN maptomat_shallow(GEN T) shallow version of maptomat.

1.3 Protection of non-interruptible code.

GP allows the user to interrupt a computation by issuing SIGINT (usually by entering control-C) or SIGALRM (usually using alarm()). To avoid such interruption to occurs in section of code which are not reentrant (in particular malloc and free) the following mechanism is provided:

BLOCK_SIGINT_START() Start a non-interruptible block code. Block both SIGINT and SIGARLM.

BLOCK_SIGALRM_START() Start a non-interruptible block code. Block only SIGARLM. This is used in the SIGINT handler itself to delay an eventual pending alarm.

BLOCK_SIGINT_END() End a non-interruptible block code

The above macros make use of the following global variables:

PARI_SIGINT_block: set to 1 (resp. 2) by BLOCK_SIGINT_START (resp. BLOCK_SIGALRM_START).

PARI_SIGINT_pending: Either 0 (no signal was blocked), SIGINT (SIGINT was blocked) or SIGALRM (SIGALRM was blocked). This need to be set by the signal handler.

Within a block, an automatic variable int block is defined which records the value of PARI_SIGINT_block when entering the block.

1.3.1 Multithread interruptions.

To support multithreaded programs, BLOCK_SIGINT_START and BLOCK_SIGALRM_START call MT_SIGINT_BLOCK(block), and BLOCK_SIGINT_END calls MT_SIGINT_UNBLOCK(block).

MT_SIGINT_BLOCK and MT_SIGINT_UNBLOCK are defined by the multithread engine. They can calls the following public functions defined by the multithread engine.

void mt_sigint_block(void)

void mt_sigint_unblock(void)

In practice this mechanism is used by the POSIX thread engine to protect against asychronous cancellation.

1.4 \mathbf{F}_{l^2} field for small primes l.

Let l > 2 be a prime ulong. A F12 is an element of the finite field \mathbf{F}_{l^2} represented (currently) by a F1x of degree at most 1 modulo a polynomial of the form $x^2 - D$ for some non square $0 \le D < p$. Below pi denotes the pseudo inverse of p, see F1_mul_pre

```
int Fl2_equal1(GEN x) return 1 if x = 1, else return 0.
```

```
GEN F12_mul_pre(GEN x, GEN y, ulong D, ulong p, ulong pi) return xy.
```

```
GEN F12_sqr_pre(GEN x, ulong D, ulong p, ulong pi) return x^2.
```

GEN F12_inv_pre(GEN x, ulong D, ulong p, ulong pi) return x^{-1} .

GEN F12_pow_pre(GEN x, GEN n, ulong D, ulong p, ulong pi) return x^n .

GEN Fl2_sqrtn_pre(GEN a, GEN n, ulong D, ulong p, ulong pi, GEN *zeta) n-th root, as Flxq_sqrtn.

GEN Fl2_norm_pre(GEN x, GEN n, ulong D, ulong p, ulong pi) return the norm of x.

GEN Flx_Fl2_eval_pre(GEN P, GEN x, ulong D, ulong p, ulong pi) return P(x).

1.5 Public functions useless outside of GP context.

These functions implement GP functionality for which the C language or other libpari routines provide a better equivalent; or which are so tied to the gp interpreter as to be virtually useless in libpari. Some may be generated by gp2c. We document them here for completeness.

1.5.1 Conversions.

GEN toser_i(GEN x) internal shallow function, used to implement automatic conversions to power series in GP (as in cos(x)). Converts a t_POL or a t_RFRAC to a t_SER in the same variable and precision precdl (the global variable corresponding to seriesprecision). Returns x itself for a t_SER, and NULL for other argument types. The fact that it uses a global variable makes it awkward whenever you're not implementing a new transcendental function in GP. Use RgX_to_ser or rfrac_to_ser for a fast clean alternative to gtoser.

GEN listinit(GEN x) a t_LIST (from List or Map) may exist in two different forms due to GP memory model:

- an ordinary *read-only* copy on the pari stack (as produced by gtolist or gtomap) to which one may not assign elements (listput will fail) unless the list is empty.
- a feature-complete GP list using (malloc'ed) blocks to allow dynamic insertions. An empty list is automatically promoted to this status on first insertion.

The listinit function creates a copy of existing t_SER x and makes sure it is of the second kind. Variants of this are automatically called by gp when assigning a t_LIST to a GP variable; the mecanism avoid memory leaks when creating a constant list, e.g. List([1,2,3]) (read-only), without assigning it to a variable. Whereas after L = List([1,2,3]) (GP list), we keep a pointer to the object and may delete it when L goes out of scope.

This libpari function allows gp2c to simulate this process by generating listinit calls at appropriate places.

1.5.2 Output.

void print0(GEN g, long flag) internal function underlying the print GP function. Prints the entries of the t_VEC g, one by one, without any separator; entries of type t_STR are printed without enclosing quotes. flagis one of f_RAW , $f_PRETTYMAT$ or f_TEX , using the current default output context.

void out_print0(PariOUT *out, const char *sep, GEN g, long flag) as print0, using output context out and separator sep between successive entries (no separator if NULL).

void printsep(const char *s, GEN g, long flag) out_print0 on pariOut followed by a newline.

void printsep1(const char *s, GEN g, long flag) out_print0 on pariOut.

char* pari_sprint0(const char *s, GEN g, long flag) displays s, then print0(g, flag).

void print(GEN g) equivalent to printO(g, f_RAW), followed by a \n then an fflush.

void printp(GEN g) equivalent to printO(g, f_PRETTYMAT), followed by a \n then an fflush.

void print1(GEN g) as above, without the \n. Use pari_printf or output instead.

void printtex(GEN g) equivalent to printO(g, t_TEX), followed by a \n then an fflush. Use GENtoTeXstr and pari_printf instead.

void writeO(const char *s, GEN g)

void write1(const char *s, GEN g) use fprintf

void writetex(const char *s, GEN g) use GENtoTeXstr and fprintf.

void printf0(GEN fmt, GEN args) use pari_printf.

GEN Strprintf(GEN fmt, GEN args) use pari_sprintf.

1.5.3 Input.

gp's input is read from the stream pari_infile, which is changed using

FILE* switchin(const char *name)

Note that this function is quite complicated, maintaining stacks of files to allow smooth error recovery and gp interaction. You will be better off using gp_read_file.

1.5.4 Control flow statements.

GEN break0(long n). Use the C control statement break. Since break(2) is invalid in C, either rework your code or use goto.

GEN next0(long n). Use the C control statement continue. Since continue(2) is invalid in C, either rework your code or use goto.

GEN return0(GEN x). Use return!

void error0(GEN g). Use pari_err(e_USER,)

void warningO(GEN g). Use pari_warn(e_USER,)

1.5.5 Accessors.

GEN vecsliceO(GEN A, long a, long b) implements A[a..b].

GEN matsliceO(GEN A, long a, long b, long c, long d) implements A[a..b, c..d].

1.5.6 Iterators.

GEN apply0 (GEN f, GEN A) gp wrapper calling genapply, where f is a t_CLOSURE, applied to A. Use genapply or a standard C loop.

GEN select0(GEN f, GEN A) gp wrapper calling genselect, where f is a t_CLOSURE selecting from A. Use genselect or a standard C loop.

GEN vecapply(void *E, GEN (*f)(void* E, GEN x), GEN x) implements [a(x)|x<-b].

GEN veccatapply(void *E, GEN (*f)(void* E, GEN x), GEN x) implements concat([a(x)|x<-b]) which used to implement [a0(x,y)|x<-b;y<-c(b)] which is equal to concat([[a0(x,y)|y<-c(b)]|x<-b]).

GEN vecselect(void *E, long (*f)(void* E, GEN x), GEN A) implements [x<-b,c(x)].

GEN vecselapply(void *Epred, long (*pred)(void* E, GEN x), void *Efun, GEN (*fun)(void* E, GEN x), GEN A) implements [a(x)|x<-b,c(x)].

1.5.7 Local precision.

Theses functions allow to change realprecision locally when calling the GP interpretor.

void push_localprec(long p) set the local precision to p.

void $push_localbitprec(long b)$ set the local precision to b bits.

void pop_localprec(void) reset the local precision to the previous value.

long get_localprec(void) returns the current local precision.

long get_localbitprec(void) returns the current local precision in bits.

void localprec(long p) trivial wrapper around push_localprec (sanity checks and convert from decimal digits to a number of codewords). Use push_localprec.

void localbitprec(long p) trivial wrapper around push_localbitprec (sanity checks). Use push_localbitprec.

1.5.8 Functions related to the GP evaluator.

The prototype code C instructs the GP compiler to save the current lexical context (pairs made of a lexical variable name and its value) in a GEN, called pack in the sequel. This pack can be used to evaluate expressions in the corresponding lexical context, providing it is current.

GEN localvars_read_str(const char *s, GEN pack) evaluate the string s in the lexical context given by pack. Used by geval_gp in GP to implement the behavior below:

```
? my(z=3); eval("z=z^2"); z
%1 = 9
```

long localvars_find(GEN pack, entree *ep) does pack contain a pair whose variable corresponds to ep? If so, where is the corresponding value? (returns an offset on the value stack).

1.5.9 Miscellaneous.

char* os_getenv(const char *s) either calls getenv, or directly return NULL if the libc does not provide it. Use getenv.

```
sighandler_t os_signal(int sig, pari_sighandler_t fun) after a
typedef void (*pari_sighandler_t)(int);
```

(private type, not exported). Installs signal handler fun for signal sig, using sigaction with flag SA_NODEFER. If sigaction is not available use signal. If even the latter is not available, just return SIG_IGN. Use sigaction.

1.6 Embedded GP interpretor.

These function provide a simplified interface to embed a GP interpretor in a program.

void gp_embedded_init(long rsize, long vsize) Initialize the GP interpretor (like pari_init does) with parisize=rsize rsize and parisizemax=vsize.

char * gp_embedded(const char *s) Evaluate the string s with GP and return the result as a string, in a format similar to what GP displays (with the history index). The resulting string is allocated on the PARI stack, so subsequent call to gp_embedded will destroy it.

1.7 Readline interface.

Code which wants to use libpari readline (such as the Jupyter notebook) needs to do the following:

```
#include <readline.h>
#include <paripriv.h>
pari_rl_interface S;
...
pari_use_readline(S);
```

The variable S, as initialized above, encapsulates the libpari readline interface. (And allow us to move gp's readline code to libpari without introducing a mandatory dependency on readline in libpari.) The following functions then become available:

char** pari_completion_matches(pari_rl_interface *pS, const char *s, long pos, long *wordpos) given a command string s, where the cursor is at index pos, return an array of completion matches.

If wordpos is not NULL, set *wordpos to the index for the start of the expression we complete.

char** pari_completion(pari_rl_interface *pS, char *text, int start, int end) the low-level completer called by pari_completion_matches. The following wrapper

```
char**
gp_completion(char *text, int START, int END)
{ return pari_completion(&S, text, START, END);)
```

is a valid value for rl_attempted_completion_function.

1.8 Constructors called by pari_init functions.

```
void pari_init_buffers()
void pari_init_compiler()
void pari_init_defaults()
void pari_init_evaluator()
void pari_init_files()
void pari_init_floats()
void pari_init_graphics()
void pari_init_homedir()
void pari_init_parser()
void pari_init_paths()
void pari_init_primetab()
void pari_init_rand()
void pari_init_seadata()
```

1.9 Destructors called by pari_close.

```
void pari_close_compiler()
void pari_close_evaluator()
void pari_close_files()
void pari_close_floats()
void pari_close_homedir()
void pari_close_mf()
void pari_close_parser()
void pari_close_paths()
void pari_close_paths()
```

1.10 Constructors and destructors used by the pthreads interface.

```
Called by pari_thread_sync
void pari_pthread_init_primetab()
void pari_pthread_init_seadata()
void pari_pthread_init_varstate()
Called by pari_thread_start
void pari_thread_init_primetab()
void pari_thread_init_seadata()
void pari_thread_init_varstate()
Called by pari_thread_close
void pari_thread_close_files()
```

Chapter 2:

Regression tests, benches

This chapter documents how to write an automated test module, say fun, so that make test-fun executes the statements in the fun module and times them, compares the output to a template, and prints an error message if they do not match.

- Pick a *new* name for your test, say fun, and write down a GP script named fun. Make sure it produces some useful output and tests adequately a set of routines.
- The script should not be too long: one minute runs should be enough. Try to break your script into independent easily reproducible tests, this way regressions are easier to debug; e.g. include setrand(1) statement before a randomized computation. The expected output may be different on 32-bit and 64-bit machines but should otherwise be platform-independent. If possible, the output shouldn't even depend on sizeof(long); using a realprecision that exists on both 32-bit and 64-bit architectures, e.g. \p 38 is a good first step. You can use sizebyte(0)==16 to detect a 64-bit architecture and sizebyte(0)==8 for 32-bit.
 - Dump your script into src/test/in/ and run Configure.
- make test-fun now runs the new test, producing a [BUG] error message and a .dif file in the relevant object directory <code>Oxxx</code>. In fact, we compared the output to a non-existing template, so this must fail.
 - Now

```
patch -p1 < 0xxx/fun.dif
```

generates a template output in the right place src/test/32/fun, for instance on a 32-bit machine.

- If different output is expected on 32-bit and 64-bit machines, run the test on a 64-bit machine and patch again, thereby producing src/test/64/fun. If, on the contrary, the output must be the same (preferred behavior!), make sure the output template land in the src/test/32/ directory which provides a default template when the 64-bit output file is missing; in particular move the file from src/test/64/ to src/test/32/ if the test was run on a 64-bit machine.
- You can now re-run the test to check for regressions: no [BUG] is expected this time! Of course you can at any time add some checks, and iterate the test / patch phases. In particular, each time a bug in the fun module is fixed, it is a good idea to add a minimal test case to the test suite.
- By default, your new test is now included in make test-all. If it is particularly annoying, e.g. opens tons of graphical windows as make test-ploth or just much longer than the recommended minute, you may edit config/get_tests and add the fun test to the list of excluded tests, in the test_extra_out variable.
 - You can run a subset of existing tests by using the following idiom:

```
cd Oxxx  # call from relevant build directory
make TESTS="lfuntype lfun gamma" test-all
```

will run the lfuntype, lfun and gamma tests. This produces a combined output whereas the alternative

make test-lfuntype test-lfun test-gamma

would not.

• By default, the test is run on both the gp-sta and gp-dyn binaries, making it twice as slow. If the test is somewhat long, it can be annoying; you can restrict to one binary only using the statest-all or dyntest-all targets. Both accept the TESTS argument seen above.

make test-lfuntype test-lfun gamma

would not.

• Finally, the get_tests script also defines the recipe for make bench timings, via the variable test_basic. A test is included as fun or fun_n, where n is an integer ≤ 1000 ; the latter means that the timing is weighted by a factor n/1000. (This was introduced a long time ago, when the nfields bench was so much slower than the others that it hid slowdowns elsewhere.)

2.1 Functions for GP2C.

2.1.1 Functions for safe access to components.

Theses function returns the adress of the requested component after checking it is actually valid. This is used by GP2C -C.

GEN* safegel(GEN x, long 1), safe version of gel(x,1) for t_VEC, t_COL and t_MAT.

long* safeel(GEN x, long 1), safe version of x[1] for t_VECSMALL.

GEN* safelistel(GEN x, long 1) safe access to t_LIST component.

GEN* safegcoeff(GEN x, long a, long b) safe version of gcoeff(x,a, b) for t_MAT .

Chapter 3:

Parallelism

3.1 The PARI MT interface.

PARI provides an abstraction for doing parallel computations.

void mt_queue_start(struct pari_mt *pt, GEN worker) Let worker be a t_CLOSURE object of arity 1. Initialize the structure pt to evaluate worker in parallel.

void mt_queue_start_lim(struct pari_mt *pt, GEN worker, long lim) as mt_queue_start, where lim is an upper bound on the number of tasks to perform. Concretly the number of threads will be min(lim,nbthreads. The values 0 and 1 of lim are special:

- 0: no limit, equivalent to mt_queue_start.
- 1: no parallelism. Evaluate the tasks sequentially.

void mt_queue_submit(struct pari_mt *pt, long taskid, GEN task) Submit task to be evaluated by worker, or NULL if no further task is left to be submitted. The value taskid is user-specified and allows to later match up results and submitted tasks.

GEN mt_queue_get(struct pari_mt *pt, long *taskid, long *pending) Return the result of the evaluation by worker of one of the previously submitted tasks. Set pending to the number of remaining pending tasks. Set taskid to the value associate to this task by mt_queue_submit. Returns NULL if more tasks need to be submitted.

void mt_queue_end(struct pari_mt *pt) End the parallel execution.

Calls to mt_queue_submit and mt_queue_get must alternate: each call to mt_queue_submit must be followed by a call to mt_queue_get before any other call to mt_queue_submit, and conversely.

The first call to mt_queue_get will return NULL until a sufficient number of tasks have been submitted. If no more tasks are left to be submitted, use

```
mt_queue_submit(handle, id, NULL)
```

to allow further calls to mt_queue_get. If mt_queue_get sets pending to 0, then no more tasks are pending and it is safe to call mt_queue_end.

The parameter taskid can be chosen arbitrarily. It is attached to a task but is not available to worker. It provides an efficient way to match a tasks and results. It is ignored when the parameter task is NULL.

3.1.1 Miscellaneous.

void mt_broadcast(GEN code): do nothing unless the MPI threading engine is in use. In that case, it evaluates the closure code on all secondary nodes. This can be sued to change the states of the MPI child nodes. This is used by install.

3.2 Initialization.

This section is technical.

void pari_mt_init(void) When using MPI, it is sometimes necessary to run initialization code on the child nodes after PARI is initialized. This can be done as follow:

- ullet call pari_init_opts with the flag INIT_noIMTm. This initializes PARI, but not the MT engine.
 - call the required initialization code.
- call pari_mt_init to initialize the MT engine. Note that under MPI, this function only returns on the master node. On the child nodes, it enters slave mode. Thus it is no longer possible to run initialization code on the child nodes.

See the file examples/pari-mt.c for an example.

void pari_mt_close(void) When using MPI, calling pari_close will terminate the MPI execution environment. If this is undesirable, you should call pari_close_opts with the flag INIT_noIMTm. This closes PARI without terminating the MPI execution environment It is allowed to call pari_mt_close later to terminate it. Note that the once MPI is terminated it cannot be restarted, and that it is considered an error for a program to end without having terminated the MPI execution environment.

\mathbf{Index}

SomeWord refers to PARI-GP concepts. SomeWord is a PARI-GP keyword. SomeWord is a generic index entry. A apply0	geval_gp 11 gp_embedded 12 gp_embedded_init 12 gp_read_file 10 gunclone 6 gunclone_deep 6
В	I
BLOCK_SIGALRM_START 8 BLOCK_SIGINT_END 8 BLOCK_SIGINT_START 8 break0 10	INIT_noIMTm
\mathbf{C}	list
	listcopy
closure	listinit 9
closure_arity	listpop
closure_get_code	listput
closure_get_data 5	list_nmax 6
closure_get_dbg	list_typ
closure_get_frame6	localbitprec
closure_get_oper 5	localprec
closure_get_text 6	localvars_find
${f E}$	localvars_read_str 11
E error0	localvars_read_str 11 M
error0	\mathbf{M}
error0	
F12_equal1	${f M}$ mapdomain
F12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8
F12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10
F12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7
F12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matsliceO 10 mklist 7 mklistcopy 7
F12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7
F12_equal1 8 F12_inv_pre 8 F12_mul_pre 8 F12_norm_pre 8 F12_pow_pre 8 F12_sqrtn_pre 8 F12_sqr_pre 8	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7
F12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17
From 10 F F F12_equal1 8 F12_inv_pre 8 F12_mul_pre 8 F12_norm_pre 8 F12_pow_pre 8 F12_sqrtn_pre 8 F12_sqr_pre 8 F12_sqr_pre 9	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17 mt_queue_end 17
F12_equal1 8 F12_inv_pre 8 F12_mul_pre 8 F12_norm_pre 8 F12_pow_pre 8 F12_sqrtn_pre 8 F12_sqrtn_pre 8 F12_sqrtn_pre 9 F1x_F12_eval_pre 9 f_PRETTYMAT 9	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17 mt_queue_end 17 mt_queue_get 17
F12_equal1 8 F12_inv_pre 8 F12_mul_pre 8 F12_norm_pre 8 F12_pow_pre 8 F12_sqrtn_pre 8 F12_sqrtn_pre 8 F12_sqrtn_pre 9 F12_sqr_pre 9 F1x_F12_eval_pre 9 f_PRETTYMAT 9 f_RAW 9	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17 mt_queue_end 17 mt_queue_start 17 mt_queue_start_lim 17 mt_queue_start_lim 17
FF12_equal1 8 F12_inv_pre 8 F12_mul_pre 8 F12_norm_pre 8 F12_pow_pre 8 F12_sqrtn_pre 8 F12_sqrtn_pre 9 F12_sqr_pre 9 F1x_F12_eval_pre 9 f_PRETTYMAT 9 f_RAW 9 f_TEX 9	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17 mt_queue_end 17 mt_queue_start 17 mt_queue_start_lim 17 mt_queue_submit 17
F12_equal1 8 F12_inv_pre 8 F12_mul_pre 8 F12_norm_pre 8 F12_pow_pre 8 F12_sqrtn_pre 8 F12_sqrtn_pre 8 F12_sqrtn_pre 9 F12_sqr_pre 9 f_PRETTYMAT 9 f_RAW 9 f_TEX 9 G genapply 11	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17 mt_queue_end 17 mt_queue_start 17 mt_queue_start_lim 17 mt_queue_submit 17 MT_SIGINT_BLOCK 8
FF12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17 mt_queue_end 17 mt_queue_start 17 mt_queue_start_lim 17 mt_queue_submit 17 MT_SIGINT_BLOCK 8 mt_sigint_block 8
F F12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17 mt_queue_end 17 mt_queue_start 17 mt_queue_start_lim 17 mt_queue_submit 17 MT_SIGINT_BLOCK 8 mt_sigint_block 8 MT_SIGINT_UNBLOCK 8
FF12_equal1	M mapdomain 7 mapdomain_shallow 7 maptomat 7 maptomat_shallow 8 matslice0 10 mklist 7 mklistcopy 7 mklist_typ 7 mkmap 7 mt_broadcast 17 mt_queue_end 17 mt_queue_start 17 mt_queue_start_lim 17 mt_queue_submit 17 MT_SIGINT_BLOCK 8 mt_sigint_block 8

next0 10	pari_thread_close
O	pari_thread_close_files
O	pari_thread_init_primetab 13 pari_thread_init_seadata 13
os_getenv	·
os_signal	·
output	pari_thread_start
out_print0	pop_localprec
D	print
P	print0
pariOut	print1
pari_close	printf0
pari_close_compiler	printp
pari_close_evaluator	printsep
pari_close_files	printsep1
pari_close_floats 13	printtex
pari_close_homedir 13	push_localbitprec
pari_close_mf	<pre>push_localprec</pre>
pari_close_opts 18	
pari_close_parser 13	${f R}$
pari_close_paths	return0
pari_close_primes	rfrac_to_ser 9
pari_completion	RgX_to_ser
pari_completion_matches	rl_attempted_completion_function 12
nari intila	
1 –	
pari_init_buffers 12	${f S}$
pari_init_buffers	
pari_init_buffers <td>safeel 16</td>	safeel 16
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13	safeel 16 safegcoeff 16
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13	safeel <t< td=""></t<>
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12
pari_init_buffers12pari_init_compiler12pari_init_defaults12pari_init_evaluator13pari_init_files13pari_init_floats13pari_init_graphics13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_parser 13 pari_init_paths 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_parths 13 pari_init_primetab 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_rand 13 pari_init_seadata 13 pari_mt_close 18	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_seadata 13 pari_mt_close 18 pari_mt_init 17, 18	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_seadata 13 pari_init_seadata 13 pari_mt_close 18 pari_mt_init 17, 18 pari_printf 10	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10 T 10 toser_i 9
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_seadata 13 pari_mt_close 18 pari_mt_init 17, 18 pari_printf 10 pari_pthread_init_primetab 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10 T 10 toser_i 9 t_CLOSURE 5
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_seadata 13 pari_mt_close 18 pari_mt_init 17, 18 pari_printf 10 pari_pthread_init_primetab 13 pari_pthread_init_seadata 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10 T 10 toser_i 9
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_seadata 13 pari_mt_close 18 pari_mt_init 17, 18 pari_printf 10 pari_pthread_init_primetab 13 pari_pthread_init_seadata 13 pari_pthread_init_varstate 13	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10 T 10 toser_i 9 t_CLOSURE 5
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_seadata 13 pari_mt_init 17, 18 pari_printf 10 pari_pthread_init_primetab 13 pari_pthread_init_seadata 13 pari_pthread_init_varstate 13 PARI_SIGINT_block 8	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10 T 10 t_CLOSURE 5 t_LIST 6
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_rand 13 pari_init_seadata 13 pari_mt_init 17, 18 pari_printf 10 pari_pthread_init_primetab 13 pari_pthread_init_seadata 13 pari_pthread_init_varstate 13 pari_pthread_init_varstate 13 PARI_SIGINT_block 8 PARI_SIGINT_pending 8	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10 T toser_i 9 t_CLOSURE 5 t_LIST 6 V vecapply 11
pari_init_buffers 12 pari_init_compiler 12 pari_init_defaults 12 pari_init_evaluator 13 pari_init_files 13 pari_init_floats 13 pari_init_graphics 13 pari_init_homedir 13 pari_init_opts 18 pari_init_parser 13 pari_init_paths 13 pari_init_primetab 13 pari_init_seadata 13 pari_mt_init 17, 18 pari_printf 10 pari_pthread_init_primetab 13 pari_pthread_init_seadata 13 pari_pthread_init_varstate 13 PARI_SIGINT_block 8	safeel 16 safegcoeff 16 safegel 16 safelistel 16 SA_NODEFER 12 select0 11 sigaction 12 signal 12 SIG_IGN 12 Strprintf 10 switchin 10 T 10 t_CLOSURE 5 t_LIST 6

vecserect		•	•	•	•	•	•	•	•	•	٠	•	•	•	•	•	٠	•	11
vecslice0)																		10
\mathbf{W}																			
warning0																			10
writeO .																			10
write1 .																			10
writetex																			10