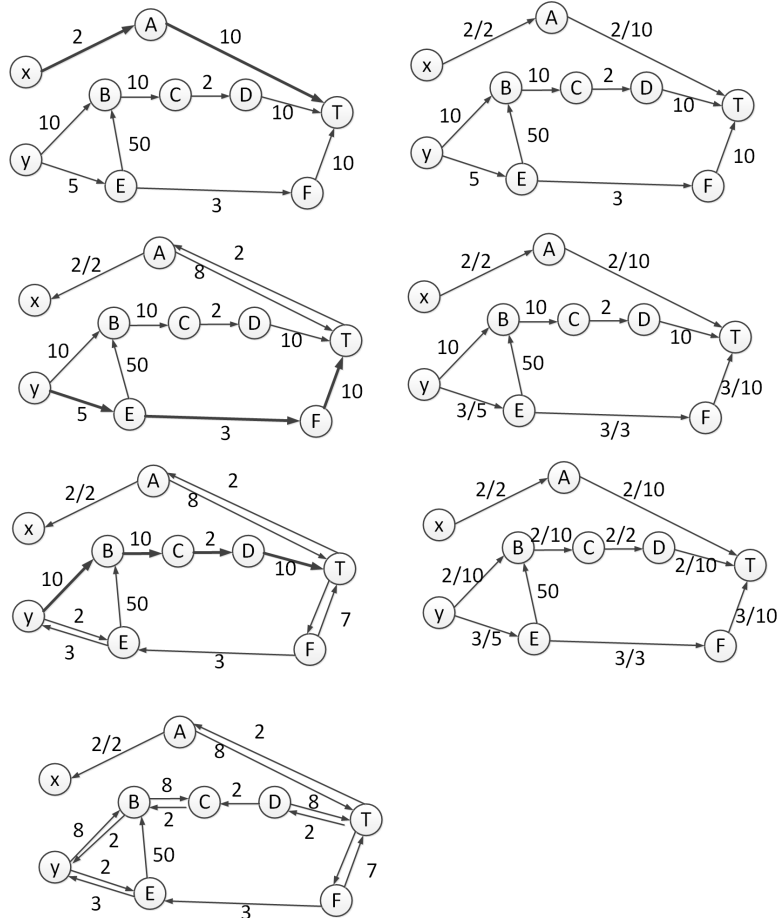


# 1 Exercise 1

1.



Critical edges: XA, EF, and CD.

Maximum flow: 7.

2. A:111 D:10

3 J

Sweep line status:

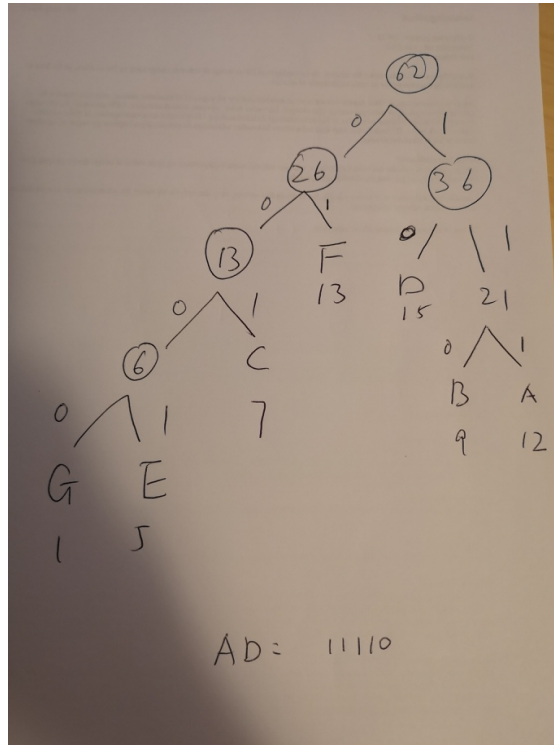
A

H, A

H

H, D

J, H, D



4 a

Range tree:  $\Theta(\lg^2 n + k)$

kd tree:  $\Theta(\sqrt{n} + k)$

2 BSTs:  $\Theta(\lg n + k_x + k_y)$

$k$  is zero in this specific case

## 2 Exercise 2

1

$i$ -th Operation	1	2	3	4	5	6	7	8	9	10
Cost	1	1	<b>3</b>	1	1	1	1	1	<b>9</b>	1
Cost	1	1	$1+(3^1-1)$	1	1	1	1	1	$1+(3^2-1)$	1

Aggregate analysis: When  $i$  is a power of 3, we write the cost into  $1 + (3^x - 1)$ , so that it also has a cost of 1 and the remaining cost  $(3^x - 1)$ .  $x$  is from 1 to  $\log_3 n$ .

Then, since we have  $n$  operations, each has at least a cost of 1, so the sum is  $n$ . Next, the sum of the remaining cost is  $\sum_{x=1}^{\log_3 n} (3^x - 1) = \sum_{x=1}^{\log_3 n} 3^x - \log_3 n = \frac{3}{2}n - \frac{3}{2} - \log_3 n \leq 1.5n$ .

So all together the cost is less than  $2.5n$ . The amortized cost is at most 2.5.  
**2 Configuration:  $(X, Y)$ :**  $X$  contains the vertices that are already in the cycle and  $Y$  contains the vertices to be considered.

From the last vertex in  $X$ , we check whether there exist an adjacent vertex that is not in  $X$ . If we find such a vertex, we add the vertex as part of the solution. If we do not find a vertex and  $Y$  is not empty, then it is a deadend. If we do not find a vertex and  $Y$  is empty, and there exists an edge connecting the last vertex in  $X$  and the first vertex in  $X$ , then it is a solution.

