## The Theoretical Minimum Classical Mechanics - Solutions L02E06

## M. Bivert

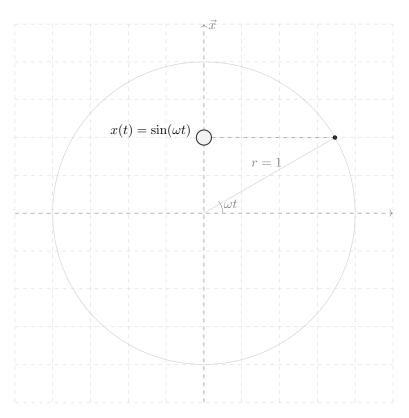
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Exercise 1. How long does it take for the oscillating particle to go through one full cycle of motion?

We're in the case of a particle oscillating in one dimension. Its motion, known as the *simple harmonic motion*, is described by:

$$x(t) = \sin(\omega t)$$

Essentially, x(t) will correspond to the vertical component of a point moving on the unit circle, located by an angle  $\omega t$ .



To fix things, consider the case of a particle starting at an extreme position, say x=1 (at the top of the north hemisphere of the unit circle). It will need to go down to x=-1, and then back up to x=1. In the mean time, the corresponding point on the unit circle would have walked a full circle, or  $2\pi$  radians.

So we're looking for the time T that it will take for us to move by an angle  $2\pi$ , knowing that we move at a speed of  $\omega$  radians per unit of time (i.e.  $\omega_{t=0}=0,\,\omega_{t=1}=\omega,\,\omega_{t=2}=2\omega,\,\ldots$ ):

$$\omega T = 2\pi \Leftrightarrow \boxed{T = \frac{2\pi}{\omega}}$$

**Remark 1.** T is commonly called the period of motion.