

There are several equivalent terms and notations for this product:

- the **dyadic product** of two vectors **a** and **b** is denoted by **ab** (juxtaposed; no symbols, multiplication signs, crosses, dots, etc.)
- the **outer product** of two **column vectors** **a** and **b** is denoted and defined as $\mathbf{a} \otimes \mathbf{b}$ or \mathbf{ab}^T , where **T** means **transpose**,
- the **tensor product** of two vectors **a** and **b** is denoted $\mathbf{a} \otimes \mathbf{b}$,

In the dyadic context they all have the same definition and meaning, and are used synonymously, although the **tensor product** is an instance of the more general and abstract use of the term.

Dirac's **bra–ket notation** makes the use of dyads and dyadics intuitively clear, see Cahill (2013)^[*dubious* – *discuss*].

Three-dimensional Euclidean space [\[edit \]](#)

To illustrate the equivalent usage, consider **three-dimensional Euclidean space**, letting:

$$\mathbf{a} = a_1 \mathbf{i} + a_2 \mathbf{j} + a_3 \mathbf{k}$$

$$\mathbf{b} = b_1 \mathbf{i} + b_2 \mathbf{j} + b_3 \mathbf{k}$$

be two vectors where **i**, **j**, **k** (also denoted **e**₁, **e**₂, **e**₃) are the standard **basis vectors** in this **vector space** (see also **Cartesian coordinates**). Then the dyadic product of **a** and **b** can be represented as a sum:

$$\begin{aligned} \mathbf{ab} = & a_1 b_1 \mathbf{ii} + a_1 b_2 \mathbf{ij} + a_1 b_3 \mathbf{ik} \\ & + a_2 b_1 \mathbf{ji} + a_2 b_2 \mathbf{jj} + a_2 b_3 \mathbf{jk} \\ & + a_3 b_1 \mathbf{ki} + a_3 b_2 \mathbf{kj} + a_3 b_3 \mathbf{kk} \end{aligned}$$

or by extension from row and column vectors, a 3×3 matrix (also the result of the outer product or tensor product of **a** and **b**):

$$\mathbf{ab} \equiv \mathbf{a} \otimes \mathbf{b} \equiv \mathbf{ab}^T = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix} \begin{pmatrix} b_1 & b_2 & b_3 \end{pmatrix} = \begin{pmatrix} a_1 b_1 & a_1 b_2 & a_1 b_3 \\ a_2 b_1 & a_2 b_2 & a_2 b_3 \\ a_3 b_1 & a_3 b_2 & a_3 b_3 \end{pmatrix}.$$

ισοδύναμα
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