

BAG  
 $n$  nuts      BAG  
 $n$  bolts

① choose 1<sup>st</sup> nut      ② compare to each bolt until match is found

③ remove nut / bolt from bags

$O(n \log n)$  ??

row[0..m] col[0..n]



2d array

$A_{11} A_{12} A_{13} A_{14} \dots A_{1N}$

$A_{21}$

$A_{31}$

:

$A_{m1}$

find  $X$

$i = 0, j = n - 1$

while  $A[i, j] < X$   
 $i++$  //next row

while  $A[i, j] > X$   
 $j--$

Question: Why can't I do rectangle and cut search area in half (about) each time?

max subarray (Kadane's algorithm)

max-so-far = 0

array A (contains pos AND neg integers)

max-to-here array (same length as A)

keep summing elements into max-to-here  
until it is  $\leq 0$

THEN

compare this value to max-sofar and keep Max()

For 2D array...

## Next Higher Number

find next higher number with same digits

$$\begin{matrix} 123 \\ 132 \end{matrix} \quad \text{(for 3-digit #)} \quad \text{permutations} = 3! = 3 \cdot 2 \cdot 1 = 6$$

$$4\text{-digit} = 4! = 4 \cdot 3 \cdot 2 \cdot 1 = 24$$

$$P(n,r) = \frac{n!}{(n-r)!} \quad \begin{matrix} n \text{ things} \\ \text{taken } r \text{ at a time} \end{matrix}$$

$$C(n,r) = \frac{n!}{(n-r)!r!} \quad \begin{matrix} \text{combination} \\ (\text{order doesn't matter}) \end{matrix}$$

DUMB WAY: Find all permutations  $\{P\}$

find min {P} that is also > X

SMARTER WAY:

~~v = [i]~~

~~while A[i] <= A[i-1] :~~

~~swap [i], [i-1]~~

~~i --~~

~~THEN~~

~~swap [i], [i-1]~~

[0 1 2 3]  
1 2 3 4

find non-increasing ending sequence : 4  
(where  $A[j]$  is  $> A[i]$ )  
 $A[i] = 3$

within sequence, smallest value  $> A[i]$   
where immediate next value  $< A[i]$  : 4  
 $\text{at } [3]$   
 $\text{so } j = 3$

1,095 digits added up (book page numbers)

1 2 3 4 5 6 7 8 9  
10 11 12 13 14 15 16 17 18 19  
20, 30, 40, 50, 60, 70, 80, 90

$$100 \rightarrow 199$$

299

$$311 \rightarrow 299$$

96      32

189

300

300

300

1,089

for 399 pgs

100 pgs = 1,092

401 pgs = 1,095

$N$  (ones digit)

$N-9$  (tens digit)

$N-99$  (100s digit)

$$N + N-9 + N-99 = 1,095$$

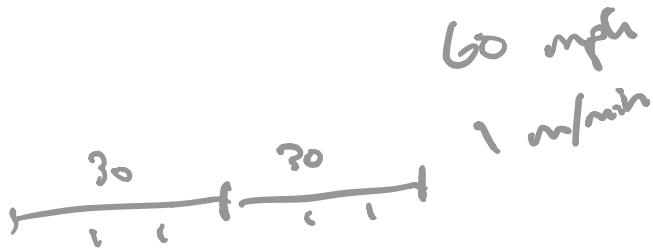
$$3N - 108 = 1,095$$

$$3N = 1,203$$

$$N = 401$$

30-minute period

95 %



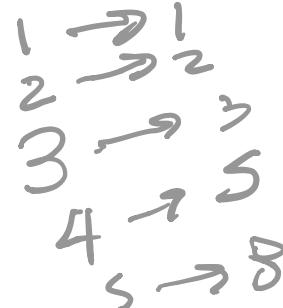
1 or 2 steps  
at a time

$N$ th step



$$N = 2x + 1$$

3    1 1 1  
      1 2  
      2 1



A    1 1 1  
      1 2  
      2 1

S    1 1 1 1  
      1 1 2

22  
211  
121

1121  
1211  
2211  
2111  
2111  
2111  
2111

# ① DEPTH-FIRST SEARCH (trees, graphs) use stack

# ② BREADTH-FIRST SEARCH

## use QUEUE

# ③ MATCHING PARENTHESES

use STACK

# ④ HASH TABLES

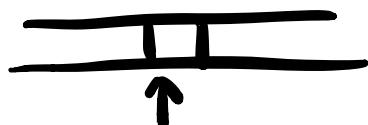
- dynamic programming
  - caching values

 MANIPULATE multiple variable pointers at once

- traversing a linked list

- pointer at start of string, end of string

i.e. Find longest palindrome

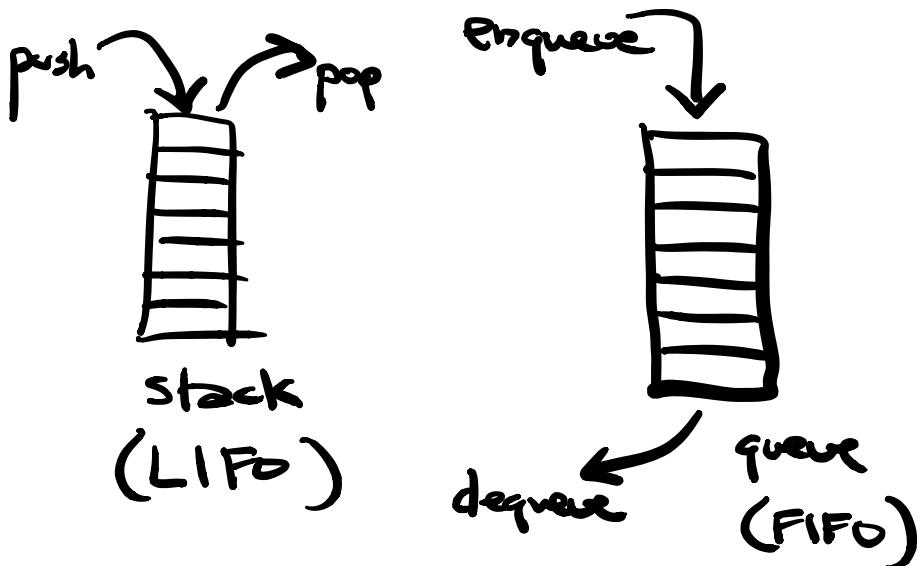


at every letter, 2 pointers that expand outward

⑥

## REVERSING A LINKED LIST

implement a queue using one or more stacks



given `rand5()` function which returns random 1-5

write `rand7()` function (each int 1-7 should have equal probability)

1	001
2	010
3	011
4	100
5	101
6	110
7	111

## "Cake Thief"

tuples of (kilograms, shillings)

(7, 160) (3, 90) (2, 15)

capacity = 20

answer:  
555

(6 of 3,90  
and 1 of 2,15)

max-duffel-bag-values (cake-tuples, capacity)

```
int max [capacity]
```

```
max [0] = 0
```

```
for (int i = 1; i <= capacity; i++)
```

```
{
```

```
    for (int j = 0; j < count; j++)
```

```
        w = cake[j].weight
```

```
        p = cake[j].price
```

takes you  $X$  seconds to eat a unit of pizza  
takes your friend  $Y$  seconds.

can't reach for new slice until current slice eaten  
# of slices to give you most pizza?

(tie reaches to friend)

pizza  
(call it 1 unit)

slice count = N

- never have less than 50% pizza (2 slices)  
(if you are slower eater —  $X > Y$ )
  - if you are faster eater, how much faster?
- so...  
floor  $\left(\frac{Y}{X}\right) + 1$   
slices?
- |            |               |                                   |
|------------|---------------|-----------------------------------|
| $Y = 2X$ ? | $\rightarrow$ | 3 slices (you get $\frac{2}{3}$ ) |
| $Y = 3X$ ? | $\rightarrow$ | 4 slices (you get $\frac{3}{4}$ ) |
| $Y = 4X$ ? | $\rightarrow$ | 5 slices (you get $\frac{4}{5}$ ) |

"anti-social bar"

25 seats in a line

Each customer sits as far away as possible

No customer will sit right next to another customer  
Where should bartender seat first customer?

10  $\leftarrow$  [•| |x| |]  $\rightarrow$  10

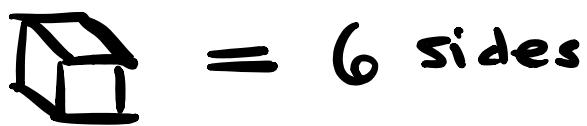
9  $\leftarrow$  [•| | |x| | |]  $\rightarrow$  9

8  $\leftarrow$  [•| | | |x| | |]  $\rightarrow$  8

7  $\leftarrow$  [•| | | | |x| | |]  $\rightarrow$  7

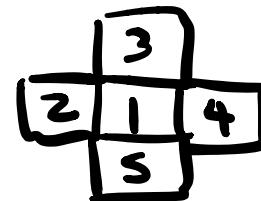
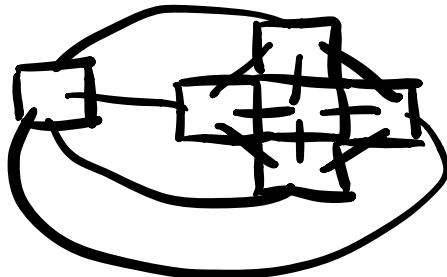
\* I think bartender can seat first customer at 1st, last, or middle seat  
(maybe at any odd seat?)

How many different ways can you paint  
a cube with 3 colors of paint?



$$3^6 = 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 = 729$$

BUT if resulting cube can be rotated to equivalent coloring, don't count it



Answer:

3 ways to paint w/ 1 color chosen from 3

24 ways to paint w/ 2 out of 3 colors

30 ways to paint w/ 3 out of 3 colors

$$3 + 24 + 30 = 57$$

C	1	$\{2, 3, 4, 5\}$
A	2	$\{5, 3, 1, 6\}$
B	3	$\{2, 4, 1, 6\}$
A	4	$\{3, 5, 1, 6\}$
B	5	$\{4, 2, 1, 6\}$
C	6	$\{2, 3, 4, 5\}$

So... I think we only have 3 sides to paint  
 $(A, B, C)$  which would be  $3 \cdot 3 \cdot 3 = 27$  (?)

draw lines in a plane equidistant from 3 non-collinear points. how many lines?

answer = 3 lines



$$3 \ 1 \ 3 \ 6 = 8$$

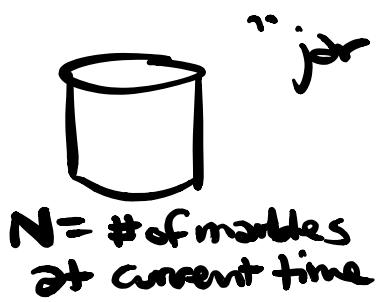
(odd standard arithmetic signs)

$$(3-1) \wedge (-3+6) = 8$$

$$(3+1) \div (3 \div 6) = 8$$

$$((3+1) \div 3) \times 6 = 8$$

$$3 - 1 + \sqrt{36} = 8$$



"jar of marbles"

- you can know  $N$  at any time
- draw 1 or 2 marbles each turn (you + friend)
- person who draws last marble wins

? left : whether drawing 1 or 2, other player will win  
So...

get it so that OTHER player has 3 marbles left

which means I want my turn with 4 or 5 marbles left

So...

after my turn, I always want multiple of 3 marbles left

Something like if  $N \% 3 == \emptyset$ , I want other player to go first OTHERWISE, I want to go first.

fleet of 50 trucks, each with full tank of gas and 100 mile range

How far can you deliver payload w/ 50 trucks?

49 w/ 49

w/N trucks

50 → and 1 w/ 99 →

50 mi (transfer gas)

50 → 50 w/ 2 → 49 w/ 0 → 1 w/ 100 → 100 mi → 198 mi

50 → 2 mi → 98 ↓ 49 → 2 mi → 98 ↓ 98 → 2 mi → (still 198 mi?)

Simulate 7-sided die with 5-sided die

roll 1

rand5()

roll 2

rand5()

roll 5-sided twice

↓  
1 - 5

↓  
0 - 4

X

↓  
1 - 5

↓  
0 - 4

Y

⇒ base 5 #

XY

0 - 24

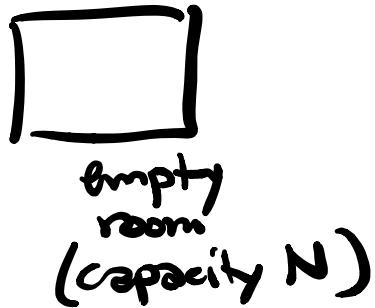
we only want 0-20, so redo if > 20

we now have 0-20

divide by 3 (integer) and add 1

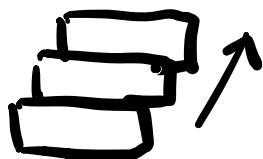
this gives us  $T =$

group of  
people outside  
room ( $n$ )



o "move" is  
(1) admit one person  
(2) let one person out

unlimited supply of bricks  
each one stacked to overhang one beneath  
what is maximum overhang you can create?



how do you find closest pairs of stars in the sky?