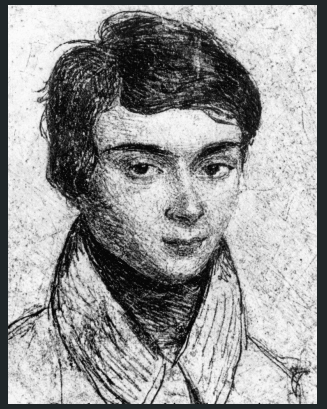


Life and Death of Evariste Galois

(galwa)

May 11, 2021 Microteaching Session
Nate Stemen (he/they)

Quadratic Formula

a general quadratic equation can always be written:

$$ax^2 + bx + c = 0$$

the solutions to a general quadratic equation are:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Cubic Formula

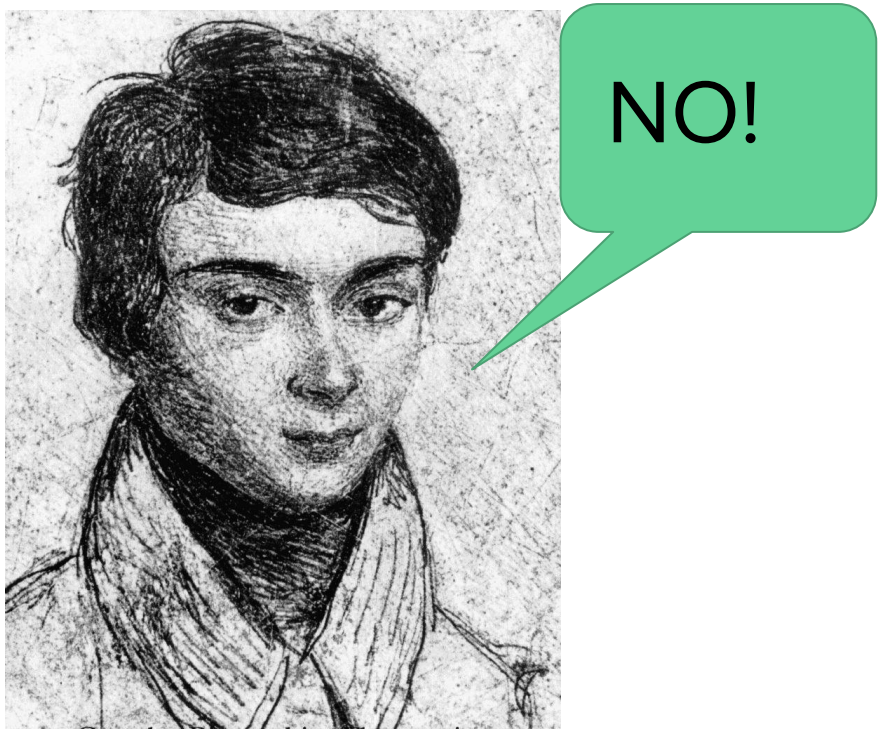
$$ax^3 + bx^2 + cx + d$$

$$x = \sqrt[3]{\left(\frac{bc}{6a^2} - \frac{d}{2a} - \frac{b^3}{27a^3}\right) + \sqrt{\left(\frac{bc}{6a^2} - \frac{d}{2a} - \frac{b^3}{27a^3}\right)^2 + \left(\frac{c}{3a} - \frac{b^2}{9a^2}\right)^3}} + \sqrt[3]{\left(\frac{bc}{6a^2} - \frac{d}{2a} - \frac{b^3}{27a^3}\right) - \sqrt{\left(\frac{bc}{6a^2} - \frac{d}{2a} - \frac{b^3}{27a^3}\right)^2 + \left(\frac{c}{3a} - \frac{b^2}{9a^2}\right)^3}} - \frac{b}{3a}$$

Quartic Formula

$$
\begin{aligned}
r_1 &= \frac{-a}{4} - \frac{1}{2}\sqrt{\left(\frac{a^2}{4} - \frac{2b}{3} + \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} + \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54}\right)} \\
&\quad - \frac{1}{2}\sqrt{\left(\frac{a^2}{2} - \frac{4b}{3} - \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} - \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54} - \right.} \\
&\quad \left. \frac{\left(-a^3 + 4ab - 8c\right)}{4\sqrt{\left(\frac{a^2}{4} - \frac{2b}{3} + \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} + \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54}\right)}}\right)} \\
r_2 &= \frac{-a}{4} - \frac{1}{2}\sqrt{\left(\frac{a^2}{4} - \frac{2b}{3} + \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} + \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54}\right)} \\
&\quad + \frac{1}{2}\sqrt{\left(\frac{a^2}{2} - \frac{4b}{3} - \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} - \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54} - \right.} \\
&\quad \left. \frac{\left(-a^3 + 4ab - 8c\right)}{4\sqrt{\left(\frac{a^2}{4} - \frac{2b}{3} + \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} + \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54}\right)}}\right)} \\
r_3 &= \frac{-a}{4} + \frac{1}{2}\sqrt{\left(\frac{a^2}{4} - \frac{2b}{3} + \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} + \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54}\right)} \\
&\quad - \frac{1}{2}\sqrt{\left(\frac{a^2}{2} - \frac{4b}{3} - \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} - \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54} + \right.} \\
&\quad \left. \frac{\left(-a^3 + 4ab - 8c\right)}{4\sqrt{\left(\frac{a^2}{4} - \frac{2b}{3} + \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} + \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54}\right)}}\right)} \\
r_4 &= \frac{-a}{4} + \frac{1}{2}\sqrt{\left(\frac{a^2}{4} - \frac{2b}{3} + \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} + \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54}\right)} \\
&\quad + \frac{1}{2}\sqrt{\left(\frac{a^2}{2} - \frac{4b}{3} - \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} - \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54} + \right.} \\
&\quad \left. \frac{\left(-a^3 + 4ab - 8c\right)}{4\sqrt{\left(\frac{a^2}{4} - \frac{2b}{3} + \frac{2^{\frac{1}{3}}\left(b^2 - 3ac + 12d\right)}{3\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}} + \frac{\left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd + \sqrt{-4\left(b^2 - 3ac + 12d\right)^3 + \left(2b^3 - 9abc + 27c^2 + 27a^2d - 72bd\right)^2}\right)^{\frac{1}{3}}}{54}\right)}}\right)}
\end{aligned}
$$

Quintic Formula



Whirlwind tour through the life of Galois

- **Born in 17th Century France**
- Father was a Republican and head of a liberal party
- Schooled by his mother for first 12 years
- Started reading current math research at age 15
- Rejected from France’s premier university
- Father commits suicide
- Rejected again
- Expelled for expressing dissent
- Tries to publish work later recognized as foundational to abstract algebra

Whirlwind tour through the life of Galois

- Born in 17th Century France
- Father was a Republican and head of a liberal party
- **Schooled by his mother for first 12 years**
- Started reading current math research at age 15
- Rejected from France’s premier university
- Father commits suicide
- Rejected again
- Expelled for expressing dissent
- Tries to publish work later recognized as foundational to abstract algebra

Whirlwind tour through the life of Galois

$$x = a_0 + \cfrac{1}{a_1 + \cfrac{1}{a_2 + \cfrac{1}{a_3 + \cfrac{1}{a_4 + \cfrac{1}{a_5 + \cfrac{1}{a_6 + \ldots.}}}}}}$$

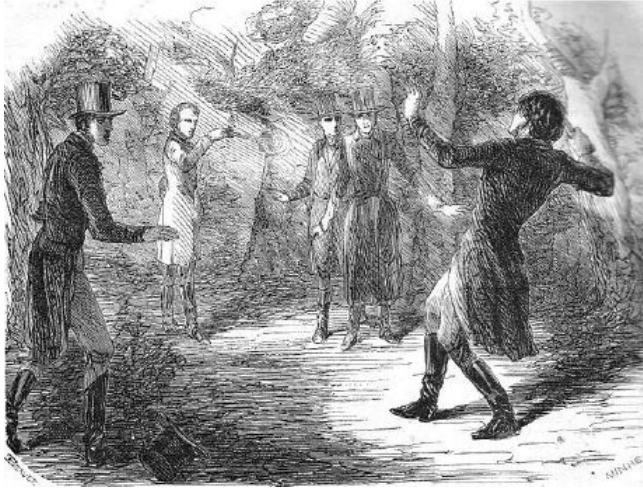
- Born in 17th Century France
- Father was a Republican and head of a liberal party
- Schooled by his mother for first 12 years
- **Started reading current math research at age 15**
- Rejected from France’s premier university
- Father commits suicide
- Rejected again
- Expelled for expressing dissent
- Tries to publish work later recognized as foundational to abstract algebra

Whirlwind tour through the life of Galois

- Born in 17th Century France
- Father was a Republican and head of a liberal party
- Schooled by his mother for first 12 years
- Started reading current math research at age 15
- **Rejected from France’s premier university**
- Father commits suicide
- **Rejected again**
- Expelled for expressing dissent
- Tries to publish work later recognized as foundational to abstract algebra

At this point, how old do you think Galois is?

Whirlwind tour through the life of Galois



- Born in 17th Century France
- Father was a Republican and head of a liberal party
- Schooled by his mother for first 12 years
- Started reading current math research at age 15
- Rejected from France’s premier university
- Father commits suicide
- Rejected again
- Expelled for expressing dissent
- Tries to publish work later recognized as foundational to abstract algebra
- **Died in a duel at 20**