

* Given = $M = P_1 L_1 P_2 L_2 U$

$$P = P_1 P_2, \quad L = P_2^T L_1 P_2 L_2$$

$$P^T M = L \cdot U$$

L.H.S.:

$$(P_1 P_2)^T (P_1 L_1 P_2 L_2 U)$$

$$= P_2^T P_1^T P_1 L_1 P_2 L_2 U \quad [\because (AB)^T = B^T A^T]$$

$$= P_2^T \cdot I \cdot L_1 P_2 L_2 U \quad [\because P^T P = P P^T = I]$$

$$= \underbrace{P_2^T L_1 P_2 L_2}_L U$$

$$= L \cdot U$$