

$$\begin{aligned}
& \text{> } f := x \rightarrow \ln(1 + x) \\
& \qquad \qquad \qquad f := x \rightarrow \ln(1 + x) \tag{1} \\
& \text{> } Tf := \text{unapply}(\text{convert}(\text{taylor}(f(x), x=0, 9), \text{polynom}), x) \\
& \qquad \qquad \qquad Tf := x \rightarrow x - \frac{1}{2} x^2 + \frac{1}{3} x^3 - \frac{1}{4} x^4 + \frac{1}{5} x^5 - \frac{1}{6} x^6 + \frac{1}{7} x^7 - \frac{1}{8} x^8 \tag{2} \\
& \text{> evalf}(Tf(1)) \\
& \qquad \qquad \qquad 0.6345238095 \tag{3} \\
& \text{> evalf}(f(1)) \\
& \qquad \qquad \qquad 0.6931471806 \tag{4} \\
& \text{> } n := 1 : \text{while evalf}\left(\left|\text{unapply}(\text{convert}(\text{taylor}(f(x), x=0, n), \text{polynom}), x)(1) - f(1)\right|\right) \\
& \qquad \qquad \qquad > \frac{1}{100000} \text{do } n := n + 1000 \text{end do: } n \\
& \qquad \qquad \qquad 50001 \tag{5} \\
& \text{> } g := x \rightarrow \ln\left(\frac{1+x}{1-x}\right) \\
& \qquad \qquad \qquad g := x \rightarrow \ln\left(\frac{1+x}{1-x}\right) \tag{6} \\
& \text{> } Tg := \text{unapply}(\text{convert}(\text{taylor}(g(x), x=0, 9), \text{polynom}), x) \\
& \qquad \qquad \qquad Tg := x \rightarrow 2x + \frac{2}{3} x^3 + \frac{2}{5} x^5 + \frac{2}{7} x^7 \tag{7} \\
& \text{> evalf}\left(Tg\left(\frac{1}{3}\right)\right) \\
& \qquad \qquad \qquad 0.6931347573 \tag{8} \\
& \text{> evalf}\left(g\left(\frac{1}{3}\right)\right) \\
& \qquad \qquad \qquad 0.6931471806 \tag{9} \\
& \text{> } n := 1 : \text{while evalf}\left(\left|\text{unapply}(\text{convert}(\text{taylor}(g(x), x=0, n), \text{polynom}), x)\left(\frac{1}{3}\right) - g\left(\frac{1}{3}\right)\right|\right) \\
& \qquad \qquad \qquad > \frac{1}{100000} \text{do } n := n + 1 \text{end do: } n \\
& \qquad \qquad \qquad 10 \tag{10} \\
& \text{> restart} \\
& \text{> } Rf := \text{unapply}\left(\frac{x^{n+1} \cdot \text{diff}(f(x), x\$n) \cdot \text{Theta} \cdot x}{(n+1)!}, [x, n, \text{Theta}]\right) \\
& \qquad \qquad \qquad Rf := (x, n, \Theta) \rightarrow \frac{x^{n+1} \left(\frac{d^n}{dx^n} f(x)\right) \Theta x}{(n+1)!} \tag{11} \\
& \text{>}
\end{aligned}$$