

# Micrograd

A presentation by Andrej Karpathy on Aug 2022: [The spelled-out intro to neural networks and backpropagation: building micrograd](https://www.youtube.com/watch?v=VMj-3S1tku0&list=PLAqHirjkxbuWI23v9cThsA9GvCAUhrvKZ&index=2) - implemented in Python.

Re-implemented in Julia.

Links:

- [micrograd on github](#)
- [Julia](#)
- [Graphviz documentation](#)
- [Julia graphviz](#)

```
• md"""
• ## Micrograd
•
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micrograd](https://www.youtube.com/watch?v=VMj-3S1tku0&list=PLAqHirjkxbuWI23v9cThsA9GvCAUhrvKZ&index=2) - implemented
in `Python`.
•
• Re-implemented in `Julia`.
•
• Links:
• - [micrograd on github](https://github.com/karpathy/micrograd)
• - [Julia](https://www.julialang.org/)
• - [Graphviz documentation](https://www.graphviz.org/documentation/)
• - [Julia graphviz](https://github.com/JuliaGraphs/GraphViz.jl)
•
• """
```

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```
• begin
•     using PlutoUI
•     PlutoUI.TableOfContents(indent=true, depth=4, aside=true)
• end
```

## Data Structure

```
• mutable struct Value{T <: Real}
•     data::T
•     _prev::Set
•     _op::Symbol
•     _backward::Function
•     label::String
•     grad::T
•
•     function Value{T}(data::T;
•         _children::Tuple=(),
•         _op::Symbol=:_ ,
•         label::String=""
•     ) where {T <: Real}
•         grad = zero(T)
•         _backward = () -> nothing # default to Nothing
•         new{T}(data, Set(_children), _op, _backward, label, grad)
•     end
• end
```

```
• import Base: +, -, *, /, ^
```

```
const DT = Float64
```

```
• const DT = Float64
```

YaValue (generic function with 1 method)

```
• # default constructor for Float64
• function YaValue(data::T; _children::Tuple=(), _op::Symbol=:_, label::String="") where {T <: Real}
•     Value{T}(data; _children, _op, label)
• end
```

```
• function Base.:+(self::Value{T}, other::Value{T}) where {T <: Real}
•     y = YaValue(self.data + other.data; _children=(self, other), _op=:+)
•     function _backward_fn()
•         self.grad += 1.0 * y.grad
•         other.grad += 1.0 * y.grad
•     end
•     y._backward = _backward_fn
•     y
• end
```

```
• function Base.:*(self::Value{T}, other::Value{T}) where {T <: Real}
•     y = YaValue(self.data * other.data; _children=(self, other), _op=:*)
•     function _backward_fn()
•         self.grad += other.data * y.grad
•         other.grad += self.data * y.grad
•     end
•     y._backward = _backward_fn
•     y
• end
```

```
• Base.show(io::IO, self::Value) = print(io, "Value(data=$(self.data))")
```

```
• function Base.tanh(self::Value{T}) where {T <: Real}
•     x = exp(2*self.data)
•     tanh = (x - 1.) / (x + 1.)
•     y = YaValue(tanh; _children=(self, ), _op=:tanh, label="tanh")
•     function _backward_fn()
•         self.grad += (1. - tanh^2) * y.grad
•     end
•     y._backward = _backward_fn
•     y
• end
```

backward (generic function with 1 method)

```
• function backward(self::Value{T}) where {T <: Real}
•     topo, visited = [], Set()
•     function build_topological_order(v::Value)
•         if v ∉ visited
•             push!(visited, v)
•             for child ∈ v._prev
•                 build_topological_order(child)
•             end
•             push!(topo, v)
•         end
•     end
•     self.grad = 1.0
•     for cnode ∈ build_topological_order(self) |> reverse
•         cnode._backward()
•     end
• end
```

"Output"

```
• begin
•     a = YaValue(2.0; label="a")
•     b = YaValue(-3.0; label="b")
•     c = YaValue(10.0; label="c")
•
•     d = a * b; d.label = "d"
•     e = d + c; e.label = "e"
•
•     f = YaValue(-2.0; label="f")
•     L = e * f; L.label="Output"
• end
```

```
(Set([Value(data=-3.0), Value(data=2.0)]), :*)
```

```
• d._prev, d._op
```

## Visualization

```
• using GraphViz, FileIO, Cairo
```

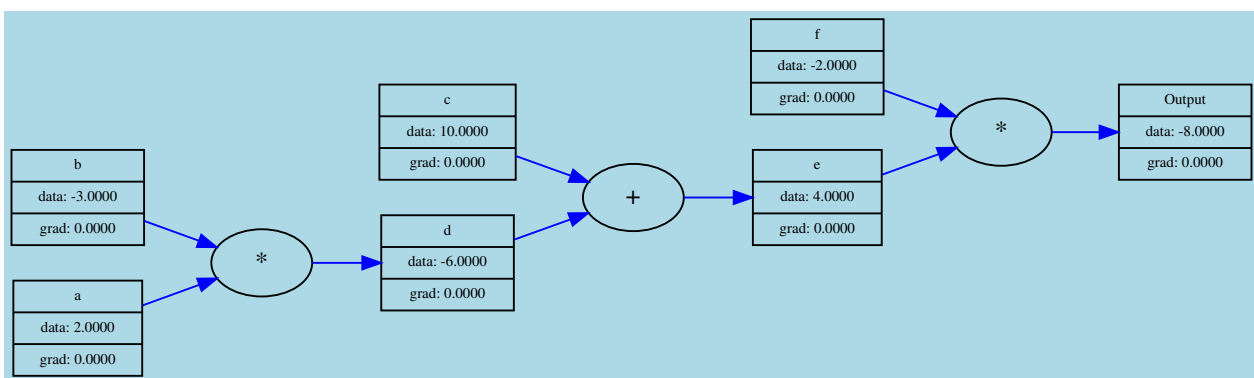
• using Printf

draw\_dot (generic function with 1 method)

```
• ## for visualization
• begin
•     function trace(root::Value)
•         # builds a set of all nodes and all edges in a graph
•         nodes, edges = Set(), Set()
•         function build(v::Value)
•             if v ∉ nodes
•                 push!(nodes, v)
•                 for child ∈ v._prev
•                     push!(edges, (child, v))
•                     build(child)
•                 end
•             end
•         end
•         build(root)
•         nodes, edges
•     end

•     function draw_dot(root::Value)
•         gr = ""
•         format=svg;
•         rankdir="LR";
•         dpi=72;
•         bgcolor=lightblue;
•         imagepos="mc";
•         landscape=false;
•         mode="hier";
•         layout=dot
•         node [shape=record];
•         "" # Left to Right
•         nodes, edges = trace(root)
•         for n ∈ nodes
•             uid = string(objectid(n))
•             gr = string(gr,
•                 ""
•                 $(uid) [name=$(uid),label="$(Printf.@sprintf "%s | data: %.4f | grad: %.4f" n.label n.data
•                 n.grad)",fontsize=8];
•                 ""
•             )
•             if n._op != :_
•                 gr = string(gr,
•                     ""
•                     "$(string(uid, n._op))" [name=$(string(uid)),label="$(string(n._op))",shape="ellipse"];
•                     "$(string(uid, n._op))" -- $(uid) [color=blue,dir=forward];
•                     ""
•                 )
•             end
•         end
•         for (n1, n2) ∈ edges
•             gr = string(gr,
•                 ""
•                 $(string(objectid(n1))) -- "$(string(objectid(n2), n2._op))" [color=blue,dir=forward];
•                 ""
•             )
•         end
•         gr = string("""graph G {""", gr, ""}""")
•         # dot""
•         # $(gr)
•         # ""
•         open("digraph.dot", "w") do io
•             write(io, gr)
•         end

•         open("digraph.dot", "r") do io
•             GraphViz.load(io)
•         end
•     end
• end
```



• draw\_dot(L)

# Manual backpropagation and gradient

try\_grad (generic function with 1 method)

```

• function try_grad()
•   h = 0.001
•
•   a = YaValue(2.0; label="a")
•   b = YaValue(-3.0; label="b")
•   c = YaValue(10.0; label="c")
•   f = YaValue(-2.0; label="f")
•   # compose
•   d = a * b; d.label = "d"
•   e = d + c; e.label = "e"
•   L = e * f; L.label="Output"
•
•   a1 = YaValue(a.data; label="a")
•   b1 = YaValue(b.data; label="b")
•   c1 = YaValue(c.data; label="c")
•   f1 = YaValue(f.data; label="f")
•   # compose
•   d1 = a1 * b1; d1.label = "d"
•   d1.data += h
•   e1 = d1 + c1; e1.label = "e"
•   L1 = e1 * f1; L1.label="Output"
•
•   Δh = (L1.data - L.data) / h
• end

```

-2.000000000000668

```

• # got 7 var =>
• try_grad()

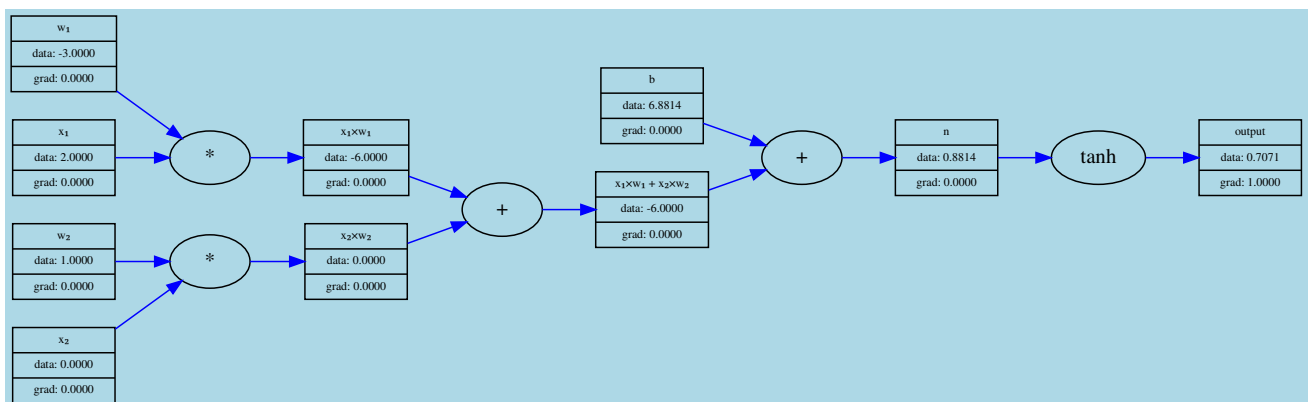
```

one\_neuron (generic function with 1 method)

```

• function one_neuron()
•   # 2 inputs
•   x1, x2 = YaValue(2.0; label="x1"), YaValue(0.0; label="x2")
•   # 2 weights
•   w1, w2 = YaValue(-3.0; label="w1"), YaValue(1.0; label="w2")
•   # bias
•   b = YaValue(6.8813735870195432; label="b")
•
•   x1w1 = x1 * w1
•   x1w1.label = "x1×w1"
•   x2w2 = x2 * w2
•   x2w2.label = "x2×w2"
•
•   # x1w1 + x2w2 + b
•   x1w1x2w2 = x1w1 + x2w2
•   x1w1x2w2.label = "x1×w1 + x2×w2"
•   n = x1w1x2w2 + b
•   n.label = "n"
•
•   o = tanh(n)
•   o.label = "output"
•   (o, n, x1w1x2w2, b, x1w1, x2w2, x1, x2, w1, w2)
• end

```



```

• begin
•   (o, n, x1w1x2w2, bias, x1w1, x2w2, x1, x2, w1, w2) = one_neuron()
•   o.grad = 1.0
•   draw_dot(o)
• end

```

Let's do backpropagation through tanh. So what is  $\frac{do}{dn}$  given  $o = \tanh(n)$ ?

By definition:  $\frac{do}{dn} = 1 - o^2 = 1 - \tanh(n)^2$

(0.5, 0.5)

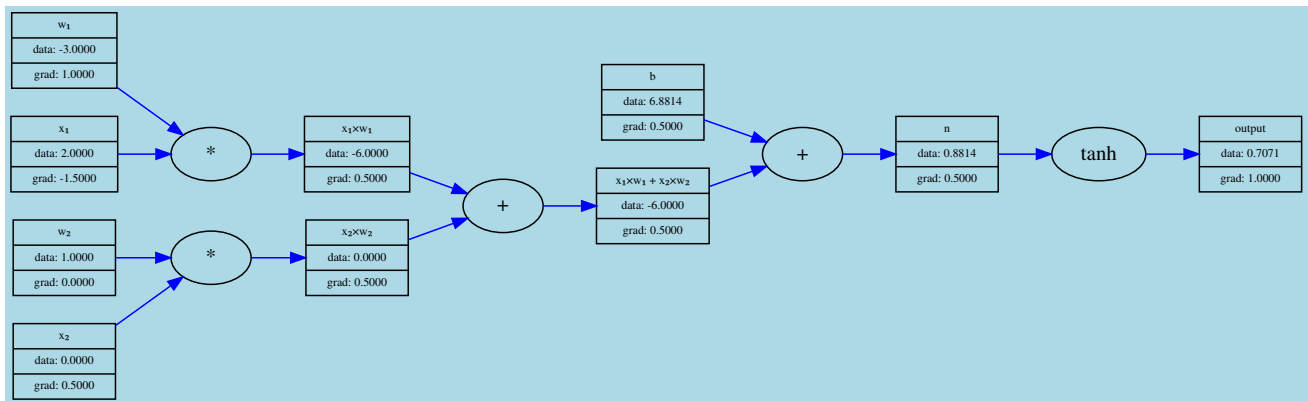
```
• begin
•   n.grad = 1 - o.data^2
•
•   # we also can fill in the gradient for  $x_1w_1x_2w_2$ ,  $b$  - applying + rule
•    $x_1w_1x_2w_2$ .grad = bias.grad = n.grad
•
•   # and for  $x_1w_1$ ,  $x_2w_2$  - applying + rule
•    $x_1w_1$ .grad,  $x_2w_2$ .grad =  $x_1w_1x_2w_2$ .grad,  $x_1w_1x_2w_2$ .grad
• end
```

(0.5, 0.0)

```
•  $x_2$ .grad,  $w_2$ .grad =  $w_2$ .data *  $x_2w_2$ .grad,  $x_2$ .data *  $x_2w_2$ .grad
```

(-1.5, 1.0)

```
•  $x_1$ .grad,  $w_1$ .grad =  $w_1$ .data *  $x_1w_1$ .grad,  $x_1$ .data *  $x_1w_1$ .grad
```



```
• # redraw graph with gradient updated
• draw_dot(o)
```

## Backpropagation programmatically

Of course, we need to update all arithmetic operations on our datatype.

backprop\_one\_neuron (generic function with 1 method)

```
• function backprop_one_neuron()
•   # 2 inputs
•    $x_1$ ,  $x_2$  = YaValue(2.0; label=" $x_1$ "), YaValue(0.0; label=" $x_2$ ")
•   # 2 weights
•    $w_1$ ,  $w_2$  = YaValue(-3.0; label=" $w_1$ "), YaValue(1.0; label=" $w_2$ ")
•   # bias
•    $b$  = YaValue(6.8813735870195432; label=" $b$ ")
•
•    $x_1w_1 = x_1 * w_1$ 
•    $x_1w_1$ .label = " $x_1 \times w_1$ "
•    $x_2w_2 = x_2 * w_2$ 
•    $x_2w_2$ .label = " $x_2 \times w_2$ "
•
•   #  $x_1w_1 + x_2w_2 + b$ 
•    $x_1w_1x_2w_2 = x_1w_1 + x_2w_2$ 
•    $x_1w_1x_2w_2$ .label = " $x_1 \times w_1 + x_2 \times w_2$ "
•    $n = x_1w_1x_2w_2 + b$ 
•    $n$ .label = " $n$ "
•
•    $o = \tanh(n)$ 
•    $o$ .label = "output"
•   # ( $o$ ,  $n$ ,  $x_1w_1x_2w_2$ ,  $b$ ,  $x_1w_1$ ,  $x_2w_2$ ,  $x_1$ ,  $x_2$ ,  $w_1$ ,  $w_2$ )
•
•   # and now the backward pass
•    $o$ .grad = 1.0
•    $o$ ._backward()
•    $n$ ._backward()
•    $x_1w_1x_2w_2$ ._backward()
•    $x_1w_1$ ._backward()
•    $x_2w_2$ ._backward()
•   #  $b$ ._backward()
•    $o$ 
• end
```



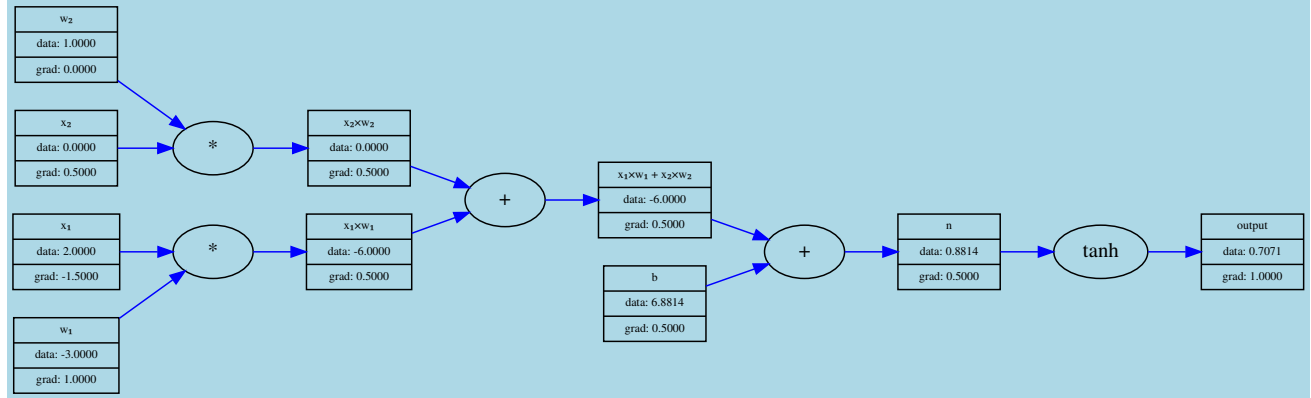
topological\_order (generic function with 1 method)

```
[Value(data=6.881373587019543), Value(data=-3.0), Value(data=2.0), Value(data=-6.0), Value(data=1.0), Value(data=0.0), Value(data=-1.0)]
• topological_order(o4)
```

```

• function auto_backprop_one_neuron()
•     # 2 inputs
•      $x_1, x_2 = \text{YaValue}(2.0; \text{label}="x_1"), \text{YaValue}(0.0; \text{label}="x_2")$ 
•     # 2 weights
•      $w_1, w_2 = \text{YaValue}(-3.0; \text{label}="w_1"), \text{YaValue}(1.0; \text{label}="w_2")$ 
•     # bias
•      $b = \text{YaValue}(6.8813735870195432; \text{label}="b")$ 
•
•     # forward pass
•      $x_1 w_1 = x_1 * w_1$ 
•      $x_1 w_1.\text{label} = "x_1 \times w_1"$ 
•      $x_2 w_2 = x_2 * w_2$ 
•      $x_2 w_2.\text{label} = "x_2 \times w_2"$ 
•
•     #  $x_1 w_1 + x_2 w_2 + b$ 
•      $x_1 w_1 x_2 w_2 = x_1 w_1 + x_2 w_2$ 
•      $x_1 w_1 x_2 w_2.\text{label} = "x_1 \times w_1 + x_2 \times w_2"$ 
•      $n = x_1 w_1 x_2 w_2 + b$ 
•      $n.\text{label} = "n"$ 
•
•      $o = \tanh(n)$ 
•      $o.\text{label} = "output"$ 
•
•     # and now the backward pass, using reverse order of the graph's topological order
•      $o.\text{grad} = 1.0$ 
•     for  $cnode \in \text{topological\_order}(o) \mid > \text{reverse}$ 
•          $cnode.\_backward()$ 
•     end
• end
• end

```



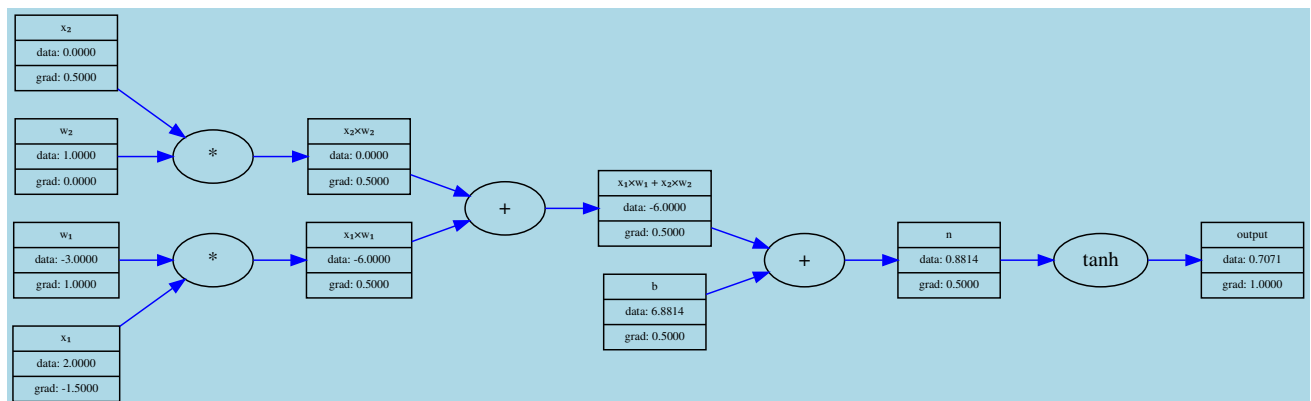
```

• begin
•    $o_2 = \text{auto\_backward\_one\_neuron}()$ 
•   draw_dot( $o_2$ )
• end

```

After defining the function `backward` on our datatype (`Value`) we can invoke it!

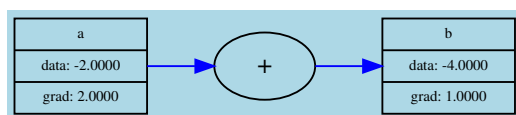
Let's do this...



```

• begin
•   ( $o_3$ ,  $\_rest\_$ ) = one_neuron()
•   backward( $o_3$ )
•   draw_dot( $o_3$ )
• end

```



```

• begin
•   # need to use += in _backward() function on Value type.
•   aa = YaValue(-2.0, label="a")
•   bb = aa + aa
•   bb.label = "b"
•   backward(bb)
•   draw_dot(bb) # double arrow from a to :+ - expected  $\nabla(aa) == 2$ .
• end

```

## Re-implementing tanh using basic building blocks

### Julia Apparte - Conversion and Promotion rules

First we want to be able to write something like

```

a = Value(2.0, label="a")
a + 1 # MethodError: no method matching +(...)

```

As it is with our datatype, this is not working because `1` is not a `Value` it is just an integer. OK, so let's add some methods (in Julia terminology) for our arithmetic operators, namely by adding promotion rules.

promote\_rule (generic function with 152 methods)

```
• begin
•   import Base: promote_rule, convert
•
•   # these two allow: promote(xr, r) where xr is Value{Float64} and r is Float64 => Value{Float64}
•   #                       promote(xi, i) where xi is Value{Int64} and i is Int64 => Value{Int64}
•   convert(::Type{Value{T}}, x::T) where {T <: Real} = Value{T}(x)
•   promote_rule(::Type{Value{T}}, ::Type{T}) where {T <: Real} = Value{T}
•
•   # Value{Float64} and Float32 => Value{Float64}
•   convert(::Type{Value{T}}, x::S) where {T <: Real, S <: AbstractFloat} = Value{T}(T(x))
•   promote_rule(::Type{Value{T}}, ::Type{S}) where {T <: Real, S <: AbstractFloat} = Value{T}
•
•   # Value{Float64} and Integer => Value{Float64}
•   convert(::Type{Value{T}}, x::S) where {T <: Real, S <: Integer} = Value{T}(T(x))
•   promote_rule(::Type{Value{T}}, ::Type{S}) where {T <: Real, S <: Integer} = Value{T}
•
•   convert(::Type{Value{T}}, x::Type{Value{S}}) where {T <: Real, S <: T} = Value{T}(T(x.data))
•   promote_rule(::Type{Value{T}}, ::Type{Value{S}}) where {T <: Real, S <: T} = Value{promote_type(T, S)}
• end
```

(Value{Float64}, Value{Float32}, Value{Int64}, Value{Int32})

```
• begin
•   vf64 = YaValue(2.0, label="vf64")
•   vf32 = YaValue(Float32(2.0), label="vf32")
•   vi64 = YaValue(2, label="vi64")
•   vi32 = YaValue(Int32(2), label="vi32")
•
•   typeof(vf64), typeof(vf32), typeof(vi64), typeof(vi32)
• end
```

((Value(data=2), Value(data=4)), (Value(data=2), Value(data=16)))

```
• begin # from Int -> Value{Int}
•   i64, i32 = 4, Int32(16)
•   promote(vi64, i64), promote(vi64, i32)
• end
```

(Value(data=2.0), Value(data=2.0))

```
• begin # from Float -> Value{Float}
•   f64 = 2.0
•   promote(vf64, f64)
• end
```

(Value(data=2.0), Value(data=3.1415927410125732))

```
• begin # from Float32 -> Value{Float64}, Float16 -> Value{Float32} ...
•   f32 = Float32(π)
•   promote(vf64, f32)
• end
```

(Value(data=2.0), Value(data=16.0))

```
• promote(vf64, i32) # from Int -> Value{Float}
```

```
• ##
• ## Extending operator for DataType Value{T}
• ##
• for op ∈ (:+, :*)
•   @eval begin
•     ## Allowing:
•     # - Value{T} :op T => Value{T}
•     # - T :op Value{T} => Value{T}
•     ($op)(self::Value{T}, other::T) where {T <: Real} = ($op)(self, Value{T}(other))
•     ($op)(other::T, self::Value{T}) where {T <: Real} = ($op)(self, Value{T}(other))
•
•     # Allowing Value{T} :op S => Value{T} where S <: T
•     ($op)(self::Value{T}, other::S) where {T <: Real, S <: Integer} =
•       ($op)(self, Value{T}(T(other)))
•     ($op)(other::S, self::Value{T}) where {T <: Real, S <: Integer} =
•       ($op)(self, Value{T}(T(other)))
•
•     # Allowing Value{T} :op Value{S} => Value{T} where S <: T
•     ($op)(self::Value{T}, other::Value{S}) where {T <: Real, S <: Real} =
•       ($op)(self, Value{T}(T(other.data)))
•     ($op)(other::Value{S}, self::Value{T}) where {T <: Real, S <: Real} =
•       ($op)(self, Value{T}(T(other.data)))
•   end
• end
```

(Value(data=6), Value(data=18), Value{Int64}, Value{Int64})

```
• vi64 + i64, vi64 + i32, typeof(vi64 + i64), typeof(vi64 + i32)
```

(Value(data=6.0), Value(data=18.0), Value{Float64}, Value{Float64})

```
• vf64 + i64, vf64 + i32, typeof(vf64 + i64), typeof(vf64 + i32)
```



```
(Value(data=4.0), Value{Float64}, Float64)
```

```
• vf64 + f64, typeof(vf64), typeof(f64)
```

```
(Value(data=4), Value{Float64}, Value{Int32})
```

```
• vf64 + vi64, typeof(vf64), typeof(vi32) # Value{Float64} + Value{Int64}
```

```
(Value(data=4.0), Value(data=4.0), Value{Float64}, Value{Float32})
```

```
• vf64 + vf32, vf32 + vf64, typeof(vf64), typeof(vf32) # Value{Float64} + Value{Float32}
```

```
(AbstractFloat, AbstractFloat)
```

```
• supertype.((Float32, Float64))
```

subtypetree (generic function with 3 methods)

```
• function subtypetree(rtype, level=1, indent=2)
•   level == 1 && (println(rtype))
•   for st ∈ subtypes(rtype)
•     println(string(repeat(" ", level * indent), st))
•     subtypetree(st, level + 1, indent)
•   end
• end
```

```
• subtypetree(Real)
```

```
Real
AbstractFloat
  BigFloat
  Float16
  Float32
  Float64
AbstractIrrational
  Irrational
FixedPointNumbers.FixedPoint
FixedPointNumbers.Fixed
FixedPointNumbers.Normed
Integer
Bool
Signed
  BigInt
  Int128
  Int16
  Int32
  Int64
  Int8
Unsigned
  UInt128
  UInt16
  UInt32
  UInt64
  UInt8
Rational
StatsBase.PValue
StatsBase.TestStat
```

```
• # subtypetree(Integer)
```

```
• # subtypetree(AbstractFloat)
```

Value(data=4.0)

```
• begin
•   z2 = YaValue(2.0)
•   2 * z2
• end
```

## tanh in terms of exp.

```
• function Base.exp(self::Value{T}) where {T <: Real}
•   x = self.data
•   y = YaValue(exp(x); _children=(self, ), _op=:exp, label="exp")
•   function _backward_fn()
•     self.grad += y.data * y.grad # because ∂exp/∂x = exp
•   end
•   y._backward = _backward_fn
•   y
• end
```

## More operators

Note that  $a / b == a \times 1/b == a \times b^{-1}$

```
• Base.:/ (self::Value{T}, other::Value{T}) where {T <: Real} = Base.:*(self, other^(-1.))
```

```

• function Base.^(self::Value{T}, p::T) where {T <: Real}
•     y = YaValue(self.data^p; _children=(self, ), _op=:^, label="^p")
•     function _backward_fn()
•         self.grad += p * self.data^(p - 1) * y.grad # because  $\partial x^p / \partial x = p x^{p-1}$ 
•     end
•     y._backward = _backward_fn
•     y
• end

```

```

• # Allow for integer value for power
• Base.^(self::Value{T}, n::S) where {T <: Real, S <: Integer} = Base.^(self, T(n))

```

```

• Base.-(self::Value{T}, other::Value{T}) where {T <: Real} = Base.+(self, other * -1.)

```

```

• Base.-(self::Value{T}, other::S) where {T <: Real, S <: Real} = Base.+(self, other * -1.)

```

```

(Value(data=0.5), Value(data=-3.0), Value(data=3.0))

```

```

• z₂ / YaValue(4.0), z₂ - YaValue(5.0), YaValue(5.0) - 2

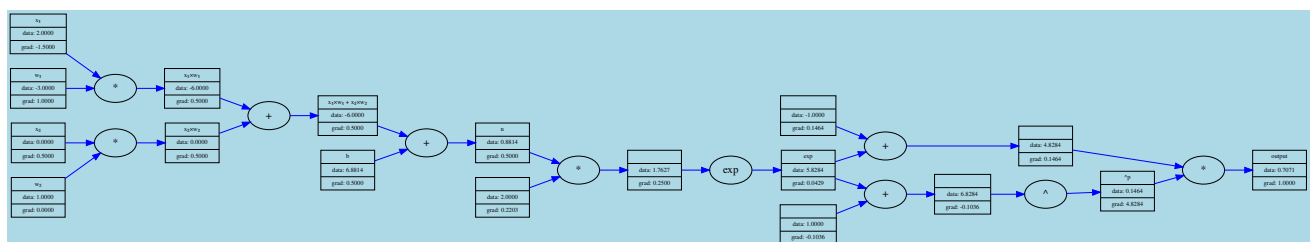
```

one\_neuron\_alt (generic function with 1 method)

```

• function one_neuron_alt()
•     # 2 inputs
•     x₁, x₂ = YaValue(2.0; label="x₁"), YaValue(0.0; label="x₂")
•     # 2 weights
•     w₁, w₂ = YaValue(-3.0; label="w₁"), YaValue(1.0; label="w₂")
•     # bias
•     b = YaValue(6.8813735870195432; label="b")
•
•     x₁w₁ = x₁ * w₁
•     x₁w₁.label = "x₁×w₁"
•     x₂w₂ = x₂ * w₂
•     x₂w₂.label = "x₂×w₂"
•
•     # x₁w₁ + x₂w₂ + b
•     x₁w₁x₂w₂ = x₁w₁ + x₂w₂
•     x₁w₁x₂w₂.label = "x₁×w₁ + x₂×w₂"
•     n = x₁w₁x₂w₂ + b
•     n.label = "n"
•
•     # -----
•     # o = tanh(n)
•     e = exp(2 * n)
•     o = (e - 1) / (e + 1)
•     o.label = "output"
•     # -----
•     # (o, n, x₁w₁x₂w₂, b, x₁w₁, x₂w₂, x₁, x₂, w₁, w₂)
•     o
• end

```



```

• begin
•     o₄ = one_neuron_alt()
•     backward(o₄)
•     draw_dot(o₄)
• end

```

## Implementing a MLP

### Neuron Datatype

```

• using Random, Distributions

```

```

TaskLocalRNG()

```

```

• Random.seed!(42)

```

```

• # const uniform_d = Uniform(-1, 1) # = Distributions.Uniform{Float64}(a=-1.0, b=1.0)

```

```

• # const uniform_df32 = Uniform{Float32}(-1, 1) # = Distributions.Uniform{Float32}(a=-1.0f0, b=1.0f0)

```

```

• # const NT = rand(uniform_d, 1) /> eltype # = Float64

```

```

• struct Neuron{T <: AbstractFloat}
•   w::Vector{Value{T}}
•   b::Value{T}
•
•   function Neuron{T}(n_inp::Integer; dist=Uniform{T}(-1., 1.)) where {T <: AbstractFloat}
•       @assert n_inp ≥ 1
•       w = Value{T}.(rand(dist, n_inp))
•       b = Value{T}(rand(dist, 1)[1])
•       new(w, b)
•   end
•
•   function Neuron{Float32}(n_inp::Integer; dist=Uniform{Float32}(-1., 1.))
•       @assert n_inp ≥ 1
•       w = [Value{Float32}(Float32(rand(dist, n_inp)[1])) for _ ∈ 1:n_inp]
•       b = Value{Float32}(Float32(rand(dist, 1)[1]))
•       new(w, b)
•   end
• end

```

Neuron\_f64 (generic function with 1 method)

```

• Neuron_f64(n_inp::Integer) = Neuron{Float64}(n_inp)

```

```

• ## not working as rand will return float64
• #
• # function Neuron_f32(n_inp::Integer)
• #     DT = Float32
• #     Neuron{DT}(n_inp; dist=Uniform{DT}(-1., 1.))
• # end

```

```

n1 =
Neuron([Value(data=-0.9528407451856364), Value(data=-0.8669645439287939), Value(data=0.572640458055439), Value(data=-0.729
• n1 = Neuron_f64(4)

```

```

n2 =
Neuron([Value(data=-0.96375597), Value(data=0.92222244), Value(data=-0.57529426), Value(data=0.3038198)], Value(data=0.446
• n2 = Neuron{Float32}(4)

```

(Float32, Float64)

```

• n2.w[1].data |> typeof, n1.w[1].data |> typeof

```

Union{Vector{T}, Array{Value{T}, 1}} where T<:AbstractFloat

```

• UVT{T} = Union{Vector{T}, Vector{Value{T}}} where {T <: AbstractFloat}

```

## forward

```

forward(...)
eval neuron by taking the dot-product between input and weights, sum, add bias and pass it to activation function

```

```

• """
•     forward(...)
•     eval neuron by taking the dot-product between input and weights, sum, add bias and pass it to activation function
• """
• function forward(self::Neuron{T}, x::UVT{T}; act_fn=tanh) where {T <: AbstractFloat}
•     # x == vector of inputs
•     @assert length(self.w) ≥ 1 && length(self.w) == length(x)
•     self.w .* x |> d -> sum(d; init=self.b) |> act_fn
• end

```

Value(data=-0.9997046316634364)

```

• forward(n, [1., 2., 3., 4.])

```

parameters (generic function with 2 methods)

```

• parameters(self::Neuron{T}) where {T <: AbstractFloat} = [self.w..., self.b]

```

## Layer Datatype

```

• struct Layer{T <: AbstractFloat}
•     neurons::Vector{Neuron{T}}
•
•     function Layer{T}(n_inp::Integer, n_out::Integer) where {T <: AbstractFloat}
•         @assert n_inp ≥ 1 && n_out ≥ 1
•         vn = [Neuron{T}(n_inp) for _ ∈ 1:n_out]
•         new(vn)
•     end
• end

```

forward (generic function with 2 methods)

```
• function forward(self::Layer{T}, x::UVI{T}) where {T <: AbstractFloat}
•   y = [forward(n, x) for n in self.neurons]
•   length(y) == 1 ? y[1] : y
• end
```

parameters (generic function with 3 methods)

```
• parameters(self::Layer{T}) where {T <: AbstractFloat} = [np for n in self.neurons for np in parameters(n)]
```

[Value(data=0.7528646988390475), Value(data=0.9514222376495296), Value(data=0.8607298734680876)]

```
• begin
•   xx₁ = [1.1, 2.0]
•   nl₁ = Layer{Float64}(2, 3) # 2 inputs, 3 outputs
•   forward(nl₁, xx₁)
• end
```

## MLP Datatype

```
• struct MLP{T <: AbstractFloat}
•   layers::Vector{Layer{T}}
•
•   function MLP{T}(n_inp::Integer, n_outs::Vector{<: Integer}) where {T <: AbstractFloat}
•   @assert n_inp ≥ 1 && length(n_outs) ≥ 1
•   sz = [n_inp, n_outs...]
•   layers = [Layer{T}(sz[ix], sz[ix + 1]) for ix in 1:length(n_outs)]
•   new(layers)
• end
• end
```

forward (generic function with 3 methods)

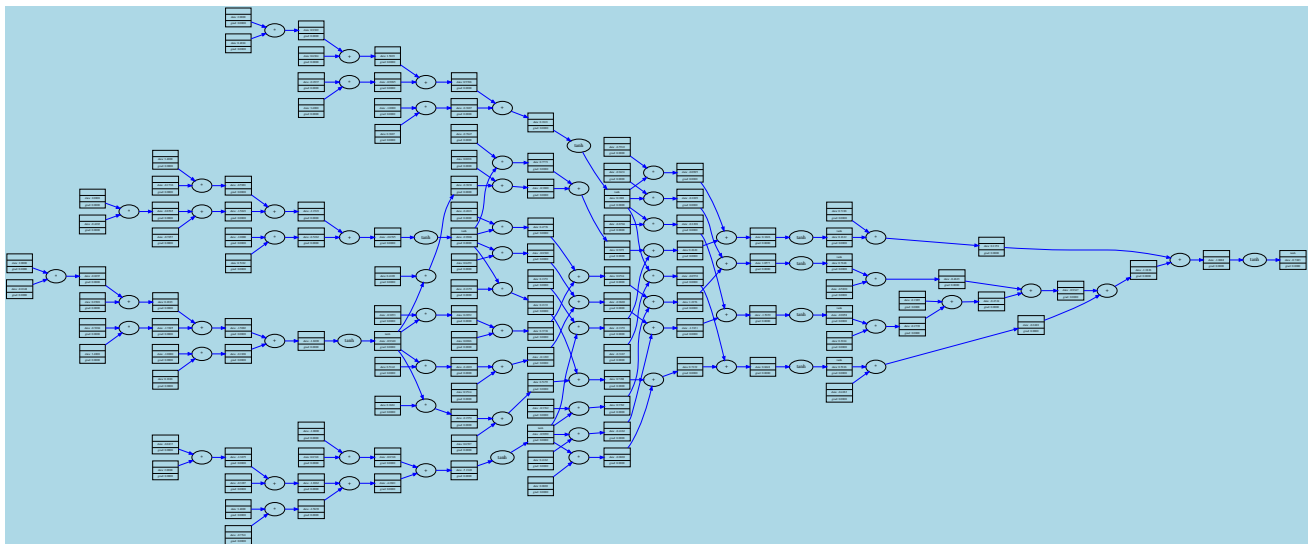
```
• function forward(self::MLP{T}, x::UVI{T}) where {T <: AbstractFloat}
•   for layer in self.layers
•       x = forward(layer, x) # mutate x
•   end
•   x
• end
```

parameters (generic function with 3 methods)

```
• parameters(self::MLP{T}) where {T <: AbstractFloat} = [np for layer in self.layers for np in parameters(layer)]
```

Value(data=-0.7882536109483105)

```
• begin
•   mlp_x = [2.0, 3.4, -1.0] # inputs
•   mlp = MLP{Float64}(3, [4, 4, 1]) # input 3 neurons, 2 hidden with 4 neurons each, 1 output neuron
•   o_x = forward(mlp, mlp_x)
• end
```



```
• draw_dot(o_x)
```

## Loss

Intro MSE [Means Squared Error]

```

Main.var"workspace#6"Value{Float64}[]
1: Value(data=-0.7883809487831563)
2: Value(data=-0.2626439073899099)
3: Value(data=-0.5203633056485637)
4: Value(data=-0.7129315096571979)
]

```

```

• begin
•   xs = [
•     [2.0, 3.0, -1.0],
•     [3.0, -1.0, 0.5],
•     [0.5, 1.0, 1.0],
•     [1.0, 1.0, -1.0]
•   ]
•   ys = [1., -1., -1., 1.] # desired output (or ground truth)
•   ŷ = [forward(mlp, x) for x ∈ xs] # predictions from our MLP
• end

```

```
loss = Value(data=6.906186140624623)
```

```

• # loss
• loss = (ŷ .- ys).^2 |> sum

```

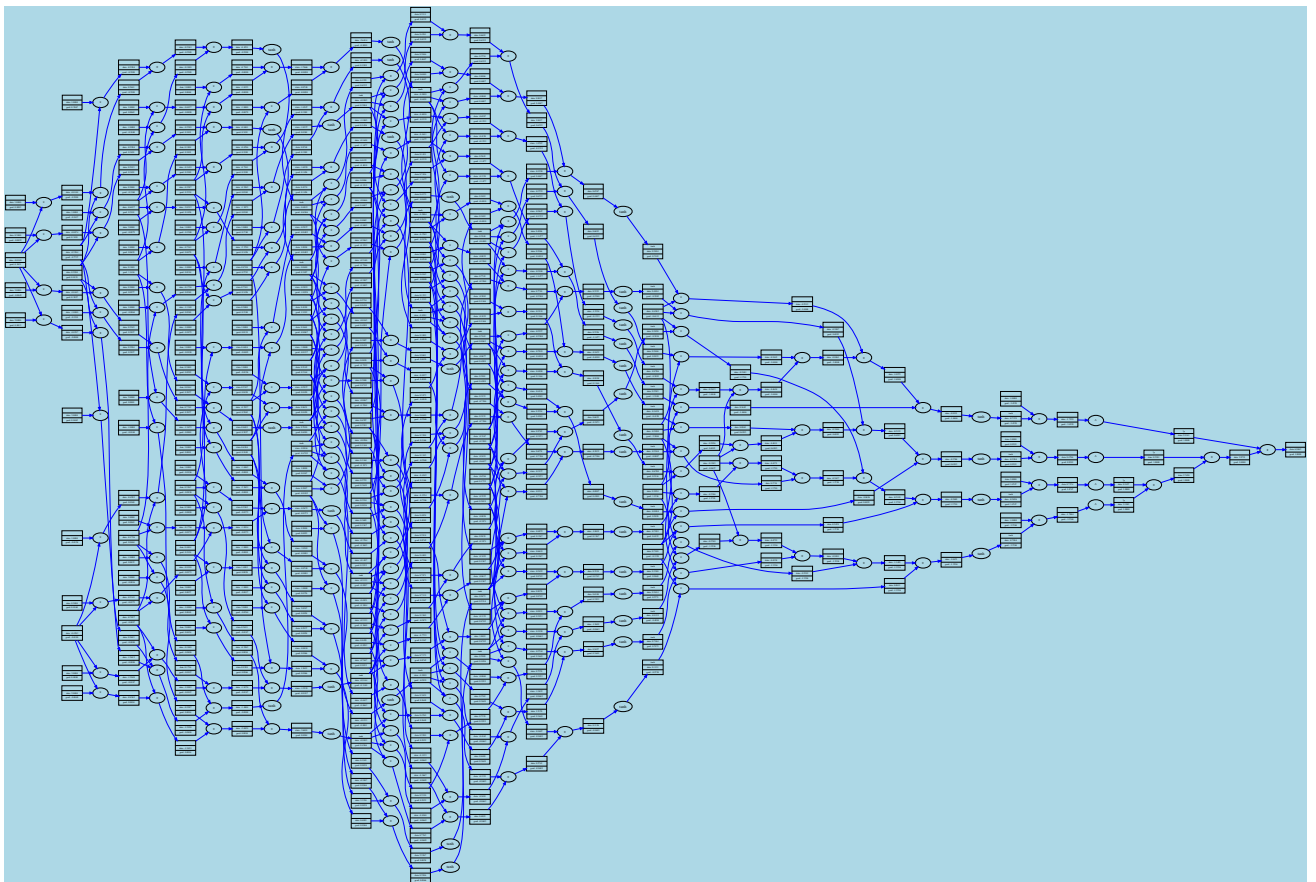
```

• # And now call the backward pass from the loss
• backward(loss)

```

```
(Value(data=-0.014833368087739496), 0.363086)
```

```
• mlp.layers[1].neurons[1].w[1], mlp.layers[1].neurons[1].w[1].grad
```



```
• draw_dot(loss)
```

```
41
```

```
• parameters(mlp) |> length
```

```
const α = 0.02
```

```
• const α = 0.02 # step size
```

```

• for p ∈ parameters(mlp)
•   p.data += -α * p.grad
• end

```

```
(Value(data=-0.022095084804144613), 0.363086)
```

```
• mlp.layers[1].neurons[1].w[1], mlp.layers[1].neurons[1].w[1].grad
```

```
Value(data=6.451046775656205)
```

```

• begin
•   # new forward pass (after the gradient update above)
•   ŷ₁ = [forward(mlp, x) for x ∈ xs] # new predictions from our MLP
•   loss₁ = (ŷ₁ .- ys).^2 |> sum      # we expect the loss to be a bit less... and indeed...
• end

```

# Learning

Ok, now we need to iterate this process: forward -> loss -> backward -> gradient update...

```
. for i ∈ 1:32
.   ŷ2 = [forward(mlp, x) for x ∈ xs]
.
.   # reset .grad to 0 (a common bug is to forget this rule!)
.   for p_ ∈ parameters(mlp)
.     p_.grad = 0.0
.   end
.
.   loss2 = (ŷ2 .- ys).^2 |> sum
.   backward(loss2)
.
.   # update
.   for p_ ∈ parameters(mlp)
.     p_.data += -g * p_.grad
.   end
.   println("""iteration $(@sprintf "%2d" i) - loss: $(@sprintf "%1.5f" loss2.data)""")
. end
```

```
iteration 1 - loss: 6.45105
iteration 2 - loss: 5.83555
iteration 3 - loss: 5.05911
iteration 4 - loss: 4.25152
iteration 5 - loss: 3.55466
iteration 6 - loss: 2.95725
iteration 7 - loss: 2.41454
iteration 8 - loss: 1.93264
iteration 9 - loss: 1.53131
iteration 10 - loss: 1.21531
iteration 11 - loss: 0.97457
iteration 12 - loss: 0.79334
iteration 13 - loss: 0.65664
iteration 14 - loss: 0.55248
iteration 15 - loss: 0.47200
iteration 16 - loss: 0.40884
iteration 17 - loss: 0.35851
iteration 18 - loss: 0.31779
iteration 19 - loss: 0.28440
iteration 20 - loss: 0.25665
iteration 21 - loss: 0.23334
iteration 22 - loss: 0.21353
iteration 23 - loss: 0.19654
iteration 24 - loss: 0.18183
iteration 25 - loss: 0.16901
iteration 26 - loss: 0.15774
iteration 27 - loss: 0.14778
iteration 28 - loss: 0.13891
iteration 29 - loss: 0.13098
iteration 30 - loss: 0.12384
iteration 31 - loss: 0.11740
iteration 32 - loss: 0.11155
```

And done!

Thanks Andrej