

$$\begin{aligned}
I\dot{\omega} &= T_M - T_L \\
v &= Ri + L \frac{\partial i}{\partial t} + \frac{\omega}{K_V} \quad \rightarrow \quad i = \frac{1}{R} \left(v - L \frac{\partial i}{\partial t} - \frac{\omega}{K_V} \right) \\
T_M &= \frac{(i-i_0)}{K_Q} \\
I\dot{\omega} &= \frac{(i-i_0)}{K_Q} - T_L \\
&= (i - i_0) \frac{1}{K_Q} - T_L \\
&= \left[\frac{1}{R} \left(v - L \frac{\partial i}{\partial t} - \frac{\omega}{K_V} \right) - i_0 \right] \frac{1}{K_Q} - T_L \\
&= \left[\frac{1}{R} \left(v - \frac{\omega}{K_V} \right) - i_0 \right] \frac{1}{K_Q} - T_L \\
\text{Linearization:} \\
\Delta\dot{\omega} &= \left[-\frac{1}{RK_V K_Q I} - \frac{2b_{D_1}\omega_0}{I} - \frac{2b_{D_2}\omega_0\alpha_0^2}{I} - \frac{b_{D_3}\alpha_0}{I} \right] \Delta\omega + \left[\frac{1}{RK_Q I} \quad \frac{-2b_{D_2}\omega_0^2\alpha_0}{I} - \frac{-b_{D_3}\omega_0}{I} \right] \begin{bmatrix} \Delta v \\ \Delta\alpha \end{bmatrix} \\
\Delta L &= [2b_L\omega_0\alpha_0] \Delta\omega + \begin{bmatrix} 0 & b_L\omega_0^2 \end{bmatrix} \begin{bmatrix} \Delta v \\ \Delta\alpha \end{bmatrix}
\end{aligned}$$