

This spec captures the actions and states of bitcoin transactions in the context of the bitcoin blockchain. These actions will be used by the *LN Contracts* spec and other layer two contract specifications.

The focus of this module is to provide:

1. Way to generate transactions that accept input and generate outputs
2. Confirm transactions so that outputs can be spent.
3. Most importantly - provide a way to verify spend conditions without building the entire cryptography machinery. This enables spec authors to focus on what the conditions achieve instead of how those conditions are achieved.

Goal A: Move environment / bitcoin transaction actions and variables from *Contracts* to here

EXTENDS *Sequences*,
Integers,
TLC,
SequencesExt

Define constants so that we can define finite sets for inputs, outputs and txids etc.

CONSTANTS	<i>CSV</i> ,	Set of <i>CSV</i> values
	<i>VOUT</i> ,	Set of <i>vout</i> values
	<i>TXID</i> ,	Set of transaction ids
	<i>AMOUNT</i> ,	Set of amounts that can be used
	<i>PARTY</i> ,	Parties participating in the <i>L2</i> protocol
	<i>KEY</i> ,	Set of keys for each party used
		in the <i>L2</i> protocol
	<i>HASH</i>	Set of all hash preimages

SighashFlag \triangleq {"all", "none", "single", "anyonecanpay"}

Set of output types supported for building contracts.

Each output type will have to provide a means to verify an input trying to spend it.

OutputTypes \triangleq {"p2wkh", "multisig", "multisig-with-csv", "hash-lock"}
OutputTypes \triangleq {"p2wkh", "multisig", "multisig-with-csv"}

NoCSV \triangleq CHOOSE $c : c \notin CSV$
MaxCSV \triangleq CHOOSE $c \in CSV : \forall y \in CSV : c \geq y$
NoHash \triangleq CHOOSE $h : h \notin HASH$
NoSpendHeight \triangleq -1

All keys available for use by the parties
Keys $\triangleq PARTY \times KEY$

Input \triangleq [
txid : *TXID*,
index : *VOUT*,

$sighash_flag : SighashFlag,$ Parts of transactions covered by signature
 $signed_by : Seq(Keys),$ One or more keys that have signed this input
 $hash_preimage : HASH \cup \{NoHash\}$

$Output \triangleq [$
 $index : VOUT,$
 $type : OutputTypes,$
 $keys : Seq(Keys),$ Sig from these keys is required to spend
 $csv : CSV \cup \{NoCSV\},$ The *CSV* should have expired before spend
 $hash : HASH \cup \{NoHash\},$ Pre-image required to spend
 $amount : AMOUNT$
 $]$

VARIABLES
 $chain_height,$
 $transactions,$
 $mempool,$
 $published$

$CreateP2WKHOutput(keys, amount) \triangleq [$
 $index \mapsto 0,$
 $type \mapsto "p2wkh",$
 $keys \mapsto keys,$
 $csv \mapsto NoCSV,$
 $hash \mapsto NoHash,$
 $amount \mapsto amount$
 $]$

$CreateMultisigOutput(keys, amount) \triangleq [$
 $index \mapsto 0,$
 $type \mapsto "multisig",$
 $keys \mapsto keys,$
 $csv \mapsto NoCSV,$
 $hash \mapsto NoHash,$
 $amount \mapsto amount$
 $]$

$CreateMultisigWithCSVOutput(keys, amount) \triangleq [$
 $index \mapsto 0,$
 $type \mapsto "multisig_with_csv",$
 $keys \mapsto keys,$
 $csv \mapsto MaxCSV,$
 $hash \mapsto NoHash,$

$amount \mapsto amount$
 $]$

Add a coinbase tx spendable with a pk. No verification is required here as no prevout is being spent.

$AddP2WKHCoinbaseToMempool(id, keys, amount) \triangleq$
 $\wedge id \notin mempool$
 $\wedge published[id] = NoSpendHeight$
 $\wedge transactions' = [transactions \text{ EXCEPT } ![id] = [inputs \mapsto \langle \rangle,$
 $\quad \quad \quad outputs \mapsto \langle CreateP2WKHOutput(keys, amount) \rangle]]$
 $\wedge mempool' = mempool \cup \{id\}$
 $\wedge UNCHANGED \langle chain_height, published \rangle$

Add a coinbase tx with a *multisig* output spendable by signature from all keys.

We don't do threshold signatures for simplicity.

$AddMultisigCoinbaseToMempool(id, keys, amount) \triangleq$
 $\wedge id \notin mempool$
 $\wedge published[id] = NoSpendHeight$
 $\wedge transactions' = [transactions \text{ EXCEPT } ![id] = [inputs \mapsto \langle \rangle,$
 $\quad \quad \quad outputs \mapsto \langle CreateMultisigOutput(keys, amount) \rangle]]$
 $\wedge mempool' = mempool \cup \{id\}$
 $\wedge UNCHANGED \langle chain_height, published \rangle$

Confirm transaction from *mempool*.

$ConfirmMempoolTx(id) \triangleq$
 $\wedge id \in mempool$
 $\wedge published[id] = NoSpendHeight$
 $\wedge LET \ tx \triangleq transactions[id]$
 $\quad IN$
 $\quad \wedge chain_height' = chain_height + 1$ Each tx is in it's own block
 $\quad \wedge published' = [published \text{ EXCEPT } ![id] = chain_height']$
 $\quad \wedge mempool' = mempool \setminus \{id\}$
 $\wedge UNCHANGED \langle transactions \rangle$

Create a transaction spending the given output/ id , and spendable by the given key.

$CreateP2WKHTx(spending, output, id, output_key, amount) \triangleq [$
 $\quad inputs \mapsto \langle [txid \mapsto spending,$
 $\quad \quad \quad index \mapsto output.index,$
 $\quad \quad \quad sighash_flag \mapsto "all",$
 $\quad \quad \quad signed_by \mapsto output.keys,$
 $\quad \quad \quad hash_preimage \mapsto NoHash] \rangle,$
 $\quad outputs \mapsto \langle CreateP2WKHOutput(output_key, amount) \rangle$
 $]$

Create a transaction spending the given output/*id*, and spendable by as a *multisig* of the given keys.

$$\text{CreateMultisigTx}(\text{spending}, \text{output}, \text{id}, \text{output_keys}, \text{amount}) \triangleq [$$

$$\text{inputs} \mapsto \langle [\text{txid} \mapsto \text{spending},$$

$$\text{index} \mapsto \text{output.index},$$

$$\text{sighash_flag} \mapsto \text{"all"},$$

$$\text{signed_by} \mapsto \text{output.keys},$$

$$\text{hash_preimage} \mapsto \text{NoHash}] \rangle,$$

$$\text{outputs} \mapsto \langle \text{CreateMultisigOutput}(\text{output_keys}, \text{amount}) \rangle$$

$$]$$

$$\text{CreateMultisigWithCSVTx}(\text{spending}, \text{output}, \text{id}, \text{output_keys}, \text{amount}) \triangleq [$$

$$\text{inputs} \mapsto \langle [\text{txid} \mapsto \text{spending},$$

$$\text{index} \mapsto \text{output.index},$$

$$\text{sighash_flag} \mapsto \text{"all"},$$

$$\text{signed_by} \mapsto \text{output.keys},$$

$$\text{hash_preimage} \mapsto \text{NoHash}] \rangle,$$

$$\text{outputs} \mapsto \langle \text{CreateMultisigWithCSVOutput}(\text{output_keys}, \text{amount}) \rangle$$

$$]$$

Add a new transaction to *mempool*.

The transaction is created and added to *mempool*.

The transaction is constructed such that it is a valid transaction.

input_type specifies the type of published output to select to spend.

output_type specifies the type of new output to create.

$$\text{AddSpendTxToMempool}(\text{id}, \text{output_keys}, \text{amount}, \text{input_type}, \text{output_type}) \triangleq$$

$$\exists s \in \text{DOMAIN published} :$$

$$\wedge \text{published}[s] \neq \text{NoSpendHeight}$$

$$\wedge$$

$$\exists o \in \text{ToSet}(\text{transactions}[s].\text{outputs}) :$$

$$\wedge \text{id} \notin \text{mempool}$$

$$\wedge o.\text{type} = \text{input_type} \quad \text{Select published tx of input_type}$$

$$\wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![\text{id}] =$$

$$\text{CASE } (\text{output_type} = \text{"p2wkh"}) \rightarrow$$

$$\text{CreateP2WKHTx}(s, o, \text{id}, \text{output_keys}, \text{amount})$$

$$\square (\text{output_type} = \text{"multisig"}) \rightarrow$$

$$\text{CreateMultisigTx}(s, o, \text{id}, \text{output_keys}, \text{amount})$$

$$\square (\text{output_type} = \text{"multisig_with_csv"}) \rightarrow$$

$$\text{CreateMultisigWithCSVTx}(s, o, \text{id}, \text{output_keys}, \text{amount})$$

$$]$$

$$\wedge \text{mempool}' = \text{mempool} \cup \{\text{id}\}$$

$$\wedge \text{UNCHANGED } \langle \text{chain_height}, \text{published} \rangle$$