

This spec captures the actions and states of bitcoin transactions in the context of the bitcoin blockchain. These actions will be used by the *LN Contracts* spec and other layer two contract specifications.

The focus of this module is to provide:

1. Way to generate transactions that accept input and generate outputs
2. Confirm transactions so that outputs can be spent.
3. Most importantly - provide a way to verify spend conditions without building the entire cryptography machinery. This enables spec authors to focus on what the conditions achieve instead of how those conditions are achieved.

Goal A: Move environment / bitcoin transaction actions and variables from *Contracts* to here

EXTENDS *Sequences*,  
*Integers*,  
*TLC*,  
*SequencesExt*

Define constants so that we can define finite sets for inputs, outputs and txids etc.

CONSTANTS	<i>CSV</i> ,	Set of <i>CSV</i> values
	<i>VOUT</i> ,	Set of <i>vout</i> values
	<i>TXID</i> ,	Set of transaction ids
	<i>AMOUNT</i> ,	Set of amounts that can be used
	<i>KEY</i> ,	Set of all keys used for signatures
	<i>HASH</i>	Set of all hash preimages

*SighashFlag*  $\triangleq$  {"all", "none", "single", "anyonecanpay"}

Set of output types supported for building contracts.

Each output type will have to provide a means to verify an input trying to spend it.

*OutputTypes*  $\triangleq$  {"p2wkh", "multisig", "multisig\_with\_csv", "hash\_lock"}  
*OutputTypes*  $\triangleq$  {"p2wkh", "multisig"}

*NoCSV*  $\triangleq$  CHOOSE  $c : c \notin CSV$   
*NoHash*  $\triangleq$  CHOOSE  $h : h \notin HASH$

*ChooseKey(k)*  $\triangleq$  CHOOSE  $e \in KEY : e \neq k$

*Input*  $\triangleq$  [  
*txid* : *TXID*,  
*index* : *VOUT*,  
*sighash\_flag* : *SighashFlag*,      Parts of transactions covered by signature  
*signed\_by* : *Seq(KEY)*,      One or more keys that have signed this input  
*hash\_preimage* : *HASH*  $\cup$  {*NoHash*}  
 ]

$Output \triangleq [$   
 $\quad index : VOUT,$   
 $\quad type : OutputTypes,$   
 $\quad keys : Seq(KEY),$       Sig from these keys is required to spend  
 $\quad csv : CSV \cup \{NoCSV\},$       The *CSV* should have expired before spend  
 $\quad hash : HASH \cup \{NoHash\},$       Pre-image required to spend  
 $\quad amount : AMOUNT$   
 $\quad ]$

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VARIABLES

$chain\_height,$   
 $transactions,$   
 $mempool,$   
 $published$

$vars \triangleq \langle chain\_height, transactions, mempool, published \rangle$

$Init \triangleq$   
 $\quad \wedge transactions = [id \in TXID \mapsto [inputs \mapsto \langle \rangle, outputs \mapsto \langle \rangle]]$   
 $\quad \wedge chain\_height = 0$   
 $\quad \wedge mempool = \{\}$   
 $\quad \wedge published = \{\}$

$TypeOK \triangleq$   
 $\quad \wedge transactions \in [TXID \rightarrow [inputs : Seq(Input), outputs : Seq(Output)]]$   
 $\quad \wedge mempool \in SUBSET TXID$   
 $\quad \wedge published \in SUBSET TXID$

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$CreateP2WKHOutput(key, amount) \triangleq [$   
 $\quad index \mapsto 0,$   
 $\quad type \mapsto "p2wkh",$   
 $\quad keys \mapsto key,$   
 $\quad csv \mapsto NoCSV,$   
 $\quad hash \mapsto NoHash,$   
 $\quad amount \mapsto amount$   
 $\quad ]$

$CreateMultisigOutput(keys, amount) \triangleq [$   
 $\quad index \mapsto 0,$   
 $\quad type \mapsto "multisig",$   
 $\quad keys \mapsto keys,$   
 $\quad csv \mapsto NoCSV,$   
 $\quad hash \mapsto NoHash,$

$amount \mapsto amount$

]

Add a coinbase  $tx$  spendable with a pk. No verification is required here as no prevout is being spent.

$AddP2WKHCoinbaseToMempool(id, key, amount) \triangleq$

$\wedge id \notin mempool$

$\wedge id \notin published$

$\wedge transactions' = [transactions \text{ EXCEPT } ![id] = [inputs \mapsto \langle \rangle,$   
 $outputs \mapsto \langle CreateP2WKHOutput(\langle key \rangle, amount) \rangle]]]$

$\wedge mempool' = mempool \cup \{id\}$

$\wedge UNCHANGED \langle chain\_height, published \rangle$

Add a coinbase  $tx$  with a *multisig* output spendable by signature from all keys.

We don't do threshold signatures for simplicity.

$AddMultisigCoinbaseToMempool(id, keys, amount) \triangleq$

$\wedge id \notin mempool$

$\wedge id \notin published$

$\wedge transactions' = [transactions \text{ EXCEPT } ![id] = [inputs \mapsto \langle \rangle,$   
 $outputs \mapsto \langle CreateMultisigOutput(keys, amount) \rangle]]]$

$\wedge mempool' = mempool \cup \{id\}$

$\wedge UNCHANGED \langle chain\_height, published \rangle$

Confirm coinbase transaction from *mempool*.

$ConfirmCoinbaseMempoolTx \triangleq$

$\exists id \in \text{DOMAIN } transactions :$

$\wedge id \in mempool$

$\wedge id \notin published$

$\wedge \text{LET } tx \triangleq transactions[id]$

IN

$\wedge tx.inputs = \langle \rangle$  A coinbase  $tx$ , has no inputs.

We are not dealing with blocks, so we ignore the block index coinbase check

$\wedge published' = published \cup \{id\}$

$\wedge mempool' = mempool \setminus \{id\}$

$\wedge chain\_height' = chain\_height + 1$  Each  $tx$  is in it's own block

$\wedge UNCHANGED \langle transactions \rangle$

Create a transaction spending the given output/ $id$ , and spendable by the given key.

$CreateP2WKHTx(spending, output, id, key, amount) \triangleq [$

$inputs \mapsto \langle [txid \mapsto spending,$   
 $index \mapsto output.index,$   
 $sighash\_flag \mapsto "all",$

$$\begin{aligned}
& \text{signed\_by} \mapsto \text{output.keys}, \\
& \text{hash\_preimage} \mapsto \text{NoHash}], \\
& \text{outputs} \mapsto \langle \text{CreateP2WKHOutput}(\langle \text{key} \rangle, \text{amount}) \rangle
\end{aligned}$$

Create a transaction spending the given output/*id*, and spendable by as a *multisig* of the given keys.

$$\begin{aligned}
& \text{CreateMultisigTx}(\text{spending}, \text{output}, \text{id}, \text{keys}, \text{amount}) \triangleq [ \\
& \quad \text{inputs} \mapsto \langle [\text{txid} \mapsto \text{spending}, \\
& \quad \quad \text{index} \mapsto \text{output.index}, \\
& \quad \quad \text{sighash\_flag} \mapsto \text{"all"}, \\
& \quad \quad \text{signed\_by} \mapsto \text{output.keys}, \\
& \quad \quad \text{hash\_preimage} \mapsto \text{NoHash}] \rangle, \\
& \quad \text{outputs} \mapsto \langle \text{CreateMultisigOutput}(\text{keys}, \text{amount}) \rangle \\
& ]
\end{aligned}$$

Add a new transaction to *mempool*.

The transaction is created and added to *mempool*.

The transaction is constructed such that it is a valid transaction.

*input\_type* specifies the type of published output to select to spend.

*output\_type* specifies the type of new output to create.

$$\begin{aligned}
& \text{AddSpendTxToMempool}(\text{id}, \text{key}, \text{amount}, \text{input\_type}, \text{output\_type}) \triangleq \\
& \quad \exists s \in \text{published} : \\
& \quad \quad \exists o \in \text{ToSet}(\text{transactions}[s].\text{outputs}) : \\
& \quad \quad \quad \wedge \text{id} \notin \text{mempool} \\
& \quad \quad \quad \wedge \text{id} \notin \text{published} \\
& \quad \quad \quad \wedge o.\text{type} = \text{input\_type} \quad \text{Select published tx of input\_type} \\
& \quad \quad \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![\text{id}] = \\
& \quad \quad \quad \quad \text{CASE } (\text{output\_type} = \text{"p2wkh"}) \rightarrow \\
& \quad \quad \quad \quad \quad \text{CreateP2WKHTx}(s, o, \text{id}, \text{key}, \text{amount}) \\
& \quad \quad \quad \quad \square (\text{output\_type} = \text{"multisig"}) \rightarrow \\
& \quad \quad \quad \quad \quad \text{CreateMultisigTx}(s, o, \text{id}, \langle \text{key}, \text{ChooseKey}(\text{key}) \rangle, \text{amount}) \\
& \quad \quad ] \\
& \quad \wedge \text{mempool}' = \text{mempool} \cup \{\text{id}\} \\
& \quad \wedge \text{UNCHANGED } \langle \text{chain\_height}, \text{published} \rangle
\end{aligned}$$


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*Next*  $\triangleq$

$$\begin{aligned}
& \vee \exists k \in \text{KEY}, \text{id} \in \text{TXID}, a \in \text{AMOUNT} : \\
& \quad \vee \text{AddP2WKHCoinbaseToMempool}(\text{id}, k, a) \\
& \vee \exists \text{keys} \in \text{KEY} \times \text{KEY}, \text{id} \in \text{TXID}, \text{amount} \in \text{AMOUNT} : \\
& \quad \vee \text{AddMultisigCoinbaseToMempool}(\text{id}, \text{keys}, \text{amount}) \\
& \vee \exists \text{id} \in \text{TXID}, a \in \text{AMOUNT}, k \in \text{KEY}, \text{input\_type} \in \text{OutputTypes}, \text{output\_type} \in \text{OutputTypes} :
\end{aligned}$$

$AddSpendTxToMempool(id, k, a, input\_type, output\_type)$   
 $\vee ConfirmCoinbaseMempoolTx$

$Spec \triangleq$   
 $\wedge Init$   
 $\wedge \Box [Next]_{\langle vars \rangle}$