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Locality/proverywhere

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- Locality everywhere.
- Locality in Computing powcoder Locality in Computing
- Local Coloring
- Coloring Assignment Project Exam Help
- Lower Bounds https://powcoder.com

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Locality/proverywhere

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- Locality is everywhere:
 - Physics
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 - Biology
 - Social Sciences
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 - Mathematics
- They have differences and similarities.

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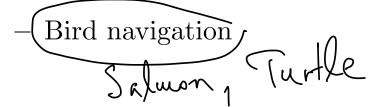
- An object is only directly influenced by its immediate surrounded WeChat powcoder
- A theory using the principle of locality is said to be a "local theory".

 **Signment Project Exam Help

 **Relativity is a local theory
- - It limits the https://powgoder.com/nces can travel to the speed of light c Add WeChat powcoder
- Quantum mechanics is not a local theory.
 - A measurement made on one of a pair of separated but entangled particles causes a simultaneous effect, the collapse of the wave function, in the remote particle (i.e. an effect exceeding the speed of light).

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- Phenotypes might be influenced by local variations and effects.
 - Shape Add WeChat powcoder
 - Size
 - Color Assignment Project Exam Help
 - Nature
 - Other environtal participation of the environtal participati
- In turn, this affected the emotion powcoder
- Quantum Biology is a newly developing field for the study of non-local biological phenomena.



Assignment Project Exam Help Social

- Local Characteristics
 - Language
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 - Behaviour
 - Culture Assignment Project Exam Help
 - Food
- Global Phenomena https://powcoder.com
 - Cascades Add WeChat powcoder
 - Rumors
- How do certain events cascade?

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- It has a proximity interpretation.
- Related somehow to distance. (Jeometric distance)
- Concerns phenomena that are geometrically close to each other.
- Locality is Assignment Project bexismo Helpsame thing as location!

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paths between nodes

paths of a certain length

u sends messages to all nodes three hops, away

Evangelos Kranakis, Carleton University, SCS (October 31, 2020)

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Localitys:/invocomputing

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- Usually it means:
 - the execution of a process depends on nearby processes.
 - there is no dependency between events that occur far away.
- It has a special role in corputing and communication.
 - What can be computed globally if there is a restriction on how far infohitest/payeqderteem
- Can you elect a Aedde We Chat powcoder



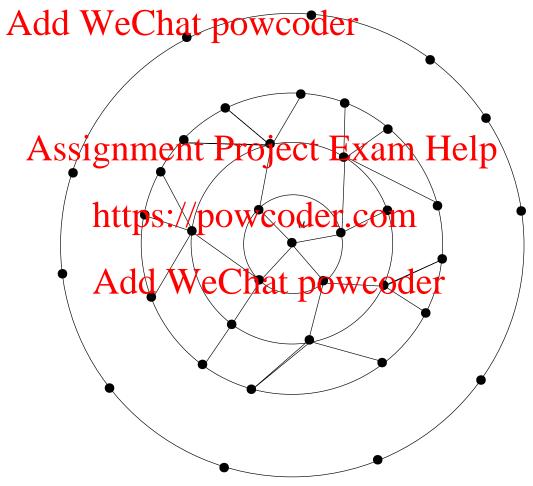
- making use only of local information?





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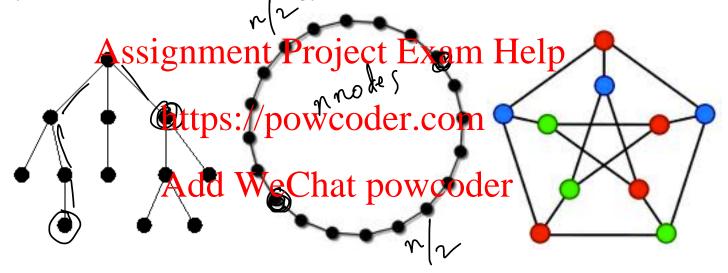
• Decision made at node u not affected by nodes far away from u.



• How do we quantify "far away" from u?

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- Given that locality is influenced by distance "how far is far away"? Add WeChat powcoder
- May depend on the topology



- How do you parametrize locality?
- Best to study specific problems!

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- Global vs Local Algorithms
- On a Line Add WeChat powcoder
- On a Tree

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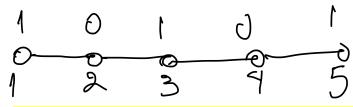
Local Algorithms in DC Assignment Project Exam Help

- An algorithm is local if messages initiated by the nodes do not propagate to Wichatherwegieter.
 - How can you ensure correctness of the algorithm?
 - Which problems can you solve this way?
 - How far is too far? Project Exam Help
- Local approach https://pawcoderecomommunication!

• Lets go back to Apporting e Chat powcoder

Assignment Project Exam Help

- A vertex coloring is an assignment of colors to vertices of a graph so And My Chatdpow Code are assigned different colors.
- How do you color a set of points on a line? Assignment Project Exam Help
- If nodes have identifies powcoder comor nodes with even identities blue, and with odd identities red. Add WeChat powcoden
 - Is the algorithm correct?
 - Is this a local algorithm?
- - Is there a local colouring algorithm?



Global vs Local Coloring Assignment Project Exam Help

- Before a node decides on its colour it must collect information about it Add how Chat powcoder
- There are two ways to do this depending on how far this information collection can spread 1. Globally Assignment Project Exam Help

 - https://powcoder.com 2. Locally

Assignment Project Exam Help

• Globally?



- You are not constrained by # of hops.

• Locally? Assignment Project Exam Help



- Constrained by # of hops.
- In a distributed setting, the difficulty des in keeping the assignment of colors consistent throughout the graph despite the fact that propagation is limited!

Why do you want a local coloring algorithm Assignment Project Exam Help https://powcoder.com If algorithadd Weglantpowedden it is not fault tolerant Local algorithms are more robust to failures (node or link)

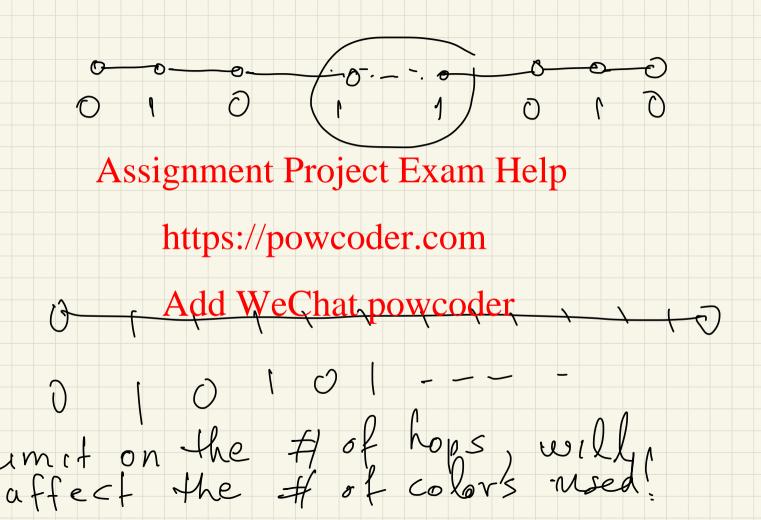
Coloring with Restricted Number of Hops Assignment Project Exam Help

• Consider nodes "independently" initiating coloring.



- If the number of hops a message can propagate is restricted you may not be able to complete the coloring!

 Assignment Project Exam Help
- If a given set of nodes start coloring at the same time how do you ensure consistent: copy goder.com
 - Nodes will start with their own identifiers.
- More than that, you may have to use more than the minimum required number of colors so as to achieve a correct coloring!
- Regardless of the number of colors you use
 - can you achieve a proper coloring, and
 - at the same time restrict the number of hops?



Quantifying Locality: Network Assignment Project Exam Help

- Consider a class \mathcal{N} of networks.
- A typical network G = (V, E) in \mathcal{N} is a graph with n vertices.
 - Line,
 - Ring, Assignment Project Exam Help
 - Tree,
 - https://powcoder.com - etc.
- The concept should be applicated that the concept should be applicated to the concept should be appl (networks).

Quantifying Locality: Distance Assignment Project Exam Help

- Locality should depend on distance.
- Let $n \to h(n)$ be an integer valued function:
 - -h(n) is the number of hops allowed in a network of size n.
- Examples: Assignment Project Example 15

-n o h(n) = 1, https://powcoder.com -n o h(n) = c, c is some constant, -n o h(n) = k del, WeChat powcoder -n o h(n) = k del, we constant, $-n o h(n) = \sqrt{n}$, $-n o h(n) = \sqrt{n}$, -n o h(n) = n, -n o h(n) = n, -n o h(n) = n,

$$-n \to h(n) = \sqrt{n}$$

$$(n \to h(n) = n,)$$

$$-n \to h(n) = \log^* n$$
, etc

Quantifying Locality: Problems Assignment Project Exam Help

- Consider a problem \mathcal{P} (e.g., colouring), and a class \mathcal{A} of synchronaud distribution powered solving \mathcal{P} for \mathcal{N} .
 - The class \mathcal{A} of distributed algorithms is h-local if during the execution of an algorithm $A \in \mathcal{A}$ on a network $G \in \mathcal{N}$ (on n vertices) ssignate that h(n) hops from its originator. https://powcoder.com

Prophet We Chat povycodence

distance (hope by

is determined by

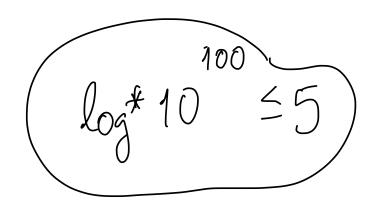
the function h.

Which Problems in DC are Local? Assignment Project Exam Help

- Not all problems are going to be h-local, for a given function h.
- Which ones are h-local, for a function $n \to h(n) = c$, where c a constant?
 - Leader Election
 Assignment Project Exam Help
 Spanning Tree

 - Maximum Interpritation of the Coloring Coloring Analysman Analysman

 - Minimum Dominating
- For which topologies?



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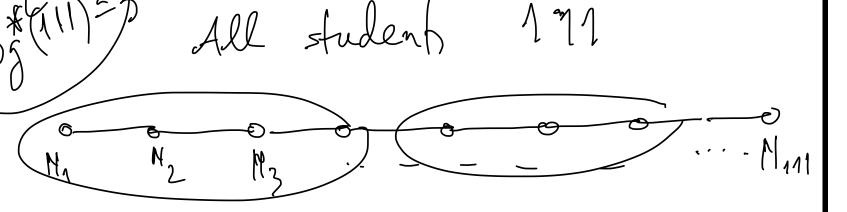
Assignment Project Exam Help

Lowering

Coloring a Line Graph: Assumptions Assignment Project Exam Help

- Assume you are on a line of n nodes.

 Add We Chat powcoder 23 21 5 6 4
- To start, assume that each node v has a distinct identity id_v (for example, either their location or the network interface card would do).
 - Identity selections: /poweodertoomhe coloring problem...besides we also know several ways to solve this problem! Add WeChat powcoder



Assignment Project Exam Help

• Our main goal is to show

• Theorem 1 WeChat powcoder
There is a coloring algorithm which can 3-color any line in $O(\log^* n)$ time, where

- log* n is the iterated lograithm of n log(log(... (log n)))
- in the algorithm all red in the algorithm all red in the algorithm all red in the algorithm.

- in the algorithm all nodes start with their identifiers.

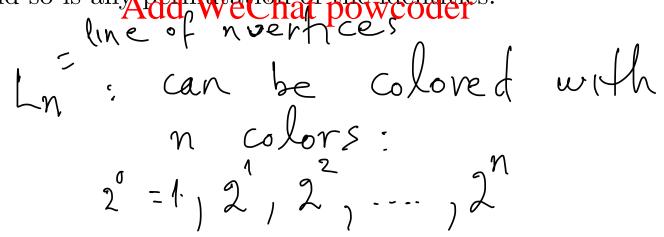
- This result is important in certain types of networks (like wireless) where messages should not propagate too far!
- **NB:** Note the important parameters taken into account:
 - Final number of colors in the graph.
 - Termination time of the coloring algorithm.

Assumptions for Coloring Assignment Project Exam Help

- Let $v \to c_v$ be an arbitrary coloring of the vertices.
 - Observe that echat powcoder coloring!
- For example,
 - the identity assignment below is a colouring using n colors,



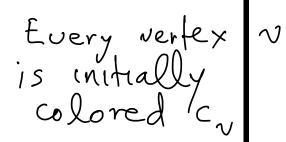
- and so is any permutation of the identities.



1,2,3,---, Assignment Project Exam Help
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Assumptions for Coloring Assignment Project Exam Help

- Represent each c_v as a sequence of bits.
 - Let c_v be the number of bits in c_v , and
 - $-c_v(i)$ the *i*-th bit of c_v .



• Example Assignment Project Exam Help

$$-c_u = 594 = 512 + 64 + 16 + 2 = 2^9 + 2^6 + 2^4 + 2^1.$$

- In binary c_u https://powcoder.com
- $-c_u(i)$ is the inhold twhere coupting starts from i=0 from left to right: $c_u(0)=1, c_u(2)=0.$

• The concatenation

- of two sequences s, s' of bits is the sequence ss'.
- **Example:** if s = 1010 and s' = 110 then ss' = 1010110

Idea for an Algorithm on a Line Assignment Project Exam Help

Assume an ordering of the vertices (left to right would do).

- Starting Rule:
 - Start watsignment Project Exam Help
 - * for example con for all v for all
 - Color "leftmost vertex" with the bit 0.^a
- Any other starting coloring would do.

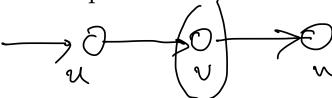
^aThis is a starting condition and we will need to justify it: will do this later!

Assignment Project Exam Help

- Since nodes $u \to v$ are neighbors (with \bar{u} preceding v), their current Add McChadipowcode c_v .
- Produce a new "legal" coloring for a vertex v from the current one, say c_v , as follows:
 - Assignment Project Exam Help

 Find the first index $1 \le i \le |c_v|$ such that v's color differs from the colour of its percentage.
- Set new color to "i concatenated with $c_v(i)$ ": $c_v \to ic_v(i)$;

 Recoloring rule guarantees that neighbors will get new
- Recoloring rule guarantees that neighbors will get new different colors.
- **NB:** Bit representation of each new color is of length logarithmic of the length of the previous color!



lor: C_{ij} $A \leq i \leq |C_{ij}|$ i C_{ij} (log C_{ij})
Assignment Project Exam Help https://powcoder.com Add WeChat powcoder

Coloring Algorithm for Vertex v Assignment Project Exam Help

• Assume an ordering of the vertices (left to right would do).

Add WeChat poweoder $\mathcal{I}_{c_{\mathcal{N}}}(\uparrow) \longrightarrow$ suc(v)prev(v)

- Coloring Algorithm: Assignment Project Exam Help
 - 1. $c_v \leftarrow id_v$;
 - 2. Repeat: https://powcoder.com
 - (a) $\ell \leftarrow |c_v|$; Add WeChat powcoder (b) if v is "leftmost vertex" then set $I \leftarrow 0$
 - else set $I \leftarrow \min\{i : c_v(i) \neq c_{pre(v)}(i)\};$
 - (c) Set $c_v \leftarrow Ic_v(I)$; /* concatenation */
 - (d) Inform the successor suc(v) of v of this choice;
 - 3. Until $|c_v| = \ell$; /*Until length does not change */

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• Given two nodes $u \to v$.

- Lets show how the color of node v changes from the old color c_v to a new color c_v .
 - A similar change occurs to the color of u but this is Assignment Project Exam Help influenced from the predecessor of u.
- Convert to binaydd WeChat powcoder $c_u = 512 + 64 + 16 + 2 = 2^9 + 2^6 + 2^4 + 2^1$

$$c_v = 512 + 64 + 32 + 16 + 4 + 2 + 1 = 2^9 + 2^6 + 2^5 + 2^4 + 2^2 + 2^1 + 2^0$$

• $c_u = 1001010010$ and $c_v = 1001110111$

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• Consider the two nodes with colors

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 $c_u = 1001010010$ and $c_v = 1001110111$

• What is the smallest i such that $c_u(i) \neq c_v(i)$?

• Line up the bits

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1001110111

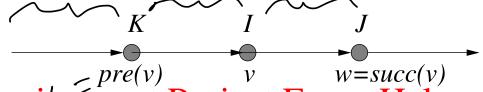
• So i = 4 (counting starts from 0); in binary 4 is 100 and the new colour of v in binary representation is

$$ic_v(i) = 1001 = 9$$

Execution of Coloring Algorithm Assignment Project Exam Help • A node receives input from its predecessor... Add WeChat powcoder Assignment Project Exam Help https://powcoder.com ...and provides input to its successor. Add WeChat powcoder

Assignment Project Exam Help (1/2)

• Consider three consecutive neighboring nodes u, v, w at some iteration Addhe WigGrham Poi Wicode prev(v), v = pre(w).



Assignment Project Exam Help

- Let I, J be the indices picked by v, w in Step 2(b), respectively.
 - $-I := \min\{i : \frac{\text{https://powcoder.com}}{c_u(i)} \text{ and } j : c_v(j) \neq c_w(j)\}$
 - v, w receive the week powcoder

$$c_v \leftarrow Ic_v(I)$$

and

$$c_w \leftarrow Jc_w(J)$$

Assignment Project Exam Help (2/2)

- We need to show that $Ic_v(I) \neq Jc_w(J)$.
- There are two cases to consider:
- - 1. If $I \neq J$ then rule 2(b) ensures that the new labels $Ac_v(I)$, $Ac_w(J)$ as defined in 2(c) differ in a bit $Ac_v(I)$, $Ac_w(J)$ as defined in 2(c) differ in a bit $Ac_v(I)$, $Ac_w(J)$ as defined in 2(c) differ in a bit $Ac_v(I)$, $Ac_w(J)$ as defined in 2(c) differ in a bit $Ac_v(I)$.
 - because I, J do
 - 2. If I = J the https://powsoeletheome new labels as defined in 2(c) differ in the last bit

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 - Recall that $c_u(I) \neq c_v(I)$ and $c_v(J) \neq c_w(J)$

 - Since I = J we have that $c_u(I) \neq c_v(I)$ and $c_v(I) \neq c_w(I)$
 - The new labels for v, w will be $Ic_v(I)$ and $Ic_w(I)$ and by choice of I we have that $c_v(I) \neq c_w(I)$.

Assignment Project Exam Help

- At the start, $K_0 = K = O(\log n)$ is the max number of bits of a node in Addrigner flow oder $5 \log n$.
- Let K_r denote the number of bits in the color representation after the rth iteration.

• Observe that $K_{r+1} = \lceil \log K_r \rceil + 1$.

- Therefore the the three independent of roughly $\log \log n$ bits, the third of roughly $\log \log \log n$ bits, etc. Add We Chat powcoder
- As a matter of fact the "sizes of the colours" shrink very rapidly!
 - The size of the colour (measured in bits) in the new step is the logarithm of the size of the colour in the previous step!

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- $\log^* n$ is not really a logarithm:
 - it is rather the number of iterations of the log function on a number n until it stops having an effect!
- Log-Star (in base 2) of nicoject Exam Help
 - Is the number of logarithms in base 2 needed so that starting from type //gov/coder ≤ 2 m
- Can be defined in anywase! Here we look only on base 2.

$$\log 4 = 2 \qquad \log 3 + 1$$

$$\log 4 = 2 \qquad \log 5 + 1 = 4$$

$$\log 5 + 1 = 5 \qquad \log 5 + 1 = 4$$

Assignment Project Exam Help

- Iterated Definition of $\log^* n$: Let
 - $-\log^{(1)} A \stackrel{dd}{=} \log^{(1)} N$, and powcoder
 - $-\log^{(x+1)} n = \log(\log^{(x)} n), \text{ for } x \ge 1.$

Then $\log^* n = \text{first integer} x \text{ such that } \log^{(x)} n \le 2$. a

• Recursive definition of $\log^* n$:

 $a \log^{(x)} n$ should not be confused with $\log^x n$: the logarithm to the power x.

Assignment Project Exam Help

• Log-star is a very slowly growing function.

Add WeChat powcoder Consider the number $n = 2^{2}$.

$$\log(2^{2^5}) = 2^5$$

Assignment 2 Project Exam Help

https://powcoder.201489 $\log(2.32) < 2.$ Add WeChat powcoder

Hence, $\log^*(2^{2^5}) = 4$.

• Log-star of all the atoms in the observable universe (estimated to be 10^{80}) is 5.

The Starting Nodes: Something Wrong? Assignment Project Exam Help

• Recall the leftmost node was given the color 0.

- It is not clear from the description of the algorithm why the identities of the nodes "located" at the beginning of the line are reduced to constant size.
 - By beginning we mean the first $O(\log^* n)$ nodes.
- Observe that the tipe with the continuous of are indeed reduced to constant size.

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- Can remedy this by adding an additional step at the end of the algorithm:
 - The first $O(\log^* n)$ nodes run a recoloring algorithm to reduce their colors to constant size.
- Note that this step takes additional time $O(\log^* n)$.

Assignment Project Exam Help

- If K_i = number of bits in the coloring after *i* iterations then
 - $-K_{r+1}$ Add We Chat powcoder
 - $-K_{r+1} < K_r$ as long as $K_r \ge 4$.
- In the final iteration r we have that Kam Help
- Therefore in the final coloring you have
 - at most three choices for an index to a bit in the (r-1) at most timee choice coloring, and add WeChat powcoder color of the bit.
 - two choices for the value of the bit, which gives a total of six colors.
- It turns out,
 - we can improve on # of colors from six to three, but $\ensuremath{\mathcal{W}}^{\ensuremath{\boldsymbol{\mathcal{C}}}}$
 - cannot improve on the $\log^* n$.

Three Colors Suffice Assignment Project Exam Help

• How do we reduce the number of colors from six to three?

• Suppose that the algorithm we discussed before has colored a line with the six colors 0, 1, 2, 3, 4, 5 as follows

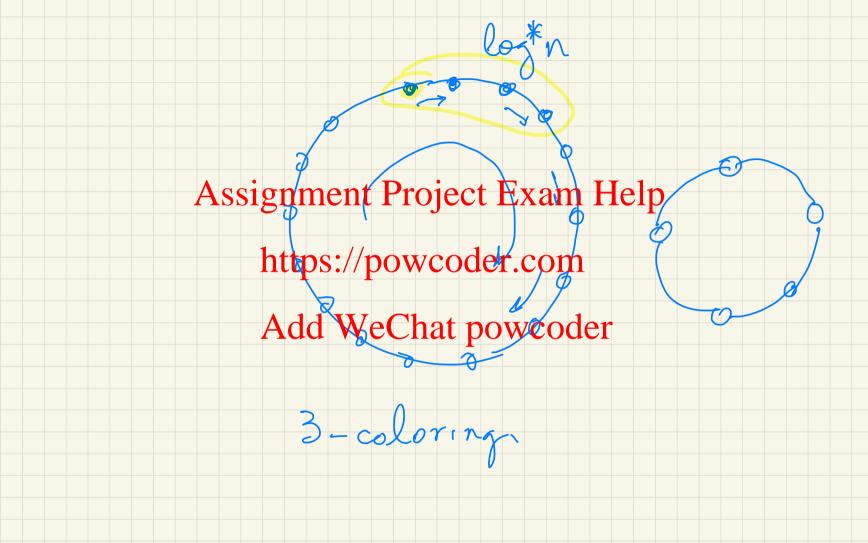
OAsigninent Project Exam Help 2 4 5

• How do you colartibusing only the relevant 0, 1, 2?

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Three Colors Suffice Assignment Project Exam Help Start with the sequence Add WeChat powcoder 0 5 4 2 5 3 0 3 1 5 4 2 3 0 1 4 3 2 4 0 1 0 2 4 5 Eliminate 5: by choosing a color from 0, 1, 2Assignment Project Exam Help 0 1 4 2 0 3 0 3 1 0 4 2 3 0 1 4 3 2 4 0 1 0 2 4 0 Eliminate 4: https://powcoder.com by choosing a color from 0, 1, 2 Eliminate 3: by choosing a color from 0, 1, 2 $0\ 1\ 0\ 2\ 0\ 1\ 0\ \emptyset\ 1\ 0\ 1\ 2\ 1\ 0\ 1\ 0\ 1\ 2\ 1\ 0$

Assignment Project Exam Help • Theorem 2 There is an algorithm which can 3-color any ring of size nAndowe Einat powcoder Same algorithm. Assignment Project Exam Help https://powcoder.com/ Add WeChat powcoder



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Cotto regger Trees

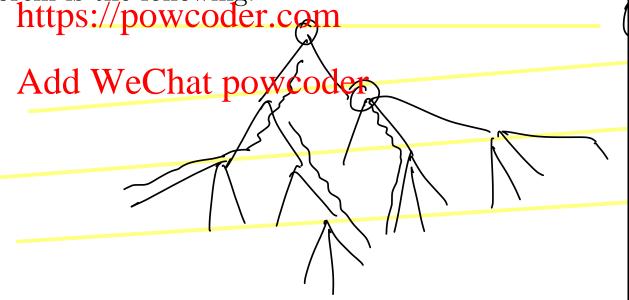
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Assignment Project Exam Help

• The line colouring algorithm also works on trees!

- Add WeChat powcoder
 The basic assumption is that you must have a node of the tree designated as the root!
- Further, other nodes must playe at perent (in predecessor)!

• The main theorem is the following.



Assignment Project Exam Help

• Theorem 3 There is an algorithm which can 6-color any tree in log* nAdde.WeChat powcoder

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6-Coloring Algorithm for Trees: Vertex v ssignment Project Exam Help

Algorithm: 6-Color





- (a) $\ell \leftarrow |c_v|$; (b) if v is the root then set f Exam Help

else set $I_{\text{https://powcoder.com}}(i)$; (c) Set $c_v \leftarrow Ic_v(I)$; /* concatenation */

- (d) Inform all Alddrive that this who cler
- 3. Until $|c_v| = \ell$;
- Why is the algorithm correct?

3-Coloring Theorem for Trees Assignment Project Exam Help

- Theorem 4 There is an algorithm which can 3-color any tree in $O(\log Addti We$ Chat powcoder
- The reason is that the coloring on the descendants of a given node is independent when done on disjoint paths.

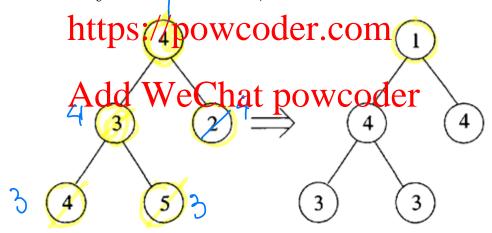
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- The color reduction method is called "shift-down".
- Algorithm Shift-Down Powcoder
 - 1. Concurrently at all vertices:
 - Recolor each non-root vertex by the color of its parent.
 Assignment Project Exam Help
 Recolor root by a new color, different from its current one.



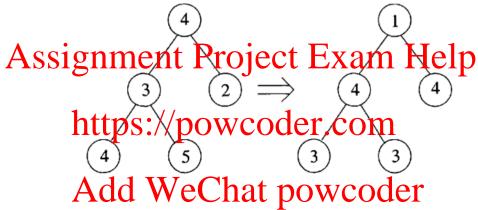
- Why is "shift-down" correct?
- Colors (of the original coloring) are shifted down.

Analysis of Shift-Down Algorithm Assignment Project Exam Help

• Lemma 1 (Analysis of Algorithm Shift Down)

Algorithm Colif Wir Chatronwe Odering legality; also siblings

are monochromatic.



- Two vertices v = parent(w), w are recolored by $c_{parent(v)}$ and c_v , which are different since c was a legal colouring.
- If v = root, then the new colors are x and c_v , where x is some color different from c_v .
- Also, all children of some vertex v get the same new color c_v .

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• Now assume the six colors employed in the tree are

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0,1,2,3,4,5

Cancellation procedure:

• The final three reduction steps involve cancelling colors

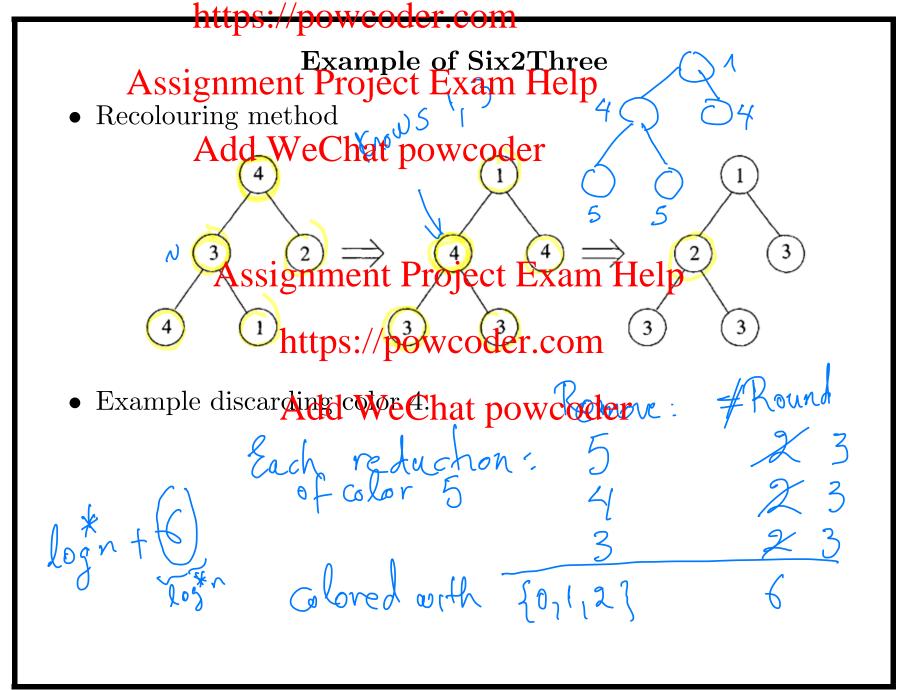
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one at a time. https://powcoder.com

- In the end, there will We that power eff. 2.
 - This is done by Algorithm Six2Three

Six2Three Algorithm Assignment Project Exam Help

- Algorithm Six2Three
 - 1. for x add WeChat powcoder x */
 - 2. Perform subroutine **Shift-Down** on the current colouring;
 - 3. if $c_v = x$ then
 - 4. v-chooses signment Project2 Exams Help any of the neighbors.
 - 5. endif https://powcoder.com
 - 6. endfor Add WeChat powcoder



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Analysis of Six2Three Assignment Project Exam Help

- Theorem 5 (Analysis of Algorithm Six to Three)

 Algorithm Color = Color =
- Each vertex colored x will find an available color from the set $\{1,2,3\}$, Assignment Project Exam Help
 - since by the Shift Down Lemma at most two of these colors are occupied, one by its parent and one by its children.
- Now note that recoloring the *x* colored vertices simultaneously creates no problem since they are all mutually nonadjacent.

It is important we have a free.

parent of v

Assignment Project Exam Help

- Fast tree-coloring with only 2 colors is more than exponentially more expended with a large weight ercolors.
 - In a tree degenerated to a line, nodes far away need to figure out whether they are an even or odd number of hops away frassignment Projectt Exam Holpring.

- To do that one has to send a message to these nodes. This nttps://powcoder.com
costs time linear in the number of nodes.

Add WeChat powcoder (
We use the

Hof rounds to

signify I sneed.

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Lower Bounds

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Assignment Project Exam Help n?

- The only thing better than $O(\log^* n)$ running time is O(1) running Med WeChat powcoder
- A 2-coloring is possible with O(1) running time in a distributed system with GPS!

 Assignment Project Exam Help

 It turns out that we can prove a lower bound of $\Omega(\log^* n)$ on
- It turns out that we can prove a lower bound of $\Omega(\log^* n)$ or the time required to $\Omega(\log^* n)$ or colors.
 - This implies a tight bound of the control of the time required for 3-coloring the line (ring).

O(logt n) (\(\int(\logt)\) logt n is not a constant

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• Theorem 6 Every deterministic, distributed algorithm to color a directed didg Well-Chat power effects at least $(\log^* n)/2 - 1$ rounds.

• The proof uses a theorem of Frank P. Ramsey.

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(22 February 1903 19 January 1930).

• We will not prove Theorem 6 here.

Generalizations and Additional Results Assignment Project Exam Help

- Linial (1992) proves that
 - in rooted d-regular tree $T_{d,r}$ of radius r, any synchronous distributed algorithm running in time $\leq \frac{2}{3}r$ cannot color $T_{d,r}$ by fewer than $\frac{1}{2}\sqrt{d}$ colors.
 - an arbitrary graph C of order n and max degree Δ , can be colored with $5\Delta^2 \log n$ colors in one time unit distributively.
 - for G labeled, in time $O(\log \mathcal{M})$ it is possible to color G with $O(\Delta^2)$ Adds We Chatipawe ode from algorithm.
- There exists a deterministic distributed algorithm for coloring arbitrary graphs with max degree Δ ;
 - can be colored with $\Delta + 1$ colors in $O(\Delta \log^* n)$ time.

d-regular tree ssignment Project Exam Help, https://powcoder.com Add WeChat powcoder

When you have a distributed Assignment Project Exam Help https://powcoder.com Add WeChat powcoder receive, process, send

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1. For any graph G = (V, E) define the chromatic numbers

 $\begin{tabular}{ll} Add We Chat powcoder \\ \chi_{centralized}(G), \chi_{distributed}(G), \chi_{local}(G) \end{tabular}$

for centralized, distributed, and local computation.

- (a) How do Athey differ? Project Exam Help
- (b) Is there a natural order of these three quantities?
- 2. Define the concepts of centralized, distributed and local for any algorithmic computation and make a comparison.
- 3. Let $n \to h(n)$ be an integer valued function, where h(n) is the number of hops allowed in a network of size n to complete the computation. Formulate the various types of computation discussed above in terms of the function h(n).
- 4. $(\star\star)$ Consider Exercise 3. If h(n) = n then the number of ^aDo not submit!

colors is 2. If h(n) = 1, then the number of colors is 3. For Assignment Project Exam Help which threshold value of h(n) does the number of colors jumps from 2 ta3d WeChat powcoder

- 5. Compute $\log^*(10^{1000})$.
- 6. Compute $\log^*(2^{2^{2^{16}}})$. Assignment Project Exam Help
- 7. Explain in more detail (than the slide presented in class) that the local coloring theoretical coloring than the local coloring.

 reduces to a six coloring.

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- 8. Show in detail that on the line graph three colors suffice.
- 9. Prove that a log* coloring algorithm is possible on a ring. How many colors does it require?
- 10. Prove in detail the correctness of the log* tree coloring algorithm.

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