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Commencetions

## Assignment Project Exam Help

- Trees
  - Add WeChat powcoder
    Canonical Form
- Distributed Views
- BroadcastAssignment Project Exam Help
- BFS/DFS https://powcoder.com
- Flooding Add WeChat powcoder
- Convergecast
- Applications

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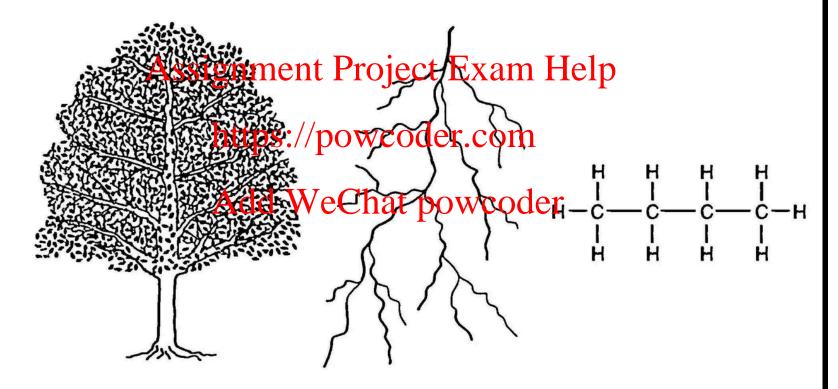
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# Trees and Communication Assignment Project Exam Help • Trees are everywhere: saplings, rivers, chemical compounds.

- - Thereistone Cine at bow and economy.

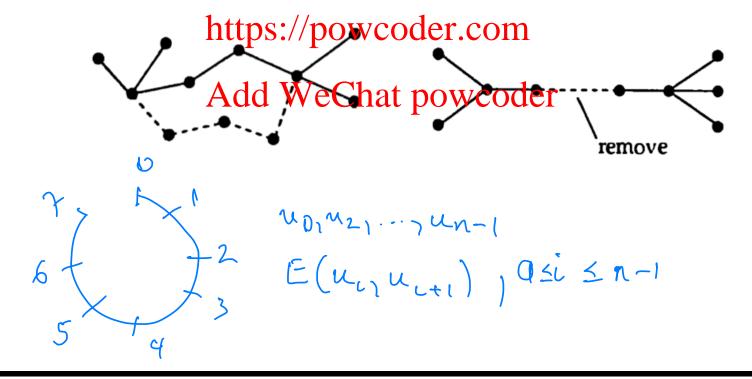


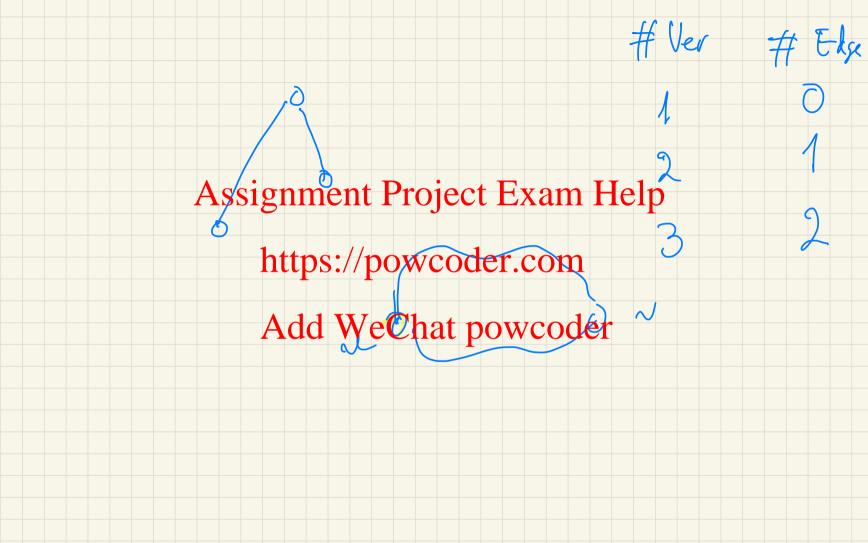
Trees form a natural communication structure in distributed computing.

## Main Concepts on Trees Assignment Project Exam Help

• A tree is a connected graph that has no cycles.

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  Start with the tree of one vertex: we can build up any tree we wish by successively adding a new edge and a new vertex.
  - At each stage, the # of vertices exceeds the number of edges Assignment Project Exam Help by 1, so every tree with n vertices has exactly n-1 edges





#### Characterization of Trees Assignment Project Exam Help

- Let T be a graph with n vertices. Then the following statements delever what powcoder
  - 1. T is connected and has no cydes.
  - 2. T has n-1 edges and has no cycles.
  - 3. T is coarseignmenta Project desam Help
  - 4. T is connected and the removal of any edge disconnects T.
  - 5. Any two vertices of P are connected by exactly one path.
  - 6. T contains no gycles but the addition of any new edge creates a cycle.

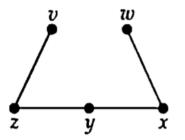
    Are equivalent

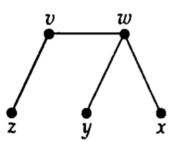
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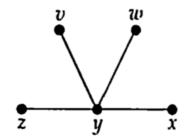
- Let G be a connected graph. Then a spanning tree in G is a subgraplAdd Whe Chattopo weoder tex and is also a tree.
- A graph ...

Count the number of spanning trees ssignment Project/Exam

Add WeChat powcoder ... and possible spanning trees







• Spanning trees emerge naturally in communication.

## Assignment Project Exam Help

• A Forest is a collection of vertex disjoint trees.

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- Forests arise naturally in clustering.
- A Spanning Forest is a collection of vertex disjoint spanning trees.

Ecsjornt. 11, 12, 11, 12 Assignment Project Exam Help https://powcoder.com/ How madd We Chatspowcoderes the forest have?

n = # of ventes in The forest = t1+t2+--+tk t1-1+t2-1+--+tp-1=n-k

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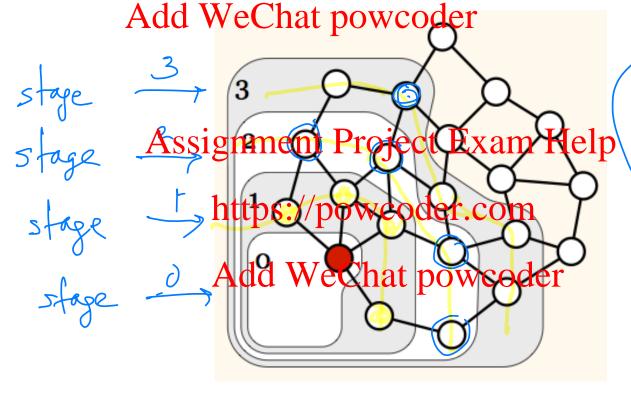
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## How Do Nodes Build their Knowledge? Assignment Project Exam Help

• They learn by exchanging messages in rounds.



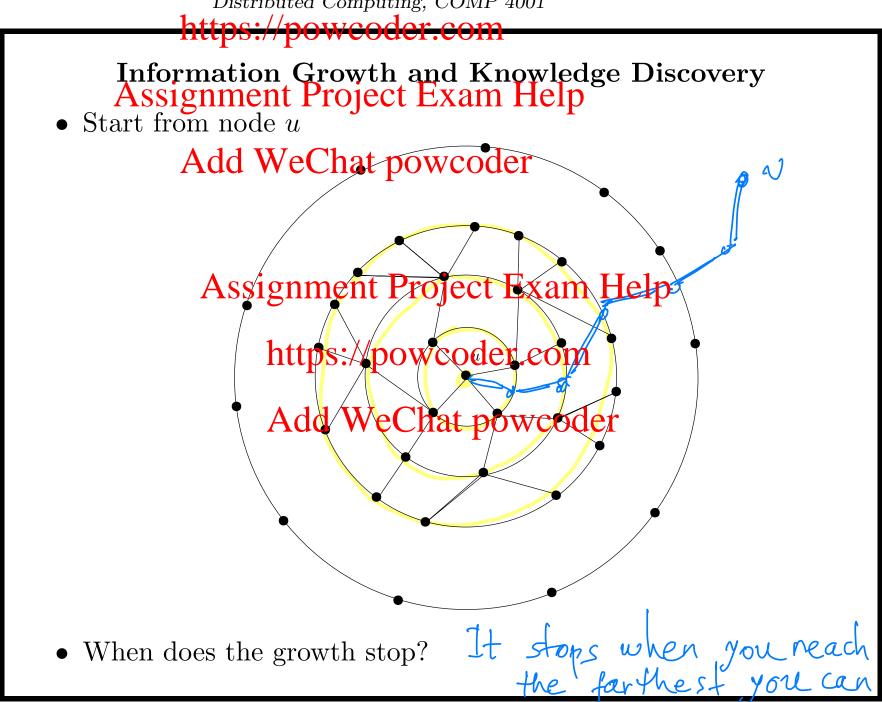
Stages =layers

the red vertex colle

• At the same time, different nodes learn different things!

nodes 3

hops and



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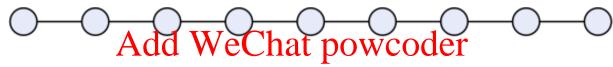
• In a typical synchronous distributed algorithm each node

• In a typical synchronous distributed algorithm each node executes Ablorows in attorium of the executes Ablorows in attorium of the executes at the executes

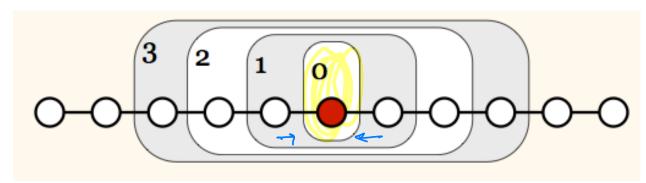
send  $\rightarrow$  receive  $\rightarrow$  process

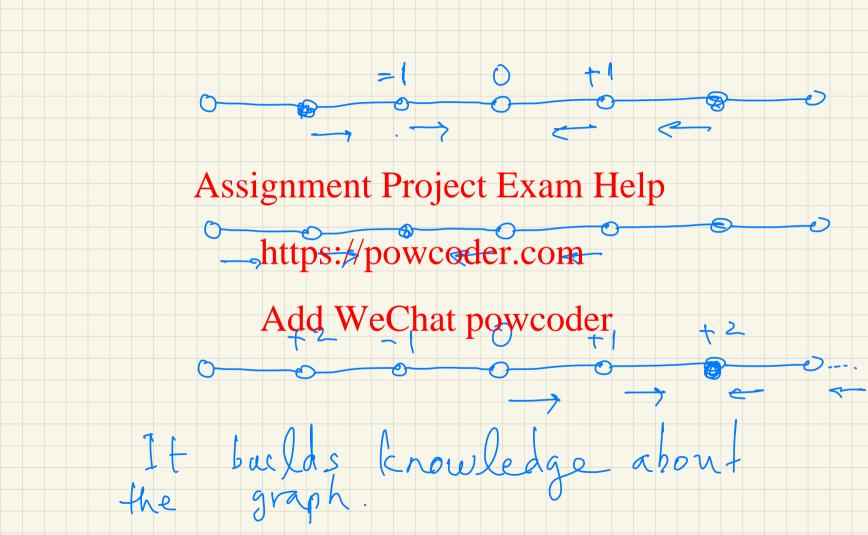
in synchronous grindent Project Exam Help

• Node v, by exchanging messages in rounds... https://powcoder.com



• ...receives information about distance  $1, 2, 3, \ldots$  nodes.



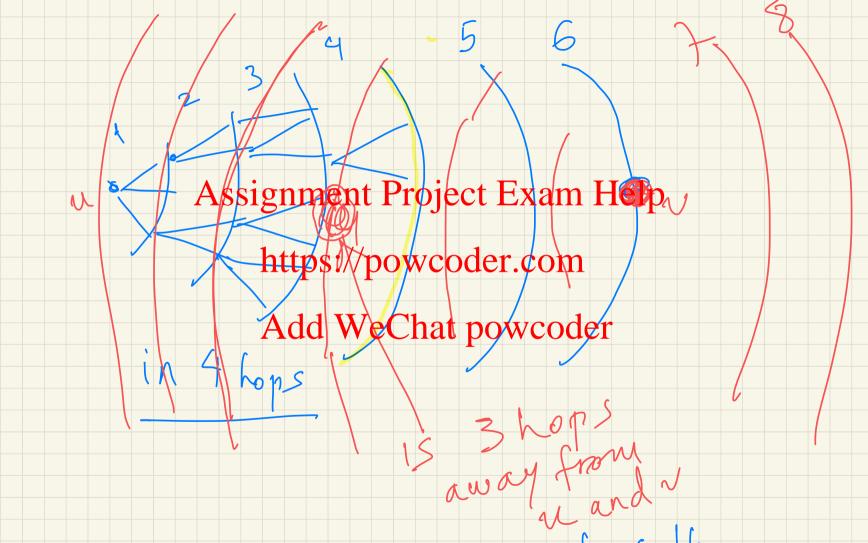


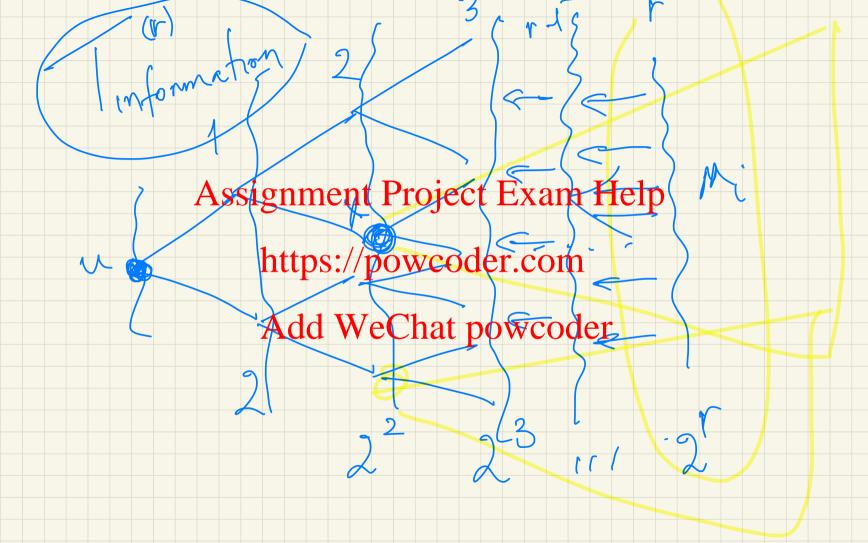
The method is not limited Assignment Project Exam Help

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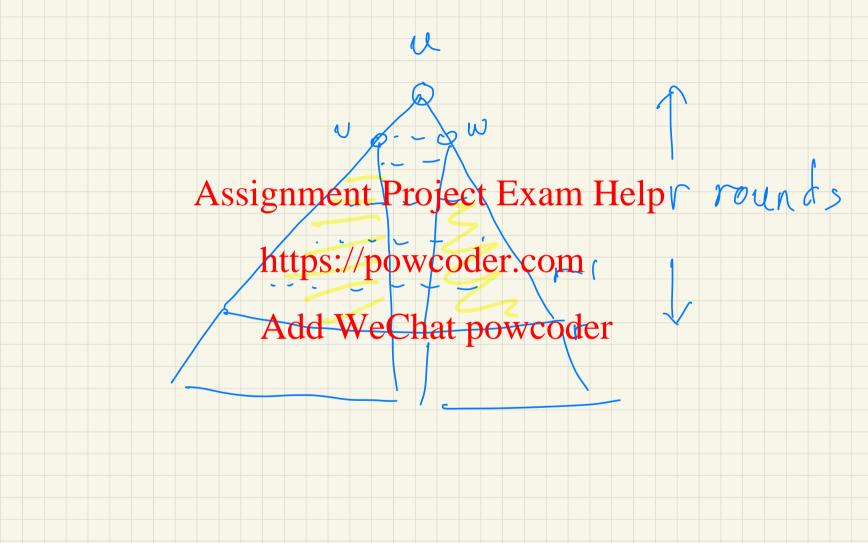
- Assume that initially, all nodes only know their own identifier and potentially and potentia
- Information needs at least r rounds to travel r hops.
- After r rounds; a node r project Example pther nodes at distance at most r.
- If message size and local computations are not restricted, it is in fact not hard to sew that powcoder
  - in r rounds, a node v can learn exactly all the node labels and inputs up to distance r from v.
- This allows us to transform every deterministic r-round synchronous algorithm into a simple canonical form.





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Hoffmessages An exponental number



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- The idea is to "simplify communication" with cumulative messages Add WeChat powcoder
- A typical synchronous distributed algorithm at each node consists of a sequence of executions\_

### Assignment Project Exam Help

send  $\rightarrow$  receive  $\rightarrow$  process

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in synchronous rounds.

- Often what matters is the source and the destination.
- Can we first do a sequence of r executions "send  $\rightarrow$  receive" followed by a single "process" at the end?
- In other words, can we send "cumulative" messages for r rounds and finally do the processing?

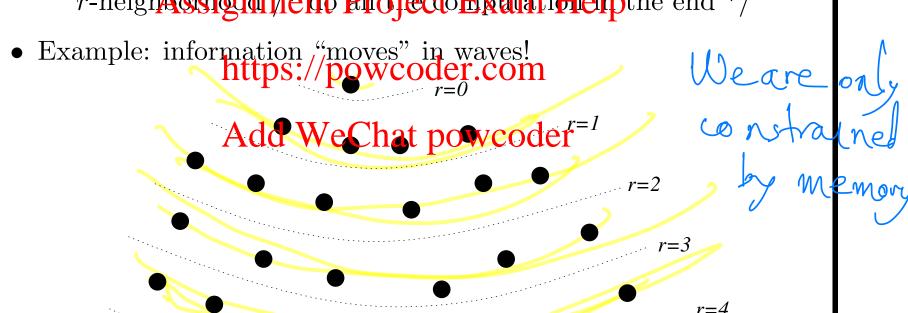
### Example: Computing the Sum in a Ring Assignment Project Exam Help

- Consider a ring of n nodes with identifiers  $ID_i$  and weights  $w_i$ at each Add WeChatpowcoder
- In a typical distributed computation for a node i: for r rounds do
  - Assignment Project Exam Help 1. i sends pair  $(ID_i, w_i)$  to i+1, and receives pair  $(ID_{i-1}, w_{i-1})$ tfps://powcoder.com
  - 2. process by adding  $w_i + w_{i-1}$ .
- Add WeChat powcoder

  This can be done in a cumulative manner at *i* as follows:
  - 1.  $i \text{ sends } (ID_i, w_i), (ID_{i-1}, w_{i-1}), \dots, (ID_{i-1}, w_{i-r}) \text{ to } i+1,$ receives  $(ID_{i-1}, w_{i-1}), (ID_{i-2}, w_{i-2}), \dots, (ID_{i-r-1}, w_{i-r-1})$ from i-1
  - 2. process by adding  $w_{i-1} + w_{i-2} + \cdots + w_{i-r-1}$

## Synchronous Algorithm: Canonical Form Assignment Project Exam Help

- Synchronous Algorithm Canonical Form
  - 1. In r radials schala prevergence at most r /\* all the communication first \*/
  - 2. Compute output based on complete information about r-neigh Assignment Blog ecto Example in the end \*/



Main Claim on Canonical Form Assignment Project Exam Help

- Theorem 1 If message size and local computations are not bounded Addry Watchati provide the bounded Addry Watchati provide to bounded algorithm be can be transformed into an algorithm having the canonical form (i.e., it is possible to first communicate for r rounds and then do all the Assignmenti Project Exam Help
- Notice the importance of being able to transmit messages of arbitrary size:
  - this size will Alexen e Chatnanton we corte irounds, and
  - it can be exponetial in r

• To handle "large size messages" you need "large memory"

A message in a distributed System can be anothing I want to be Provided that I do not exceed memory

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- Consider an r-round algorithm  $\mathcal{A}$ . We want to show that  $\mathcal{A}$  can be broughted Weachatapfowcoder
- First, let the nodes communicate for r rounds.
- Assume that in every round, every node sends its complete state to all of its neighbors.
- By induction, althors in poly evolution was the initial state of all other nodes at distance at most i.

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- Hence, after r rounds, a node v has the combined initial knowledge of all the nodes in its r-neighborhood.
- We can show that this suffices to simulate locally (at node v) enough of Algorithm  $\mathcal{A}$  to compute all the messages that v receives in the r communication rounds of a regular execution of Algorithm  $\mathcal{A}$ .

### Assignment Project Exam Help

- It is straightforward to generalize the canonical form to randomized algorithms to powcoder
  - Every node first computes all the random bits it needs throughout the algorithm.
- The random bits are then part of the initial state of a node.

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In Canonical form of distributed
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Computation we as gregate the
messages into trees.

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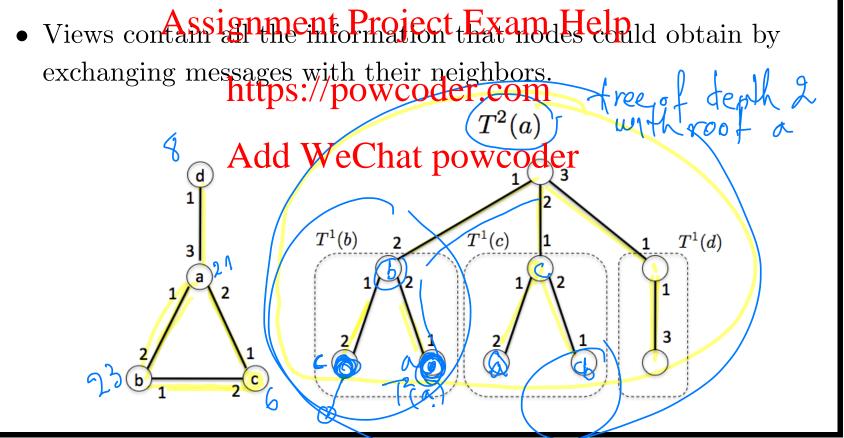
Distributed views

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Views: Undirected Networks
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• Each node has port labels and can build a view accumulating

- Each node has port labels and can build a view accumulating its knowledge. WeChat powcoder
- The view of depth k of a node is a tree containing information on all the walks of length k leaving that node.



#### *r*-View (or *r*-Hop View or *r*-Neighborhood) Assignment Project Exam Help

- Collection of initial states of all nodes in the r-neighborhood of a node validate chap power about the remaining of v.
  - For a given graph G, it is denoted by

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- We usually omit mention of G (when clear from the https://powcoder.com
context) and denote it by

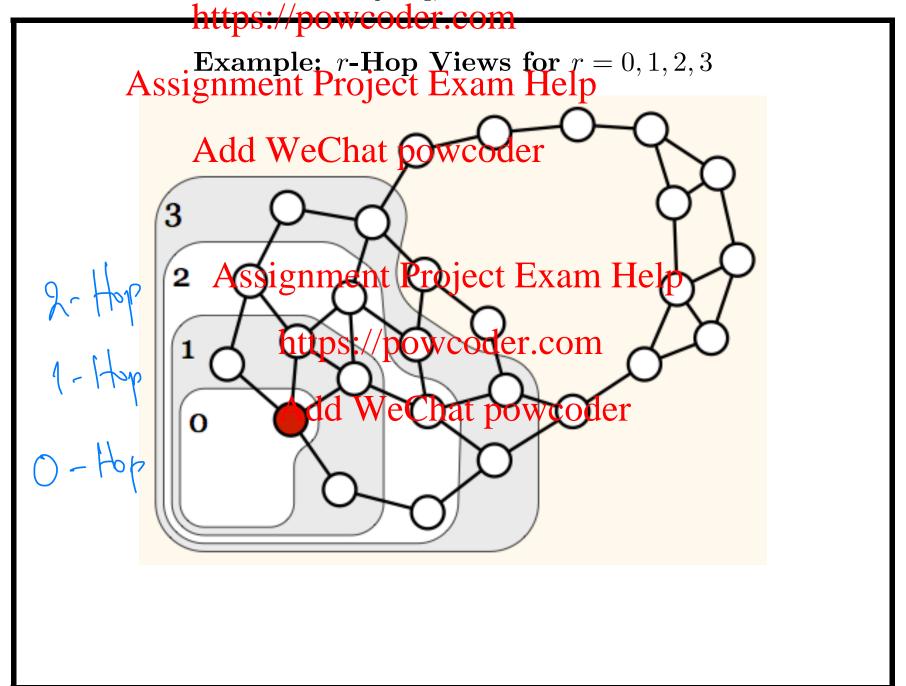
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• A view can be enriched as needed by including information:

- on node states,

- node topology r hops away from the source v,

- etc



## Assignment Project Exam Help

- Assume that initially, every node knows its degree, its label (identificated declarational input.
- The r-hop view of a node v then includes
  - the complete topology of the r-neighborhood,
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    possibly edges between nodes at distance r in the subgraph,
  - possibly edges between nodes at distance r in the subgraph, and https://powcoder.com
  - the labels and additional inputs of all nodes in the Add WeChat powcoder r-neighborhood.

#### The View as a Function Assignment Project Exam Help

- Theorem 2 A deterministic r-round algorithm A is a function that mand der we shat powered to the set of possible outputs.
- By Theorem 1, we know that we can transform Algorithm A to the canonical signment Project Exam Help
- After r communitation/powdsocleryconde v knows exactly its r-hop view.

• This information suffices to compute the output of node v.

### Assignment Project Exam Help

- Two nodes with equal r-hop views
  - have to compute that same outder in every r-round algorithm.
- For coloring algorithms, the only input of a node v is its label.

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  The r-hop view of a node therefore is its labeled

*r*-neighborh**https://powcoder.com** 

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<del>https://powcoder.com</del>

Assignment Project Exam Help A graph of n nodes

• For a graph of n nodes, Norris (1995) proved that if two nodes have the saide West Tateprovice of then they have the same views for all depths.

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• Taking the diameter  $\delta$  of a graph into account, can improve n-1 to

$$O(\delta + \delta \log(n/\delta))$$

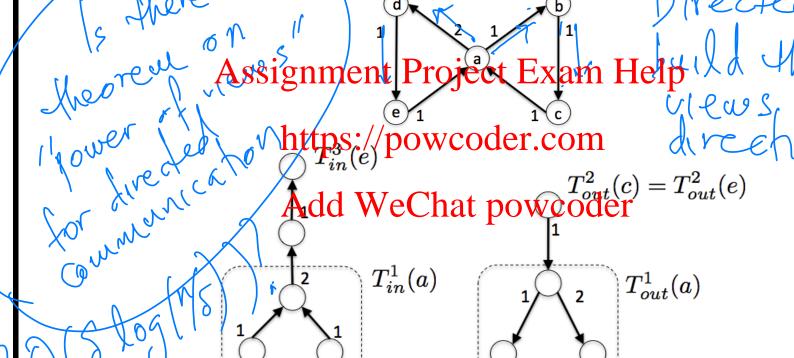
for bidirectional graphs with port numberings

<sup>&</sup>lt;sup>a</sup>We won't discuss details for these claims.

#### <del>https://powcoder.com</del>

Views: Directed Networks Assignment Project Exam Help

• A view can be computed by a node on a network using a distributed determinant power der



• In directed networks we have "in" and "out" views at a node.

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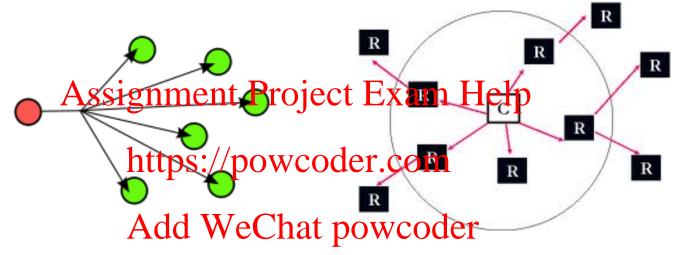
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Browedsting

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## Assignment Project Exam Help

• Broadcasting refers to a method of transferring a message to all recipients dd WeChat powerder



- It is initiated by a single processor, the source.
- The source sends a message to all other nodes in the system.
- In a typical network it may not be possible to send a message "at once" since there might be multiple hops from the source to the rest of the nodes.

### Graph Concepts in Broadcasting Assignment Project Exam Help

• The distance d(u, v) between nodes u and v in an undirected graph GAsdele Wie Chat powscorde minimum length path between u and v.

• The radius

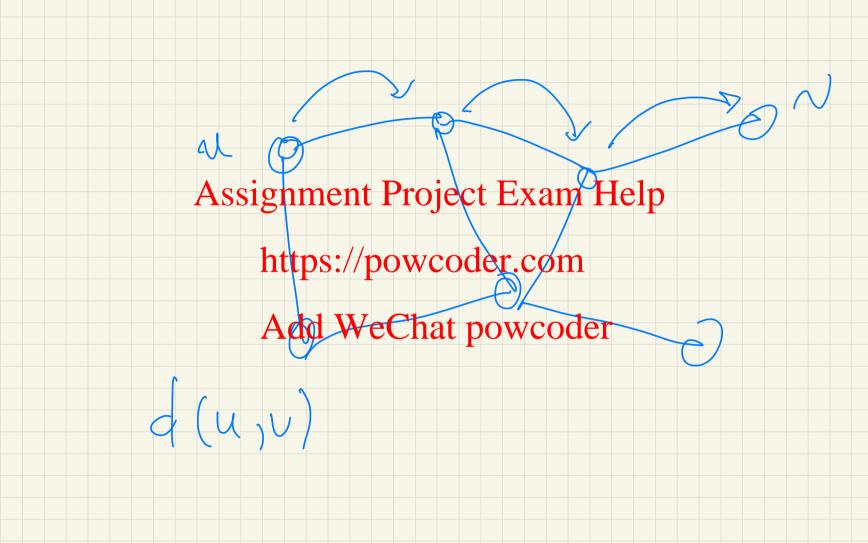
- of a node *u* is the maximum distance between *u* and any other node inthese powcoder.com

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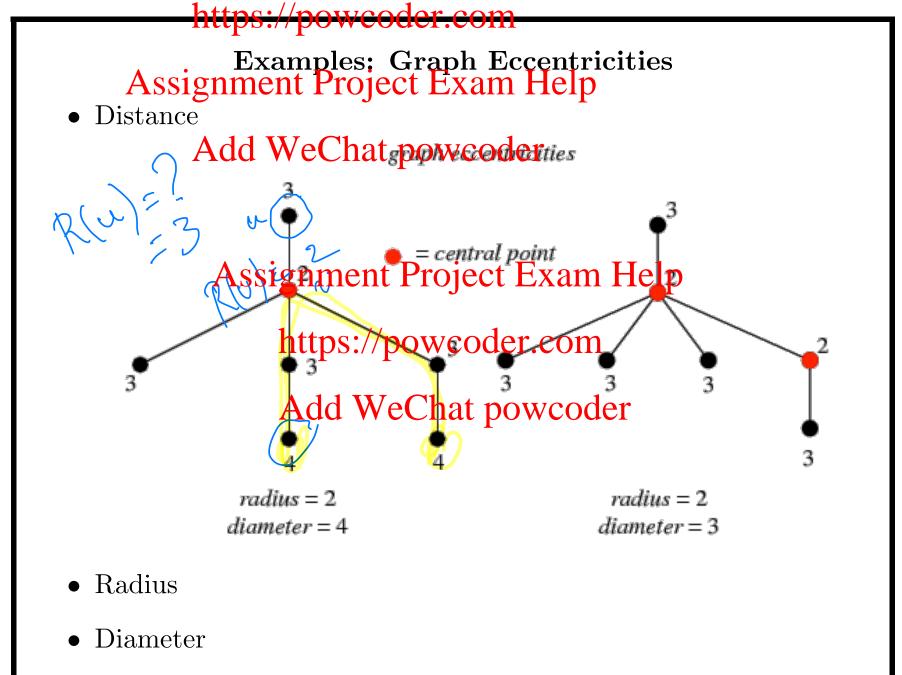
- of a graph is the minimum radius of any node in the graph.

$$R = \min_{u} R(u)$$

• The radius and diameter of a graph are called graph eccentricities.



(Assignment Project Exam Help (u https://powcoder.com Add WeChat powdoder ( w, v) Hw



Examples: Graph Eccentricities Assignment Project Exam Help

• Radius, Diameter

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ullet There is a close relationship between the radius R and the diameter D of a graph

$$-R < D < 2R.$$

RSD S2R

## Examples: Graph Eccentricities Assignment Project Exam Help

• What are the Radius and Diameter?

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- Assignment Project Exam Help

   Traversal of a graph is performed by visiting all of its vertices in some Arddef Wed Chaer powcoder
- Breadth-First-Search Tree. A breadth-first-search tree T of a graph G is a spanning tree of G such that for every node of G, the tree saily is menini Property Example 4 poot.



• Of course a root must be specified!

Assignment Project Exam Help

- BFS Algorithm: Input a graph G = (V, E)Proceed Ayddy We Chat powcoder
  - 1. mark the root r;
  - 2. mark all neighbor vertices that are one hop away from  $\eta$ ;
  - 3. mark new vertices that are one hop away from these neighbors (these are/two hopslaway from r);
  - 4. and so on.

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- It uses a FIFO queue
- It checks whether a vertex has been discovered before enqueueing the vertex rather than delaying this check until the vertex is dequeued from the queue

<sup>a</sup>Invented in 1945 by Konrad Zuse

## Assignment Project Exam Help

• How do you construct a BFS tree from a given graph?



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• First choose any vertex as a root!

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### Assignment Project Exam Help (1/2))

- It starts by placing the source node s at distance d(s) = 0; the distance d(s) = 0 the distance d(s) = 0.
- At the kth step (starting at k = 0), all nodes i at distance d(i) = k are examined, and any neighbors j with  $d(j) = \infty$  (i.e., not yet discovered) have their distance d(j) set to k + 1.
- The process haltstyken prove odds normal neighbors; d(j) is then the length of the shortest path from s to j, or  $d(j) = \infty$  if there is no such path. We Chat powcoder

## Assignment Project Exam Help (2/2))

• BFS is the simplest way to search a graph.

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   It is suited only for unweighted graphs: ignores edge weights.
- Example 1:

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• Example 2: In a social network, your friends are at level one and your friends of friends are at level two in a BFS starting at your node.

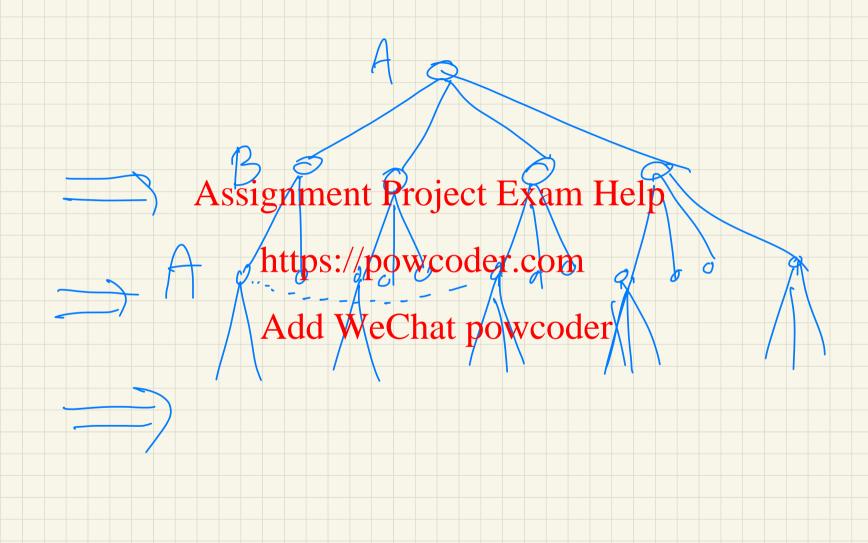
## What is BFS Tree Used for? Assignment Project Exam Help

- Finding all nodes within one connected component
  - BFS by itself is not enough. Some message passing is needed!
- Finding the shortest path between two nodes u and v (with path length measured by number of edges)
  - respectively.

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Testing a graph for bipartiteness

- - Construct a BFS tree from a vertex v and look at all other vertices at odd or even distance from v.
- Doing efficient broadcast
  - from any any node.





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• For a rooted spanning tree T of a graph G,

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let us denote by Add WeChat powcoder

- -S(u) all the nodes in the subtree of u, and
- -P(u) denote all the vertices that exist in a path between u and the root.

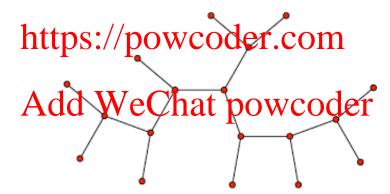
- **DFS Algorithm:** Input a graph  $G = (\overline{V}, E)$ 
  - 1. Start Add WeChat, powcoder
  - 2. visit all possible vertices as far as you can reach;
  - 3. when all vertices are visited, return to the current parent node. Assignment Project Exam Help



### Assignment Project Exam Help (1/2)

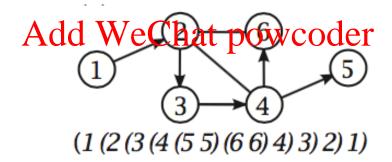
• DFS visits the same nodes as BFS but in a different order.

• If it sees an unvisited node j while examining node i, it fully discovers all unvisited nodes reachable from j and then backtracks to node i to consider the remainder of the nodes adjacent to Assignment Project Exam Help



• It is best described recursively.

- All nodes start out unvisited.
  - Add WeChat powcoder
- DFS(i):
  - 1. mark i as visited
  - 2. for all nodes j adjacent to i do: 3. if node j is not visited DFS(j) Exam Help
- https://powcoder.com • Example



### What is DFS Tree Used for? Assignment Project Exam Help

- Finds all of the vertices reachable from a source vertex r in a graph Add WeChat powcoder
  - unlike BFS it does not need to search the whole graph.
- Topological sorting.
   Assignment Project Exam Help
   this is because of the way it traverses a directed graph.
- Finding the bridgers fapowcoder.com
  - these are edges whose cemaval disconnects the graph.
- Finding connected components.
  - like BFS.
- Finding strongly connected components.
  - these are maximal "strongly connected components" of a directed graph.

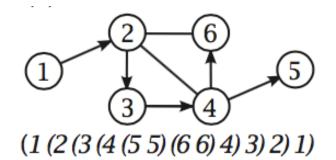
### Assignment Project Exam Help

- The message complexity of broadcast in an n node graph is at least n -Add WeChat powcoder
  - This is because every node must receive the message.
  - Which graphs require n-1 message complexity? Assignment Project Exam Help
- The source's radius is a lower bound for the time complexity.
  - This is becauters in engaged early ones from a source.
- You can use a preceptive tech snapping tree to do broadcast with tight message complexity.
- If the spanning tree is a BFS spanning tree (for a given source), then the time complexity is tight as well.

Jent.

## More on BFS and DFS Assignment Project Exam Help

- Both BFS and DFS describe a tree; i is the parent of j if the unvisited adde weather worder amining node i.
- The DFS tree has a rich set of mathematical properties.
  - For example, if "(i" is printed at the start of DFS(i) and "i)" when it finishes (after traversing all its neighbors j), then the result is any expression with properly nested and matching parentheses.
  - The parenthese of two hodes pand 9 der either nested one within the other, or they are disjoint.



- If the graph is stored in adjacency list form, both BFS and DFS take add a worth at the woods linear in the size of the graph: O(|V| + |E|), where |V| and |E| are the number of nodes and edges, respectively.
- Knowledge calignment Project Exam Help
- Call a graph (nattypsk)/powifotdenoonado not know the topology of the graph.
- If the nodes do not know the topology of the graph (i.e., for a clean network) then the number of edges is a lower bound for the broadcast message complexity.
  - If you do not try every edge, you might miss a whole part of the graph behind it.

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## Assignment Project Exam Help

- Flooding
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- OptFloodMax

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- Used by nodes to identify themselves
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   Flooding Algorithm
  - 1. The source (root) sends the message to all neighbors.
  - 2. Each other node warper receiving the message the first time forwards the message to all (other) neighbors.
  - 3. Upon later reterring provided again (over other edges), a node can discard the message.

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# Assignment Project Exam Help • Let A be the initiating node: <del>ld-</del>WeChat powcoder Assignment Project Exam Help https://powcoder.com WeChat powcoder

• Note that node D receives two messages.

- If node v receives the message first from node u, then node v calls node departmental powcoder
  - Parent relation defines a spanning tree T (nodes receiving more than one message keep message only from one initiate) ssignment Project Exam Help
  - If flooding algorithm is executed in a synchronous system, https://powcoder.com/ then T is a BFS spanning tree (with respect to the root).
- Let R(s) be the Addus of Chatherson Chather network.
  - In asynchronous systems the flooding algorithm terminates after R(s) time units.
  - However, the spanning tree constructed may not be a BFS spanning tree.

- We give a simple algorithm that causes both leaders and non-leaders to Westihathpoweder
- The algorithm
  - requires that the processes know the diameter of the Assignment Project Exam Help
     network;
  - floods the maxips of power of the network,
    - \* so we call it the FloodMaxID algorithm. Add WeChat powcoder
- The algorithm makes leader election possible in a general network.

### Assignment Project Exam Help

- | FloodMaxID Algorithm
  - 1. Every process maintains a record of the maximum ID it has seen so far (initially its own).
  - 2. At each round, each process propagates this maximum on all of its suigning edges, roject Exam Help
  - 3. After D (diameter)/rounds of the coaximum value seen is the process's own ID, the process elects itself the leader; otherwise, it Acada Macahat powcoder

• FloodMax elects the process with the maximum ID.

## Analysis of FloodMax Assignment Project Exam Help

- Define  $i_{\text{max}}$  to be the index of the process with the maximum ID, and Add We Chat powcoder
- Theorem 3 In the FloodMax algorithm, process  $i_{max}$  outputs leader and each other process outputs non-leader, within diameter Assignment Project Exam Help
- Main Claim Aftenstin petwoodels com
  - $\begin{array}{l} \ status_{i_{\max}} = \ leader \ and \\ \ status_{j} = non leader, \ for \ every \ j \neq i_{\max}. \end{array}$
- The key to the proof of this Claim is the fact that
  - after r rounds, the maximum ID has reached every process that is within distance r of  $i_{\text{max}}$ , as measured along directed paths in G.



- The FloodMax algorithm does not extend directly to the asynchrohold setal algorithm does not extend directly to the asynchronous model.
- However, it is possible to simulate the rounds asynchronously.
   Assignment Project Exam Help
   We simply require each process that sends a round r
  - We simply require each process that sends a round r message to tag that/pessage with its round number r.
  - The recipient waits to receive round r messages from all its neighbors before performing inspection.
- By simulating diameter rounds, the algorithm can terminate correctly.

In a way, we make the

Aforthur "message & nicen"

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messiges of Add WeChat powcoder my neghbor

### OptFloodMax Algorithm Assignment Project Exam Help

- There is a simple improvement that can be used to decrease the communication that the communication of the com not decrease the order of magnitude in the worst case.
- Namely, processes can send their current max user ID values only when Assignment Project Exam Helpery round.

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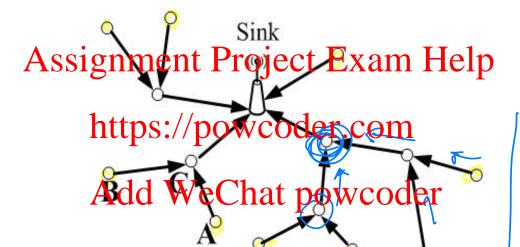
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Convergeeast

# Assignment Project Exam Help

- Convergecast is reversed broadcast:
  - Instead of a root sending a message to all other nodes, all other nodes send information to a root.



• Convergecast is useful for input collection.



# Assignment Project Exam Help

Echo Algorithm

• Requirement: This algorithm is initiated at the leaves.

- 1. A leaf sends a message to its parent.
- 2. If an inner node has received a message from each child, it sends a message to the parent.

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Broddcast Jawel

### Complexity Issues: Broadcast and Convergecast (1/2) Assignment Project Exam Help

- The echo algorithm is paired with the flooding algorithm, which is Asid the Character that they should start the echo process; this is known as flooding/echo.
- One can use convergecast for termination detection.
   Assignment Project Exam Help
   If a root wants to know whether all nodes in the system have finished to the finished
  - \* the message in the echo algorithm then means "This subtree has dds We Chat now coder
- Message complexity of the echo algorithm is n-1,
  - but together with flooding it is O(m), where m = |E| is the number of edges in the graph.

### Complexity Issues: Broadcast and Convergecast (2/2) Assignment Project Exam Help

- The time complexity of the echo algorithm is determined by the depth of the schange (P.el., Ethe radius of the root within the tree) generated by the flooding algorithm.
- The flooding/echo algorithm can do much more than collecting acknowledgements from subtrees. Exam Help
  - For instance hepself puscit designing the number of nodes in the system, or the maximum ID (for leader election), or the sum of and duly scheatipers system.
- By combining results one can compute even fancier aggregations, e.g., with the number of nodes and the sum one can compute the average. With the average one can compute the standard deviation. And so on . . .

#### Application to Leader Election Assignment Project Exam Help

- Asynchronous broadcast and convergecast can be used to solve the lead Add CWo Chatepow and arry graphs
  - without any distinguished source node and
  - without the processes having any knowledge of the number of nodes of the number effect Exam Help
- The processes rettps://provisodes.com

#### Basic Leader Election Algorithm Assignment Project Exam Help

- Every node can initiate
  - first abroadcast, and powcoder
  - next a convergecast

in order to discover the maximum user ID in the network. Assignment Project Exam Help

- The node that finds that the maximum is equal to its own ID elects itself as latters://powcoder.com
- This algorithm Asds Own Chareson Coder

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(Directed Graph) BFS https://powcoder.com

anddApplications

- How do we perform breadth-first search (BFS) in a network based on Addrive Chatrony Condected directed graph having a distinguished source node?
- We consider how to establish a breadth-first spanning tree for the (di)-graph ignment Project Exam Help
- Motivation for https://tpowwoderreemmes from the desire to have a convenient structure to use as a basis for broadcast communication. Add WeChat powcoder
- The BFS tree minimizes the maximum communication time from the process at the distinguished node to all other processes in the network
  - To do this run BFS from each node of the graph and compare values obtained ateach node.

- We suppose that the network is strongly connected and that there is  $\mathbf{AdstiNyashbatspowsoder}_{0}$ .
- The algorithm is supposed to output the structure of a breadth-first directed spanning tree of the network graph, rooted at Assignment Project Exam Help
- The output shohtdpsp/poiwcodeributed fashion: each process other than  $i_0$  should have a parent component that gets set to indicate the node that power parent in the tree.
- As usual, processes only communicate over directed edges.
- Processes are assumed to have user IDs but to have no knowledge of the size or diameter of the network.

# Assignment Project Exam Help

• The basic idea for this algorithm is the same as for the standard addiented by the chatque wise standard and the same as for the standard and the chatque wise standard and the same as for the standard and the same as same as

#### • | SynchBFS Algorithm

- 1. At any point during execution, there is some set of Assignment Project Exam Help processes that is marked: mitially just  $i_0$ .
- 2. Process  $i_0$  sentepow/powecodersegmat round 1, to all of its outgoing neighbors.
- 3. At any round, if an unmarked process receives a search message, it marks itself and chooses one of the processes from which the search has arrived as its parent.
- 4. At the first round after a process gets marked, it sends a search message to all of its outgoing neighbors.

#### Analysis of SynchBFS Assignment Project Exam Help

- We can prove the invariant that
  - after r rounds, every process at distance d from  $i_0$  in the graph,  $1 \le d \le r$ , has its parent pointer defined; moreover, each such pointer points to a node at distance d-1 from  $i_0$ . This invariant land, as usual, the proved by mountain on the number of rounds  $f(x) = \frac{1}{r} \int_0^r \frac{1}{r} dx \, dx$
- The time complexity is at most diameter rounds.

- The number of messages is just |E|
  - a search message is transmitted exactly once on each directed edge.

# Assignment Project Exam Help

- Message Broadcast
- Add WeChat powcoder Global computation
- Electing a leader
- Computin Assignment Project Exam Help

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# Message Broadcast: Piggybacking Assignment Project Exam Help

- The SynchBFS algorithm can easily be augmented to implemented essection implemented to impleme
- If a process has a message M that it wants to communicate to all of the processes in the network,
  - Assignment Project Exam Help—
    it can simply initiate an execution of SynchBFS with itself
    as the root, piggsbacking message
    it sends in round 1.
- Other processes continue to piggyback M on all their search messages as well.
  - Since the tree eventually spans all the nodes, message M is eventually delivered to all the processes.

# Assignment Project Exam Help

- This means
  - Collection of information wronger oughout the network or,
  - more generally, the computation of a function based on distributed inputs.

- For example,
  - consider the problem prower encourses has a nonnegative integer input value and we want to find the sum of all the inputs in the network.
  - Using a BFS tree, this can be done easily (and efficiently) as follows.

- Starting from the leaves, "fan in" the results in a convergecast procedure de two chat powcoder
  - 1. Each leaf sends its value to its parent;
  - 2. each parent waits until it gets the values from all its children, saignment Project Exam Help that then sends the sum to its own parent. The sum to its own parent.
- The sum calculated by the root of the BFS tree is the final answer. Add WeChat powcoder

- Using SynchBFS, an algorithm can be designed to elect a leader in Add two Chiant posycool when the processes have no knowledge of n or diameter.
  - 1. Namely, all the processes can initiate breadth-first searches in paradesignment Project Exam Help
  - 2. Each process i uses the tree thereby constructed and the https://powcoder.com/global computation procedure just described to determine the maximum de diverging constructed and the maximum described where the maximum described are two described and the maximum described and the described and the described and the maximum described and the described and
  - 3. The process with the maximum ID then declares itself to be the leader, and all others announce that they are not the leader.
- If the graph is undirected, the time is O(diameter) and the number of messages is O(n|E|).

# Computing the Diameter Assignment Project Exam Help

- The diameter of the network can be computed by having all processes iddia. Clear processes in parallel.
  - 1. Each process i uses the tree thereby constructed to determine  $\max -dist$ , defined to be the maximum distance from i Assignment Project Example 1
  - 2. Each process *i* then reuses its breadth-first tree for a global computation to discover the maximum of the max -dist values. Add WeChat powcoder
- If the graph is undirected, the time is O(diam) and the number of messages is O(n|E|), where diam is the diameter of the graph.
- The diameter thus computed could be used, for example, in the leader-election algorithm FloodMax.

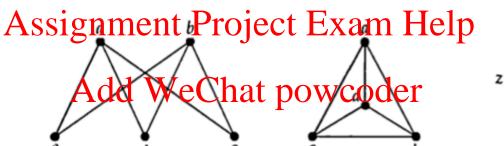
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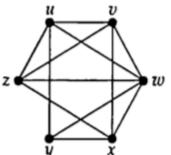
1. Explain why every tree is a bipartite graph.

- 2. Let T be add a We Chat payce define the following statements are equivalent.
  - (a) T is connected and has no cydes.
  - (b) T has Assignmentd Project Exam Help
  - (c) T is connected and has n-1 edges.
  - (d) T is connected and the removal of any edge disconnects T.
  - Any two vertices of Taxe connected by exactly one path.
  - T contains no cycles, but the addition of any new edge creates a cycle.
- 3. Give an algorithm to compute the diameter and radius of a tree.
- 4. Determine the size of a message which propagates for r hops in <sup>a</sup>Not to hand in!

Assignment Project Exam Help "Synchronous Algorithm Canonical Form". More specifically, consider Adom Wete binary over college with height n. Label the ports at an interior node as L, R (for the Left and Right siblings at a node), and P for its parent. Do the same in an analogous Assign for the protect end the leaves of each  $r \leq n$ and each node v construct the r-view at this node.

5. A connected graph is Hamiltonian if there is a cycle, that includes every vertex exactly once (such a cycle is called Hamiltonian). A connected graph is semi-Hamiltonian if there is a path (but not a cycle) that includes every vertex exactly once (such a path is called semi-Hamiltonian). Determine which of the following graphs are semi-Hamiltonian, and write down a corresponding semi-Hamiltonian path where possible:

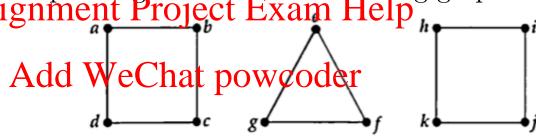




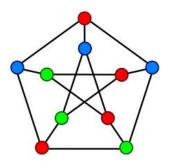
- 6. A forest is Assignment in prosperity Example the light of whose components is a tree.
  - (a) Let G be a https://powcoder.com/k components. How many edges does WeChat powcoder
    (b) Construct a forest with 12 vertices and 9 edges.

  - (c) Is it true that every forest with k components has at least 2k vertices of degree 1?
- 7. A spanning forest in a graph G (not necessarily connected) is obtained by constructing a spanning tree for each component of G.

(a) Find a spanning forest for the following graph. Assignment Project Exam Help



- (b) Let G be a graph, and let F be a subgraph of G. If F is a forest winding all voices Examily a spanning forest of G? powcoder.com
- 8. Find three spanning trees in the Petersen graph (depicted below): Add WeChat powcoder



9. Prove that trees and forests are bipartite graphs.

10. Prove that, in a bipartite graph, every cycle has an even assignment Project Exam Help number of edges. Conversely, prove that, if every cycle of a graph has an even number of edges, then the graph is bipartite. Hint: Consider a connected graph G. Choose a vertex v in G and consider those vertices whose minimum distance from v is even and those whose minimum distance from v is odd. To Assignment Project Exam Help which vertices are the "odd" vertices adjacent? To which vertices are the "odd" vertices adjacent?