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Companyaming (1)

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Based on (Cormen et al., 2002) & (Kleinberg & Tardos, 2005)

Assignment Project Exam Help Algorithms paradigms

Greedy:

- o Build up Asso by incrementally am Help
- Iteratively decompose and reduce the size of the problem.
- o Top-down apattach/powcoder.com

• Dynamic programming. We Chat powcoder

- Solve all possible sub-problems.
- Assemble them to build up solutions to larger problems.
- Bottom-up approach.

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Principle: Use answers previously computed for a smaller instance

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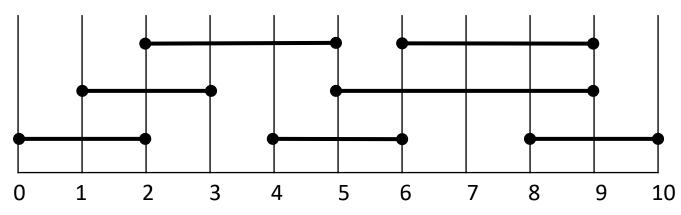
INTRODUCTION

Activity selection Problem

- Input: Set S of n activities, a_1 , a_2 , ..., a_n .
 - $-s_i$ = start time of activity *i*.
 - $-f_i$ = finish time of activity i. Assignment Project Exam Help
- Output: Subset A of maximum number of compatible https://powcoder.com activities.
 - 2 activities are and pathole, if the refer vals do not overlap.

Example:

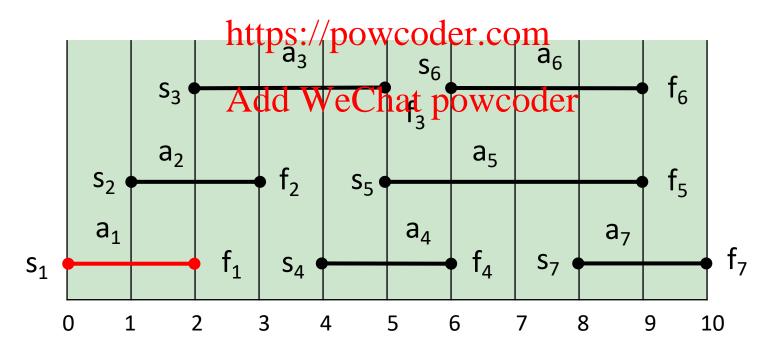
Activities in each line are compatible.



Activity selection Problem

							7
S _i	0	1	2	4	5	6	8
f_i	2	3	5	6	9	9	10

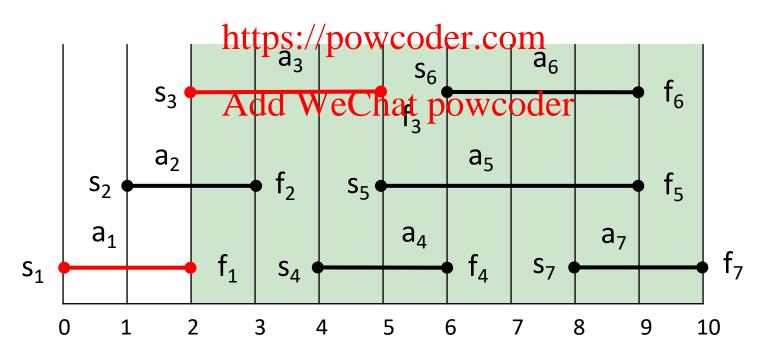
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Activity selection Problem

				4			
S _i	0	1	2	4	5	6	8
f_i	2	3	5	6	9	9	10

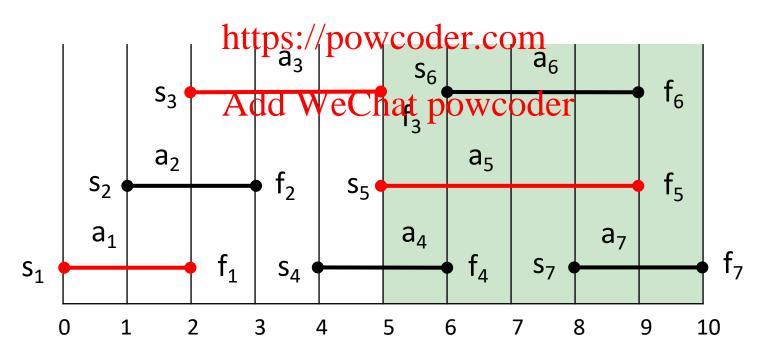
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Activity selection Problem

				4			
				4			
f_i	2	3	5	6	9	9	10

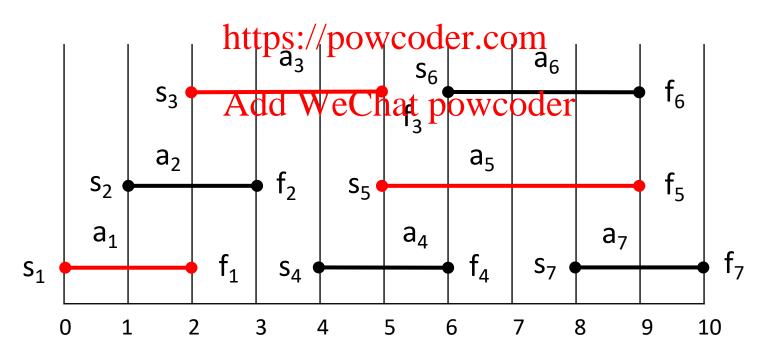
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Activity selection Problem

i	1	2	3	4	5	6	7
S _i	0	1	2	4	5	6	8
f_i	2	3	5	6	9	9	10

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Assignment Project Exam Help Optimal sub-structure

- Let S_{ij} = subset of activities in S that start after a_i finishes and finish before a_i starts.

 Assignment Project Exam Help $S_{ij} = \left\{ a_k \in S : \forall i, j \quad f_i \leq s_k < f_k \leq s_j \right\}$ https://powcoder.com
- A_{ij} = optimal solation WeShat powcoder
- $A_{ij} = A_{ik} U \{ a_k \} U A_{kj}$

Assignment Project Exam Help AdGweedty choice

```
# subproblems in optimal solutions ignment Project Exam Help # choices to consider https://powcoder.com

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```

We can solve the problem S_{ij} top-down:

- Consider all $a_k \in S_{ij}$
- Solve S_{ik} and S_{kj}
- Pick the best m such that $A_{ij} = A_{im} \cup \{a_m\} \cup A_{im}$

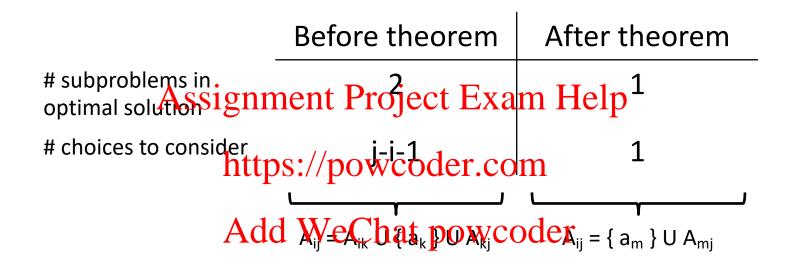
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Theorem:

Let $S_{ij} \neq \emptyset$, and let a_m be the activity in S_{ij} With the earliest finish time $f_{ij} \neq f_{ij}$. Then:

- 1. a_m is used in some maximum sizes μ bset of mutually compatible activities of S_{ii} .
- 2. $S_{im} = \emptyset$, so that choosing a_m leaves S_{mj} as the only nonempty subproblem.

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We can now solve the problem S_{ii} top-down:

- Choose $a_m \in S_{ii}$ with the earliest finish time (greedy choice).
- Solve S_{mi} .

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- Greedy choice is not always available. Assignment Project Exam Help
- How to solve efficiently problems that exhibit an optimal substructures problems that exhibit an optimal problems that exhibit an optimal substructures problems that exhibit an optimal substructures problems that exhibit an optimal substructures problems that exhibit an optimal substructure of the substructure o

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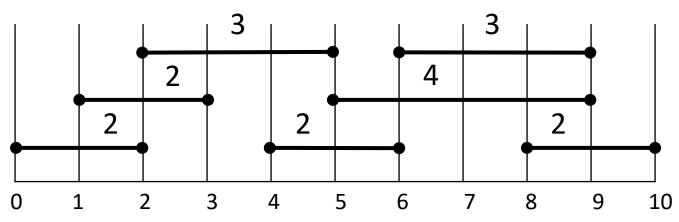
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WEIGHTED INTERVAL SCHEDULING

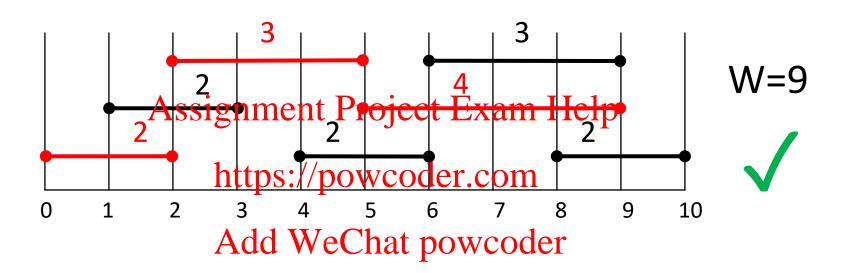
Weighted interval scheduling

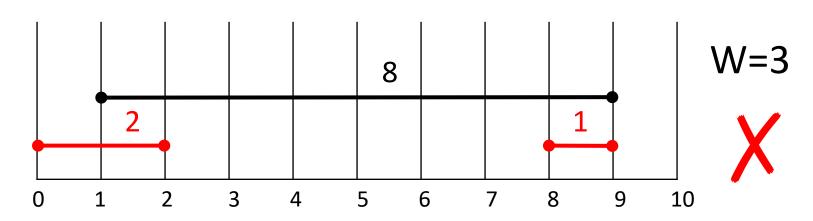
- Input: Set S of n activities, a_1 , a_2 , ..., a_n .
 - $-s_i$ = start time of activity *i*.
 - $-f_i$ = finish time of activity *i*.
 - w_i= weigh Assignment Project Exam Help
- Output: find maximum weight subset of mutually compatible activities.
 - 2 activities are 40m partiol haif pheircingervals do not overlap.

Example:



Assignment Project Exam Help Application of the greedy algorithm





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- Optimal substructure:
 Assignment Project Exam Help
 Assignment Solution to Sij
 - A_{ii} = A_{ik}https://paycoder.com

• Greedy Choice: X eChat powcoder

- - Select the activity with earliest finish time.

AdPatahatructure

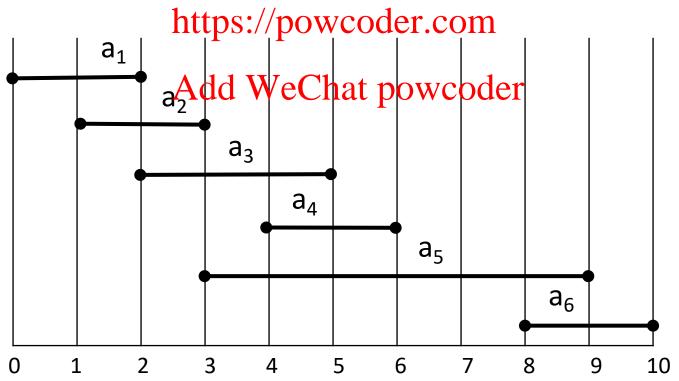
Notation: All activities are sorted by finishing time $f_1 \le f_2 \le ... \le f_n$

Definition: p(j) = largest index i < j such that activity/job i is

compatible with activity/job j.

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Examples: p(6)=4, p(5)=2, p(4)=2, p(2)=0.



Add Binary Choice

Notation: OPT(j) = value of the optimal solution to the problem including activities 1 to j

= max total weight of compatible activities 1 to j

Case 1: OPT selectis gottivetrytj Project Exam Help

- Add weight w_i
- Cannot use incompanie le com
- Must include optimal solution on remaining compatible activities { 1, 2, ..., p(j) }.

Case 2: OPT does not select activity j

Optimal substructure property

Must include optimal solution on other activities { 1, 2, ..., j-1 }.

$$OPT(j) = \begin{cases} 0 & if j = 0\\ max\{w_j + OPT(p(j)), OPT(j-1)\} & Otherwise \end{cases}$$

Assignment Project Exam Help Add Recursive Call

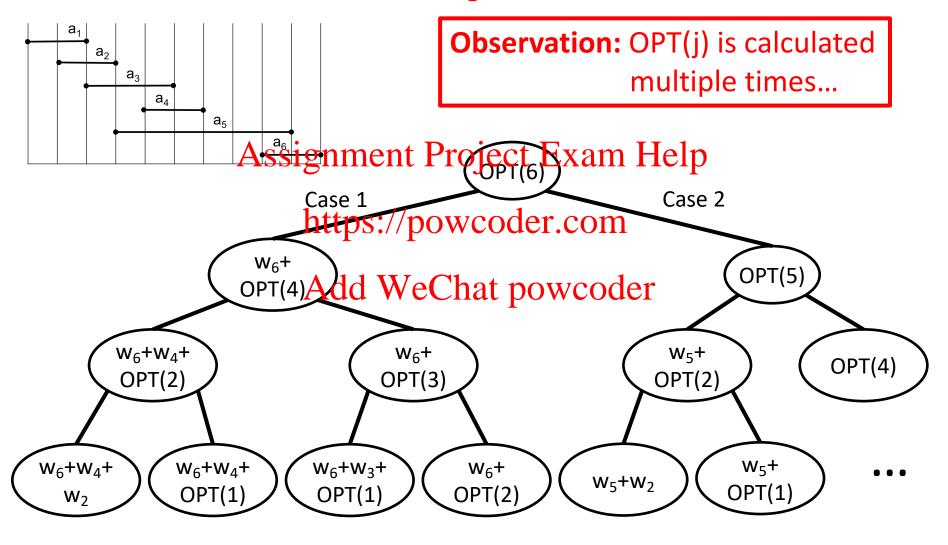
```
Input: n, s[1..n], f[1..n], v[1..n]
Sort jobs by finish time sortifet Exam Help ... ≤ f[n].

Compute p[1], p[2 https://powcoder.com

Compute-Opt(j) Add WeChat powcoder

if j = 0
   return 0.
else
   return max(v[j] + Compute-Opt(p[j]), Compute-Opt(j-1)).
```

Brute Ferce Approach



AddWempization

Memoization: Cache results of each subproblem; lookup as needed.

```
Input: n, s[1..n], f[1..n], v[1..n]
Sort jobs by Aissighnhing Protect Exams Help ... ≤f[n].
Compute p[1], p[2], ..., p[n].
                  https://powcoder.com
for j = 1 to n
   M[j] ← empty. Add WeChat powcoder
M[0] \leftarrow 0.
M-Compute-Opt(j)
if M[j] is empty
   M[j] \leftarrow \max(v[j]+M-Compute-Opt(p[j]),
                M-Compute-Opt(j-1)
return M[j].
```

AddRynaningstime

Claim. Memoized version of algorithm takes $O(n \log n)$ time.

- Sort by finish time: $O(n \log n)$.
- Computing $p(\cdot)$: $O(n \log n)$ via sorting by start time.

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- M-COMPUTE-OPT(j): each invocation takes O(1) time and either
 - (i) returns antepistin powerder.com
 - (ii) fills in one new entry M[j] and makes two recursive calls Add WeChat powcoder
- Progress measure $\Phi = \#$ nonempty entries of M[].
 - initially $\Phi = 0$, throughout $\Phi \leq n$.
 - (ii) increases Φ by $1 \Rightarrow$ at most 2n recursive calls.
- Overall running time of M-Compute-Opt(n) is O(n).

Remark. O(n) if jobs are presorted by start and finish times.

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DYNAMIC PROGRAMMING

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Observation: When we compute M[j], we only need values M[k] for k < j.

```
BOTTOM-UP (n; s1, ..., sn; f1, ..., fn; v1, ..., vn)
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Sort jobs by finish time so that f1 \le f2 \le ... \le fn.

Compute p(1), p(p), p(p), p(p), com

M[0] \leftarrow 0
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for j = 1 TO n

M[j] \leftarrow \max \{ vj + M[p(j)], M[j-1] \}
```

Main Idea of Dynamic Programming: Solve the sub-problems in an order that makes sure when you need an answer, it's already been computed.

Assignment Project Exam Help Finding Solution

Dyn. Prog. algorithm computes optimal value.

Q: How to find solution itself?

A: Bactrack! Assignment Project Exam Help

```
Find-Solutings: powcoder.com

if j = 0

return Add WeChat powcoder

else if (v[j] + M[p[j]] > M[j-1])

return { j } U Find-Solution(p[j])

else

return Find-Solution(j-1).
```

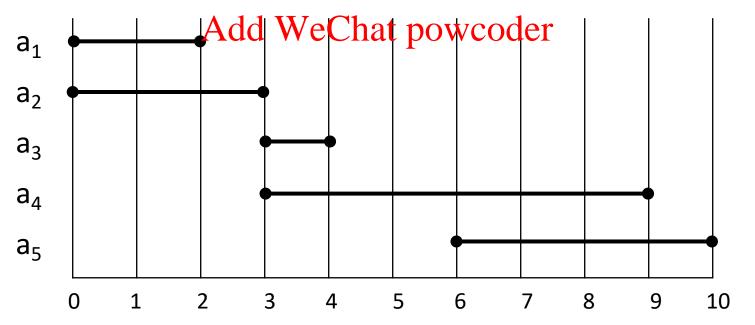
Analysis. # of recursive calls $\leq n \Rightarrow O(n)$.

Example: Computing solution

activity	1	2	3	4	5
predecessor	0	0	2	2	3
Best weight M	-	_	-	-	-
V _j +M Ap(j)] gn	ment l	Projec	t Exan	n Help	-
M[j-1]	-,,	-	_	-	-

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(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.

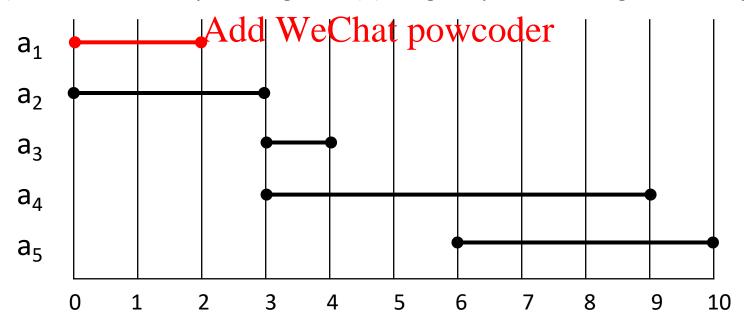


Example: Computing solution

activity	1	2	3	4	5
predecessor	0	0	2	2	3
Best weight M	2	-	-	-	-
V _j +M Ap(j)]g n	m e nt]	Projec	t Exan	n Help	-
M[j-1]	0	-	-	-	-
h 44	t-10 0 1 / 10	OTTIOO	044 0044		

M[0]=0

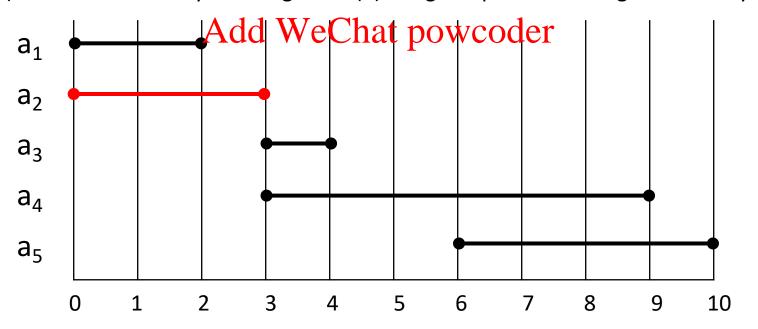
https://powcoder.com
 (1) Activities sorted by finishing time. (2) Weight equal to the length of activity.



Example: Computing solution

activity	1	2	3	4	5
predecessor	0	0	2	2	3
Best weight M	2	3	-	-	-
V _j +M /(p(j)]g n	m ∂ nt Ì	Projec	t Exan	n Help	-
M[j-1]	0,,	2	_	-	-

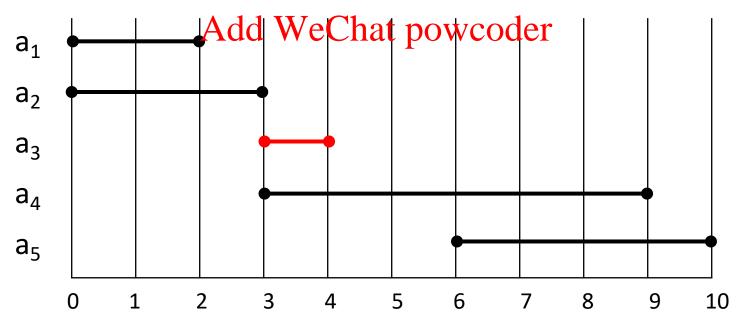
https://powcoder.com
(1) Activities sorted by finishing time. (2) Weight equal to the length of activity.



Example: Computing solution

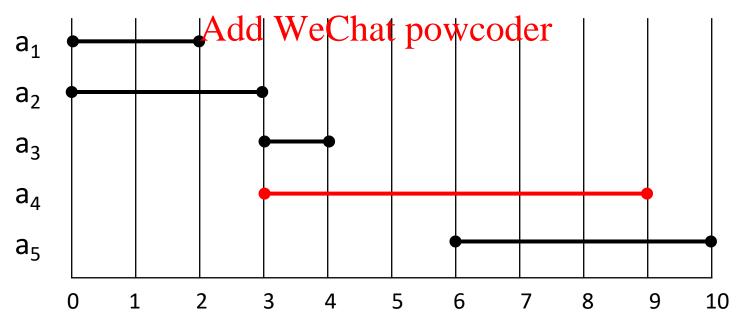
1	2	3	4	5
0	0	2	2	3
2	3	4	-	-
m e nt i	Projec	t E x an	n Help	-
0	2	3	-	-
	1 0 2 ment 0	1 2 0 0 2 3 ment Projec 0, 2	1 2 3 0 0 2 2 3 4 ment Project Exan 0 2 3	1 2 3 4 0 0 2 2 2 3 4 - ment Project Exam Help 0, 2 3 -

nttps://powcoder.com
 (1) Activities sorted by finishing time. (2) Weight equal to the length of activity.



Example: Computing solution

activity	1	2	3	4	5		
predecessor	0	0	2	2	3		
Best weight M	2	3	4	9	-		
V _j +Masilignment Project Estam Help -							
M[j-1]	0	2	3	4	-		
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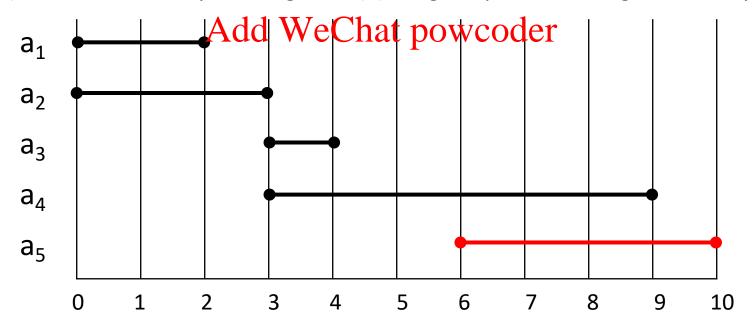


Example: Computing solution

Your

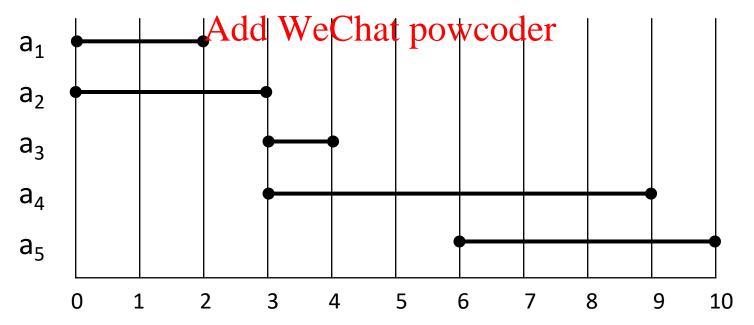
solution

activity	1	2	3	4	5	
predecessor	0	0	2	2	3	
Best weight M	2	3	4	9	9	
V _j +M Ap(j)]gn	m ∉ nt]	Projec	t Exar	n Help	8	
M[j-1]	0	2	3	4	9	
ht1	tng·//n	OWCOC	er cor	n		



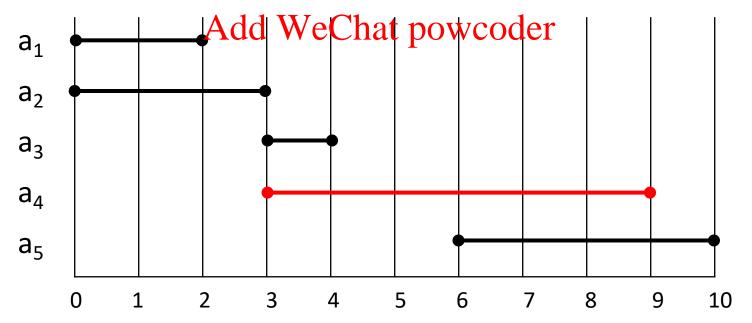
Example: Reconstruction

activity	1	2	3	4	5	
predecessor	0	0	2	2 \	3	
Best weight M	2	3	4	9	9	
V _j +M Ap(j)] gn	m e nt	Projec	t Exar	n Help	8	
M[j-1]	0	2	3	4	\ 9	
https://powcoder.com						



Example: Reconstruction

activity	1	2	3	4	5		
predecessor	0	0	2	2	3		
Best weight M	2	3	4	9	9		
V _j +M Ap(j)]g n	m ∉ nt l	Project	t E x an	n Help	8		
M[j-1]	0	2	3	4	9		
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Example: Reconstruction

activity	1	2	3	4	5
predecessor	0	0	2	2	3
Best weight M	2	3	4	9	9
V _j +M Ap(j)]g n	m e nt	Projec	t Extan	n Help	8
M[j-1]	0	2	3	4	9
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