

Lecture 2

- Theory
 - Unification
 - Unification in Prolog
 - Proof search
- Exercises
 - Exercises of LPN chapter 2
 - Practical work

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Aim of this lecture

- Discuss **unification** in Prolog
 - Show how Prolog unification differs from standard unification
- Explain the search strategy that Prolog uses when it tries to deduce new information from old, using modus ponens

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Unification

- Recall previous example, where we said that Prolog unifies

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woman(X)
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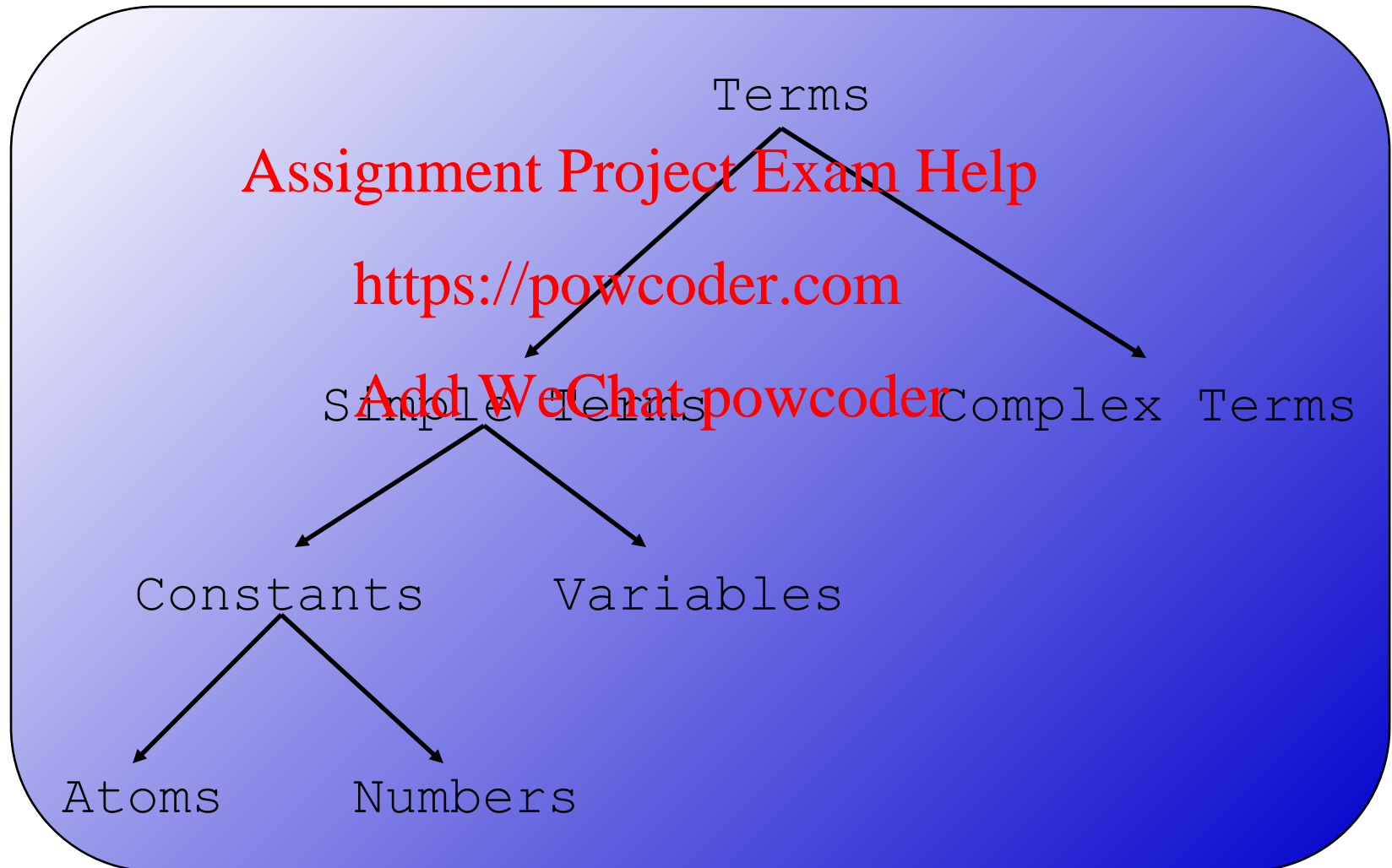
with

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woman(mia)

thereby instantiating the variable **X** with the atom **mia**.

Recall Prolog Terms



Unification

- Working definition:
 - Two terms unify if they are the same term or if they contain variables that can be uniformly instantiated with terms in such a way that the resulting terms are equal

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Unification

- This means that:
 - **mia** and **mia** unify
 - **42** and **42** unify
 - **woman(mia)** and **woman(mia)** unify
- This also means that:
 - **vincent** and **mia** do not unify
 - **woman(mia)** and **woman(jody)** do not unify

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Unification

- What about the terms:

- **mia** and **X**

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Unification

- What about the terms:
 - **mia** and **X**
 - **woman(Z)** and **woman(mia)**
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Unification

- What about the terms:
 - **mia** and **X**
 - **woman(Z)** and **woman(mia)**
 - **loves(mia,X)** and **loves(X,vincent)**

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Instantiations

- When Prolog unifies two terms it performs all the necessary instantiations, so that the terms are equal afterwards
- This makes unification a powerful programming mechanism

Revised Definition 1/3

1. If T_1 and T_2 are constants, then T_1 and T_2 unify if they are the same atom, or the same number.

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Revised Definition 2/3

1. If T_1 and T_2 are constants, then T_1 and T_2 unify if they are the same atom, or the same number.
2. If T_1 is a variable and T_2 is any type of term, then T_1 and T_2 unify, and T_1 is instantiated to T_2 . (and vice versa)

Revised Definition 3/3

1. If T_1 and T_2 are constants, then T_1 and T_2 unify if they are the same atom, or the same number.
2. If T_1 is a variable and T_2 is any type of term, then T_1 and T_2 unify, and T_1 is instantiated to T_2 . (and vice versa)
3. If T_1 and T_2 are complex terms then they unify if:
 - a) They have the same functor and arity, and
 - b) all their corresponding arguments unify, and
 - c) the variable instantiations are compatible.

Prolog unification: =/2

?- mia = mia.

yes Assignment Project Exam Help

?- <https://powcoder.com>

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Prolog unification: =/2

?- mia = mia.

yes

?- mia = vincent.

no

?-

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Prolog unification: =/2

?- mia = X.

X=mia

yes

?-

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How will Prolog respond?

?- X=mia, X=vincent.

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How will Prolog respond?

?- X=mia, X=vincent.

no Assignment Project Exam Help

?- <https://powcoder.com>

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Why? After working through the first goal, Prolog has instantiated X with **mia**, so that it cannot unify it with **vincent** anymore. Hence the second goal fails.

Example with complex terms

?- $k(s(g), Y) = k(X, t(k))$.

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Example with complex terms

?- $k(s(g), Y) = k(X, t(k))$.

$X = s(g)$ Assignment Project Exam Help

$Y = t(k)$ <https://powcoder.com>

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?-

Example with complex terms

?- $k(s(g), t(k)) = k(X, t(Y))$.

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Example with complex terms

?- $k(s(g), t(k)) = k(X, t(Y))$.

$X = s(g)$ Assignment Project Exam Help

$Y = k$ <https://powcoder.com>

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?-

One last example

?- loves(X,X) = loves(marsellus,mia).

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Prolog and unification

- Prolog does not use a standard unification algorithm
- Consider the following query:
 $?- \text{father}(X) = X.$
- Do these terms unify or not?

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?- father(X) = X.

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Infinite terms

?- father(X) = X.

X=father(father(father(...)))

yes

?-

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Occurs Check

- A standard unification algorithm carries out an occurs check
- If it is asked to unify a variable with another term it checks whether the variable occurs in the term
- In Prolog:

?- unify_with_occurs_check(father(X), X).
no

Programming with Unification

```
vertical( line(point(X,Y),  
              point(X,Z))).
```

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```
horizontal( line(point(X,Y),  
                point(Z,Y))).
```

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Programming with Unification

```
vertical( line(point(X,Y),  
              point(X,Z))).
```

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```
horizontal( line(point(X,Y),  
                point(Z,Y))).
```

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?-

Programming with Unification

```
vertical( line(point(X,Y),  
              point(X,Z))).
```

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```
horizontal( line(point(X,Y),  
                point(Z,Y))).
```

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?- vertical(line(point(1,1),point(1,3))).

yes

?-

Programming with Unification

```
vertical( line(point(X,Y),  
              point(X,Z))).
```

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```
horizontal( line(point(X,Y),  
                point(Z,Y))).
```

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?- vertical(line(point(1,1),point(1,3))).

yes

?- vertical(line(point(1,1),point(3,2))).

no

?-

Programming with Unification

```
vertical( line(point(X,Y),  
              point(X,Z))).
```

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```
horizontal( line(point(X,Y),  
                point(Z,Y))).
```

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```
?- horizontal(line(point(1,1),point(1,Y))).
```

```
Y = 1;
```

```
no
```

```
?-
```


Programming with Unification

```
vertical( line(point(X,Y),  
              point(X,Z))).
```

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```
horizontal( line(point(X,Y),  
                point(Z,Y))).
```

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```
?- horizontal(line(point(2,3),Point)).
```

```
Point = point(_554,3);
```

```
no
```

```
?-
```

Exercise: unification

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Proof Search

- Now that we know about unification, we are in a position to learn how Prolog searches a knowledge base to see if a query is satisfied.
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- In other words. we are ready to learn about proof search
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Example

f(a).

f(b).

g(a).

g(b).

h(b).

k(X):- f(X), g(X), h(X).

?- k(Y).

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Example: search tree

f(a).

f(b).

g(a).

g(b).

h(b).

k(X):- f(X), g(X), h(X).

?- k(Y).

?- k(Y).

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Example: search tree

f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).

?- k(Y).

$Y=X$

?- f(X), g(X), h(X).

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Example: search tree

f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).

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?- k(Y).

Y=X

?- f(X), g(X), h(X).

X=a

?- g(a), h(a).

Example: search tree

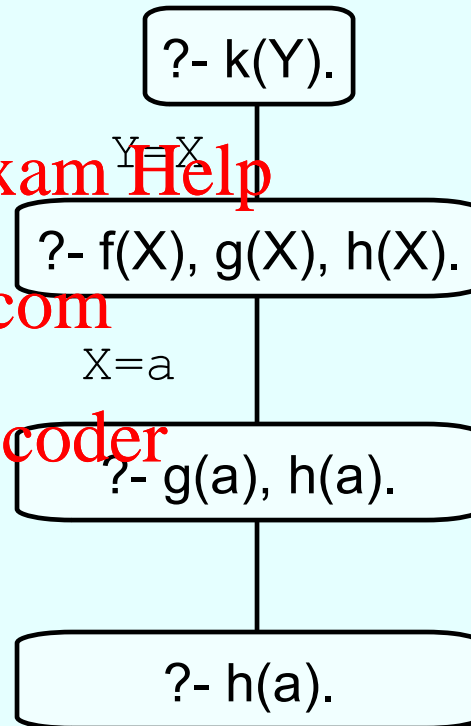
f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).

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Example: search tree

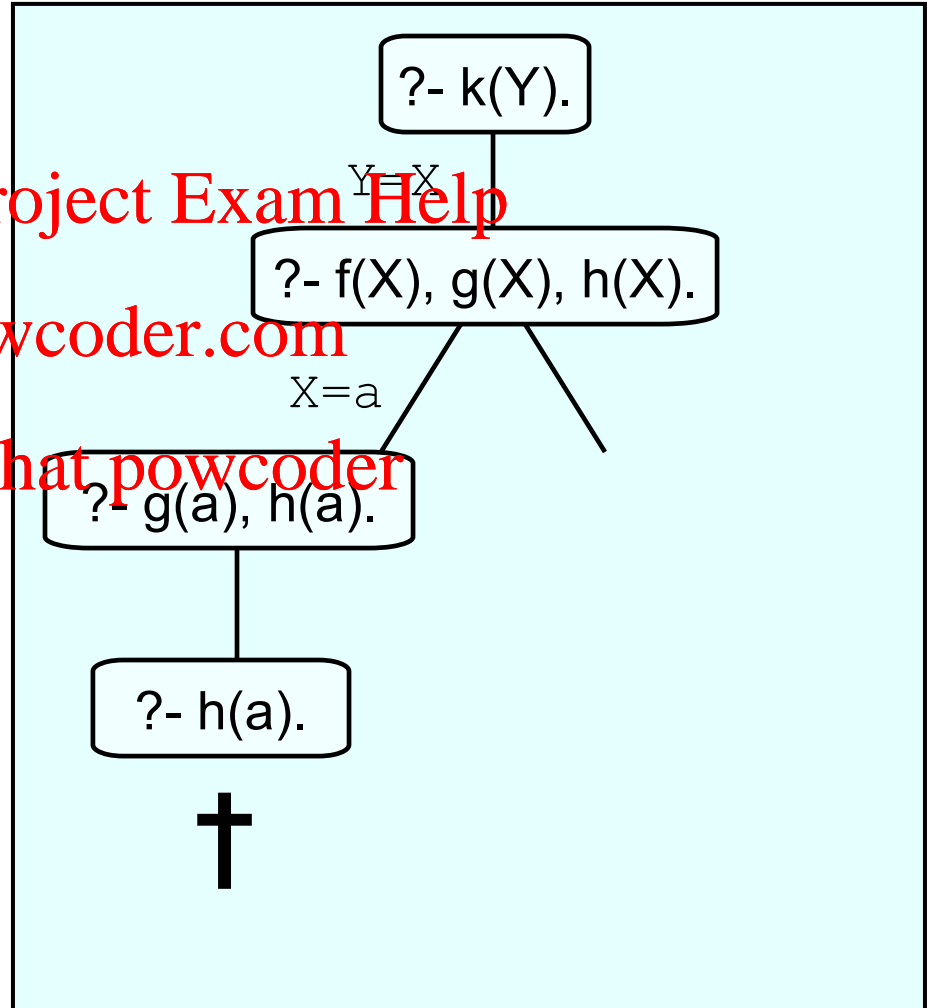
f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).

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Example: search tree

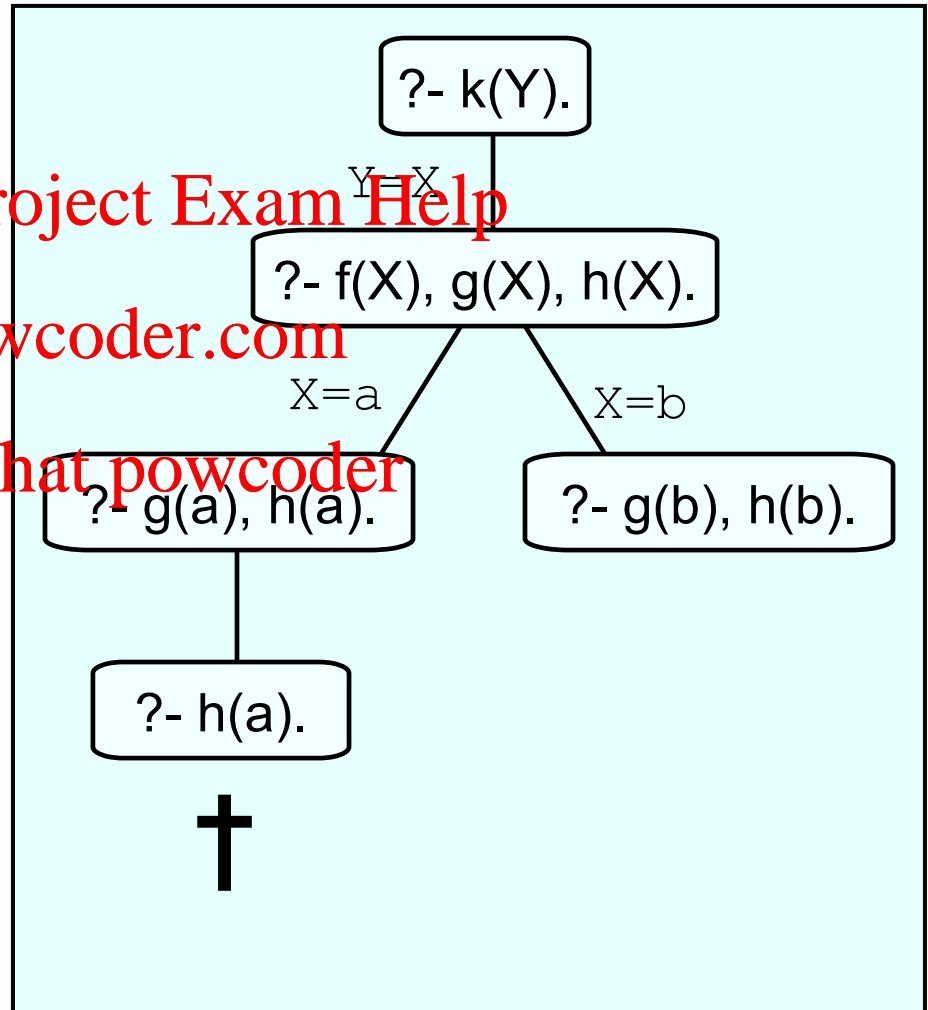
f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).

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Example: search tree

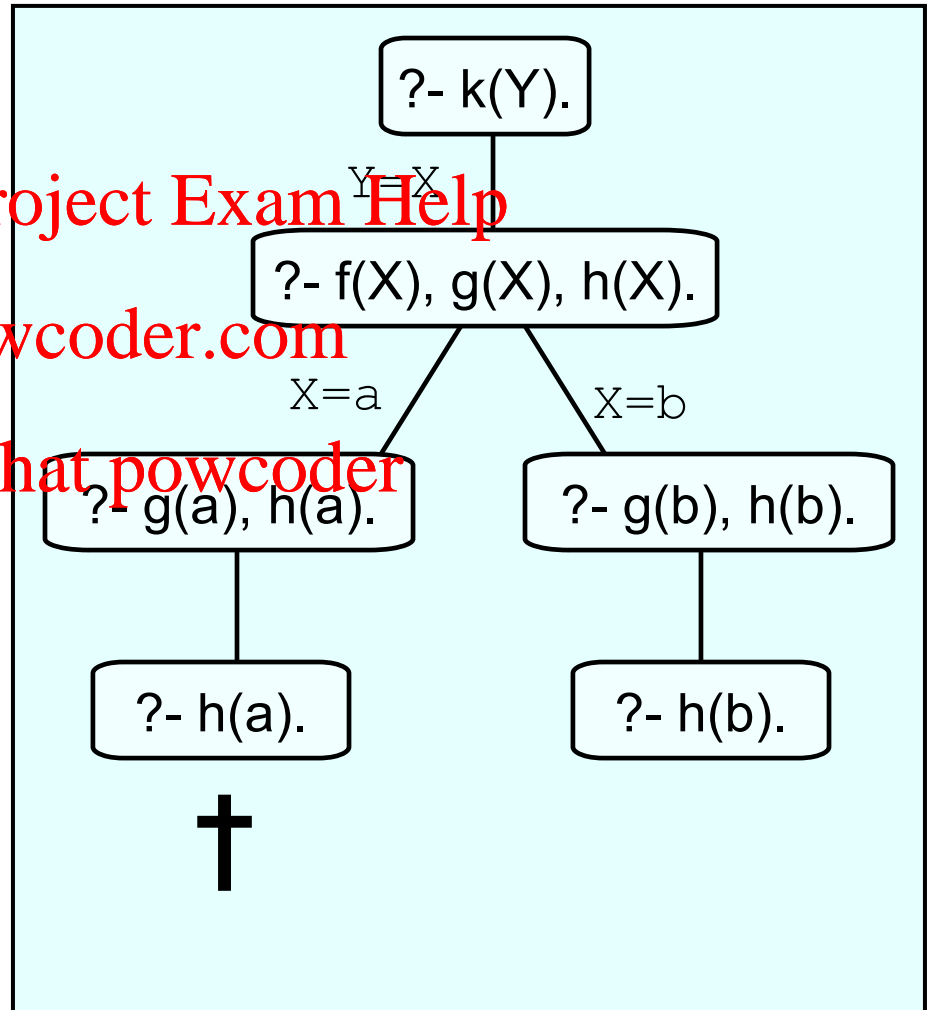
f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).

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Example: search tree

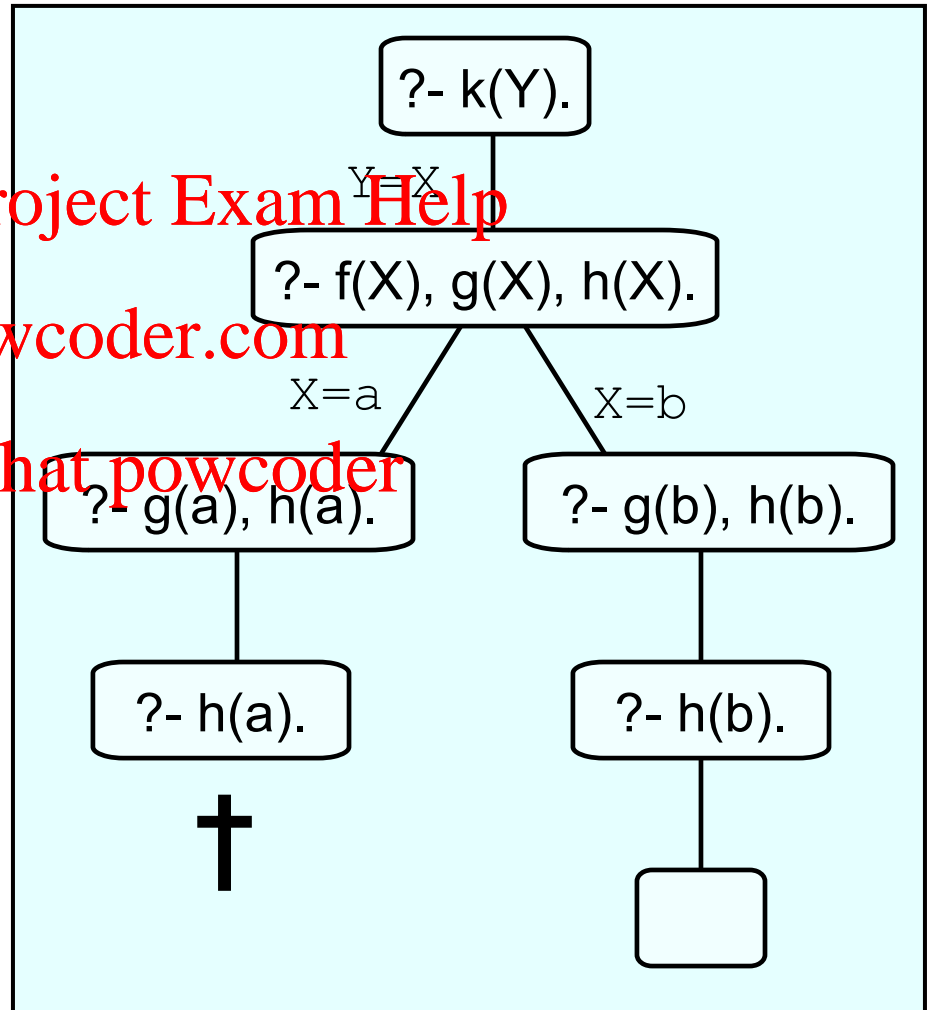
f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).
Y=b

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Example: search tree

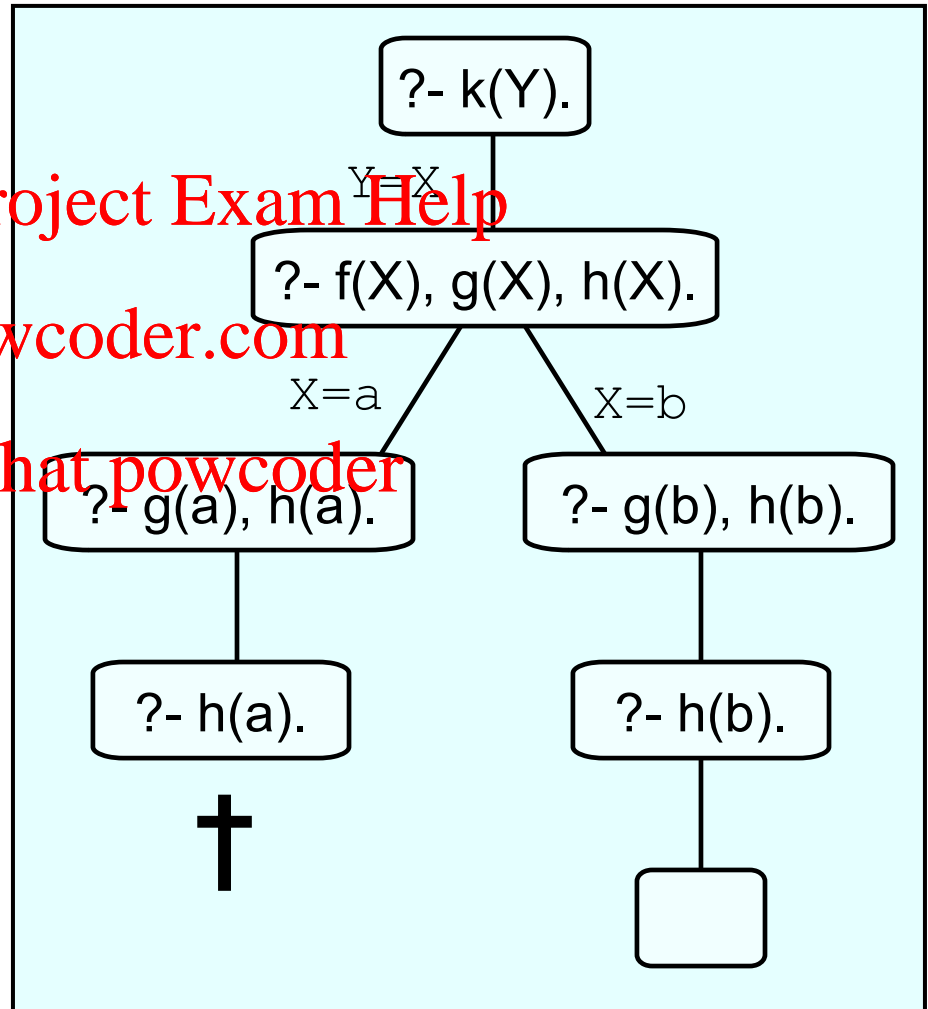
f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).
Y=b;
no
?-

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
?- jealous(X,Y).
```

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
?- jealous(X,Y).
```

```
?- jealous(X,Y).
```

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
?- jealous(X,Y).
```

```
?- jealous(X,Y).
```

X=A Y=B

```
?- loves(A,C), loves(B,C).
```

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
?- jealous(X,Y).
```

```
?- jealous(X,Y).
```

X=A Y=B

```
?- loves(A,C), loves(B,C).
```

A=vincent

C=mia

```
?- loves(B,mia).
```

Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

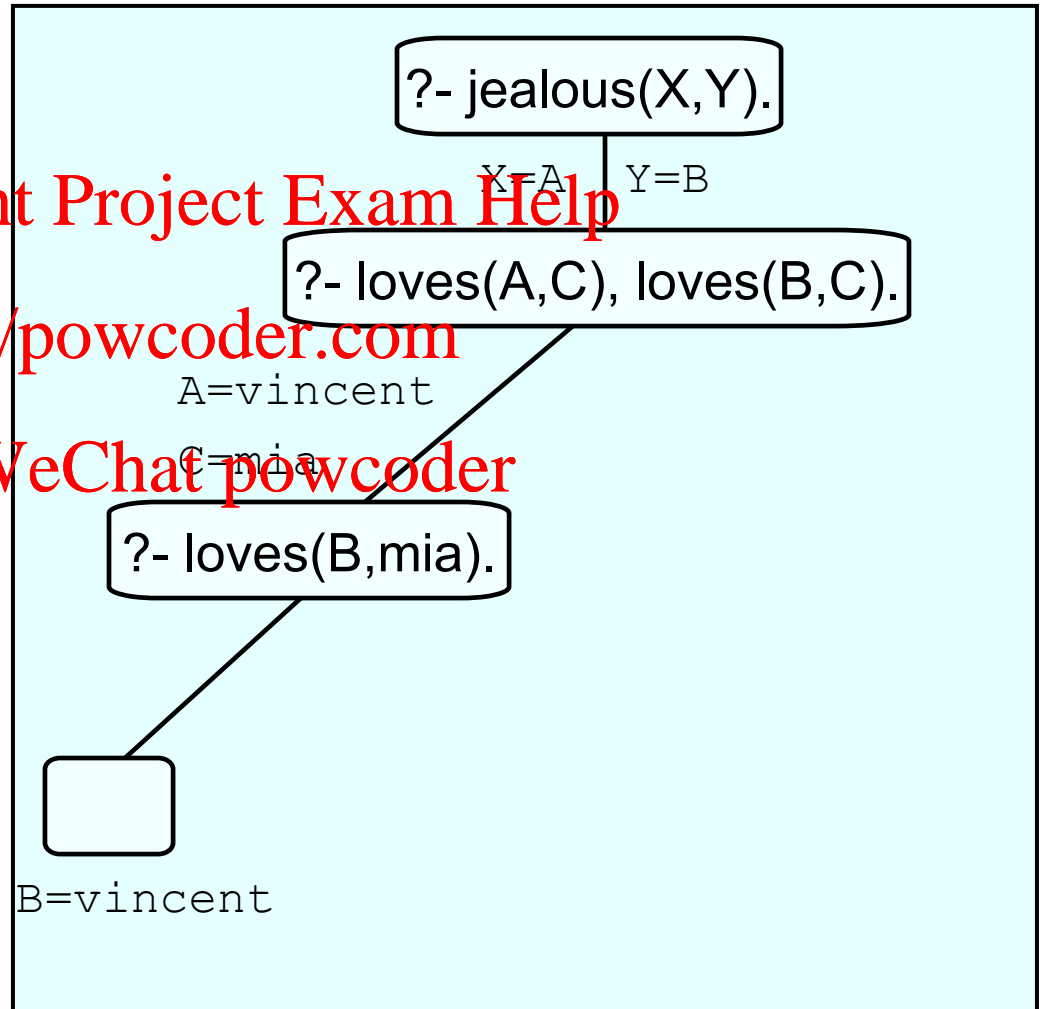
```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
?- jealous(X,Y).  
X=vincent  
Y=vincent
```

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

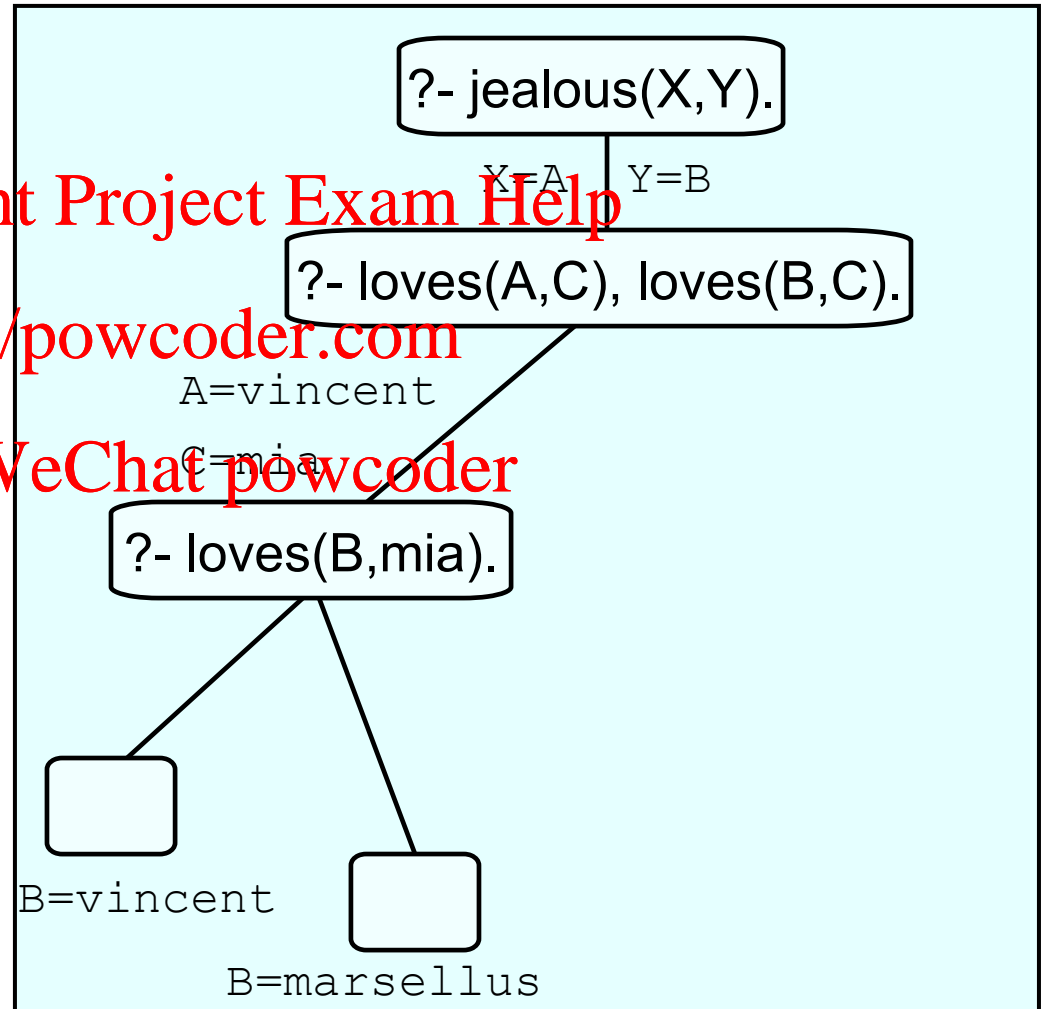
```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
?- jealous(X,Y).  
X=vincent  
Y=vincent;  
X=vincent  
Y=marsellus
```

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

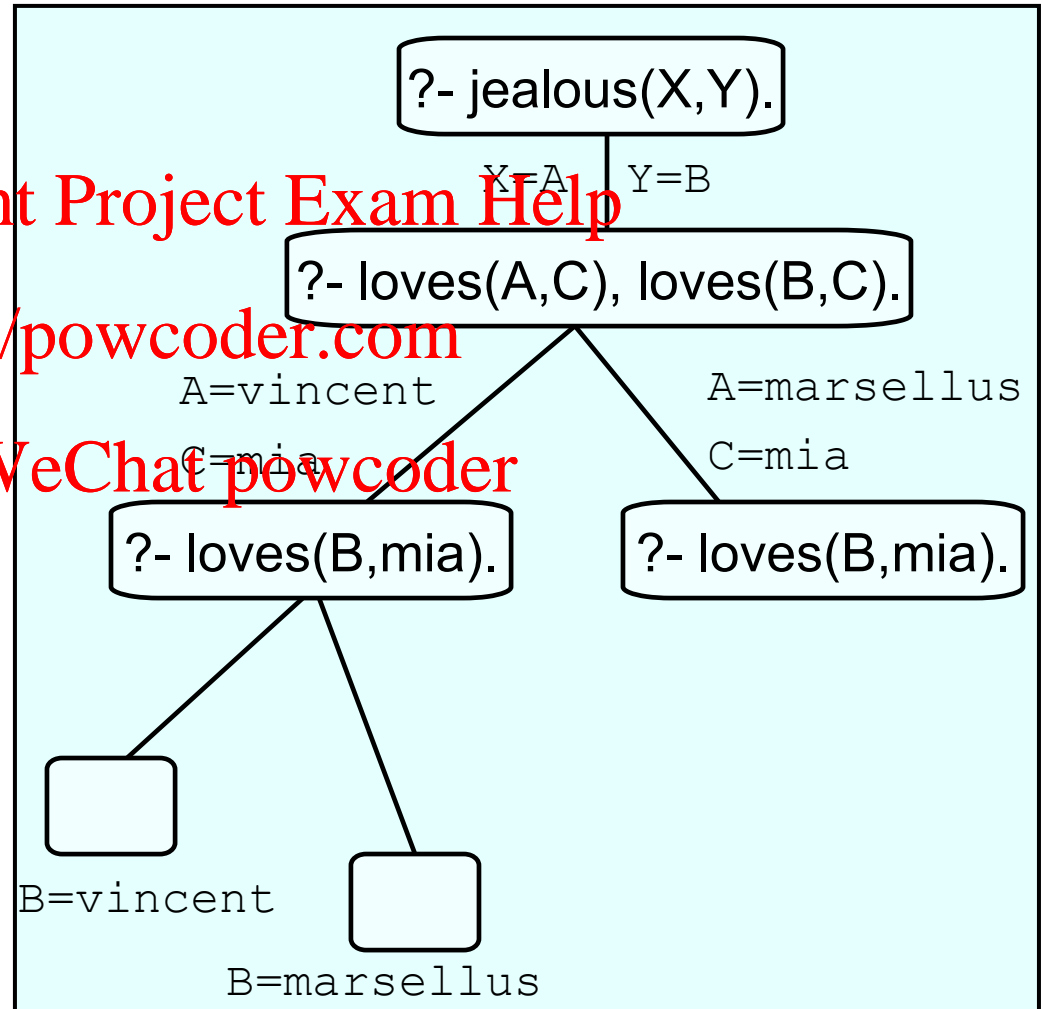
```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
?- jealous(X,Y).  
X=vincent  
Y=vincent;  
X=vincent  
Y=marsellus;
```

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

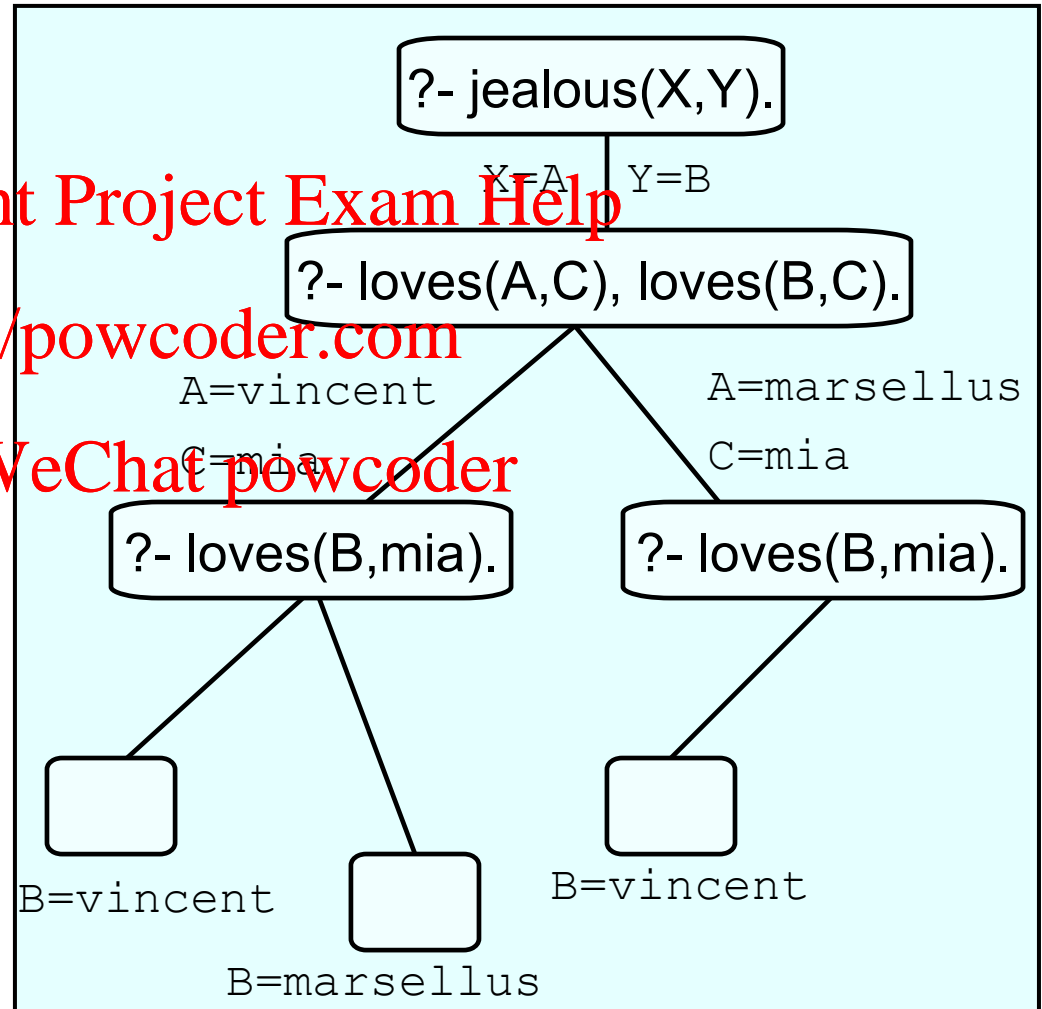
```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
....  
X=vincent  
Y=marsellus;  
X=marsellus  
Y=vincent
```

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

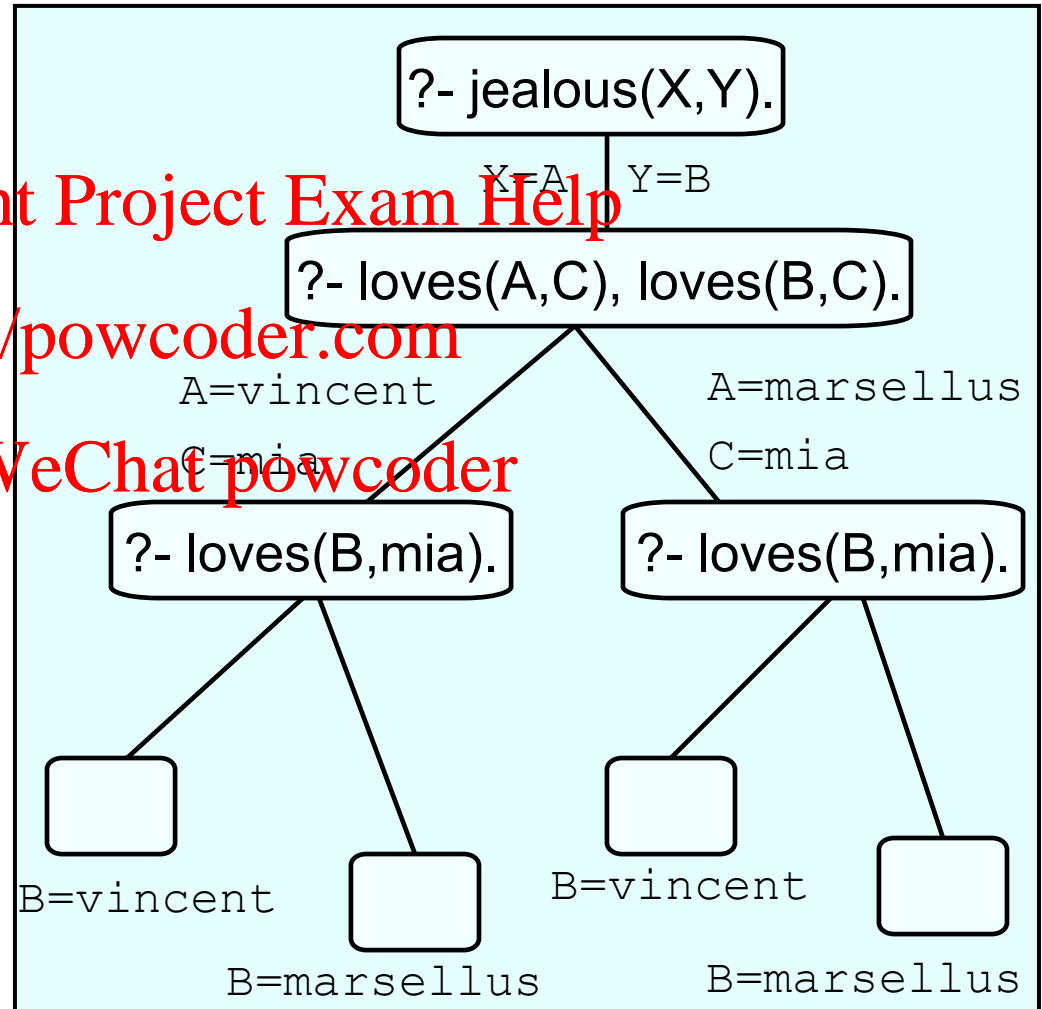
```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
....  
X=marsellus  
Y=vincent;  
X=marsellus  
Y=marsellus
```

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Another example

```
loves(vincent,mia).  
loves(marsellus,mia).
```

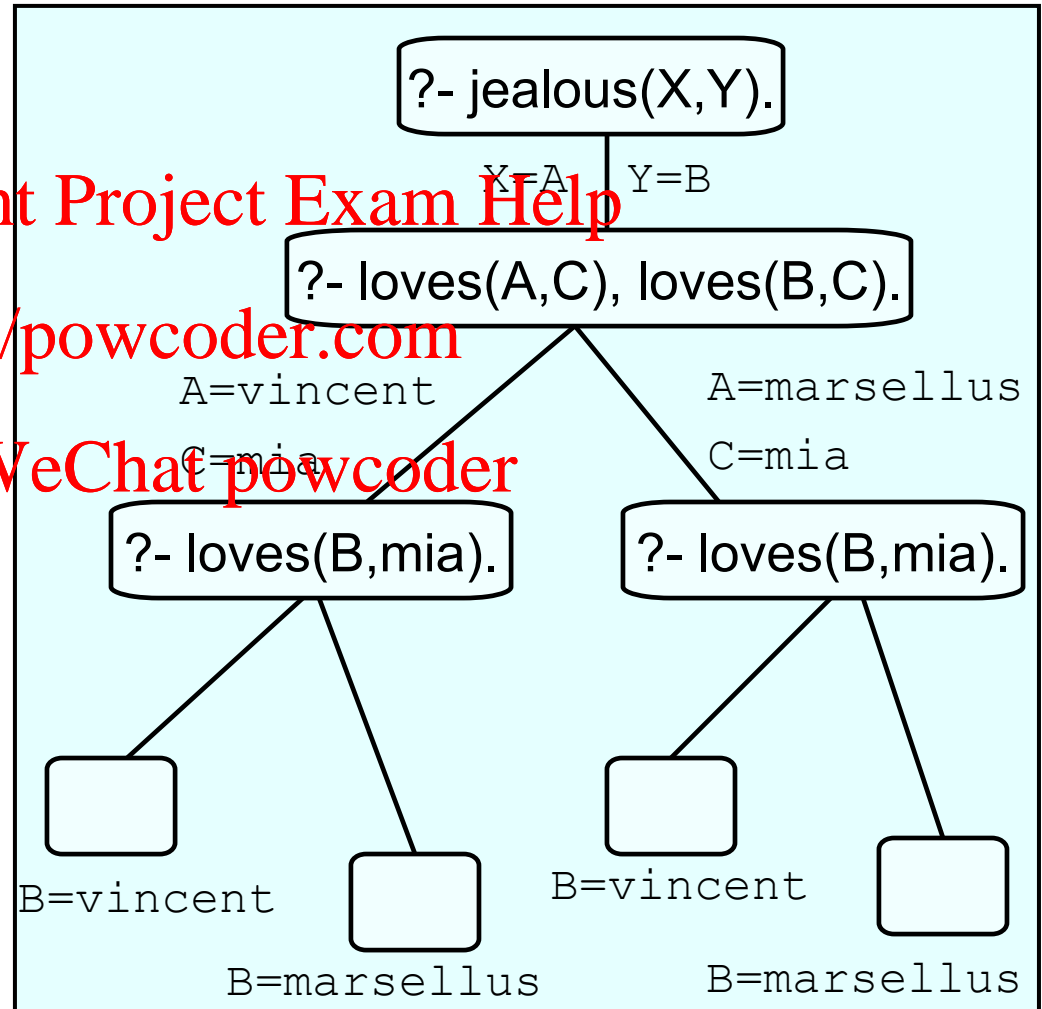
```
jealous(A,B):-  
    loves(A,C),  
    loves(B,C).
```

```
....  
X=marsellus  
Y=vincent;  
X=marsellus  
Y=marsellus;  
no
```

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Exercises

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Summary of this lecture

- In this lecture we have
 - defined unification
 - looked at the difference between standard unification and Prolog unification
 - introduced search trees

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Next lecture

- Discuss **recursion** in Prolog
 - Introduce recursive definitions in Prolog
 - Show that there can be mismatches between the declarative meaning of a Prolog program and its procedural meaning.