Chapter 4

Definelang: A Language with Global Variables

Our goal in this paper is to learn about global definitions and usage, and to contrast them with locally scoped definitions discussed in the previous chapter.

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4.1 Local vs. Global Definitions

So far each variable that we have defined at lap expression (let ((a 3)(b 4)(c 2)) (+ a b c)), variables a, b, and c are defined only during the evalution of (+ a b c) and not outside it. Sometimes it is useful to define a variable and have it available for the entire duration of our interaction with the interpreter. For example, we can define the roman numerals using such a feature.

\$ (define i 1)

We will call this feature a *define declaration*. A define declaration has three parts: the **define** keyword, name that is being defined (here i), and the initial value given to the name (here 1). We can similarly define other roman numerals.

- \$ (define ii 2)
- \$ (define iii 3)
- \$ (define iv 4)
- \$ (**define** v 5)

We can then use these definitions in all of our programs as shown below.

```
$ (+ (* iii iv v v) (* ii iv v) ii)
342
$ (- (* v v v v) (+ i ii iii iv) (* iii v v))
540
$ (+ (* v ii iv) i (* v v iv v))
541
$ (+ (+ v v i) (* v v v v))
641
```

Note that this is different from extending the initial environment of programs in Varlang with predefined values. Those definitions would have effect on each run of the interpreter, whereas names defined by the define form during a particular run of the interpreter would not be automatically

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4.2 Define, define https://powcoder.com

To support the define form, we extend the syntax of Varlang as shown in figure 4.1 to create a new language that we will call *Definelang*.

There are two national danger Five the green of the program changes in this language. A program in Definelang consists of zero or more definitions, represented as DefineDecl* followed by an optional expression, represented as Exp?. We have also added the syntax for define declarations. The syntax of DefineDecl takes an identifier (name being defined) and an expression (value of the name being defined). Here are some additional examples.

```
$ (define R 8.3145) // The gas constant R
$ (define n 2) // 2 moles of gas
$ (define V 0.0224) // Volume of gas 0.0224 m^2
$ (define T 273) // Temperature of gas 273 K
$ (define P (/ (* n R T) V)) // Using Boyles law to compute pressure
$ P //What is the pressure?
202665.93750000003
```

Notice that the expression in a define declaration can make use of previously defined names, but it cannot utilize those that might appear later.

Program	::=	DefineDecl* Exp?	Program
DefineDecl	::=	(define Identifier Exp)	Define
Exp	::=		Expressions
		Number	NumExp
		(+ Exp Exp ⁺)	AddExp
		(- Exp Exp ⁺)	SubExp
		(* Exp Exp ⁺)	MultExp
		(/ Exp Exp ⁺)	DivExp
		Identifier	VarExp
		(let ((Identifier Exp) ⁺) Exp)	LetExp
Number	::=	Digit	Number
		DigitNotZero Digit ⁺	
Digit	::=	[0-9]	Digits
${\tt DigitNotZero}$::=	[1-9]	Non-zero Digits
IdentiAisrsignnetert Project Exam Heltifer Letter			
Letter 1001	5 <u>;</u> ; <u></u> <u>1</u> 1	Ta-za-zs-1 Toject Lixa	Litter
LetterOrDigit	::=	[a-zA-Z0-9\$_]	Letter Or Digit

Figure 1 Cramby pfor the Postnel are Larguage

Each line in the previous example is a separate Definelang program according to the syntax in Igure 11. Hach of the Vpc grant Tefines a single variable, but it is possible to define multiple variables at once, e.g. both Faraday and Rydberg constant¹.

\$ (define F 96454.56) (define R 10973731.6)

The Definelang language also permits defining one or more constants and then computing the value of an expression.

\$ (define R 8.3145) (/ (* 2 R 273) 0.0224) 202665.93750000003

We will now explore the semantics and implementation of this new language feature, and changes in the semantics of programs to add define declarations.

¹For the curious reader, Faraday's constant is the charge on a mole of electrons.

Extending the AST, the visitor, and the formatter

Besides the grammar, we would also need to extend the AST, and the visitor infrastructure to accommodate these language changes. These changes include adding a new AST node DefineDecl, modifying the AST node for Program to also store define declarations, modifying the visitor interface to support new AST node, and finally modifying the formatter to print the new AST node. The reader is encouraged to review these changes in the companion code before proceeding further.

4.3 Semantics and Interpretation of Programs with Define Declarations

A correct Varlang program cannot have any free variables. A Definelang program that the program the interpreter if a Definelang programmer types the following program the interpreter will evaluate the program to a dynamic error.

\$ (/ (* https://powcoder.com No binding found for name: R

On the other hand, if the interaction of the programmer was like the following the same program would bridge We at the value.

\$ (define R 8.3145) unit \$ (/ (* 2 R 273) 0.0224) 202665.93750000003

To understand the difference between these two behaviors, it would help to ask: when both of these programs start running, what was the value of the environment? In Varlang, when a program starts running, no variables have been defined yet. If you would recall from the realization of Varlang, we started evaluating every program in an empty environment. The semantics of Definelang is slightly different — when an interpreter starts running, no variables have been defined yet; when a program starts running all variables that have been declared since the interpreter started running are defined. To a reader familiar with interpreters or similar systems, this distinction will not come as a surprise, but it is important to make a note of it as we develop the realization of Definelang.

Recall from previous chapters that in our interpeter, a single Evaluator object persists through the lifetime of the interpreter. In Definelang, we want definitions to be retained across runs, which can be achieved by making the initial environment an attribute of the Evaluator object. Following implementation changes model that.

```
1 class Evaluator implements Visitor<Value> {
    Env initEnv = new EmptyEnv(); //New for definelang
    Value valueOf(Program p) {
 5
      return (Value) p.accept(this, initEnv);
    public Value visit (Program p, Env env) {
9
      for(DefineDecl d: p.decls())
10
        d.accept(this, initEnv);
                           ient Project Exam Help
11
12
13
14 }
      nttps://powcoder.com
The set of legal values for Varlang was limited to NumVal, however, for
  Defineling this set needs to be extended as shown in figure 4.2 to model
  the semantics that define declarations to not produce any values
```

Figure 4.2: The Set of Legal Values for the Definelang Language

The figure defines a new kind of value UnitVal, for unit values. A UnitVal is like a void type in Java. It allows programming language definitions and implementations to uniformly treat programs and expressions as evaluating to 'a value', which could be a UnitVal when producing other kinds of value is not sensible.

The semantics of define declarations is very similar to the let expressions, except that each definition changes the global initEnv to add a new binding from name to value.

```
public Value visit (DefineDecl d, Env env) { // New for definelang .

String name = d.name();

Exp value_exp = d.value_exp();

Value value = (Value) value_exp.accept(this, env);

initEnv = new ExtendEnv(initEnv, name, value);

return new Value.UnitVal();

}
```

The implementation evaluates the value expression on line 4, creates a new environment by extending the current value of initEnv on line 5. The value of a define declaration is a UnitVal.

Exercise

- A.3.1. [Volume of Sphere] Define a constant pi with the usual value of SS1.241111659 Define Constant Example with Pvalue of 1.33333. Using the definition of pi and fourByThree, compute the volume of a sphere with radius 1.42. Recall that the volume of a sphere ip 133 */powits or redrustration.
 - 4.3.2. [Lazy Definitions] Extend the Definelang programming language from this chapter such that it supports a variation of the define declaration of the define declaration in an expression such as the following, first the value of the expression (/ (* n R T) V) is computed, then the global environment is extended with a mapping from name P to this value.

```
$ (define P (/ (* n R T) V))
```

In a lazy define declaration, the value of the expression (/ (* n R T) V) will be computed when the name P is used. An example appears below.

```
$ (define P (/ (* n R T) V))
$ (define R 8.3145) // The gas constant R
$ (define n 2) // 2 moles of gas
$ (define V 0.0224) // Volume of gas 0.0224 m^2
$ (define T 273) // Temperature of gas 273 K
$ P //What is the pressure?
202665.93750000003
```

Notice that the interaction above would not have worked with the regular define declaration because the names n, R, T, and V would not be defined. In the lazy define declaration, since the value of the expression (/ (* n R T) V) is computed when P is looked up the interaction works.

4.3.3. [Macros] Extend the Definelang programming language from this chapter such that it supports declaring macros and macro expansion.

A macro definition has the following form.

\$ (define (macro_name argument1, argument2, ...) expression)

Example:

- (define (square x) (* x x))
- Square: 2) // This is expanded to (* 2 2) Exam Help
- \$ (define (pressure n R T V) (/ (* n R T) V))
- \$ (pressure 21843145 273/p334wcoder.com

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Template Metaprogramming

The macros described in the exercise were a simplified form of a more general idea known as template metaprogramming. Template metaprogramming, broadly, refers to a collection of technique that consume user facing syntax to generate more source code at compile-time. Template metaprogramming is utilized by a number of programming languages most notably C++, but also in Haskell and Curl.

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Chapter 5

Functions A Language with

Our goal in this chapter is to learn about functions in full detail. We will especially focus on first-class functions, lambda abstraction, closures, higher-order functions, currying, and on functional data structures. We will also learn about https://pasawws.ou/fileson

5.1 Functodds Westrhatopowcoder

We have already discussed variables, the most elementary abstraction mechanism in computer programming languages, in previous chapters. A variable name is a proxy for a piece of computation. For example, the variables **x** and **y** below stand for the definitions on the right.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
 $y = \frac{-b' \pm \sqrt{b'^2 - 4a'c'}}{2a'}$

which allows us to write x * (y - x) instead of the following more complex form.

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} * (\frac{-b' \pm \sqrt{b'^2 - 4a'c'}}{2a'} - \frac{-b \pm \sqrt{b^2 - 4ac}}{2a})$$

We can think of these variables as an opaque, fixed abstraction, once we define them we cannot customize their functionalities. For some abstractions it might be desirable to alter some portion of its functionality. For example, for variable definitions x and y above it may be sensible to change values of a, b, and c and get a different instantiation of the abstraction. Functions, procedures, and methods in computer programming languages provide such an abstraction. This ability to instantiate an abstraction by assigning concrete values in place of formal parameters is known as parametrization.

There are many variations of programming language features that can be used for parameterization of a computation. Each such feature is a variation of two elementary concepts: the ability to define a procedure, and the ability to call a procedure. In this chapter, we first focus on these concepts and then study some variations. We will gradually define a programming language with these features that we will call *Functang*.

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We will start by studying two features: lambda abstraction, and call. Think of a lambda abstraction as a tool for defining anonymous function. Let us start with simple examples of such feature. For example, the listing below defines an anonymous function that takes a single parameter **x** and the value of the function is **x**. It may be useful for you to try out these examples using the interpreter for the flatter lat **DOWCOGET**

```
lambda //Lambda special function for defining functions
(x) //List of formal parameter names of the function
x //Body of the function
```

If you are familiar with the notion of procedure or methods in ALGOL family of languages like C, C++, Java, C#, etc..., you should notice three key differences in syntax and one key difference in semantics. Key differences in syntax are:

- 1. We are not specifying the name of the function.
- 2. The formal parameter name is neither preceded nor followed by the type of the formal parameter.

3. We don't have to write an explicit "return" statement to specify the value returned by the function. In the function definition above, the value of the formal parameter \mathbf{x} is the return value of the function.

In ALGOL family of languages as well as in lower-level languages like assembly language, procedures and methods are thought of as a subsection of the code section, procedure/method names are thought of as a proxy for the location of that subsection in the code section, and procedure/method call as a jump to that location after adjusting the environment. Unlike this mental model, it is perhaps best to think of a lambda abstraction as a generator of runtime values that represent functions. A lambda abstraction can be used to create many such function values, and each of these function values have a different identity. Each such function value can be used multiple times.

The Allowing listing slave fan There in a ympus Live tion that the psingle parameters and the value of the function is x + 1.

```
lambda
(x)
(+ x 1)

//Body of the function
```

The listing belows defines an anonymous function that takes two parameters x, y and the value of the function is x + y.

```
(lambda (x y) (+ x y))
```

We can call an anonymous function also. Here, is an example of calling the identity function.

The value of this program is 1. Notice the prefix notation for function calls. The operator here is the function (lambda (x) x). Here, is another example of calling the addition function.

```
( //Begin function call syntax (lambda (x) (+ x 1)) //Operator: function being called
```

```
//Operands: list of actual parameters
//End function call syntax
```

The value of this program is 2. The operator here is the function (lambda (x) (+ x 1)). Here, is a third example of calling the function that adds two numbers. The value of this program is 2.

If we desire, we can also give these lambda abstractions lexically scoped name using the let expression. For example, we can give the name identity to the lambda abstraction that we defined previously.

```
Assignment x) Project / Examulatelp (identity 1)
```

We data so see the first with the define declaration.

```
$ (define identity (lambda (x) x))
$ (identity dd WeChat powcoder
```

As is usual, functions can be defined in terms of other helper functions.

```
$ (define square (lambda (x) (* x x)))
$ (square 1.2)
1.44
$ (define cube (lambda (x) (* (square x) x)))
$ (cube 1.2)
1.728
```

Exercise

5.2.1. [Area] Using the define declaration, define a constant pi with the usual value of 3.14159265359. Use the definition of pi to define a function area of a circle that takes a radius and computes the area using the standard formula pi * radius * radius.

5.2.2. [sumsquares] Define a function sumsquares that takes two integers as a parameter and computes the sum of square of numbers from the first number to the second number.

```
$ (sumsquares 0 0)
0
$ (sumsquares 1 2)
5
$ (sumsquares 3 5)
50
```

5.2.3. [sumseries] Define a function sumseries that takes a number n as argument and computes the series below. Take the value of (sumseries 0) to be 0.

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5.3 Functions for Pairs and Lists

Most programming languages provide some built-in functions, i.e. functions that programmers do not have to define from scratch and can assume to be available. In Funclang, we have several such built-in functions, mostly related to list manipulation. Funclang programmers have access to list, car, cdr, cons, and null? built-in functions. These functions car, cdr, cons, and null? operate on both pairs and lists in Funclang.

A pair in Funclang is a 2-tuple written as (fst.snd). A list in Funclang is a pair, where the second element is a list. There is a special list, empty

list, which is not a pair. Not all pairs are lists. Each list except for the empty list is a pair.

The function list is a constructor for list and it takes zero or more values as arguments, and produces a list containing these values. The function car takes a single argument, a pair or a list, and produces the first element of that pair or list. The function cdr also takes a single argument, a pair or a list, and produces the second element of that pair or list. The function cons takes two values as arguments. If the second value is a list, it produces a new list with the first value appended to the front of the second value list. Otherwise, it produces a pair of two argument values. The function null? takes a single argument and evaluates to #t if that argument is an empty list. Exercises in this section will help you become more familiar with the semantics of these functions.

Using these basic functions, other functions over lists can also be defined.

For example, the current of the accument list.

The length function is an excellent first example of a recursive function over list. A recursive function's definition should mirror the definition of the input data types. For example, a list can be thought of as follows.

```
List := (list) \mid (cons \ val \ List), \ where \ val \in Value
```

The definition says that a list is either an empty list, or a pair constructed by joining an element and another list. Notice that the function length is structured just like the definition of list into two cases. First case handles empty lists. Second case handles non-empty list.

The append function below combines two lists.

```
(define append
(lambda (lst1 lst2)

(if (null? lst1) lst2

(cons (car lst1) (append (cdr lst1) lst2))

) https://powcoder.com
)
```

Notice that for Applied the Continuous structure should have four cases.

- 1. 1st1 is empty, 1st2 is empty.
- 2. lst1 is empty, lst2 is not empty.
- 3. 1st1 is not empty, 1st2 is empty.
- 4. 1st1 is not empty, 1st2 is not empty.

On closer observation, we realize that the value of the function append in the first and second case will be the same, so to optimize function definition we merge these two cases. Thus, we arrive at a suggested recursive function structure with three cases. In summary, when writing recursive functions that process data types such as lists, the structure of the data type provides useful hint for creating the structure of the function.

Exercise

- 5.3.1. Experiment with built-in functions for lists.
 - 1. Use (list) to create an empty list,
 - 2. Use (list 342) to create a list with a single element 342.
 - 3. Use (car (list 342)) to get the first element of the previously defined list.
 - 4. Use (cdr (list 342)) to get the rest of the elements of the previously defined list.
 - 5. Use (null? (list)) to check if the list created in part 1 is an empty list.
 - 6. Use (cons 541 (list 342)) to append an element at the beginning

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- 7. Use (cadr (list 541 342)) to get second element of the list.
- 10. Use function append to concatenate a list with a single element A30 with a wile list with a lingle Weber 41CT
- 5.3.2. [Sum of Even Numbers] Write a function, sumeven, that takes a list of numbers and returns the summation of the even numbers in this list. For example

```
$ (sumeven (list 1 1 1 1 1))
0
$ (sumeven (list 1 1 1 1 2))
2
```

5.3.3. [Frequency] Write a function, frequency, which takes a list, 1st, and an element, elem, and returns the frequency of that element in that list. For example:

```
$ (frequency (list) 5)
0
$ (frequency (list #t "hello") 5)
```

```
0
$(frequency (list #t 5 "hello") 5)
1
$(frequency (list #t 5 "hello" 5) 5)
2
```

5.3.4. [Reverse] Write a function, reverse, which takes a list, 1st and returns the reverse of that list. For example:

```
$(reverse (list))
()
$(reverse (list 3))
(3)
$(reverse (list 3 4))
(43)
$(reverse interpretation Project Exam Help
(2 4 3)
```

5.3.5. [Sum of Thips recupio When Got a list of numbers, and computes the sum of 2 to the power of each element in the list.

The following in critical equilibrates political er:

```
$ (sumPower (list))
0
$ (sumPower (list 0))
1
$ (sumPower (list 1))
2
$ (sumPower (list 3))
8
$ (sumPower (list 1 3))
10
```

5.3.6. [Get books] Write a function, getbooks that takes in a list of lists with author/book string pairs and returns a single list of only the books. Assume the author is the first element and the book is the second

```
$ (get-books (list "C. S. Lewis" "The Last Battle")

( list "Charles Dickens" "A Christmas Carol")

( list "Arthur C. Clarke" "Rama")))

("The Last Battle" "A Christmas Carol" "Rama")
```

5.3.7. [Triangle] Write a function, triangle, which takes a number and produces a list each element of which is a list of symbols.

When triangle is called with a non-negative integer, n, it returns a list containing n number of lists. The first inner list has n elements, the second inner list has n-1 element, and so on until you reach the top with only one element list, which forms the shape of a triangle. Each of the inner lists contain only the numbers 0 and 1 and they alternate across lists. The result always has the 0 as the first element of the first inner list, if any

ASSIGNMENT examples Cave for attn the Lepupto show the result more clearly, but your output will not look the same; it is sufficient to just get the outputs that are equal to those shown. Spares in Seclister was Condiscaving on poses and you are not required to print them.

\$ (triangle 0) Add WeChat powcoder

```
$ (triangle 1)
((0))
```

\$ (triangle 2) ((0 1) (1))

\$ (triangle 3) ((0 1 0) (1 0) (0))

\$ (triangle 4) ((0 1 0 1) (1 0 1)

```
(0 1)

(1))

$ (triangle 5)

((0 1 0 1 0)

(1 0 1 0)

(0 1 0)

(1 0)

(0))

$ (triangle 6)

((0 1 0 1 0 1)

(1 0 1 0 1)

(0 1 0 1)

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(1))
```

5.3.8. [Board] White Land County Coun

When boar Ascalled What Connective Ottow, C.O cath is a list containing n lists each of which have n elements. These lists form the shape of a square board. Each of the inner lists contain only numbers 0 and 1 and they alternate across lists. The result always has 0 as the first element of the first inner list, if any.

The following examples, shows a formatted output of the board, but your output does not need look the same regarding spaces. For your output it is sufficient to just produce the list. Spaces in the lists are just for displaying purposes and you are not required to print them.

```
$ (board 0)
()
$ (board 1)
((0))
$ (board 2)
```

```
((0\ 1)
       (1\ 0))
       $ (board 3)
       ((0\ 1\ 0)
        (1 \ 0 \ 1)
        (0\ 1\ 0))
       $ (board 4)
       ((0\ 1\ 0\ 1)
        (1\ 0\ 1\ 0)
        (0\ 1\ 0\ 1)
        (1 \ 0 \ 1 \ 0))
Assignment Project Exam Help
        (1 \ 0 \ 1 \ 0 \ 1)
        https://powcoder.com
        (0\ 1\ 0\ 1\ 0))
       $ And WeChat powcoder
       ((0\ 1\ 0\ 1\ 0\ 1)
        (1\ 0\ 1\ 0\ 1\ 0)
        (0\ 1\ 0\ 1\ 0\ 1)
        (1\ 0\ 1\ 0\ 1\ 0)
        (0\ 1\ 0\ 1\ 0\ 1)
        (1\ 0\ 1\ 0\ 1\ 0))
```

5.4 Higher-order Functions

A higher-order function is a function that accepts a function as argument or returns a function as value. In Funciang we can define higher-order functions. For example, here is a function that returns (lambda (x) c), which is also a function.

```
(lambda (c) //Lambda abstraction with a single argument
```

```
(lambda (x) c)
                   //Result of running this lambda expression
   If we call this function with argument 1 as follows:
                                //Function call
  (lambda (c)(lambda (x) c))
                                //Operator
                                //Operand
   the result would be (lambda (x) 1). If we call this function with ar-
gument 2 as follows:
                                 //Function call
 (lambda (c) (lambda (x) c)) //Operator
 2
                                //Operand
(lambda (x) c)) as a constant function generator.
               https://powcoder.com
(define
 constgen
 (lambda (c) (lambda (x) c))
   We can also define functions that take other functions as parameter. For
example, the listing below defines a function that takes a function f and
applies it to 1.
(define
 applytoone
 (lambda (f) (f 1))
   To try out this function, we can define another function.
(define add3
 (lambda (x) (+ x 3))
   We can then use add3 as an argument to applytoone.
$ (applytoone add3)
```

We can also create a function on the fly and give it as an argument to applytoone.

```
$ (applytoone (lambda (x) x))
1
$ (applytoone (constgen 342))
342
```

The second call to function applytoone is specially noteworthy. It makes use of the previous higher-order function constgen to create a function that when called returns 342, and calls applytoone with this function as argument.

Higher-order functions can be particularly useful for defining reusable algorithmic structures. For example, the listing below shows a higher-order function that accepts an operation and a <u>list</u> and applies the operation on

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```
(define map
(lambda (op lst)
    (if https://ipowcoder.com
         (cons (op (car lst)) (map op (cdr lst)))

)
Add WeChat powcoder
```

Here are some examples of using this function.

```
$ (define num1to10 (list 1 2 3 4 5 6 7 8 9 10))
$ (define identity (lambda (x) x))
$ (map identity num1to10)
(1 2 3 4 5 6 7 8 9 10)
$ (define square (lambda (x) (* x x)))
$ (map square num1to10)
(1 4 9 16 25 36 49 64 81 100)
```

Exercise

5.4.1. Define a function filter with the signature.

```
(define filter (lambda (test_op lst) ...))
```

The function takes two inputs, an operator test_op that should be a single argument function that returns a boolean, and lst that should be a list of elements. The function outputs a list containing all the elements of "lst" for which the test_op function returned #t.

```
$ (define gt5? (lambda (x) (if (> x 5) #t #f)))
$ ( filter gt5? (list ))
()
$ ( filter gt5? (list 1))
()
$ ( filter gt5? (list 1 6))
(6)
$ ( filter gt5? (list 1 6 2 7))
(6 7)
$ ( filter •gt5? (list 1 6 2 7 5 9))
(6 A SSIGNMENT Project Exam Help
```

5.4.2. Define a function foldl (fold left) with three parameters op, zero_element and lst. The parameter op itself is a two argument function, zero_element is the zero element of the operator function, e.g. 0 for plus function or 1 for multiply function, and lst is a list of elements. (plus function takes two parameters and adds them, multiply function takes two parameters and adds them) nat powcoder

The function successively applies the op function to each element of the list and the result of previous op function (where no such results exists the zero element is used). The following interaction log illustrates fold! function

```
$ (define plus (lambda (x y) (+ x y)))
$ (foldl plus 0 (list))
0
$ (foldl plus 0 (list 1))
1
$ (foldl plus 0 (list 1 2))
3
$ (foldl plus 0 (list 1 2 3))
6
$ (foldl plus 0 (list 1 2 3 4))
10
```

5.4.3. Define a function foldr (fold right) with three parameters op, zero_element and lst. The parameter op itself is a two argument function, zero_element is the zero element of the operator function, e.g. 0 for '+' operator or 1 for multiply operator, and lst is a list of elements. (plus function takes two parameters and adds them, multiply function takes two parameters and multiplies them.)

The function successively applies the op function to each element of the list and the result of previous op function (where no such results exists the zero element is used). The following interaction log illustrates foldr function

```
$ (define minus (lambda (x y) (- x y)))
$ (foldr minus 0 (list))
```

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```
$ (foldr minus 0 (list 1 2 3 4))

$ \begin{align*} -2 & \powsell &
```

- 5.4.4. [ACP] Greatest common divisor (GCP) of two numbers a and b is defined as follows. If a > b then (gcd a b) is gcd of a b and b. Else if a < b then (gcd a b) is gcd of a and b a. Otherwise, it is a.
 - 1. Define a function gcd that computes greatest common divisor according the definition above.

The following interaction log illustrates the function:

```
$ (gcd 4 2)
2
$ (gcd 12 15)
3
```

2. Use the function gcd to define gcds that takes two list of numbers and produces a third list that contains the list of gcd of corresponding elements from the first list and the second list.

The following interaction log illustrates the function:

```
$(gcds (list) (list))

()

$ (gcds (list 4) (list 2))
(2)

$ (gcds (list 4 12) (list 2 15))
(2 3)
```

5.5 Functional Data Structures

Our ability is light installing that offects a pix an empirical is essential to creating meaningful software systems, but we also need to be able to represent data structures. Fortunately, first-class functions of Funciang can ser a pin surpose outly colder. Com

To illustrate, imagine that we want to create a data type that holds a pair of values. In order to define the data type, from the perspective of the client of the data type it would be sufficient to provide definition for all operations that can be applied to that data type: a constructor for creating pairs, an observer for getting the first element of the pair, and another observer for getting the second element of the pair. We can define a constructor operation that can be used to create values of that data type as follows.

```
(define pair
(lambda (fst snd)
(lambda (op)
(if op fst snd)
)
```

We can then use this operator to create a new pair value.

```
$ (pair 3 4)
(lambda ( op ) (if op fst snd))
```

Here, pair is a higher-order function. It returns a function value that takes a single parameter op and based on the value of op evaluates to fst or snd. We can also store this pair to use later.

```
$ (define apair (pair 3 4))
```

An important property to re-emphasize here is that apair is a function value. This function can be called by providing a value for the parameter op, which will then run its body (if op fst snd). The body of the function has two variables fst and snd. So in addition to the code, the function value apair also stores mappings from fst to 3 and snd to 4.

Now, we can define observer operations first and second.

```
$ (define first (lambda (p) (p #t)))
$ (define second (lambda (p) (p #f)))
$ ( first apair)

A SS1gnment Project Exam Help
$ (second apair)
```

The **hitchin Sirst and sevent a superthat their argument** p is a function. We can implement runtime checks, but for simplicity let us avoid them at the moment. These functions then call p with argument #t and #f respectively. Relatition before that when a function value created by the constructor pair is called with argument #t and #f it returns the value of fst or snd.

Exercise

5.5.1. [Procedural representation of records] Define a function, record, which takes a list of strings, fields, and a list of values, values, and returns a procedural representation of record. Write a second procedure lookup, which takes a procedural representation of record and a string and and returns the ith element of the list values if i is the index of name in list fields. For example:

```
$ (define roman (record ( list "i" "v" "x") ( list 1 5 10)))
$ (lookup roman "i")
1
$ (lookup roman "v")
```

5.6. CURRYING 95

```
$ (define empty (record (list) (list)))
$ (lookup empty "a")
"error"
$ (define bad (record (list) (list 1 2 3)))
$ (lookup bad "a")
"error"
$ (define bad2 (record (list a b c) (list)))
$ (lookup bad2 "a")
"error"
```

5.5.2. [Procedural representation of tree] Define a procedural representation of binary tree. A binary tree is either a terminal node that contains a value or a non-terminal node containing two children that are both binary trees. Define two constructors leaf and interior for creating terminal ind propagate tree Define at obsever naversection traverses the tree in a depth-first manner, applies op to each value stored in the tree, and applies combine to combine values from root node, left subtree, and right subtree to produce a single value.

(define leaf (lambda (leafval) ...))

(define interior (lambda (rootval lefttree righttree) ...))

(define traverse (lambda (tree cp combine) ...))

5.6 Currying

All functions that we have written are defined using lambda abstractions that could take zero or more arguments. The ability to take zero or more arguments isn't an essential property of a lambda abstracton. In fact in a programming language with support for first-class functions it is possible to model multiple argument lambda abstractions as a combination of single argument lambda abstraction. Take the function plus that we defined previously as follows.

```
(define plus
(lambda (x y)
(+ x y)
)
```

We can easily redefine plus using single argument lambda abstractions as follows.

```
(define plusCurry
(lambda (x)
(lambda (y)
(+ x y)
)
```

This form where a function is defined using only single argument lambda abstraction is called its *curried form*. Since a curried form accepts only a single argument, calling it is slightly different. An example appears below.

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Note that the expression (plusCurry 3) only partially evaluates the function. The value of this expression is a function, which when applied on 4 evaluations in a function when applied on the function of th

Exercise

5.6.1. Food Write a Carriel and of Convict Order bda abstraction that takes length, width, and height of a cuboid, and computes the volume of cuboid by multiplying length, width and height.

Use that function, to compute volume of a cuboid with length equal to 3, width equal to 4 and height equal to 2.

5.6.2. [speed-mph] Define a curried version of the following procedure, call it speed-mph.

```
(define (speed kms kmToMile hours)
  (/ (* kms kmToMile) hours) )
```

Test your code by executing the following.

```
$ //Speed of carA that traveled 150 km in 2 hours in mph
$ (speed 150 0.62 2)
46.5
```

\$ //Speed of carB that traveled 250 miles in 3 hours in mph

\$ (speed 250 0.62 3) 51.66666666664

5.6.3. [speed-miles-per-two-hours] Using your solution from the previous problem, define a procedure,

speedMilesPerTwoHours

which takes a single number (kilometers) as an argument and computes the speed of a car in miles per two hours.

Test your code by executing the following.

- \$ (speedMilesPerTwoHours 50)
- \$ (speedMilesPerTwoHours 120)

In the SS 1919 Page 1 we will use Gold infixed aspects of the semantics of function definitions and calls by building an implementation of Function. As with Varlang, we will build an interpreter as opposed to a compiler. Fortunately, we have the Defineland implementation to work with. So the interpreter discussed in this chapter will build on that.

5.7 Syntax of Land Calmat Contessions

We will first build support for lambda abstractions and calls, and differ discussions about other features such as the list-related functions, if expression, conditional expressions, etc...

Like the grammar for Definelang, in the grammar for Funclang a program consists of zero or more definitions (define declarations) followed by an optional expression (exp)?. We also have two new expressions lambdaexp and callexp. We have used the syntax of these expressions often in previous sections of this chapter. We also need to extend the AST representation to support these two new nodes as shown in figure 5.2.

The AST node for a lambda expression has fields to store the formal parameter names and the body of the lambda expression, whereas the call expression has fields to store the operator expression and zero or more operand expressions.

We would also need to extend the visitor infrastructure to accommodate these language changes. That will include adding new methods to the

```
Program
                     DefineDecl* Exp?
                                                              Program
DefineDecl
                     (define Identifier Exp)
                                                                Define
                ::=
                                                           Expressions
Exp
                ::=
                                                              NumExp
                     Number
                     (+ Exp Exp^+)
                                                              AddExp
                     (- Exp Exp^+)
                                                               SubExp
                     (* Exp Exp^+)
                                                              MultExp
                     (/ Exp Exp^+)
                                                               DivExp
                     Identifier
                                                               VarExp
                     (let ((Identifier Exp)<sup>+</sup>) Exp)
                                                               LetExp
                     (Exp Exp<sup>+</sup>)
                                                             CallExp
                     (lambda (Identifier<sup>+</sup>) Exp)
                                                         LambdaExp
Number
                     Digit
                                                               Number
                     DigitNotZero Digit+
                             iect Exam Help Digits Digits
                     Letter LetterOrDigit*
                                                             Identifier
Identifier
                     [a-zA-Z\$_{-}]
                                                                Letter
Lette https://powcoder.com
                                                         LetterOrDigit
```

Figure 5.1: Grammar for the Funclang Language. Non-terminals that are not defined in this grammar are exactly the same as that in Definelang.

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Visitor interface for CallExp and LambdaExp types. The standard visitors such as the Formatter would need to provide functionality to handle AST nodes of these new types. The reader is encouraged to review these changes in the companion code before proceeding further.

5.8 Value of a Lambda Expression

Functions are a *first-class feature* in Funclang, since values of type functions are treated just like numeric, string, boolean and list values. They can be passed as parameters, returned as values, and stored in environments¹. This enables us to program higher-order functions, and procedural representation of data structure as discussed in previous sections.

 $^{^{1}}$ An expression (let ((identity (lambda (x) x))) ...) stores a 2-tuple: a name identity and a value of type FunVal in the environment

```
1
                  class LambdaExp extends Exp {
   2
                          List < String > _formals;
    3
                         Exp _body;
    4
                         LambdaExp(List<String> formals, Exp body) {
    5
                                  _formals = formals;
   6
                                 \_body = body;
   7
    8
                          List < String > formals() { return _formals; }
                         Exp body() { return _body; }
   9
                         Object accept( Visitor visitor, Env env) {
10
                                 return visitor . visit (this, env);
11
12
13
                 }
                 class Assignment Project Exam Help
15
16
                         Exp _operator;
17
                          List \langle Exp \rangle _operands;
                         CallExp(Exp Porter S List Power and S Li
18
19
20
                                 _operands = operands;
21
                         Exp operator (A Octurn Vp Cor; hat powcoder
22
23
                          List <Exp> operands() { return _operands; }
24
                         Object accept( Visitor visitor, Env env) {
25
                                 return visitor . visit (this, env);
26
27
                 }
```

Figure 5.2: New AST nodes for the Funclang Language.

Since Funclang program and expressions can produce functions as values, it becomes essential to extend the set of legal values to include a new kind of value: FunVal.

From our previous discussion about the lambda expression, recall that a lambda expression evaluates to a function value.

```
Values
Value
         ::=
                                                     Numeric Values
               NumVal
                                                     Function Values
               FunVal
                                                             Num Val
               (NumVal n)
NumVal
         ::=
FunVal
                                                              Fun Val
               (FunVal var_0, ..., var_n e env)
         ::=
               where var_0, \ldots, var_n \in Identifier,
               e \in Exp, env \in Env
```

Figure 5.3: The Set of Legal Values for the Funclang Language

```
VALUE OF LAMBDAEXP

(FunVal var_i, for i = 0...k exp_b env) = v
```

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Here, FunVal is a new kind of value for Funclang. It encapsulates the names of the formal parameter, the body of the lambda expression, and the current printengent / policytics of durval is charm in figure 5.4.

```
class FunVal implements Value {
 2
      private distinge Chat powcoder
 3
 4
      private Exp _body;
 5
      public FunVal(Env env, List < String > formals, Exp body) {
 6
        _{env} = env;
 7
         _{formals} = formals;
 8
        \_body = body;
 9
10
      public Env env() { return _env; }
      public List < String > formals() { return _formals; }
11
      public Exp body() { return _body; }
12
13
    }
```

Figure 5.4: FunVal: A New Kind of Value for Functions

The implementation of the lambda expression case in the interpreter is shown below.

```
Value visit (LambdaExp e, Env env) {
  return new Value.FunVal(env, e.formals(), e.body());
}
```

This implementation exactly models the semantics. It creates a function value that encapsules formal parameter names, function body, and the current environment.

5.9 Value of a Call Expression

Evaluating a call expression has three key steps.

- 1. Evaluate operator. Evaluate the expression whose value will be the function for expression identity's value will be the function value.
- 2. Evaluate of crudes For each expression that is in place of a formal parameter, evaluate it to a value. For example, for the call expression (identity i) the variable expression i's value will be the only operand value.

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- 3. Evaluate function body. This step has three parts.
 - a) Find the expression that is the body of the function value,
 - b) create a suitable environment for that body to evaluate, and
 - c) evaluate the body.

For example, for the call expression (identity i) if the function value is (lambda (x) x), then the body of the function would be x. A suitable environment for running the body of this function would have a binding from formal parameter name x to actual parameter value, 1 for our example call expression. Evaluating that body would result in the value 1.

The value relation below models this intent.

```
VALUE OF CALLEXP  \text{value } \exp_b \ \text{env}_{k+1} = \text{v}  value \exp_b \ \text{env}_{i+1} = 0...k \ \exp_b \ \text{env}_0)   \text{value } \exp_i \ \text{env} = \text{v}_i, \text{for } i = 0...k   \text{env}_{i+1} = (\text{ExtendEnv } \text{var}_i \ \text{v}_i \ \text{env}_i), \text{for } i = 0...k  value (CallExp \exp_i, \text{for } i = 0...k) \text{env} = \text{v}
```

The case for CallExp in the interpreter implements this semantics as shown below. To improve user experience, it also implements some checks. For example, if the result of evaluating the operator is not a function value, e.g. in expression (1 2), the result is a dynamic error. Similarly, if the number of trial parameters do not much the two trials arguments, the call expression results in a dynamic error also.

Dynamic Errors To support dynamic error as a legal value, we redefine the set of legal values in Funclang as shown in figure 5.5. A dynamic error encapsulates a string s e.g. for describing the cause of the error.

There are no expressions that the programmer can use to directly produce dynamic errors with their own custom string. However, programmers can easily produce dynamic errors indirectly, e.g. by using a call expression incorrectly.

Implementation of Call Expression The implementation also mirrors the value relation and the informal semantics of call expressions.

```
Value visit (CallExp e, Env env) {
  //Step 1: Evaluate operator
  Object result = e.operator().accept(this, env);
```

```
Values
Value
                 ::=
                                                             Numeric Values
                      NumVal
                      FunVal
                                                            Function Values
                                                             Dynamic Error
                      DynamicError
NumVal
                      (NumVal n)
                                                                    Num Val
                 ::=
FunVal
                      (FunVal var_0, ..., var_n e env)
                                                                      Fun Val
                 ::=
                      where var_0, \ldots, var_n \in Identifier,
                      e \in Exp, env \in Env
DynamicError
                 ::=
                      (DynamicError s),
                                                              DynamicError
                      where s \in \text{the set of Java strings}
```

Figure 5.5: The set of Legal Values for the Funclang Language with new dynamic error value

```
if (Arsult galance Cate. Hunt 10) 1 ect
  return new Value.DynamicError("Operator not a function");
Value.FunVal operator = (Value.FunVal) result;
List < Exp> details 5. Powcoder.com
//Step 2: Evaluate operands
List <Value> actuals = new ArrayList < Value> (operands.size());
for (Exp exp Apelans) We Lnat now Code 1
  actuals.add((Value)exp.accept(this, env));
//Step 3: Evaluate function body
List < String > formals = operator.formals();
if (formals. size()!=actuals. size())
  return new Value.DynamicError("Argument mismatch in call ");
Env fenv = appendEnv(operator.env(), initEnv);
for (int i = 0; i < formals. size(); i++)
 fenv = new ExtendEnv(fenv, formals.get(i), actuals.get(i));
return (Value) operator.body().accept(this, fenv);
```

In the third step, evaluate function body, an environment for running the function body **fenv** is created by first appending the bindings from function value and the initial environment, and then successively adding mapping from formal parameters to actual parameters. First step makes use of a recursively defined helper function appendEnv below.

```
Env appendEnv(Env fst, Env snd){
   if ( fst .isEmpty())
     return snd;
   ExtendEnv f = (ExtendEnv) fst;
   return new ExtendEnv(appendEnv(f.saved_env(),snd), f.var(),f.val());
}
```

In summary, to support function definition and calls we included a new kind of value, FunVal for encapsulating aspects of a function definition, added support for lambda and call expressions in the read phase, supported new AST nodes to store lambda and call expressions, and changed the evaluator to add semantics for lambda and call expressions. We also added a new kind of value DynamicError for representing error conditions in the

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Exercise

5.9.1. Environment projective Optimize the function call semantics by reducing the size of the environment saved in FunVal so that it only contains mappings from free variables in the function body to their bindings in the corresponding of the contains and the contains and the corresponding of the contains and t

- 5.9.2. [Substitution-based Call Expression] Extend the Funciang programming language from previous question to implement a substitution-based variation of the call expression, say [] expression. Recall that a substitution-based semantics works as follows. The value of [(lambda (x y) (+ x y)) 3 4] is the value of a new expression created from the original function body (+ x y) by replacing x with 3 and y with 4. According to the substitution-based semantics the value of the call expression is the value of (+ 3 4) that is 7.
 - The grammar of this new language feature should be exactly the same as the grammar of the call expression in the Funclang language, except for the syntax [].
 - Implement substitution as a method subst for each AST node such that given a list of variable names, and a list of values the subst method returns a copy of current AST node with each free variable name substituted with corresponding value.

- 5.9.3. [Tracing Lambda Abstractions] Extend the Funclang programming language to implement a tracing lambda expression tlambda that prints "Entering a function" before starting to run the function body and "Exiting a function" after returning.
- 5.9.4. [Dynamic Binding] An alternative to static binding is dynamic binding in which the function body is evaluated in an environment obtained by extending the environment at the function call point (instead of the environment at the function declaration point that is used for static binding).

Extend FungLang with a dynamic call expression that has syntax '('dynamic' expr expr*')'. A dynamic call expression is evaluated using dynamic binding.

The following examples illustrate the difference between dynamic and state of the fine time of the partial part of the control of the control

```
((a 3))
(let https://powcoder.com
((p (lambda (x) (- * a))))
(let
((a 5)) dd WeChat powcoder
)
)
)
```

The value of this program is 0. In the expression above variable a is bound to 3.

Now consider another version of the program that uses dynamic call expression.

```
(let

((a 3))

(let

((p (lambda (x) (- x a))))

(let

((a 5))

(- (p 11) (dynamic p 11))
```

```
)
```

The value of this program is 2. Here variable a is bound to 5.

Consider another program that uses static binding only.

```
(let
	((a 3))
	(let
		((p (lambda (x) (- x a))))
	(let
		((a 5))
		(- a (p 2))
```

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```
The talp of this power derivation bound to 3.

(let

((a 3))

Atdd WeChat powcoder

((p (lambda (x) (- x a))))

(let

((a 5))

(- a (dynamic p 2))

)
```

If the program used dynamic binding, since the variable a will be bound to 5, value of this program will be 8.

5.9.5. [Default parameters] In this question you will explore a semantic variation of function call and return.

A function definition can provide default values for the function's parameters. Extend the Funciang interpreter to support functions with the default value for their last parameters (not all parameters).

The following interaction log illustrates the syntax and semantics for our desired extension:

```
$ (define func (lambda ((v = 342)) v) )
$ (func)
342

$ (func 541)
541

$ (define add (lambda (a (b = 5)) (+ a b)) )
$ (add 8)
13

$ (add 8 4)
1 ASS1gnment Project Exam Help
```

5.9.6. [Implicit parameters] In this question you will explore a semantic variation of interior call and return of the community of the commun

A function can take an implicit parameter. Extend the Funclang language to support function calls that can (optionally) provide an implicit parameter this // Chart pour coder.

The following interaction log illustrates the syntax and semantics of our desired extension:

```
$ (define f (lambda () this))
```

Here, the function f is making use of the implicit parameter 'this' in its body.

```
$ (define obj (list 3 4 2))
$ (obj.f)
(3 4 2)
```

In the function call, obj is being provided as the value of the implict parameter 'this' to be used in the function body f.

Here are some more examples of defining and using such functions.

```
$ (define first (lambda () (car this)))
$ (obj. first )
```

```
3
$ (define second (lambda () (car (cdr this))))
$ (obj.second)
4
```

5.9.7. [Variable argument functions] In this question you will explore a semantic variation of function call and return.

A function can take variable number of parameters. Such functions are known as variages or varidiac function. Extend the Funciang language to support variable argument functions with the following syntax.

```
'(' lambda '( ldentifier ... ')' exp ')'
```

ASSTERMANCES PECILITY OF CITE (dots) XARVIN Imbed Spression with variable number of parameters. Parameters of variadic functions are treated as a list in the body of the function. For example (lambda (x1, 11), (caf/x)) defines an adopymous function with variable parameter x where the body of the function, returns the first parameter of the function.

Variable rimber of a guinents could be passed when calling a variadic function. For example, in the program (Clambia (x ...) (car x)) 8 2 3) the three parameters 8, 2 and 3 are passed to the function. The program returns the first argument in the list of arguments, i.e. it returns 8.

```
$ ( (lambda (x ...) (car x)) 8 2 3)

$ ( (lambda (x ...) (cdr x)) 8 2 3)
(2 3)
$ ( define vardiacFunc (lambda (y ...) (car y)))
$ (vardiacFunc 2)
2
$ (vardiacFunc 2 3 4)
2
$ (vardiacFunc 2 3 4 5)
2
```

5.10 Semantics of Conditional Expressions

We have also added a conditional expression, if and three comparison expressions <, =, and> to the Funclang language to improve expressiveness of the language. The syntax for these extensions is given in figure 5.6.

An if expression is different from if statement in ALGOL-like languages. In Java for example, an if statement can have a condition, a then block of statements and optionally an else block of statements. An if expression in function consists of three expressions: the condition expression, the then expression, and the else expression. All parts are mandatory, and all three of them are expressions.

The comparison expressions are standard, except like other expressions in Funclang are written using the prefix form.

```
Exp
        ssignment Project Exam
         (+ Exp Exp^+)
                                            AddExp
         (- Exp Exp^+)
                                            SubExp
                   s://powcoder.com
         Identifier
                                            VarExp
         (let ((Inlentifie
                                         LambdaExp
         (lambda (Identifier<sup>+</sup>) Exp)
         (if Exp Exp Exp)
                                             IfExp
         (< Exp Exp)
                                          LessExp
         (= Exp Exp)
                                         EqualExp
         (> Exp Exp)
                                       GreaterExp
         #t | #f
                                          BoolExp
```

Figure 5.6: Extended Grammar for the Funclang Language. Non-terminals that are not defined in this grammar are same as that in figure 5.1.

To add these new expressions to the language, we should first decide about the legal values produced by these expressions. Here, we have two options.

1. Encode using NumVal: We could choose to use the domain of NumVal as legal values produced by the comparison expressions and that con-

Value	::=		Values
		NumVal	Numeric Values
		BoolVal	Boolean Values
		FunVal	Function Values
	j	DynamicError	Dynamic Error
NumVal	::=	(NumVal n)	NumVal
BoolVal	::=	(BoolVal true)	BoolVal
		(BoolVal false)	
FunVal	::=	(FunVal var_0, \ldots, var_n e env)	Fun Val
		where $var_0, \ldots, var_n \in Identifier$,	
		$e \in Exp, env \in Env$	
DynamicError	::=	(DynamicError s),	DynamicError
•		where $s \in \text{the set of Java strings}$	

Figure 5.7: The set of Legal Values for the Fundlang Language with new Assignment Project Exam Help

subject by the if expressions. For example, a greater expression (> a b) could produce a statue when a is not greater than b, otherwise it can produce a nonzero value. Similarly, an if expression (if (> a b) ...) could assume that any value of its condition expression (> a b) greater than zero would at taking a value of the otherwise.

2. Introduce new kind of values: We could also choose to introduce a new kind of value to model boolean conditions. A disadvantage of this option is that the language definition and implementation must support an additional feature. A distinct advantage is that the results of a boolean comparison may not be confused with results of arithmetic operations since they would be values of different kind. This has the potential to reduce errors, therefore most modern languages introduce boolean as a new kind of value.

In Funclang, following recent trends, we will also extend the set of legal values produced by Funclang programs to include boolean values. This extended set of values is shown in figure 5.7. A true literal is represented as #t and false literal as #f as shown in figure 5.6. A BoolVal can either be true or false.

With new set of legal values, and syntax, we can give the semantics of the three comparison expressions in Funciang as shown below.

```
Value of GreaterExp value \exp_0 env = (\text{NumVal } n_0) value \exp_1 env = (\text{NumVal } n_1) n_0 > n_1 = b value (GreaterExp \exp_0 \exp_1) env = (\text{BoolVal } b) 

Value of EqualExp value \exp_0 env = (\text{NumVal } n_0) value \exp_1 env = (\text{NumVal } n_1) n_0 == n_1 = b value (EqualExp \exp_0 \exp_1) env = (\text{BoolVal } b)
```

Value of LessExp

Assignificant Profest Exam Help

value (LessExp exp() exp() env = (BoolVal b)

The semantic of first pressing is which the place of the semantic pressing is which the place of the semantic pression is the case when the boolean condition \exp_{cond} evaluates to true, and second rule handles the false case.

VALUE OF IFEXP (BoolVal true) value
$$\exp_{cond}$$
 env = (BoolVal true) value \exp_{then} env = v value (IfExp \exp_{cond} \exp_{then} \exp_{else}) env = v

VALUE OF IFEXP - FALSE value \exp_{cond} env = (BoolVal false) value \exp_{else} env = v value (IfExp \exp_{cond} \exp_{then} \exp_{else}) env = v

The reader is encouraged to review the implementation of these expressions in the companion code before proceedings further.

Exercise

5.10.1. [Logical conjunction and disjunction expressions] Extend the syntax and semantics of the Funclang language to add support for the logical conjunction (and) and logical disjunction (or) expressions. Examples:

5.10.2. [Switch expression] Extend the syntax and semantics of the Funclang language to add support for a switch expression.

Examples:

```
$ (define x 0)

$ (switch (x) (case 0 3) (case 1 4) (case 2 2))

3

$ (define x 1)

$ (switch (x) (case 0 3) (case 1 4) (case 2 2))

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2

$ (switch (x) (case 0 3) (case 1 4) (case 2 (+ 1 1)))

2 (switch (x) (case 0 3) (case 1 4) (case 2 (+ 1 1)))

2 https://powcoder.com
```

5.11 Asechalwie Charaip ouw bister

A Funclang programmers also has access to pair values, list values and related expressions. Recall that a pair in Funclang is a 2-tuple. A list is either an empty list or a pair, where the second element is a list.

Funciang supports several built-in expressions such as list for creating a new list, car for getting the first element of a pair, cdr for getting the second element of a pair, cons for constructing a pair, and null? for checking for empty list. Support for these expressions is orthogonal to function-related features (as we have discussed in section 5.5), but Funciang includes this support to make it easier to write interesting programs.

To support these expressions, we include two additional kinds of value PairVal and Null. This is an inductively-defined value. A ListVal is either an empty list, represented as the type EmptyList, or a pair that consists of a value as the first element and a ListVal as a second element, represented as the type ExtendList. New AST nodes ListExp, CarExp, CdrExp, ConsExp, and NullExp are also added to store these expressions.

```
Exp ::=
                                            Expressions
          Number
                                               NumExp
          (+ Exp Exp^+)
                                                AddExp
          (- Exp Exp^+)
                                                SubExp
          (* Exp Exp<sup>+</sup>)
                                               MultExp
          (/ Exp Exp^+)
                                                DivExp
          Identifier
                                                VarExp
          (let ((Identifier Exp)<sup>+</sup>) Exp)
                                                 LetExp
          (Exp Exp^+)
                                                CallExp
          (lambda (Identifier<sup>+</sup>) Exp)
                                             LambdaExp
          (if Exp Exp Exp)
                                                  IfExp
          (< Exp Exp)
                                                LessExp
          (= Exp Exp)
                                               EqualExp
          (> Exp Exp)
                                             GreaterExp
          signment Project
                                               CdrExp
          (cdr Exp)
          (null? Exp) / powcode for the list Exp
          (list Exp*)
                                               ListExp
```

Figure 5.8: Extended Grammar for the Funciang Language. Non-terminals that are not defined at the property of the Funciang Language.

The semantics of list-related expressions is given in terms of the list values. The value of a ListExp is given by the following relation.

```
value (ListExp \exp_0 \ldots \exp_n) env = (ListVal \operatorname{val}_0 \operatorname{lval}_1)

where \exp_0 \ldots \exp_n \in \operatorname{Exp} \quad \operatorname{env} \in \operatorname{Env}

value \exp_0 \operatorname{env} = \operatorname{val}_0, \ldots, \operatorname{value} \exp_n \operatorname{env} = \operatorname{val}_n

\operatorname{lval}_1 = (\operatorname{ListVal} \operatorname{val}_1 \operatorname{lval}_2), \ldots,

\operatorname{lval}_n = (\operatorname{ListVal} \operatorname{val}_n (\operatorname{EmptyList}))

A corollary of the relation is:

value (ListExp) \operatorname{env} = (\operatorname{EmptyList})
```

Value	::=		Values		
		NumVal	Numeric Values		
		BoolVal	Boolean Values		
	j	FunVal	Function Values		
	j	PairVal	Pair Values		
		NullVal	$Null\ Value$		
		DynamicError	$Dynamic\ Error$		
NumVal	::=	(NumVal n)	Num Val		
BoolVal	::=	(BoolVal true)	BoolVal		
		(BoolVal false)			
FunVal	::=	(FunVal var_0, \ldots, var_n e env)	Fun Val		
		where $var_0, \ldots, var_n \in Identifier$,			
		$e \in Exp, env \in Env$			
PairVal	::=	(PairVal v_0 v_1)	PairVal		
Assignment Project Exam Help Null Val					
Nullvan	::=	- ·	-		
DynamicError	::=	(DynamicError s),	DynamicError		
https://where s \in the set of Java strings					
Figure 5.9: The set of Legal Varues for the Functang Language with new					
pair and null values					

$\underset{\mathrm{The\ value\ of\ a\ CarExp\ is\ given\ by.}}{\mathbf{Add}} \underbrace{\mathbf{WeChat\ powcoder}}_{}$

value (CarExp exp) env = val

where $\exp \in \operatorname{Exp} \quad \operatorname{env} \in \operatorname{Env}$

value exp env = (ListVal val lval) where lval \in ListVal The value of a CdrExp is given by:

value (CdrExp exp) env = lval

 $\texttt{where} \ \texttt{exp} \in \texttt{Exp} \quad \texttt{env} \in \texttt{Env}$

value exp env = (ListVal val lval) where lval \in ListVal The value of a ConsExp is given by:

value (ConsExp exp exp') env = (ListVal val lval)

```
where \exp, \exp' \in \operatorname{Exp} \quad \operatorname{env} \in \operatorname{Env} \quad \operatorname{value} \ \exp \ \operatorname{env} = \operatorname{val} value \exp' \ \operatorname{env} = \operatorname{lval}
```

The value of a NullExp is given by:

```
value (NullExp exp) env = #t if value exp env = (EmptyList)  value \  \, (NullExp \ exp) \ env = \#f \\ \\ if value exp env = (ListVal \ val \ lval') \ where \ lval' \in ListVal \\ \\ where \ exp \in Exp \ env \in Env \\ \\
```

Exercise

- 5.11.1. Pairs and Lists In some programming languages such as Scheme, pairs are the batic vices and lists be colored in town diffpair. To find a pair as a 2-tuple, and redefine the value relations for list, car, cdr, cons, and null? in terms of pair values.
- 5.11.2. [equal? expression] Extend the Functaing language to support a new expression equal? that takes two subexpressions and returns #t if their values are equal and #f_otherwise.

The following ideactive equations to the following ideactive the state of the following ideactive equations of the following equations

```
$(equal? #t #t)
#t
$(equal? #t 1)
#f
$(equal? #t "Hello")
#f
$(equal? (list) (list))
#t
$(equal? (list) (list 1))
#f
$(equal? (list (list 1)) (list (list 0)))
#f
$(equal? (list (list 1)) (list (list 1)))
#t
$(equal? (list (list 1)) (list (list 1)))
#t
$(equal? (+ 2 3) (+ 2 3))
```

```
#t \$(equal? (let ((x 2)) x) (let ((y 2)) y)) #t \$(equal? (let ((x 2)) y) (let ((y 2)) x)) funclang .Env\$Lookup\impliesException: No binding found for name: y
```

5.11.3. [List comprehension] Extend the Funclang programming language to support a new list comprehension expression. A list comprehension is a concise way of representing higher-order functions that operate over list. It should have the following syntax:

```
comp-exp: '[' exp ']' identifier '<-' exp ', ' exp ']'
```

The following interaction log illustrates the list comprehension expression:

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```
$ (define list1 (list 3 4 2)) https://powcoder.com
$ [ (add2 x) | x - list1 , #t] (5 6 4)
$ Add (list) We (hist) at powcoder
()
$ [ (add2 x) | x <- list1 , (> x 2)] (5 6)
```