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- Knowledge and possible worlds:
  - the knowledge relation
  - Profession Sof group Knowledge der.com
- Knowing how to play

  - combining knowledge and strategy
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Bob has a strategy to win...

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Bob has a strategy to win... but does he know which one?

# The main inderlying assumption benificative theory or knowledge in the multi-agent systems (and in game theory) is that we live in one world and this world collects all the relevant facts (for instance, those that are true now, were put in the past and with better interfucion.

However, we are typically not able to fully determine it:

- "is my mom thinking of me now?"
- "was Aed den Wee ristang tomple" WCOder
- "will Berlusconi be president again?"



#### Example (Cristiano Ronaldo)

I'm watching Ontuge of the public WCOCCT I've missed a penalty on Cristiano Ronaldo.

If Ronaldo is all that matters to me, there are two possible worlds:

- A world in which Ronaldo dives
- A world in which Ronaldo does not dive

I cannot say which one of these two worlds I'm living at.



Red is dive, blue is mum, purple is both, black is none.

- Typhaly there Wood on the that down even der
- I might be able to distinguish some of their combination



Red is dive, blue is mum, purple is both, black is none.

#### Definition (Flat) WeChat powcoder

Call any  $E \subseteq W$  a **fact**, i.e., a fact is a subset of the possible worlds.

Name two facts in the example. What can you say about what I know?

Let us start with one agent, i, and their knowledge relation:

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Intuitively  $(w_1, w_2) \in \sim_i$  means that agent i cannot distinguish between

worlds  $w_1$  and  $w_2$ . So if i lives the world rit paintle provided the  $w_2$ . We call this relation the indistinguishability relation.

### Assignment Project Exam Help Again: $(w_1, w_2) \in \sim_i$ means i cannot distinguish between $w_1$ and $w_2$ .

What are the intuitive properties of the indistinguishability relation?

Is it reflexive?

Reflexivity: for all  $w \in W$ ,  $(w, w) \in \sim_i$ Does this made case where the power of the power o

### Assignment Project Exam Help Again: $(w_1, w_2) \in \sim_i$ means i cannot distinguish between $w_1$ and $w_2$ .

What are the intuitive properties of the indistinguishability relation?

Is it symmetric?

Symmetry: for all  $w_1, w_2 \in W$  IF  $(w_1, w_2) \in \sim_i$  THEN  $(w_2, w_1) \in \sim_i$  Does this material see the condition of the property of the pr

### Assignment Project Exam Help Again: $(w_1, w_2) \in \sim_i$ means i cannot distinguish between $w_1$ and $w_2$ .

What are the intuitive properties of the indistinguishability relation? https://powcoder.com

Is it transitive?

**Transitivity**: for all  $w_1, w_2, w_3 \in W$ , IF  $(w_1, w_2) \in \sim_i$  and  $(w_2, w_3) \in \sim_i$ 

THEN (WAWA WARDOWN Chat powcoder Does this make sense to you? Chat powcoder

### Assignment Project Exam Help Again: $(\mathbf{w}_1, \mathbf{w}_2) \in \sim_i$ means i cannot jistinguish between $w_1$ and $w_2$ .

What are the intuitive properties of the indistinguishability relation? <a href="https://powcoder.com">https://powcoder.com</a>

Is it serial?

**Seriality**: for all  $w_1 \in W$ , there exists  $w_2 \in W$  such that  $(w_1, w_2) \in \sim_i$ .

Does this Address Wee Chat powcoder

Can you possibly accept seriality without accepting the previous properties?

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There is no ultimate model of knowledge, it depends on what *kind* of knowledge we want to capture.

For the timelten Sye/are progression Classic ico-chivalence relation over the set of all states: reflexive, transitive, symmetric.

It is therefore a partition of the set of all states

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Red is dive, blue is mum, purple is both, black is none.

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I'm going add pactly represent that elapower croixed earcs between indistinguishable worlds, omitting reflexive and transitive links.

Notice how this visually partitions the set of all worlds.

Red is dive, blue is mum, purple is both, black is none.

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Now knowledge...

I know that omething is rue flated only the visit of true at all the worlds that I cannot distinguish from the one I'm at.

Red is dive, blue is mum, purple is both, black is none.

We say that i knows fact E at w whenever  $\sim_i [w] \subseteq E$ We denote the whole V the denote V the denote

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What does the agent know?

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What does the agent know?

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What does the agent know?

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Now let us populate the world with other agents, each with their in with new shaking relation world. Notice the relations don't need to be related in any way.

What do these agents know?

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Knowledge

- Does Bob know Ann knows red?
- Does Bob know Ann does not know Bob knows red?
- Does Bob know Bob knows Ann does not know Bob knows red?

Agent-based Systems

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We can talk about the knowledge of many agents.
But we can to take a control of the knowledge of many agents.

But we can talk about the knowledge of many agents.

What does this mean? Any intuitions?



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- What everyone knows already?
   Practitude minimization? nat powcoder
- Or joint observation?

As always, we need to make choices and restrict our study to some interesting forms of group knowledge.



### Assignment Project Exam Help Let N be the set of agents and W the set of worlds.

Let E be a fact.

#### Definition (Central Knowledge)

It is general knowledge that E at w if everyone knows E at w.

General knowledge is what everyone knows. For example and knows EGI Bhahw DOWCOCET

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Tell me two facts that are general knowledge at  $w_3$ . Add WeChat powcoder

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Tell me two facts that are general knowledge at  $w_3$ . At w Add WeChat powcoder

### Assignment Project Exam Help Let N be the set of agents and W the set of worlds.

Let E be a fact.

is the set of worlds where everyone knows E.

Notice: A Green Matter Diator Ontw. Coder

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Tell me one fact that is general knowledge everywhere.

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Tell me one fact that is general knowledge everywhere.

Can it tellar can of one men with a move country of the can of th

#### Definition (Distributed Knowledge)

We say that it is **distributed knowledge** that Eat wifevery agent knew E by intersecting their indistinguishability relation.

Distributed knowledge is the implicit knowledge the agents have, what they would communicate no ther words, what they would know as a group. WCOder

For example: if Ann cannot distinguish  $w_1$  from  $w_2$  and Bob cannot distinguish  $w_2$  from  $w_3$  then, talking, they would know they are at  $w_2$ .

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Tell me one fact that is distributed knowledge at  $w_2$ . Tell prepared at that is distributed knowledge at  $w_2$ .

Let  ${\cal N}$  be the set of agents and  ${\cal W}$  the set of worlds.

Let *E* be a fact.

is the set Awald where it is distributed knowledge, that the control of the contr

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Tell me one fact that is distributed knowledge everywhere.

Tell me one fact that is distributed knowledge everywhere.

Tell me one fact that is distributed knowledge everywhere.



#### Common Knowledge

Let N be the set of agents and W the set of worlds.

Let Set of worlds.

Let N be the set of agents and W the set of worlds.

Let N be the set of agents and W the set of worlds.

#### Definition

It is **common knowledge** that *E* at *w* if everyone knows *E* at *w* and knows that transfer knows, and knows, and knows, and knows, and knows to write)

Common knowledge is what is experienced by everyone, e.g., a result of a joint public of the property of the p

It is an idealised setting, but - with some lenience - it can reasonably be assumed in certain circumstances.

For instance: look at the clock now. Its time is common knowledge.

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What is common knowledge at w<sub>3</sub>?
What Arold We Chat powcoder

Let  ${\it N}$  be the set of agents and  ${\it W}$  the set of worlds.

Let E be a fact.

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$$CE = \bigcap_{k=1}^{K^k} K^k E = KE \cap KKE \cap KKKE \dots$$

is the set Avold where comparing the coder

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What is common knowledge everywhere?
What Arold WeChat powcoder



Red is dive, blue is mum, purple is both, black is none.

Add Sweet that at a down oder How does the model change if I learn a new fact?

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Suppose I'm told Ronaldo did dive.

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Here Bob knows what Afrin has chosen.

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In other words, there are two worlds that Bob cannot distinguish:

- the one in which Ann has chosen to go left
- and the other in which Ann has chosen to go right.

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There is a difference between:

- knowing that I have a winning strategy
- and knowing which one it is.

Bob knows he has a winning strategy, but does not know which one.

It makes sense to assume that players will choose the same actions in situations that the scarn players will choose the same actions in After all, how can I say "if Ann has chosen left, then I go right", if I cannot observe any sign of this?

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#### Knowing that versus knowing how

#### Definition (Uniform Strategies)

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A strategy  $\sigma_i$  is said to be **uniform** if  $\sigma_i(h) = \sigma_i(h')$  whenever  $h \sim_i h'$ . In words, he teap't distinguish two situations lengoing to have to play the same action in both.

<sup>a</sup>This is not a rigorous definition at this stage, but it's easy to see that it can fall under our case if we interpret a history as a possible world. We will make it precise later in the course Chat powcoder

> If I have a uniform strategy to win, then I know how to win. Otherwise, I don't.

Bob, in the previous example, knows he can win, but does not know how.

Knowledge Agent-based Systems

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Which strategies are uniform?

Which strategies are uniform?
Which ones aren't?

- A mathematical model of knowledge and ignorance
- Mulhteps://powcoder.com
- Group knowledge: general, distributed, common
- Knowing that versus knowing know

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We are going to look at logical decisions in computational environments: actions, however by WCOGET.COM
We start with one agent, others will follow.

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