

# Assignment Project Exam Help Learning in Games

https://powcoder.com (Artificial) Poker Stars

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We have seen extensive games of imperfect information, where players are typically uncertainty about the current state of the game being played.

We are going to look at the relevance of this to Artificial Intelligence:

- Learning through self-play: the key to many game-playing engines (AlphaGo);
- \* Regret why it's important to minimise it. powcoder

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"Robots are unlikely to be welcome in casinos any time soon, especially now that a poker-playing computer has learned to play a virtually perfect game — including bluffing."

(Philip Ball: Game theorists crack poker, Nature News, 2015.)

Agent-based Systems

### Poker and Artificial Intelligence

### Assignment Project Exam Help Bluffing, aggressive play

- Still... a game
  - Atetta se gamen in white the formation of the strategies

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T.W. Sandholm.

Solving Imperfect-Information Games.

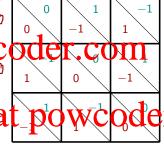
Science, 347(6218):122-123, 2015.



- Everyone who has played poker knows how critical "emotions" are in the game;
- Well it turns out that there is one emotion that computers use better than anyoreest DS://DOWCOCET.COM
- This emotion is regret: how bad I've played with respect to how I could have played;
- What iAregat WeChat powcoder

• If you play paper and I play paper, my regret for not playing stiggers is 1/(the DOWC payoff wilkference!).

o If you play paper and I play rock, my regret for not playing salsors is WeChat\_p



- regret for not playing  $\textcircled{\ }$  in  $(\textcircled{\ },\textcircled{\ })=0$
- regret for not playing  $\bigcirc$  in  $(\bigcirc, \bigcirc) = -1$  ttps://powcoder.com

Let  $\langle N, A, u \rangle$  be a normal-form game. At action to ite, the get of player for rot lawar a Go of CT  $u_i(a_i', a_{-i}) - u_i(a)$ .

### Avoiding feeling bad (without saying it)

## Assignment Project Exam Help

How can we use regret to inform future play?

- The ilea fist that twent to take actions that wish head played in the past;
- Obviously if ny opponent knew exactly what I was doing it would not be good;
- My strategy needs to be good and not exploitable.

### Add twice restriction would be a second to the contract of the

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We do this blaret mitating character and wide, and end distribution that is proportional to positive regrets.

This means regrets that are proportional to the relative losses one has experienced for not having selected actions in the past.

## Assignment we reject Exam Help regret for not playing Tin (E), (E) = 2

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We do this blaret mitain Celoragact po MdG, order distribution that is proportional to positive regrets.

This means regrets that are proportional to the relative losses one has experienced for not having selected actions in the past.

# • regret for not playing ① in (②, ①) = 1 • regret for not playing ② in (♡, ①) = 1

In the next to Schoole Don William et al. COM

 $\bigcirc$  with probability  $\frac{1}{3}$ ,  $\bigcirc$  with probability 0.

Notice: positive regrets divided by their sum.

We do this blogret mitain Character DO MIC OLDET distribution that is proportional to positive regrets.

This means regrets that are proportional to the relative losses one has experienced for not having selected actions in the past.

## Assignment Project Fram Help ... and it turns out to be ©;

• Suppose my opponent plays 🖱.

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### Assignment Project Exam Help and it turns out to be 🕚 Suppose my opponent plays

My regret for this land obviously for not playing and obviously for not playing and obviously for not playing

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Assignment Project Tan Help
... and it turns out to be ...

Suppose my opponent plays ...

Suppose my opponent plays ...

My regret for this partie 1/for my playing coder. Com

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We add the new regrets to the old ones, and play accordingly.

# Assignment Project Tan Help ... and it turns out to be ... • Suppose my opponent plays ...

My regret for thirt hand is 1/for my playing ender. Con 2 for not playing pand obviously of or Not playing ender.

We have 2 total regrets for ©, 2 total regrets for ©, 2 total regrets for ©.

Our next state (if going to expect for ©) DOWCOGET

We add the new regrets to the old ones, and play accordingly.

 If our opponent knows that we are using cumulative regrets, then they are always in a position to best respond.

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- The key idea, as often the case in modern AI, is to play against ourselves;
- We explict hypothet a gam s a fimile of the fine our strategies.

#### Learning in Games

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Objective: you want to learn their strategies.

A good hypothesis might be that the **frequency** with which player *i* plays action  $a_i$  is approximated in the property of the contract of th

Now suppose you always best-respond to those hypothesised strategies. And suppose everyone else does the same. What will happen?

We are going to see that of zero-similarnes this process converges to a NE.

This yields a method for computing a NE for the mon-repeated) game: just imagine players engaging in such "fictitious play".

Given a **history** of actions  $H_i^\ell = a_i^0, a_i^1, \dots, a_i^{\ell-1}$  played by player i in  $\ell$  prior plays of game  $\langle N, A, u \rangle$ , fix her **empirical mixed strategy**  $s_{i,j}^\ell \in S_i$ :

$$s_i^{\ell}(a_i) = \underbrace{\text{powcoder.com}}_{\text{relative frequency of } a_i \text{ in } H^{\ell}} \underbrace{\text{for all } a_i \in A_i}_{\text{relative frequency of } a_i \text{ in } H^{\ell}}$$

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#### Best Pure Responses

# Access representation of the state of the s

#### Proposition

For any given (par ial) strategy profile  $Y_i$ , the set of test responses for player i must include at least one pure strategy.

So we can restrict attention to best pure responses for player i to  $s_{-i}$ :  $a_i^* \in \underset{a \in A}{\operatorname{argmax}} u_i(a_i, s_{-i}) \text{ eChat powcoder}$ 

### Fictitious Play

## Take any action profile $a^0 \in A$ for the normal-form game (A, A, u). Action 19 April 19 A

- In round  $\ell = 0$ , each player  $i \in N$  plays action  $\mathbf{a_i^0}$ .
- In any round  $\ell > 0$ , each player  $i \in N$  plays a **best pure response** to her oppolents rempirical mixed strategies:

$$\inf_{\mathbf{a}_i^* \in \operatorname{algmax}_{a \in A}} u_i(a_i, \mathbf{p}_{-i}), \text{ where}$$

$$s_{i'}^\ell(a_{i'}) = \frac{1}{\ell} \cdot \#\{k < \ell \mid a_{i'}^k = a_{i'}\} \text{ for all } i' \in N \text{ and } a_{i'} \in A_{i'}$$

Assum A some deterministic way of breaking ties between maximal this yields a sequence  $a^0 \rightarrow a^1 \rightarrow a \rightarrow \cdots$  with a corresponding sequence of empirical-mixed-strategy profiles  $s^0 \rightarrow s^1 \rightarrow s^2 \rightarrow \cdots$ 

 $\underline{\text{Question:}} \ \ \mathsf{Does} \ \lim_{\ell \to \infty} \mathbf{s}^\ell \ \ \mathsf{exist} \ \ \mathsf{and} \ \ \mathsf{is} \ \ \mathsf{it} \ \ \mathsf{a} \ \ \mathsf{meaningful} \ \ \mathsf{strategy} \ \ \mathsf{profile?}$ 



### Example: Matching Pennies

Let's see what happens when we start in the upper lefthand corner HH (and break ties between equally good responses in favour of H):

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Any strategy Addepresented Cingle Atability Of Why Co. der

Exercise: Can you guess what this will converge to?



### Convergence Profiles are Nash Equilibria

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#### Lemma

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<u>Proof:</u> Suppose  $s^* = \lim_{\ell \to \infty} s^{\ell}$  exists. We need to show that  $s^*$  is a NE.

To see that it really is, note that  $s_i^*$  is the strategy that player i seems to be playing, when in fact the best responds against  $s_i^*$ , which she believes to be the profile of strategies of heropopents. Could be profile of Strategies of heropopents. This lemma is true for arbitrary (not just zero-sum) games.

### Convergence for Zero-Sum Games

#### Good news:

Theorem (Robinson, 1951)

An Say sees such gard and in titial action or bite, tic liting is play will do we get that D

Nash equilibrium.

We know that if FP converges then to a NE Thus, we still lave to show that the Ptoll Winner OCT The proof of this fact is difficult and we are not going to discuss it here.

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(1919–1985)



I. Robinson

An Iterative Method of Solving a Game.

Annals of Mathematics, 54(2):296-301, 1951.

### Playing against ourselves: the procedure

## As Single remaining Parison of Exam Help

- Add the strategy profile played to the strategy profile history;
- Select each player action profile according the strategy profile;
- Competers/powcoder.com
- 6 Add player regrets to the cumulative regrets;
- Repeat, for a fixed number of iterations;
- \* Return Aheader Weiger Chat powcoder

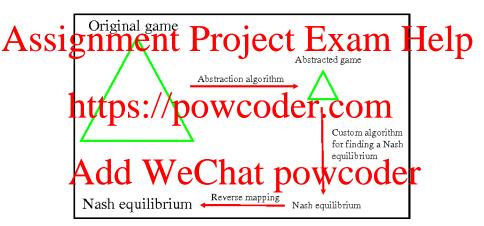
Hart and Mas-Colell (Econometrica, 2000) have shown that this simple procedure converges to a correlated equilibrium, in general, and to the unique NE in two-player zero sum games (like rock-paper-scissors).

- We have all the basics to tackle difficult games;
- The impletting of basis power of the mesting the mesting of the second of the second
- I'm going to present the general procedure

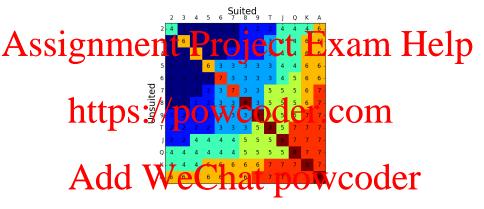
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We are not going to be able to compute the Nash equilibria of Poker. What can we do instead?



General game-theoretic approach for solving large games.



Preflop hands by strength distance, against various opponents' hands.



M.Johanson, N.Burch, R.A. Valenzano and M.Bowling Evaluating state-space abstractions in extensive-form games.

## Awsplayers Am Beauth Projecting Exam? Help

|       | Ann  | Bob          | Ann        | outcome            |
|-------|------|--------------|------------|--------------------|
| -     | pass | pass         |            | +1 to higher card  |
| 1 44  | pass | / bet        | pass       | +₁ to Bob          |
| nttos | pass | <b>1b</b> )† | <b>b</b> # |                    |
| Trop. | bet  | pass         |            | + 1 to Ann         |
|       | bet  | bet          |            | + 2 to higher card |

### Exercise: ACC VEC181100WCOCE

Represent Kuhn Poker as an extensive game of perfect information. How many are the information sets?

### Assignment, Project. Exam. Help Basically, CRM ...

- represents the game as a suitably abstracted extensive game of imperfect
- information power information in procedure, which is the regression matching procedure, which is the regression of the procedure.
- uses behavioural strategies.
- M. Zinkvich et dl. We Chat powcoder

  Regret Minimization in Games with Incomplete Information. NIPS. 2012.

### CRM in action: behavioural strategies

## Assignment Project Exam Help

#### Let:

- $r_i(h, h)$  be the regret for not taking action a affection  $r_i^t(h, h)$  be  $v_i(h, h)$  be  $v_i(h, h)$  at time  $v_i(h, h)$  at time  $v_i(h, h)$  be  $v_i(h, h)$  at time  $v_i(h, h)$  at  $v_i(h)$  a
- $r_i^T(h, a)$  be the sum of each  $r_i^t(h, a)$  over t, i.e., the cumulative regret.

Let moreover  $\mathbf{r}_i(h,a) = \sum_{h \in h} r_i(h',a)$  be the regret for not taking action a at Finally, let  $r_i$  (h, a) be the corresponding cumulative regret, setting negative regrets to 0.

### CRM: behavioural strategies

## Assissemmente. Repoject taki Excamistry lelp iteratively as follows:

### Theorem ACC VEC121 DOWCOCE1

The average strategy profile approaches (Nash) equilibrium as T approaches infinity.

We have seen how players can "learn" their opponents' strategies.

- Self-play as learning in a repeated game
   Convergence NE-if bot Polayers to C. Older Learning III.
- Application to Poker

Next: Look at learning in Al and then get back to GT with the new machinery  $Add \ WeCnat \ powcoder$