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Relational Algebra

CS430/630
Lecture 2

Relational Query Languages

- ▶ Query languages:
 - ▶ Allow manipulation and retrieval of data from a database
- ▶ Relational model supports simple, powerful QLs:
 - ▶ Strong formal foundation based on logic
 - ▶ Allows for much optimization
- ▶ Query Languages != programming languages
 - ▶ QLs not intended to be used for complex calculations
 - ▶ QLs support easy, efficient access to large data sets

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Formal Relational Query Languages

- ▶ Two languages form the basis for SQL:

- ▶ Relational Algebra:

- ▶ operational
 - ▶ useful for representing execution plans
 - ▶ very relevant as it is used by query optimizers!

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- ▶ Relational Calculus:

- ▶ Lets users describe the result, NOT how to compute it - declarative
 - ▶ We will focus on relational algebra



Preliminaries

- ▶ A query is applied to *relation instances*, and the result of a query is also a relation instance
 - ▶ *Schemas of input* relations for a query are *fixed*
 - ▶ The *schema for the result* of a given query is determined by operand schemas and operator type
- ▶ Each operation returns a relation
 - ▶ *operations can be composed !*
 - ▶ **Well-formed expression:** a relation, or the results of a relational algebra operation on one or two relations

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Relational Algebra

► Basic operations:

- Selection σ Selects a subset of rows from relation
- Projection π Derives invariant columns from relation
- Cross-product \times Allows us to combine several relations
- Join \bowtie Combines several relations using conditions
- Division \div A bit more complex, will cover later on
- Set-difference $-$ Union \cup Intersection \cap
- Renaming ρ Helper operator, does not derive new result, just renames relations and fields

$$\rho(R(F), E)$$

- F contains *oldname* \rightarrow *newname* pairs



Example Schema

Sailors

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

Boats

<u>bid</u>	name	color
101	interlake	red
103	clipper	green

Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96



Relation Instances Used

Sailors

S2

S1

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

Reserves

R1

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

Projection

- ▶ Unary operator
- ▶ Deletes (projects out) attributes that are not in *projection list*

$\pi_{attr1, attr2, \dots} relation$

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- ▶ Result Schema contains the attributes in the projection list
 - ▶ With the same names that they had in the input relation
- ▶ Projection operator has to eliminate *duplicates!*
 - ▶ Real systems typically do not do so by default
 - ▶ Duplicate elimination is *expensive!* (sorting)
 - ▶ User must explicitly asks for duplicate eliminations (**DISTINCT**)



Projection Example

S2

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

sname	rating
yuppy	9
lubber	8
guppy	5
rusty	10

$\pi_{sname, rating}(S2)$



Selection

- ▶ Unary Operator
- ▶ Selects rows that satisfy *selection condition*

$\sigma_{\text{condition}}$ *relation*

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- ▶ Condition contains constants and attributes from relation
 - ▶ Evaluated for each **individual** tuple
 - ▶ May use logical connectors AND (\wedge), OR (\vee), NOT (\neg)
- ▶ No duplicates in result! **Why?**
- ▶ *Result Schema* is identical to schema of the input relation



Selection Example

S2

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
58	rusty	10	35.0

$\sigma_{rating > 8}(S2)$

sname	rating
yuppy	9
rusty	10

Selection and Projection

$\pi_{sname, rating}(\sigma_{rating > 8}(S2))$



Cross-Product

- ▶ Binary Operator

$$R \times S$$

- ▶ Each row of relation R is paired with each row of S

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- ▶ *Result Schema* has one field per field of R and S

- ▶ Field names `inherited` when possible



Cross-Product Example

S1

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

R1

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

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$C = S1 \times R1$

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
31	lubber	8	55.5	58	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

Conflict: Both *R* and *S* have a field called *sid*



Cross-Product + Renaming Example

C

sid1	sname	rating	age	sid2	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
31	lubber	8	55.5	58	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

Renaming operator $\rho(C(1 \rightarrow sid1, 5 \rightarrow sid2), S1 \times R1)$



Condition Join (Theta-join)

$$R \bowtie_{\theta} S = \sigma_{\theta}(R \times S)$$

- ▶ Result Schema is same as that of cross-product

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Condition Join (Theta-join) Example

$S1 \times R1$

sid1	sname	rating	age	sid2	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
31	lubber	8	55.5	58	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

$$S1 \bowtie_{S1.sid < R1.sid} R1$$

sid1	sname	rating	age	sid2	bid	day
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	58	103	11/12/96

Equi-Join

- ▶ A special case of condition join where the condition contains only **equalities**

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$R \bowtie_{R.attr1=S.attr2} S$

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- ▶ Result Schema similar to cross-product, but only one copy of fields for which equality is specified

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Equi-Join Example

S1 X R1

sid1	sname	rating	age	sid2	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
31	lubber	8	55.5	58	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

S1 ⋈ *R1*
sid

sid	sname	rating	age	bid	day
22	dustin	7	45.0	101	10/10/96
58	rusty	10	35.0	103	11/12/96

Natural Join

- ▶ Equijoin on *all* common fields

$$R \bowtie S$$

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- ▶ Common fields are **NOT** duplicated in the result
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Union, Intersection, Set-Difference

- ▶ All of these operations take two input relations, which must be union-compatible
 - ▶ Same number of fields.
 - ▶ Corresponding fields have the same domain (type)
- ▶ What is the *schema* of result?

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Union Example

S_1

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

S_2

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0
44	guppy	5	35.0
28	yuppy	9	35.0

$S_1 \cup S_2$



Intersection Example

$S1$

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

$S2$

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

<u>sid</u>	sname	rating	age
31	lubber	8	55.5
58	rusty	10	35.0

$S1 \cap S2$



Set-Difference Example

$S1$

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

$S2$

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

<u>sid</u>	sname	rating	age
22	dustin	7	45.0

$S1 - S2$

