Add WeChat powcoder CSC373

Astigment Project Desigh,
Analysis & Complexity
Add WeChat powcoder

Nisarg Shah

Introduction powcoder

- Instructors
 - Nisarg Shah
 - o cs.toronto.edu/~nisarg, nisarg@cs, \$F-2301C Assignment Project Exam Help
 - o LEC 0101 and 0102
- TAs: Too many to list https://powcoder.com
- Disclaimer!

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Totally useless

this semester!

- > First online version of the course, so expect a bumpy ride at the start, but hopefully, we'll get through together
- > Use any of the feedback mediums (email, Piazza, ...) to let me know if you have any suggestions for improvement

Assignment Project Exam Help Course Information

- Course Page www.cs.toronto.edu/~nisarg/teaching/373f20/
 - All the information below is in the course information sheet, available on Piazza
 Assignment Project Exam Help
- Discussion Board piazzattes // ptowenterca/fall2020/csc373
- Grading MarkUs Add WeChat powcoder
 - > Link will be distributed after about a week or two
 - > LaTeX preferred, scans are OK!
- All times in Eastern time zone, all zoom links on the course page

Assignment Project Exam Help Lectures WeChat powcoder

- Time & Place: Tue 4-5pm, Thu 1-3pm, Zoom
- Details

 - > 10 minute break after every 50 minutes of lecture
 - > Students can ask questions using Zoom's chat feature
 - > One TA will be present to the through tapower questions
 - > I might also answer questions once in a while

Assignment Project Exam Help Tutorials WeChat powcoder

- Time & Place: Tue 5-6pm, Zoom
- Details
 - > Delivered live by TAS Assignment Project Exam Help
 - > Problem sets will be posted early on the course webpage
 - Easier problems that are warm-up to assignments/exams

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- > Please try them before coming to the tutorials
- > TAs will explain the problems, allow you to discuss them in breakout rooms, and then go over key parts of the solutions
- Solutions will be posted later on the course webpage

Assignment Project Exam Help Tutorials WeChat powcoder

- Further details
 - > Each section is divided into three parts (A,B,C)
 - Assignment Project Exam Help

 > Students divided by birth month: A = Jan-Apr, B = May-Aug, C = Sep-Dec

 https://powcoder.com
 - > Feel free to attend a different tutorial than the one you're assigned o EXCEPT when the tutorial slot is being used to be the chat power oder
 - > If the attendance is low, the number of tutorials per section may be reduced

Assignment Project Exam Help Office Hours Chat powcoder

- Time & Place: Wed 4-5pm, Fri 10-11am, Zoom
 - > Do you have conflicts with these slots? Poll!
- Details

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- > I will conduct them https://powcoder.com
- Use the "raise hand" feature
- > I will call upon the raised hand win Chatrowcoder
- > When called upon, unmute and ask the question
- > Always phrase your question in a way that doesn't give away your solutions or approach to an assignment problem

Just like in a physical office

Assignment Project Exam Help Tests Add WeChat powcoder

- 2 term tests, one end-of-term test (final exam)
- Time & Place: Tue 5-6pm (tutorial slot)

 Need to be able to attend live!

 Need to be able to attend live!
 - > I'm considering using parters the Tue 4-5pm lecture slot to give you more time
- Tentative Plan Add WeChat powcoder
 - > Open book, closed internet
 - > You may be asked to join a zoom link and keep your video on
 - > If you have a question, you can "raise hand", and I or a TA can take you to a breakout room to answer your question
 - > Upload scanned answer sheet at the end (we'll do a mock run of this)

Assignments hat powcoder

- 4 assignments, best 3 out of 4
- Group work
 - > In groups of up to three grundents Project Exam Help
 - Best way to learn is for each member to try each problem https://powcoder.com
- Questions will be more difficult
 - > May need to mull them over for several days; do not expect to start and finish the assignment on the same day!
 - > May include bonus questions
- Submission on MarkUs, more details later
 - > May need to compress the PDF

Assignment Project Exam Help Grading Policy powcoder

- 3 homeworks * 10% = 30%
- 2 term tests *Assignment=Project@xam Help
- Final exam * h3tp%://powcode/com

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NOTE: To pass, you must earn at least 40% on the final exam

Assignment Project Exam Help Approximate Due Dates

Please note the word approximate!

> Assignment 1: Apx. Oct 9

Apx. Oct 30 Assignment Project Exam Help Apx. Nov 13 Assignment 2:

Assignment 3:

Apx. Nottp3://powcoder.com Assignment 4:

Apx. Oct 20 > Midterm 1:

Apx. Nov 17 WeChat powcoder Midterm 2:

Conflicts

- > The tests are during the tutorial slot, so there should ideally be no conflict
- > That said, if you think you'll have a conflict, let me know at the earliest

Assignment Project Exam Help Textbook WeChat powcoder

Primary reference: lecture slides

- Primary textbook (Assigined) nt Project Exam Help
 - > [CLRS] Cormen, Leiserson, Rivest, Stein: *Introduction to Algorithms*. https://powcoder.com
- Supplementary textbooks (optional) powcoder
 - > [DPV] Dasgupta, Papadimitriou, Vazirani: Algorithms.
 - > [KT] Kleinberg; Tardos: *Algorithm Design*.

Assignment Project Exam Help Other Policies powcoder

Collaboration

- > Free to discuss with classmates or read online material
- Must write solutions in your own words
 Assignment Project Exam Help
 Easier if you do not take any pictures/notes from discussions

https://powcoder.com

Citation

- > For each question, must cite the peer (white frame) or the online sources (provide links), if you obtained a significant insight directly pertinent to the question
- > Failing to do this is plagiarism!

Assignment Project Exam Help Other Policies powcoder

- "No Garbage" Policy
 - Borrowed from: Prof. Allan Borodin (citation!)
 Assignment Project Exam Help
 - 1. Partial marks for viable approaches https://powcoder.com
 - 2. Zero marks if the answer makes no sense Add WeChat powcoder
 - 3. 20% marks if you admit to not knowing how to approach the question ("I do not know how to approach this question")
- 20% > 0%!!

Assignment Project Exam Help Other Policies powcoder

Late Days

- > 4 total late days across all 4 assignments
- Assignment Project Exam Help

 Managed by MarkUs
- > At most 2 late days can be applied to a single assignment
- > Already covers legitimate red styles light as olynesolem iversity activities, etc.
 - Petitions will only be granted for circumstances which cannot be covered by this

Zoom Features powcoder

- Just to get acquainted, let's try out the following features:
 - > Polls (already tried)

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> Chat

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> Reactions

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- > Raise hand
- > Yes/No
- > Breakout rooms

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What will we study?

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Why will every stardy it?



Muhammad ibn Musa al-Khwarizmi c. 780 – c. 850

- Algorithms
 - > Ubiquitous in the real world
 - o From your smartphonests self-driving project Exam Help
 - From graph problems to graphics problems
 - o ... https://powcoder.com
 - > Important to be able to design and analyze algorithms
 - > For some problems, good algorithms are hard to find
 - For some of these problems, we can formally establish complexity results
 - We'll often find that one problem is easy, but its minor variants are suddenly hard

Algorithms

- > Algorithms in specialized environments or using advanced techniques
 - o Distributed, parallel, Atseaming Subliner Time Texting Pectral, Repetic...
- > Other concerns with algorithms powcoder.com
 - Fairness, ethics, ... Add WeChat powcoder
- > ...mostly beyond the scope of this course

- Topics in this course
 - Divide and Conquer
 - > Greedy

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- > Dynamic programming
- > Network flow

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- > Linear programming
- > NP-completeness (not really an algorithm design paradigm)
- > Approximation algorithms (if time permits)
- Randomized algorithms (if time permits)

- How do we know which paradigm is right for a given problem?
 - > A very interesting question!
 - Subject of much ongoing research
 Sometimes, you just know it when you see it...
- How do we analyze an algorithm?
 - > Proof of correctness Add WeChat powcoder
 - > Proof of running time
 - We'll try to prove the algorithm is *efficient* in the *worst case*
 - In practice, average case matters just as much (or even more)

- What does it mean for an algorithm to be efficient in the worst case?
 - > Polynomial time
 - > It should use at most poly(n) steps on any n-bit input Assignment Project Exam Help $\circ n, n^2, n^{100}, 100n^6 + 237n^2 + 432, ...$

- https://powcoder.com

 If the input to an algorithm is a number x, the number of bits of input is $\log x$
 - o This is because it takes log A dick Wre present phevioporte in binary
 - \circ So the running time should be polynomial in $\log x$, not in x

> How much is too much?

Picture-Hanging Puzzles*

Erik D. Demaine[†] Martin L. Demaine[†] Yair N. Minsky[‡] Joseph S. B. Mitchell[§]

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Theorem 7 For any $n \ge k \ge 1$, there is a picture hanging on n nails, of length $n^{c'}$ for a constant c', that falls upon the removal of any k of the nails.

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 $n^{6,100\log_2 c}$. Using the $c \leq 1,078$ upper bound, we obtain an upper bound of $c' \leq 6,575,800$. Using

So, while this construction is polynomial, it is a rather large polynomial. For small values of n, we can use known small sorting networks to obtain somewhat reasonable constructions.

Better Balance by Being Biased:

A 0.8776-Approximation for Max Bisection

Assignment Project Exam Help Per Austrin Siavosh Benabbas, and Konstantinos Georgiou[†]

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has a lot of flexibility, indicating that further improvements may be possible. We remark that, while polynomial, the running time of the algorithm is somewhat abysmal; loose estimates places it somewhere around $O(n^{10^{100}})$; the running time of the algorithm of [RT12] is similar.

- What if we can't find an efficient algorithm for a problem?
 - > Try to prove that the problem is hard
 - > Formally establish considerity energy Project Exam Help
 - > NP-completeness, NP-hardness, ... https://powcoder.com
- We'll often find that one problem ham by weeksy, but its simple variants may suddenly become hard
 - > Minimum spanning tree (MST) vs bounded degree MST
 - > 2-colorability vs 3-colorability

Add WeChat powcoder I'm not convinced.

Will I really ever need to https://powcoder.com know.how.to.design abstract algorithms?

Add WeChat powcoder At the very least...

This will help you prepare for your technical obginterview et Exam Help

Real Microsoft interview question:

- Given an array a, find indices (i, j) with the largest j i such that a[j] > a[i]
- Greedy? Divide & conquer?

Assignment Project Exam Help Disclaimer. Chat powcoder

- The course is theoretical in nature
 - You'll be working with abstract notations, proving correctness of algorithms, analyzing the running time of algorithms, designing new algorithms, and proving complexity resugnment Project Exam Help

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- Something for everyone Add WeChat powcoder
 - > If you're somewhat scared going into the course
 - > If you're already comfortable with the proofs, and want challenging problems

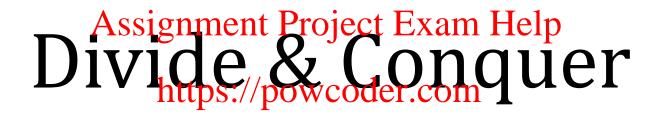
Assignment Project Exam Help Related/Follow-up Courses

- Direct follow-up
 - > CSC473: Advanced Algorithms
 - CSC438: Computability and Logic Assignment Project Exam Help
 CSC463: Computational Complexity and Computability

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- Algorithms in other contexts WeChat powcoder
 - > CSC304: Algorithmic Game Theory and Mechanism Design (self promotion!)
 - > CSC384: Introduction to Artificial Intelligence
 - > CSC436: Numerical Algorithms
 - > CSC418: Computer Graphics

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History? Add WeChat powcoder

- Maybe you saw a subset of these algorithms?
 - \rightarrow Mergesort $O(n \log n)$
 - > Karatsuba algorithm for fast multiplication $EQ(n^{\log_2 3})$ rather than $O(n^2)$
 - > Largest subsequence sum in O(n)
 - https://powcoder.com > ...

- Add WeChat powcoder

 Have you seen some divide & conquer algorithms before?
 - > Maybe in CSC236/CSC240 and/or CSC263/CSC265
 - Write "yes"/"no" in chat

Assignment Project Exam Help Divide & Conquer Exam Help

- General framework
 - Break (a large chunk of) a problem into two smaller subproblems of the same type
 - > Solve each subproblem recursively and independently
 - > At the end, quickly combines of the original problem

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- Hard to formally define when a given algorithm is divide-andconquer...
- Let's see some examples!

Assignment Project Exam Help Master Theorem weoder

- Here's the master theorem, as it appears in CLRS
 - > Useful for analyzing divide-and-conquer running time
 - > If you haven't already seen it, please spend some time understanding it

Theorem 4.1 (Master theorems: //powcoder.com Let $a \ge 1$ and b > 1 be constants, let f(n) be a function, and let T(n) be defined

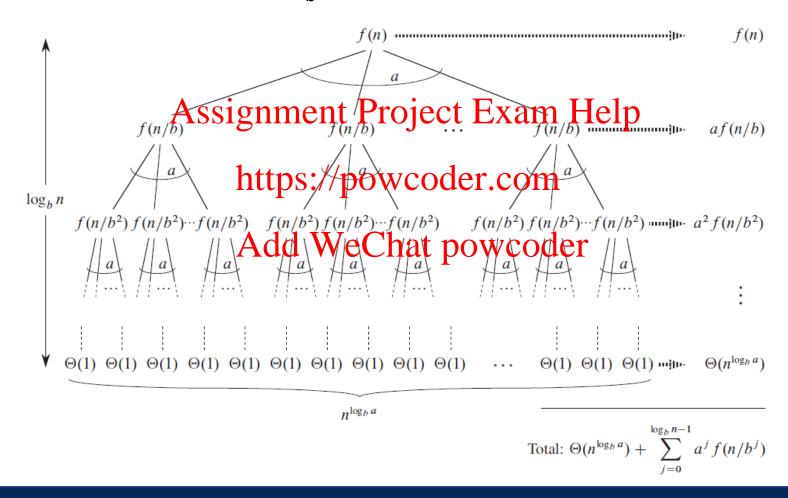
on the nonnegative integers by the recurrence
$$T(n) = aT(n/b) + f(n),$$
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where we interpret n/b to mean either $\lfloor n/b \rfloor$ or $\lceil n/b \rceil$. Then T(n) has the following asymptotic bounds:

- 1. If $f(n) = O(n^{\log_b a \epsilon})$ for some constant $\epsilon > 0$, then $T(n) = \Theta(n^{\log_b a})$.
- 2. If $f(n) = \Theta(n^{\log_b a})$, then $T(n) = \Theta(n^{\log_b a} \log n)$.
- 3. If $f(n) = \Omega(n^{\log_b a + \epsilon})$ for some constant $\epsilon > 0$, and if $af(n/b) \le cf(n)$ for some constant c < 1 and all sufficiently large n, then $T(n) = \Theta(f(n))$.

Master Theorem wcoder

Intuition: Compare f(n) with $n^{\log_b a}$. The larger determines the recurrence solution.



Counting Inversions

Problem

> Given an array a of length n, count the number of pairs (i,j) such that i < j but a[i] > a[j]Assignment Project Exam Help

Applications

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- > Voting theory
- > Collaborative filtering Add WeChat powcoder
- > Measuring the "sortedness" of an array
- > Sensitivity analysis of Google's ranking function
- > Rank aggregation for meta-searching on the Web
- > Nonparametric statistics (e.g., Kendall's tau distance)

Assignment Project Exam Help Counting Inversions

- Problem
 - \triangleright Count (i,j) such that i < j but a[i] > a[j]
- Brute force Assignment Project Exam Help
 - > Check all $\Theta(n^2)$ pairs

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- Divide & conquer
 - > Divide: break array into the diameter array into the bound of the bo
 - Conquer: count inversions in each half recursively
 - > Combine:
 - \circ Solve (we'll see how): count inversions with one entry in x and one in y
 - Merge: add all three counts

Assignment Project Exam Help Counting Inversions

From Kevin Wayne's slides

DIVIDE And Hist Wet with all the power oder

$$(r_A, A) \leftarrow \text{SORT-AND-COUNT}(A).$$

 $(r_B, B) \leftarrow \text{SORT-AND-COUNT}(B).$
 $(r_{AB}, L') \leftarrow \text{MERGE-AND-COUNT}(A, B).$

RETURN $(r_A + r_B + r_{AB}, L')$.

Counting Inversions

input											
1	5	4	8	10	2	6	9	3	7		
count in Assignmental Project Contamer Helip right half B											
1	5	1 ht	tps:	// / 8c)WC	ode	r.co	m	9	3	7
5-4 6-3 9-3 9-7											
Add WeChat powcoder count inversions (a, b) with a A and b B											
Count inversions (a, b) with a e A and b e b											
1	5	4	8	10			2	6	9	3	7
4-2 4-3 5-2 5-3 8-2 8-3 8-6 8-7 10-2 10-3 10-6 10-7 10-9											
output 1 + 3 + 13 = 17											

Assignment Project Exam Help Counting Inversions

- Q. How to count inversions (a, b) with $a \in A$ and $b \in B$?
- A. Easy if A and B are sorted!

Count inversions (a, b) with $a \in A$ and $b \in B$, assuming A and B are sorted.

- Scan A and B from left to right.
- CARRIGATION
 If a_i < b_j, then a_i is not inverted with any element left in B.

- If a_i > b_j, then b_j is inverted with every element left in A.
 Append smaller element to sorted is the community of the communit

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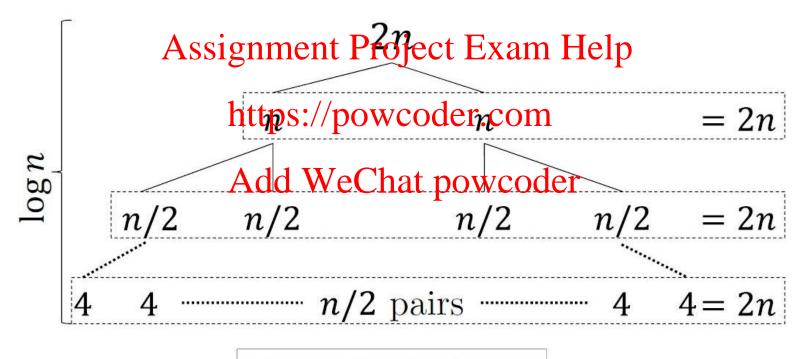
count inversions (a, b) with $a \in A$ and $b \in B$ 3 7 10 *ai* 18 2 11 *b_j* 17 23 merge to form sorted list C 3 7 10 11

Assignment Project Exam Help Counting Inversions

- How do we formally prove correctness?
 - \triangleright Induction on n is usually very helpful
 - > Allows you to assume correctness of subproblems Help
- Running time analysis https://powcoder.com
 - > Suppose T(n) is the run Aidelt We for an expect symposister n
 - > Our algorithm satisfies T(n) = 2 T(n/2) + O(n)
 - > Master theorem says this is $T(n) = O(n \log n)$

Assignment Project Exam Help Without Waster Theorem

Let's say
$$T(n) = 2 T(n/2) + 2n$$



Overall: $2n \log n$

Assignment Project Exam Help Closest Pair in R² Chat powcoder

Problem:

 \triangleright Given n points of the form (x_i, y_i) in the plane, find the closest pair of points.

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Applications:

- > Basic primitive in graphics to compute of the sign of the second secon
- Geographic information systems, molecular modeling, air traffic control
 Special case of nearest neighbor

• Brute force: $\Theta(n^2)$

Assignment Project Exam Help Intuition from 1D? Assignment Project Exam Help Intuition from 1D?

- In 1D, the problem would be easily $O(n \log n)$
 - > Sort and check!

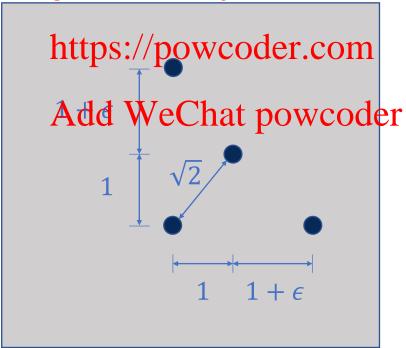
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- Sorting attempt in 2D
 - > Find closest points by x detapoinate wcoder.com
 - > Find closest points by y coordinate Add WeChat powcoder
- Non-degeneracy assumption
 - > No two points have the same x or y coordinate

Assignment Project Exam Help Intuition from 1D? Intuition from 1D?

- Sorting attempt in 2D
 - > Find closest points by x or y coordinate
 - Doesn't work!

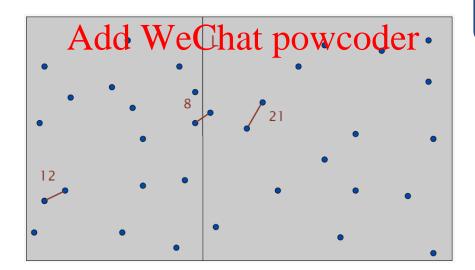
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Assignment Project Exam Help Closest Pair in R2 Closest Pair in R2 Wednat Powcoder

- Let's try divide-and-conquer!
 - > Divide: points in equal halves by drawing a vertical line L
 - Conquer: solve each half recursively
 Combine: find closest pair with one point on each side of L

 - > Return the best of 3 soluttoms://powcoder.com



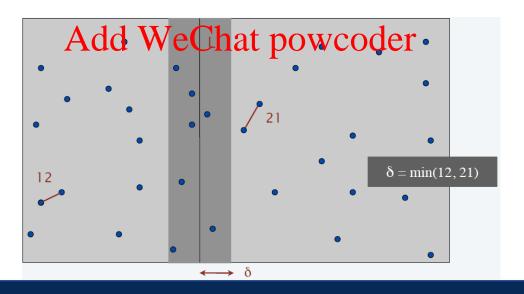
Seems like $\Omega(n^2)$ \odot

Assignment Project Exam Help Closest Pair in R² Chat powcoder

Combine

> We can restrict our attention to points within δ of L on each side, where δ = best of the solutions in two halves Assignment Project Exam Help

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Assignment Project Exam Help Closest Pair in R² Chat powcoder

- Combine (let δ = best of solutions in two halves)
 - \succ Only need to look at points within δ of L on each side,
 - Sort points on the strip by y coordinate
 Only need to check each point with next 11 points in sorted list!

https://powcoder.com Wait, what? Why 11? Add WeChat powcoder • $\delta = \min(12, 21)$

Assignment Project Exam Help Why 112 WeChat powcoder

• Claim:

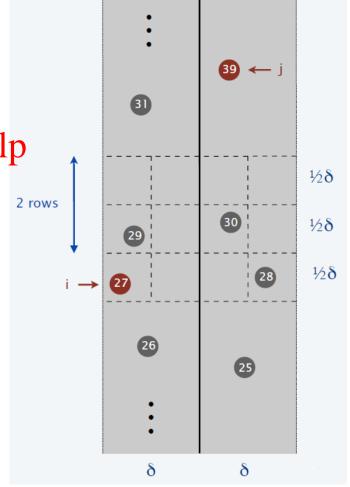
> If two points are at least 12 positions apart in the sorted list, their distance is at least δ .

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Proof:

> No two points lie in the https://powcoder.com $\delta/2 \times \delta/2$ box

> Two points that are more than two rows apart are at distance at least δ



Recap: Karatsuba's Algorithm

- Fast way to multiply two n digit integers x and y
- Brute force: $O(n^2)$ operations
- Karatsuba's observationment Project Exam Help
 - Divide each integer into two parts of the suppose of the suppose
 - > Four $^n/_2$ -digit multiplications can be replaced by three

$$x_1y_2 + x_2y_1 = (x_1 + x_2)(y_1 + y_2) - x_1y_1 - x_2y_2$$

> Running time

$$\circ T(n) = 3 T(n/2) + O(n) \Rightarrow T(n) = O(n^{\log_2 3})$$

Strassen's Algorithm

- Generalizes Karatsuba's insight to design a fast algorithm for multiplying two $n \times n$ matrices
 - > Call *n* the "size" of the problem Project Exam Help

$$\begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix} \text{tps} \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \text{er.} \begin{bmatrix} B_{11} & B_{12} \\ B_{21} & B_{22} \end{bmatrix}$$

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 \triangleright Naively, this requires 8 multiplications of size n/2

$$\circ A_{11} * B_{11}, A_{12} * B_{21}, A_{11} * B_{12}, A_{12} * B_{22}, \dots$$

> Strassen's insight: replace 8 multiplications by 7

$$\circ$$
 Running time: $T(n) = 7 T(n/2) + O(n^2) \Rightarrow T(n) = O(n^{\log_2 7})$

Strassen's Algorithm

$$\begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} * \begin{bmatrix} B_{11} & B_{12} \\ B_{21} & B_{22} \end{bmatrix}$$

STRASSEN(n, A, B)Stignment^BProject Exam Help assume n is Partition A and B into 2-by-2 block matrices. a power of 2 $P_1 \leftarrow \text{STRASSEN}(n/2, A_{11}, (B_{12} - B_{22}))$ $P_2 \leftarrow \text{STRASSEN}(n/2, A_{11}, (B_{12} - B_{22}))$ $P_3 \leftarrow \text{STRASSEN}(n/2, A_{11}, (B_{12} - B_{22}))$ $P_4 \leftarrow \text{STRASSEN}(n/2, A_{11}, (B_{12} - B_{22}))$ $P_5 \leftarrow \text{STRASSEN}(n/2, A_{11}, (B_{12} - B_{22}))$ $P_6 \leftarrow \text{STRASSEN}(n/2, A_{11}, (B_{12} - B_{22}))$ $P_7 \leftarrow \text{STRASSEN}(n/2, A_{11}, (B_{12} - B_{22}))$ $P_8 \leftarrow \text{STRASSEN}(n/2, A_{11}, (B_{12} - B_{22}))$ (don't copy matrix entries) $P_3 \leftarrow \text{STRASSEN}(n / 2, (A_{21} + A_{22}), B_{11}).$ P4 - ACCOMENTATION CODER $P_5 \leftarrow \text{STRASSEN}(n/2, (A_{11} + A_{22}) \times (\overline{B}_{11} + B_{22})).$ $P_6 \leftarrow \text{STRASSEN}(n/2, (A_{12} - A_{22}) \times (B_{21} + B_{22})).$ $P_7 \leftarrow \text{STRASSEN}(n/2, (A_{11} - A_{21}) \times (B_{11} + B_{12})).$ $C_{11} = P_5 + P_4 - P_2 + P_6$ $C_{12} = P_1 + P_2.$ $C_{21} = P_3 + P_4$. $C_{22} = P_1 + P_5 - P_3 - P_7$. RETURN C.

Assignment Project Exam Help Median & Selection er

- Selection:
 - \triangleright Given array A of n comparable elements, find kth smallest
 - > k = 1 is min, k = n is max, $k = \lfloor (n+1)/2 \rfloor$ is median
 - > O(n) is easy for min/maxignment Project Exam Help
- What about k-selection https://powcoder.com
 - > O(nk) by modifying bubble sort
 - > $U(n \log n)$ by sorting Add WeChat powcoder > $O(n + k \log n)$ using min-heap $> O(n \log n)$ by sorting

 - $> O(k + n \log k)$ using max-heap
- Q: What about just O(n)?
- A: Yes! Selection is easier than sorting.

Assignment Project Exam Help QuickSelect Chat powcoder

- Find a pivot p
- Divide A into two sub-arrays
 - > A_{less} = elements < Aps A grameral Project Exam Help
 - > If $|A_{less}| \ge k$, return kth smallest in A_{less} , otherwise return $(k |A_{less}|)$ th smallest in A_{more} https://powcoder.com

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Problem?

- > If pivot is close to the min or the max, then we basically get $T(n) \le T(n-1) + O(n)$, which only gives $T(n) = O(n^2)$
- > Want to reduce n-1 to a fraction of n (like n/2, 5n/6, etc)

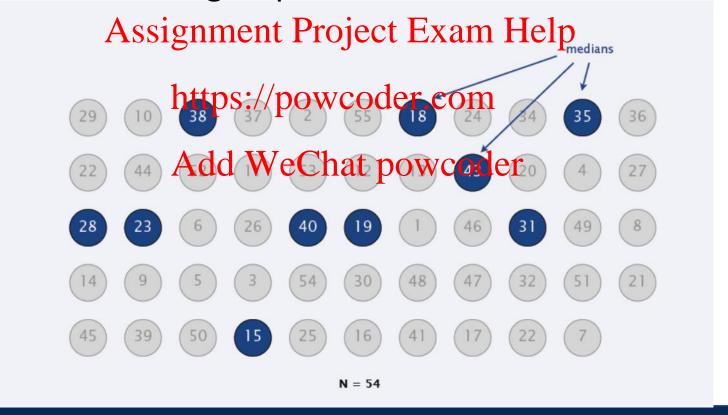
Assignment Project Exam Help Finding a Good Pivot

• Divide n elements into n/5 groups of 5 each

Assignment Project Exam Help And Weshat powcoders 26 40 19 31 (21) 30 48 16 N = 54

Assignment Project Exam Help Finding a Good Pivot

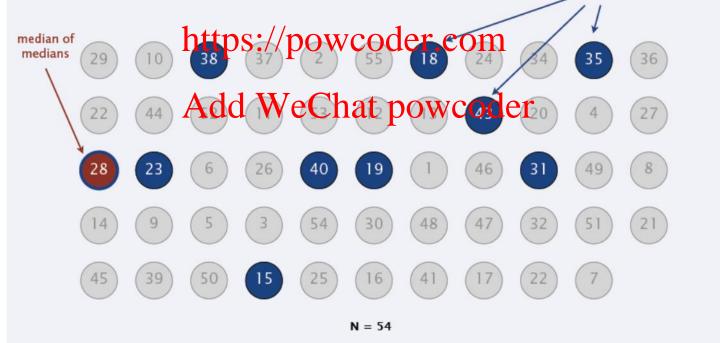
- Divide n elements into n/5 groups of 5 each
- Find the median of each group



Assignment Project Exam Help Finding a Good Pivot Finding a Good Pivot

- Divide n elements into n/5 groups of 5 each
- Find the median of each group

• Find the median of hyis median Reoject Exam Helpmedians



Assignment Project Exam Help Finding a Good Pivot

- Divide n elements into n/5 groups of 5 each
- Find the median of each group
- Find the median of signments Reoject Exam Help
- Use this median of medians as the pivotein quickselect

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Q: Why does this work?

Analysis WeChat powcoder

- How many elements can be $\leq p^*$?
 - \gt Out of n/5 medians, n/10 are $\gt p^*$

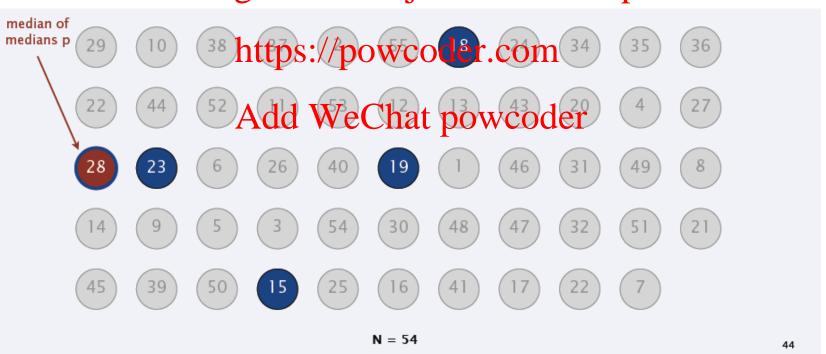
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Analysis WeChat powcoder

- How many elements can be $\leq p^*$?
 - \gt Out of n/5 medians, n/10 are $\gt p^*$

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Assignment Project Exam Help Analysis WeChat powcoder

- n/10 of the n/5 medians are $\leq p^*$
 - > For each such median, there are 3 elements $\leq p^*$
 - > So there can be at most $^{7n}/_{10}$ elements that can be > p^* Assignment Project Exam Help



Assignment Project Exam Help Analysis WeChat powcoder

- Thus, $|A_{more}| \le {}^{7n}/_{10}$
 - > Similarly, $|A_{less}| \le ^{7n}/_{10}$
 - > (These are rough calculations...)
 Assignment Project Exam Help
- How does this factor in the well-was defined analysis?

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Analysis WeChat powcoder

- Divide n elements into n/5 groups of 5 each
- Find the median of each group
- Find p^* = median of signments Reoject Exam Help
- Create A_{less} and A_{mor} and A_{mor} are some solution of the second secon
- Run selection on one of A_{lew} or $A_{moreweeder}$

$$O(n)$$

$$T(n/5)$$

$$O(n)$$

$$T(7n/10)$$

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- $T(n) \le T(n/5) + T(7n/10) + O(n)$
- Note: $n/5 + \frac{7n}{10} = \frac{9n}{10}$
 - > Only a fraction of n, so by the Master theorem, T(n) = O(n)

Residual Notes powcoder

- Best algorithm for a problem?
 - > Typically hard to determine
 - > We still don't know best algorithms for multiplying two n-digit integers or two Assignment Project Exam Help $n \times n$ matrices
 - Integer multiplication • Breakthrough in March 2019: first $O(n \log n)$ time algorithm

 - It is conjectured that this is a strong to the strong that t
 - Matrix multiplication
 - 1969 (Strassen): $O(n^{2.807})$
 - 1990: $O(n^{2.376})$
 - 2013: $O(n^{2.3729})$
 - 2014: $O(n^{2.3728639})$

Residual Notes powcoder

- Best algorithm for a problem?
 - > Usually, we design an algorithm and then analyze its running time

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> Sometimes we can do the reverse:

- - \circ E.g., if you know you want an $0(n^2\log n)$ algorithm
 - Master theorem suggests that down ghat by owcoder $T(n) = 4 T(n/2) + O(n^2)$
 - \circ So maybe you want to break your problem into 4 problems of size n/2 each, and then do $O(n^2)$ computation to combine

Assignment Project Exam Help Residual Notes powcoder

Access to input

- > For much of this analysis, we are assuming random access to elements of input
- > So we're ignoring underlying data structures (e.g. doubly linked list, binary tree, etc.)

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- Machine operations
 - Add WeChat powcoder

 > We're only counting the number of comparison or arithmetic operations
 - > So we're ignoring issues like how real numbers are stored in the closest pair problem
 - > When we get to P vs NP, representation will matter

Assignment Project Exam Help Residual Notes powcoder

- Size of the problem
 - > Can be any reasonable parameter of the problem
 - > E.g., for matrix multiplication, we Use less to Examize lelp
 - > But an input consists of two matrices with n^2 entries https://powcoder.com
 - > It doesn't matter whether we call n or n^2 the size of the problem
 - > The actual running time of the algorithm won't change